

```
In [1]: import numpy as np
import cv2
import scipy.io
import os
from numpy.linalg import norm
from matplotlib import pyplot as plt
from numpy.linalg import det
from numpy.linalg import inv
from scipy.linalg import rq
from numpy.linalg import svd
import matplotlib.pyplot as plt
import numpy as np
import math
import random
import sys
from scipy import ndimage, spatial
from tqdm.notebook import tqdm, trange
```

```
In [2]: from google.colab import drive
# This will prompt for authorization.
drive.mount('/content/drive')
```

Mounted at /content/drive

```
In [3]: class Image:
    def __init__(self, img, position):
        self.img = img
        self.position = position

    inlier_matchset = []
    def features_matching(a, keypointlength, threshold):
        #threshold=0.2
        bestmatch=np.empty((keypointlength), dtype= np.int16)
        img1index=np.empty((keypointlength), dtype= np.int16)
        distance=np.empty((keypointlength))
        index=0
        for j in range(0, keypointlength):
            #For a descriptor fa in Ia, take the two closest descriptors fb1 and fb2 in Ib
            x=a[j]
            listx=x.tolist()
            x.sort()
            minval1=[0]
            minval2=[1]
            itemindex1 = listx.index(minval1) #min
            itemindex2 = listx.index(minval2) #index of second min value
            ratio=minval1/minval2 #Ratio Test

            if ratio

```

```
def compute_Homography(im1_pts,im2_pts):
    """
    im1_pts and im2_pts are 2xn matrices with
    4 point correspondences from the two images
    """
    num_matches=len(im1_pts)
    num_rows = 2 * num_matches
    num_cols = 9
    A_matrix_shape = (num_rows,num_cols)
    A = np.zeros(A_matrix_shape)
    a_index = 0
    for i in range(0,num_matches):
        (a_x, a_y) = im1_pts[i]
        (b_x, b_y) = im2_pts[i]
        row1 = [a_x, a_y, 1, 0, 0, 0, -b_x*a_x, -b_y*a_y, -b_x]
        # First row
        row2 = [0, 0, 0, a_x, a_y, 1, -b_y*a_x, -b_y*a_y, -b_y] # Second row

        # place the rows in the matrix
        A[a_index] = row1
        A[a_index+1] = row2
        a_index += 2
    U, s, Vt = np.linalg.svd(A)

    #s is a 1-D array of singular values sorted in descending order
    #U, Vt are unitary matrices
    #Rows of Vt are the eigenvectors of A^T A.
    #Columns of U are the eigenvectors of A A^T.
    H = np.eye(3)
    H = Vt[-1].reshape(3,3) # take the last row of the Vt matrix
    return H

def displayplot(img,title):
    plt.figure(figsize=(15,15))
    plt.title(title)
    plt.imshow(cv2.cvtColor(img, cv2.COLOR_BGR2RGB))
    plt.show()
```

```
In [4]: def RANSAC_alg(f1, f2, matches, nRANSAC, RANSACthresh):
```

```
    minMatches = 4
    nBest = 0
    best_inliers = []
    H_estimate = np.eye(3,3)
    global inlier_matchset
    inlier_matchset=[]
    for iteration in range(nRANSAC):
        #Choose a minimal set of feature matches.
        matchSample = random.sample(matches, minMatches)

        #Estimate the Homography implied by these matches
        im1_pts=np.empty((minMatches,2))
        im2_pts=np.empty((minMatches,2))
        for i in range(0,minMatches):
            m = matchSample[i]
            im1_pts[i] = [m.pt1.x, m.pt1.y]
            im2_pts[i] = [m.pt2.x, m.pt2.y]
```

```

im1_pts[i] = f1[m.queryIdx].pt
im2_pts[i] = f2[m.trainIdx].pt
#im1_pts[i] = f1[m[0]].pt
#im2_pts[i] = f2[m[1]].pt

H_estimate=compute_Homography(im1_pts,im2_pts)

# Calculate the inliers for the H
inliers = get_inliers(f1, f2, matches, H_estimate, RANSACthresh)

# if the number of inliers is higher than previous iterations, update the best estimates
if len(inliers) > nBest:
    nBest= len(inliers)
    best_inliers = inliers

print("Number of best inliers",len(best_inliers))
for i in range(len(best_inliers)):
    inlier_matchset.append(matches[best_inliers[i]])

# compute a homography given this set of matches
im1_pts=np.empty((len(best_inliers),2))
im2_pts=np.empty((len(best_inliers),2))
for i in range(0,len(best_inliers)):
    m = inlier_matchset[i]
    im1_pts[i] = f1[m.queryIdx].pt
    im2_pts[i] = f2[m.trainIdx].pt
    #im1_pts[i] = f1[m[0]].pt
    #im2_pts[i] = f2[m[1]].pt

M=compute_Homography(im1_pts,im2_pts)
return M

```

In [5]:

```

def get_inliers(f1, f2, matches, H, RANSACthresh):

    inlier_indices = []
    for i in range(len(matches)):
        queryInd = matches[i].queryIdx
        trainInd = matches[i].trainIdx

        #queryInd = matches[i][0]
        #trainInd = matches[i][1]

        queryPoint = np.array([f1[queryInd].pt[0], f1[queryInd].pt[1], 1]).T
        trans_query = H.dot(queryPoint)

        comp1 = [trans_query[0]/trans_query[2], trans_query[1]/trans_query[2]] # normalize with respect to z
        comp2 = np.array(f2[trainInd].pt)[2]

        if(np.linalg.norm(comp1-comp2) <= RANSACthresh): # check against threshold
            inlier_indices.append(i)
    return inlier_indices

def ImageBounds(img, H):

    h, w = img.shape[0], img.shape[1]
    p1 = np.dot(H, np.array([0, 0, 1]))
    p2 = np.dot(H, np.array([0, h - 1, 1]))
    p3 = np.dot(H, np.array([w - 1, 0, 1]))
    p4 = np.dot(H, np.array([w - 1, h - 1, 1]))
    x1 = p1[0] / p1[2]
    y1 = p1[1] / p1[2]
    x2 = p2[0] / p2[2]
    y2 = p2[1] / p2[2]
    x3 = p3[0] / p3[2]
    y3 = p3[1] / p3[2]
    x4 = p4[0] / p4[2]
    y4 = p4[1] / p4[2]
    minX = math.ceil(min(x1, x2, x3, x4))
    minY = math.ceil(min(y1, y2, y3, y4))
    maxX = math.ceil(max(x1, x2, x3, x4))
    maxY = math.ceil(max(y1, y2, y3, y4))

    return int(minX), int(minY), int(maxX), int(maxY)

def Populate_Images(img, accumulator, H, bw):

    h, w = img.shape[0], img.shape[1]
    minX, minY, maxX, maxY = ImageBounds(img, H)

    for i in range(minX, maxX + 1):
        for j in range(minY, maxY + 1):
            p = np.dot(np.linalg.inv(H), np.array([i, j, 1]))

            x = p[0]
            y = p[1]
            z = p[2]

            _x = int(x / z)
            _y = int(y / z)

            if _x < 0 or _x >= w - 1 or _y < 0 or _y >= h - 1:
                continue

            if img[_y, _x, 0] == 0 and img[_y, _x, 1] == 0 and img[_y, _x, 2] == 0:
                continue

            wt = 1.0

            if _x >= minX and _x < minX + bw:
                wt = float(_x - minX) / bw
            if _x <= maxX and _x > maxX - bw:
                wt = float(maxX - _x) / bw

            accumulator[j, i, 3] += wt

            for c in range(3):
                accumulator[j, i, c] += img[_y, _x, c] *wt

```

In [6]:

```

def Image_Stitch(Imagesall, blendWidth, accWidth, accHeight, translation):
    channels=3
    #width=720

```

```

acc = np.zeros((accHeight, accWidth, channels + 1))
M = np.identity(3)
for count, i in enumerate(Imagesall):
    M = i.position
    img = i.img
    M_trans = translation.dot(M)
    Populate_Images(img, acc, M_trans, blendWidth)

height, width = acc.shape[0], acc.shape[1]

img = np.zeros((height, width, 3))
for i in range(height):
    for j in range(width):
        weights = acc[i, j, 3]
        if weights > 0:
            for c in range(3):
                img[i, j, c] = int(acc[i, j, c] / weights)

Imagefull = np.uint8(img)
M = np.identity(3)
for count, i in enumerate(Imagesall):
    if count != 0 and count != (len(Imagesall) - 1):
        continue
    M = i.position
    M_trans = translation.dot(M)
    p = np.array([0.5 * width, 0, 1])
    p = M_trans.dot(p)

    if count == 0:
        x_init, y_init = p[2] / p[0]
    if count == (len(Imagesall) - 1):
        x_final, y_final = p[2] / p[0]

A = np.identity(3)
croppedImage = cv2.warpPerspective(
    Imagefull, A, (accWidth, accHeight), flags=cv2.INTER_LINEAR
)
displayplot(croppedImage, 'Final Stitched Image')

```

```

In [8]: files_all = os.listdir('/content/drive/My Drive/Aerial/')
files_all.sort()
folder_path = '/content/drive/My Drive/Aerial/'

centre_file = folder_path + files_all[5]
left_files_path_rev = []
right_files_path = []

for file in files_all[1:6]:
    left_files_path_rev.append(folder_path + file)

left_files_path = left_files_path_rev[::-1]

for file in files_all[5:10]:
    right_files_path.append(folder_path + file)

```

```

In [10]: from PIL import Image, ExifTags
img = Image.open(f'{left_files_path[0]}')
exif = {ExifTags.TAGS[k]: v for k, v in img._getexif().items() if k in ExifTags.TAGS}
from PIL.ExifTags import TAGS

def get_exif(filename):
    image = Image.open(filename)
    image.verify()
    return image._getexif()

def get_labeled_exif(exif):
    labeled = {}
    for (key, val) in exif.items():
        labeled[TAGS.get(key)] = val

    return labeled

exif = get_exif(f'{left_files_path[0]}')
labeled = get_labeled_exif(exif)
print(labeled)
from PIL.ExifTags import GPSTAGS

def get_geotagging(exif):
    if not exif:
        raise ValueError("No EXIF metadata found")

    geotagging = {}
    for (idx, tag) in TAGS.items():
        if tag == 'GPSInfo':
            if idx not in exif:
                raise ValueError("No EXIF geotagging found")

            for (key, val) in GPSTAGS.items():
                if key in exif[idx]:
                    geotagging[val] = exif[idx][key]

    return geotagging
all_files_path = left_files_path[::-1] + right_files_path[1:]
for file1 in all_files_path:
    exif = get_exif(f'{file1}')
    geotags = get_geotagging(exif)
    def get_decimal_from_dms(dms, ref):
        degrees = dms[0][0] / dms[0][1]
        minutes = dms[1][0] / dms[1][1] / 60.0
        seconds = dms[2][0] / dms[2][1] / 3600.0

        if ref in ['S', 'W']:
            degrees = -degrees
            minutes = -minutes
            seconds = -seconds

        return round(degrees + minutes + seconds, 5)

    def get_coordinates(geotags):
        lat = get_decimal_from_dms(geotags['GPSLatitude'], geotags['GPSLatitudeRef'])
        lon = get_decimal_from_dms(geotags['GPSLongitude'], geotags['GPSLongitudeRef'])

```



```
In [13]: from matplotlib.offsetbox import OffsetImage, Annotation
```

```

fig, ax = plt.subplots()
fig.set_size_inches(20,10)
ax.set_xlabel('Latitude')
ax.set_ylabel('Longitude')
ax.set_xlim(100,101)
#ax.set_xlim(12,16)

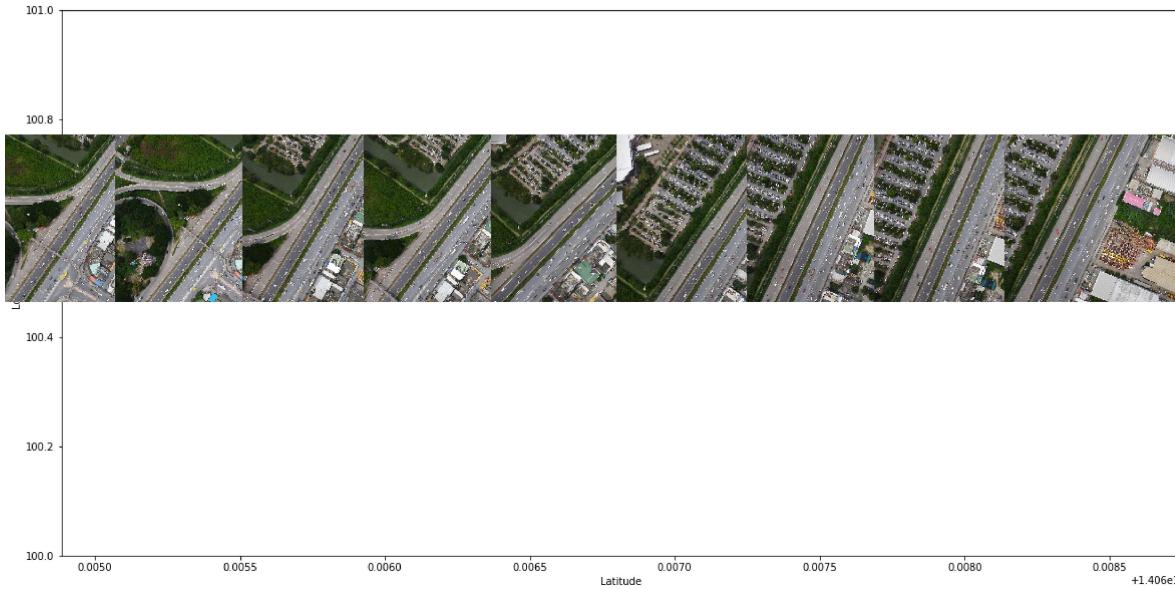
len1 = 50
ex.plot(np.array(all_geocoords)[:len1,0], np.array(all_geocoords)[:len1,1], linestyle='None')

def aerial_images_register(x, y, ax=None):
    ax = ax or plt.gca()
    for count,points in enumerate(zip(x,y)):
        lat,lon = points
        image = plt.imread(all_files_path[count])
        #print(ax.figure.dpi)
        im = OffsetImage(image, zoom=3/ax.figure.dpi)
        im.image.axes = ax
        ab = AnnotationBbox(im, (lat,lon), frameon=False, pad=0.0,)

        ax.add_artist(ab)

aerial_images_register(np.array(all_geocoords)[:len1,0], np.array(all_geocoords)[:len1,1], ax=ax)

```



```
In [14]: images_left = []
images_right = []

for file in tqdm(left_files_path):
    left_image_sat= cv2.imread(file)
    left_img = cv2.resize(left_image_sat,None,fx=0.75, fy=0.75, interpolation = cv2.INTER_CUBIC)
    images_left.append(left_img)

for file in tqdm(right_files_path):
    right_image_sat= cv2.imread(file)
    right_img = cv2.resize(right_image_sat,None,fx=0.75, fy=0.75, interpolation = cv2.INTER_CUBIC)
    images_right.append(right_img)
```

```
In [15]: #brisk = cv2.KAZE_create()
Threshl=60;
Octaves=6;
#PatternScales=1.0f;
brisk = cv2.BRISK_create(Threshl,Octaves)
#brisk = cv2.SIFT_create()
#brisk = cv2.AKAZE_create()

keypoints_all_left = []
descriptors_all_left = []
points_all_left=[]

keypoints_all_right = []
descriptors_all_right = []
points_all_right=[]

for imgs in tqdm(images_left):
    kpt = brisk.detect(imgs,None)
    kpt,descrip = brisk.compute(imgs, kpt)
    keypoints_all_left.append(kpt)
    descriptors_all_left.append(descrip)
    points_all_left.append(np.asarray([[p.pt[0], p.pt[1]] for p in kpt]))

for imgs in tqdm(images_right):
    kpt = brisk.detect(imgs,None)
    kpt,descrip = brisk.compute(imgs, kpt)
    keypoints_all_right.append(kpt)
    descriptors_all_right.append(descrip)
    points_all_right.append(np.asarray([[p.pt[0], p.pt[1]] for p in kpt]))
```

```
In [16]: def get_Hmatrix(imgs,keypts,pts,descripts,disp=True):
    #FLANN INDEX KDTREE = 1
    #index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)
    #search_params = dict(checks=50)
    #flann = cv2.FlannBasedMatcher(index_params, search_params)
    flann = cv2.BFMatcher()

    lff1 = np.float32(descripts[0])
    lff = np.float32(descripts[1])

    matches_lf1_lf = flann.knnMatch(lff1, lff, k=2)

    #print(len(matches_Lf1_Lf))

    matches_4 = []
    ratio = 0.8
    # loop over the raw matches
    for m in matches_lf1_lf:
        # ensure the distance is within a certain ratio of each
        # other (i.e. Lowe's ratio test)
        if len(m) == 2 and m[0].distance < m[1].distance * ratio:
            #matches_1.append((m[0].trainIdx, m[0].queryIdx))
            matches_4.append(m[0])

    print("Number of matches",len(matches_4))

    # Estimate homography
```

```

#Compute H1
imm1_pts=np.empty((len(matches_4),2))
imm2_pts=np.empty((len(matches_4),2))
for i in range(0,len(matches_4)):
    m = matches_4[i]
    (a_x, a_y) = keypoints[0][m.queryIdx].pt
    (b_x, b_y) = keypoints[1][m.trainIdx].pt
    imm1_pts[i]=(a_x, a_y)
    imm2_pts[i]=(b_x, b_y)
H=compute_Homography(imm1_pts,imm2_pts)
#Robustly estimate Homography 1 using RANSAC
Hn=RANSAC_alg(keypts[0] ,keypts[1], matches_4, nRANSAC=1500, RANSACthresh=6)
global inlier_matchset

if disp==True:
    dispimg1=cv2.drawMatches(imgs[0], keypoints[0], imgs[1], keypoints[1], inlier_matchset, None,flags=2)
    displayplot(dispimg1,'Robust Matching between Reference Image and Right Image')

return Hn/Hn[2,2]

```

In [17]:

```

H_left = []
H_right = []

for j in tqdm(range(len(images_left))):
    if j==len(images_left)-1:
        break

    H_a = get_Hmatrix(images_left[j:j+2][::-1],keypoints_all_left[j:j+2][::-1],points_all_left[j:j+2][::-1],descriptors_all_left[j:j+2][::-1])
    H_left.append(H_a)

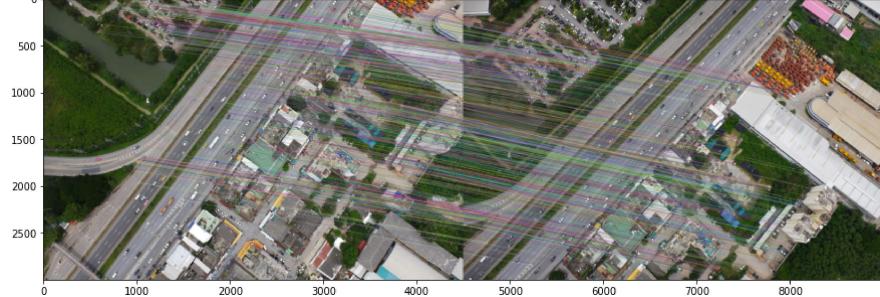
for j in tqdm(range(len(images_right))):
    if j==len(images_right)-1:
        break

    H_a = get_Hmatrix(images_right[j:j+2][::-1],keypoints_all_right[j:j+2][::-1],points_all_right[j:j+2][::-1],descriptors_all_right[j:j+2][::-1])
    H_right.append(H_a)

```

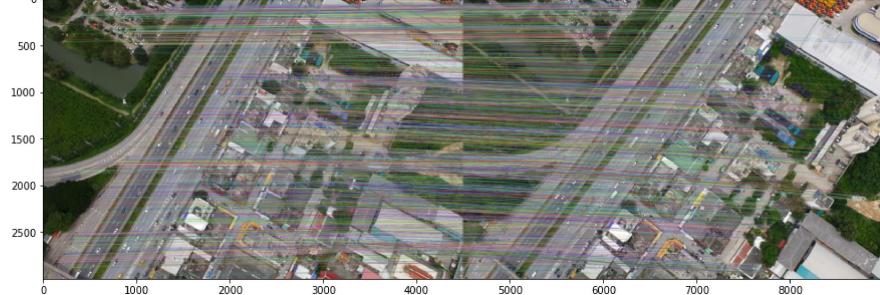
Number of matches 2238
Number of best inliers 1229

Robust Matching between Reference Image and Right Image



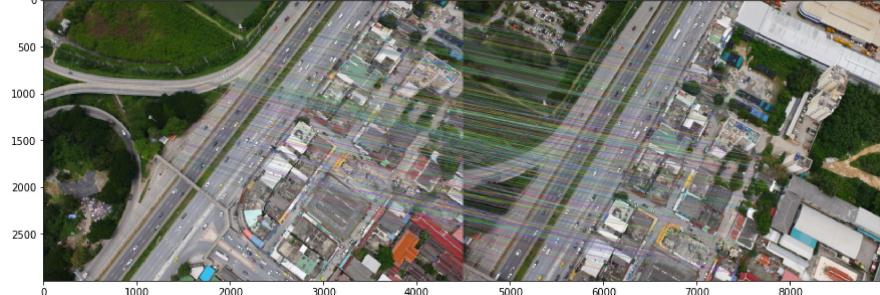
Number of matches 3884
Number of best inliers 1998

Robust Matching between Reference Image and Right Image

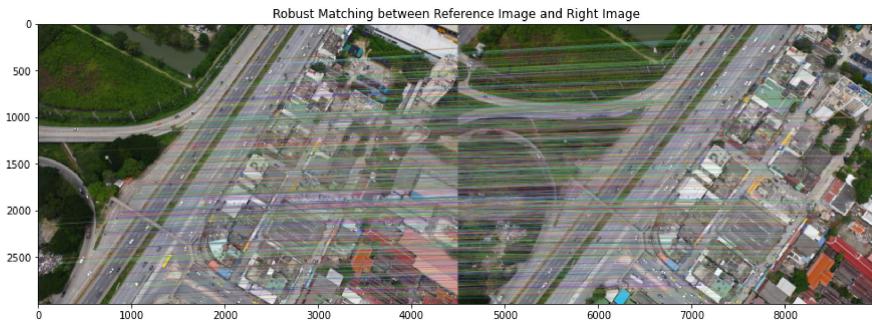


Number of matches 2094
Number of best inliers 856

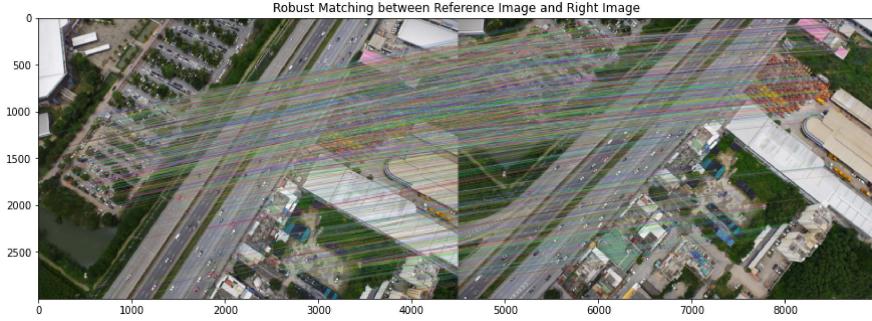
Robust Matching between Reference Image and Right Image



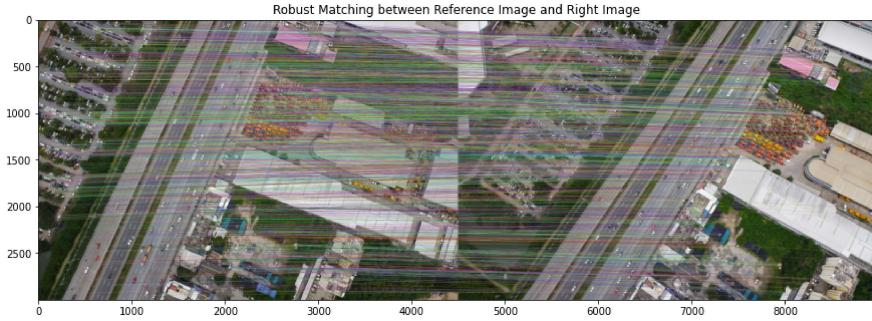
Number of matches 3446
Number of best inliers 1502



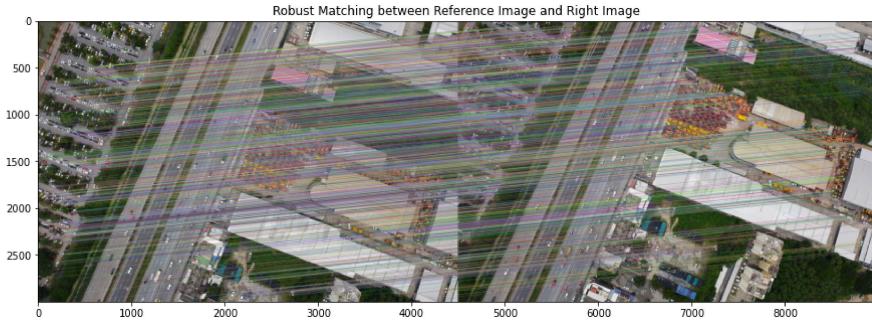
Number of matches 2981
Number of best inliers 2049



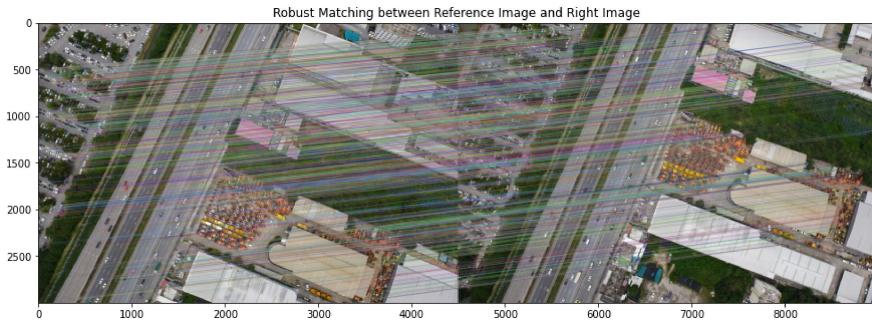
Number of matches 2378
Number of best inliers 1698



Number of matches 2981
Number of best inliers 2269



Number of matches 2224
Number of best inliers 1636



In [18]: `def warpnImages(images_left, images_right,H_left,H_right):`

```
#img1-centre, img2-left, img3-right
h, w = images_left[0].shape[:2]
pts_left = []
pts_right = []
pts_centre = np.float32([[0, 0], [0, h], [w, h], [w, 0]]).reshape(-1, 1, 2)
```

```

for j in range(len(H_left)):
    pts = np.float32([[0, 0], [0, h], [w, h], [w, 0]]).reshape(-1, 1, 2)
    pts_left.append(pts)

for j in range(len(H_right)):
    pts = np.float32([[0, 0], [0, h], [w, h], [w, 0]]).reshape(-1, 1, 2)
    pts_right.append(pts)

pts_left_transformed=[]
pts_right_transformed=[]

for j,pts in enumerate(pts_left):
    if j==0:
        H_trans = H_left[j]
    else:
        H_trans = H_trans@H_left[j]
    pts_ = cv2.perspectiveTransform(pts, H_trans)
    pts_left_transformed.append(pts_)

for j,pts in enumerate(pts_right):
    if j==0:
        H_trans = H_right[j]
    else:
        H_trans = H_trans@H_right[j]
    pts_ = cv2.perspectiveTransform(pts, H_trans)
    pts_right_transformed.append(pts_)

#pts = np.concatenate((pts1, pts2_), axis=0)

pts_concat = np.concatenate((pts_centre,np.concatenate(np.array(pts_left_transformed),axis=0),np.concatenate(np.array(pts_right_transformed),axis=0)), axis=0)

[xmin, ymin] = np.int32(pts_concat.min(axis=0).ravel() - 0.5)
[xmax, ymax] = np.int32(pts_concat.max(axis=0).ravel() + 0.5)
t = [-xmin, -ymin]
Ht = np.array([[1, 0, t[0]], [0, 1, t[1]], [0, 0, 1]]) # translate
print('Step2:Done')

warp_imgs_left = []
warp_imgs_right = []

for j,H in enumerate(H_left):
    if j==0:
        H_trans = Ht@H
    else:
        H_trans = H_trans@H
    result = cv2.warpPerspective(images_left[j+1], H_trans, (xmax-xmin, ymax-ymin))

    if j==0:
        result[t[1]:h+t[1], t[0]:w+t[0]] = images_left[0]

    warp_imgs_left.append(result)

for j,H in enumerate(H_right):
    if j==0:
        H_trans = Ht@H
    else:
        H_trans = H_trans@H
    result = cv2.warpPerspective(images_right[j+1], H_trans, (xmax-xmin, ymax-ymin))

    warp_imgs_right.append(result)

print('Step3:Done')

#Union

warp_images_all = warp_imgs_left + warp_imgs_right

warp_img_init = warp_images_all[0]

warp_final_all=[]

for j,warp_img in enumerate(warp_images_all):
    if j==len(warp_images_all)-1:
        break
    warp_final = np.maximum(warp_img_init,warp_images_all[j+1])
    warp_img_init = warp_final
    warp_final_all.append(warp_final)

print('Step4:Done')

return warp_final,warp_final_all

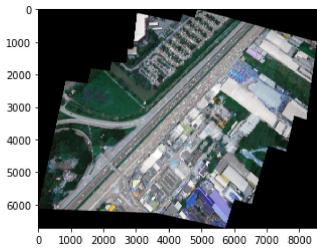
```

In [19]: combined_warp_n,warp_all = warpnImages(images_left, images_right,H_left,H_right)

Step2:Done
Step3:Done
Step4:Done

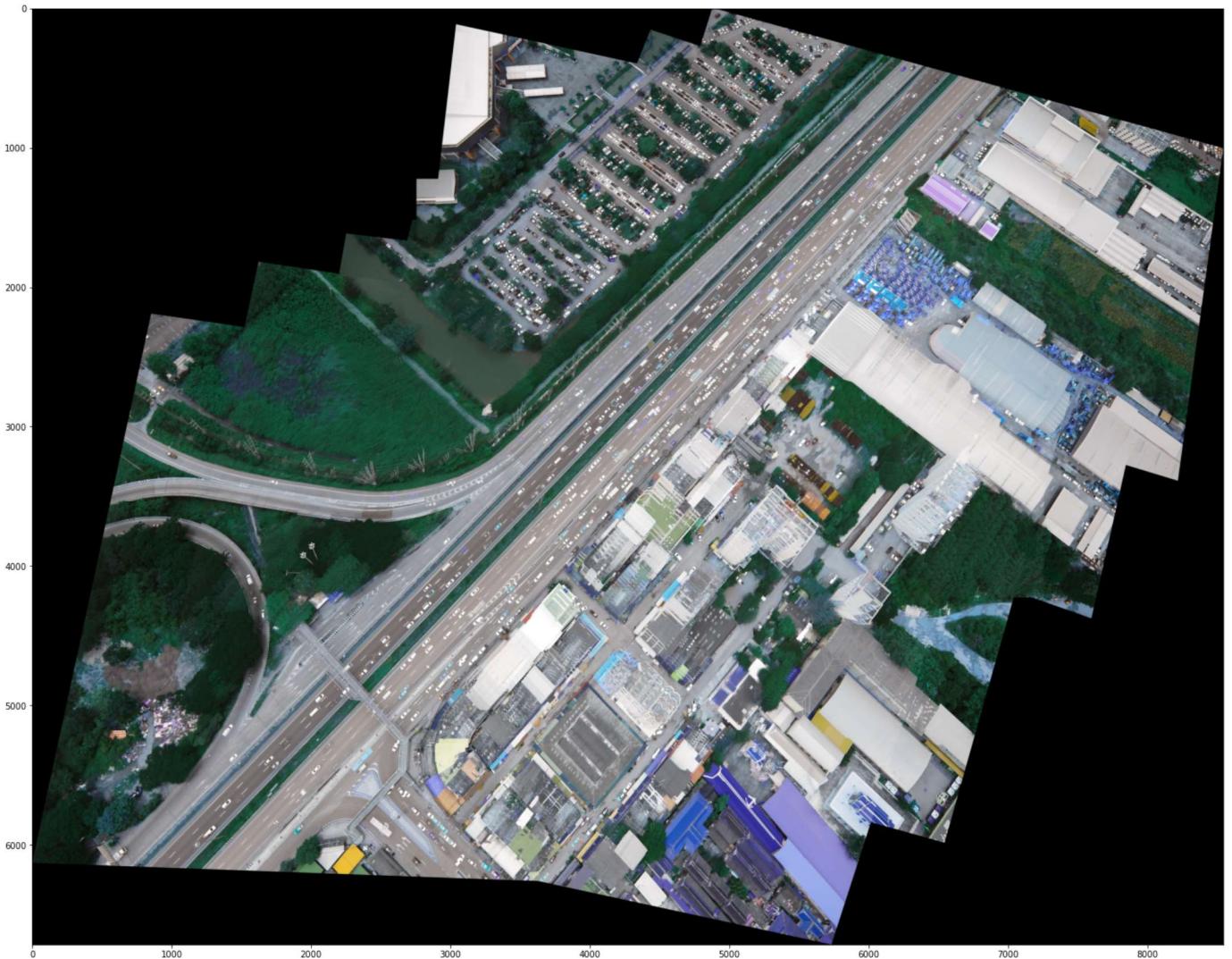
In [20]: plt.imshow(warp_all[6])

Out[20]: <matplotlib.image.AxesImage at 0x7f78c23ebf50>



```
In [21]: plt.figure(figsize = (25,20))  
plt.imshow(combined_warp_n)
```

```
Out[21]: <matplotlib.image.AxesImage at 0x7f78c29214d0>
```



```
In [22]: combo_rgb = cv2.cvtColor(combined_warp_n, cv2.COLOR_BGR2RGB)
```

```
In [23]: plt.figure(figsize = (25,15))
```

```
plt.imshow(combo_rgb)  
plt.title('10 Images Mosaic')
```

```
Out[23]: Text(0.5, 1.0, '10 Images Mosaic')
```

10 Images Mosaic

