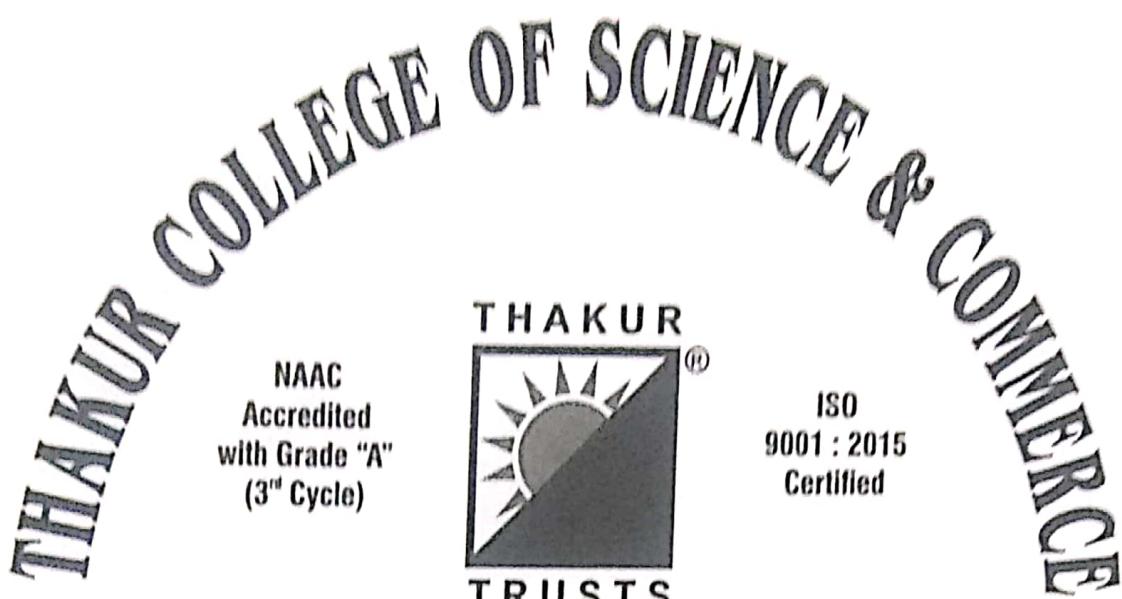


Exam Seat No.



Degree College

Computer Journal

CERTIFICATE

SEMESTER 2 UID No. _____

Class FYBSc(CS) A Roll No. 1742 Year 2019-2020

This is to certify that the work entered in this journal is the work of Mst. / Ms. Raj Waghela

who has worked for the year 2019-20 in the Computer Laboratory.

Teacher In-Charge

Head of Department

Date : 14/03/20

Examiner

★ ★ INDEX ★ ★

No.	Title	Page No.	Date	Staff Member's Signature
1	Basic of R software	39		G
2	Probability distribution	41		G
3	Binomial distribution	45		
4	Normal distribution	47		G
5	Normal & t-test.	49		G
6	Large sample test.	51		G
7	Small sample test	55		
8	large and small test.	57		G
9	Non parametric test of hypothesis	61		G
10	Chi sq & ANOVA	64		

Q8 Practical - 1

Aim: Basics of R software.

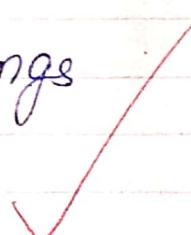
- 1) It is a software for statistical analysis and data computing.
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display.
- 4) It is a free software.

Q.1 Solve the followings

$$1. \quad 4+6+8 \div 2-5$$

$$> 4+6+8/2-5$$

[I] 9



$$2. \quad 2^0 + 1-3 + \sqrt{45}$$

$$> 2^0 + 1 - 3 + \sqrt{45}$$

[I] 13.7082

$$3. \quad 5^3 + 7 \times 5 \times 8 + 46/5$$

$$> 5^3 + 7 \times 5 \times 8 + 46/5$$

[I] 414.2

$$4. \quad \sqrt{4^2 + 5 \times 3 + 7/6}$$

$$> \sqrt{4^2 + 5 \times 3 + 7/6}$$

[I] 5.671567

5. round off

40

$$46 \div 7 + 9 \times 8 \\ > \text{round}(46/7 + 9 \times 8)$$

[1] 79

Q2
82
 $> C(2, 3, 5, 7) * 2$

$$\rightarrow 4 \ 6 \ 10 \ 14$$

$$> C(2, 3, 5, 7) * C(2, 3, 6, 2) \rightarrow C(1, 6, 2, 3) * C(2, -3, -4, 1)$$

$$\rightarrow 4 \ 9 \ 30 \ 14$$

$$> C(2, 3, 5, 7)^2$$

$$\rightarrow 4 \ 9 \ 25 \ 49$$

$$> C(6, 2, 7, 5) / C(4, 5)$$

$$\rightarrow 1.50 \ 0.40 \ 1.75 \ 1.00$$

$$> C(2, 3, 5, 7) * C(2, 3)$$

$$\rightarrow 4 \ 9 \ 10 \ 21$$

$$> C(1, 6, 2, 3) * C(2, -3, -4, 1) \rightarrow -2 \ -18 \ -8 \ -3$$

$$> C(4, 6, 8, 9, 4, 5) ^ 1 C(1, 2, 3)$$

$$\rightarrow 4 \ 36 \ 5182 \ 9 \ 16 \ 128$$

Q3

$$> x = 20 \quad > y = 30 \quad > z = 2$$

$$> x^2 + y^2 + z$$

[1] 27402

$$> \sqrt{x^2 + y^2 + z}$$

[1] 20.73644

$$> x^2 + y^2$$

[1] 1300

Q4. > x <- matrix(nrow=4, ncol=2, data=c(1, 2, 4, 5, 6, 7, 8))
> x

$$\begin{bmatrix} [1,1] & 1 & 4 \\ [1,2] & 1 & 5 \\ [2,1] & 2 & 6 \\ [2,2] & - & - \\ [3,1] & 3 & 7 \\ [3,2] & - & - \\ [4,1] & 4 & 8 \\ [4,2] & - & - \end{bmatrix}$$

Q5 Find $2x + 3y$ and $2x + 3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 4 \\ 9 & -5 & 3 \end{bmatrix}$
 $y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$

> x <- matrix(nrow=3, ncol=3, data=c(4, 7, 9, -2, 0, -5, 6, 2, 3))
> x

$$\begin{bmatrix} [1,1] & 4 & -2 & 6 \\ [1,2] & 7 & 0 & 7 \\ [1,3] & 9 & -5 & 3 \end{bmatrix}$$

> y <- matrix(nrow=3, ncol=3, data=c(10, 12, 15, -5, -4, -6, 7, 9, 5))
> y

$$\begin{bmatrix} [1,1] & 10 & -5 & 7 \\ [1,2] & 12 & -4 & 9 \\ [1,3] & 15 & -6 & 5 \end{bmatrix}$$

	[,1]	[,2]	[,3]
x^t	14	-7	13
[1,]	19	-4	6
[2,]	24	-11	8
[3,]			

	$2^x + 3^y$	$[,1]$	$[,2]$	$[,3]$
x^t	38	-19	33	
[1,]	50	-12	41	
[2,]	63	-28	21	
[3,]				

Q6 marks of statistic of CS Batch B

$n = c(58, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)$

$x = c(\text{data})$

$\text{breaks} = \text{seq}(20, 60, 5)$

$a = \text{cut}(n, \text{breaks}, \text{right} = \text{FALSE})$

$b = \text{table}(a)$

$c = \text{transform}(b)$

d

	a	freq
1	[20, 25]	3
2	[25, 30]	2
3	[30, 35]	1
4	[35, 40]	4
5	[40, 45]	1
6	[45, 50]	3
7	[50, 55]	2
8	[55, 60]	4



5A

Practical - 2

Topic - Probability distribution

- 1) Check whether the following are P.M.F or not

x	$P(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is pmf then $\sum P(x) = 1$

$$\begin{aligned} & \therefore P(0) + P(1) + P(2) + P(3) + P(4) + P(5) = P(x) \\ & = 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ & = 1 \end{aligned}$$

$\because P(2) = -0.5$, it can be a probability mass function.

$$\therefore P(x) \geq 0 \quad \forall x$$

2)

x	$P(x)$
1	0.2
2	0.2
3	0.3
4	0.2
5	0.2

The condition for Pmp is $\sum P(x_i) = 1$

$$\begin{aligned} \sum P(x_i) &= P(1) + P(2) + P(3) + P(4) + P(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1 \end{aligned}$$

The given data is not a PMF because $\sum p(x) \neq 1$

x	p(x)
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for PMF is

$$1) p(x_i) \geq 0 \quad \forall x_i \text{ satisfy}$$

$$2) \sum p(x_i) = 1$$

$$\begin{aligned} \sum p(x_i) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1 \end{aligned}$$

∴ The given data is PMF

Code :

```
> prob = c(0.2, 0.2, 0.35, 0.15, 0.1)
```

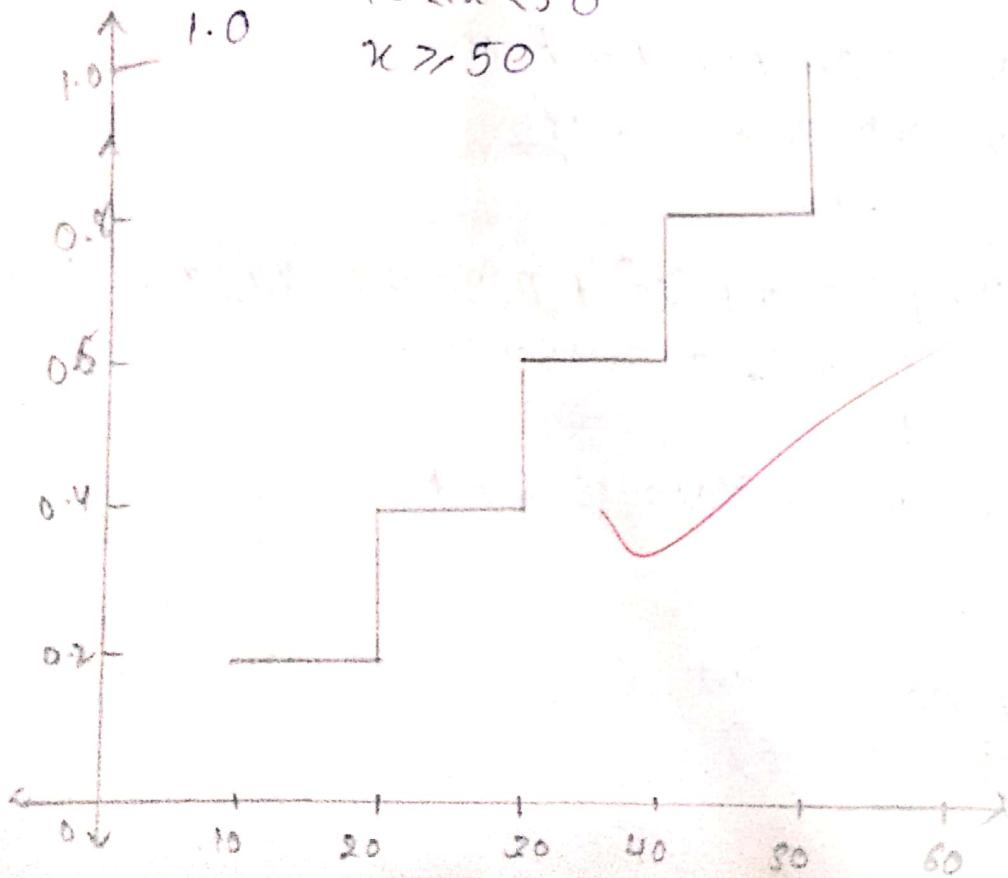
```
> sum(prob)
```

```
[1] 1
```

Q2 Find the Cdf for the following PmF and sketch the graph

x	10	20	30	40	50
$P(x)$	0.2	0.2	0.35	0.15	0.1

$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.90 & 40 \leq x < 50 \\ 1.0 & x \geq 50 \end{cases}$$



> $x = \ell(10, 20, 30, 40, 50)$

> $\text{plot} = (\text{x}, \text{cumsum}(\text{prob}), "s")$

Q) Find

x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$$\begin{aligned}
 F(x) &= 0 & x < 1 \\
 &= 0.15 & 1 \leq x < 2 \\
 &= 0.40 & 2 \leq x < 3 \\
 &= 0.50 & 3 \leq x < 4 \\
 &= 0.70 & 4 \leq x < 5 \\
 &= 0.90 & 5 \leq x < 6 \\
 &= 1.00 & x \geq 6
 \end{aligned}$$

$> Prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$
 $> sum(Prob)$

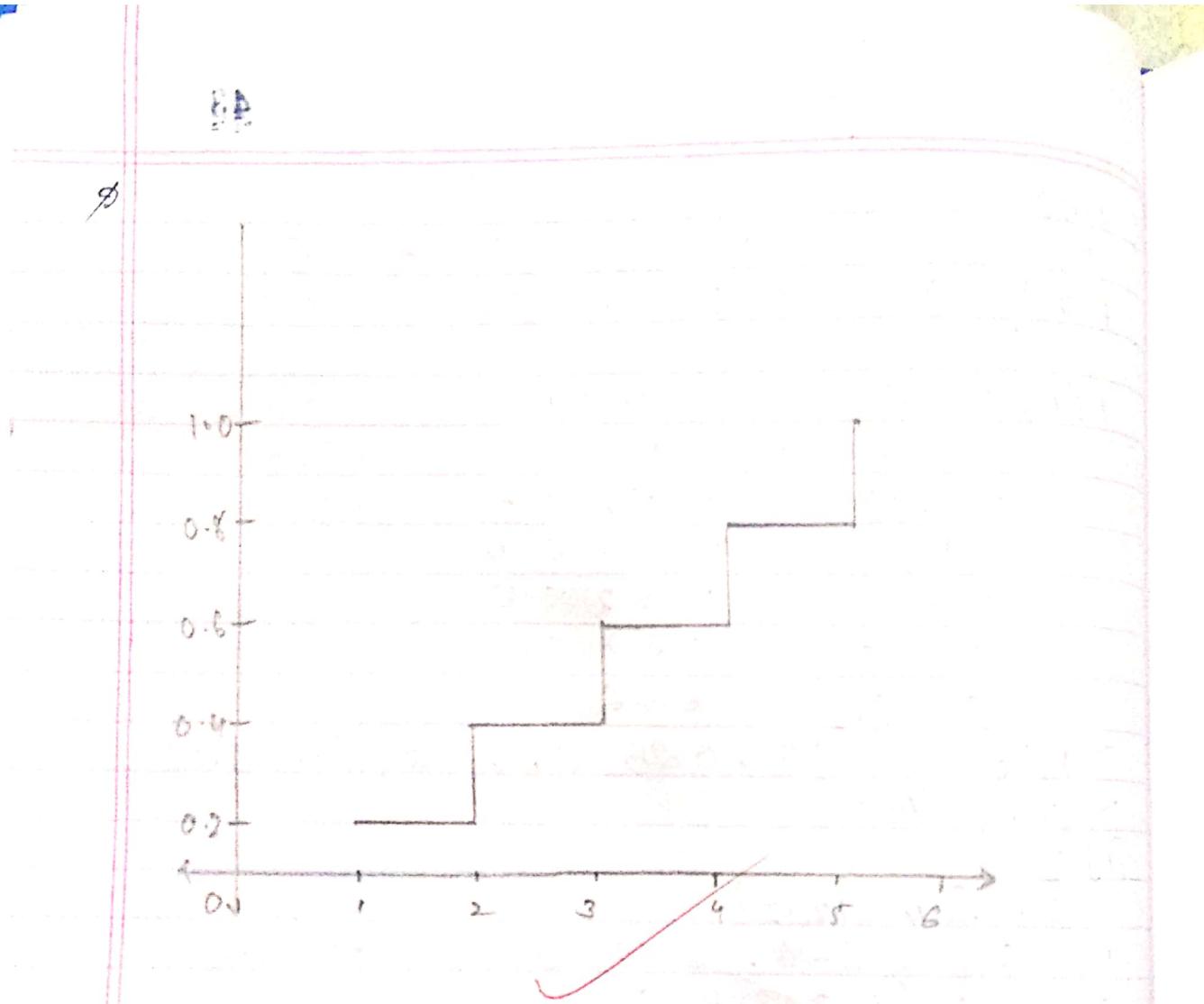
[1] 1

$> cumsum(Prob)$

[1] 0.15 0.40 0.50 0.70 0.90 1.00

$> x = c(1, 2, 3, 4, 5, 6)$

$> plot(x, cumsum(Prob), "s", xlab = "value",$
 $ylabel = "Cumulative probability",$
 $main = "CDF graph", col = "brown")$



3. Check that whether the following is P.d.f or not

$$(i) f(x) = 3 - 2x ; 0 \leq x \leq 1$$

$$(ii) f(x) = 3x^2 ; 0 < x < 1$$

$$\begin{aligned}
 (iii) f(x) &= 3 - 2x \\
 &= \int f(x) dx \\
 &= \int (3 - 2x) dx \\
 &= 3x - 2x^2 \Big|_0^1 = 3 - 2 = 1
 \end{aligned}$$

$$= [3x - x^2]_0^1 = 2$$

$\therefore \int_0^1 f(x) dx = 1 \therefore$ it is not a pdf

44

2) $f(x) = 3x^2; 0 < x < 1$

$$\int_0^1 f(x)$$

$$= \int_0^1 3x^2$$

$$= 3 \int_0^1 x^2$$

$$= \left[3 \frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The $\int_0^1 f(x) dx = 1 \therefore$ It is a pdf.



Q. 44

1) $\text{d}x = \text{dbinom}(10, 100, 0.1)$

[1] 0.13

2) i) $\text{dbinom}(4, 12, 0.2)$

[1] 0.1328756

(ii) $\text{pbinom}(4, 12, 0.2)$

[1] 0.427445

(iii) $1 - \text{pbinom}(5, 12, 0.2)$

[1] 0.01940528

3) $\text{dbinom}(0:5, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

4) i) $\text{dbinom}(5, 12, 0.25)$

[1] 0.1032414

2) $\text{pbinom}(5, 12, 0.25)$

[1] 0.9465978

3) $1 - \text{pbinom}(6, 12, 0.25)$

[1] 0.08298157

(4) $\text{dbinom}(6, 12, 0.25)$

[1] 0.04014945

Practical - 3

45

TOPIC: Binomial distribution.

$P(X=x) = \text{dbinom}(x, n, p)$

$P(X \leq x) = \text{pbinom}(x, n, p)$

$P(X > x) = 1 - \text{pbinom}(x, n, p)$

If x is unknown

$P_I = P(X \leq x) = \text{qbinom}(p_I, n, p)$

i) Find the probability of exactly 10 success in hundred trials with $p = 0.1$

ii) Suppose there are 12 MCQ, each question has 5 options out of which one is correct find the probability of having exactly 4 correct answers.

iii) atmost 4 correct answer.

iv) More than 5 correct answer.

v) Find the complete distribution when $n=5$ &

$p = 0.1$

vi) $n=12, p=0.25$ find the following probabilities.

i) $P(X=5)$

iii) $P(X>7)$

ii) $P(X \leq 5)$

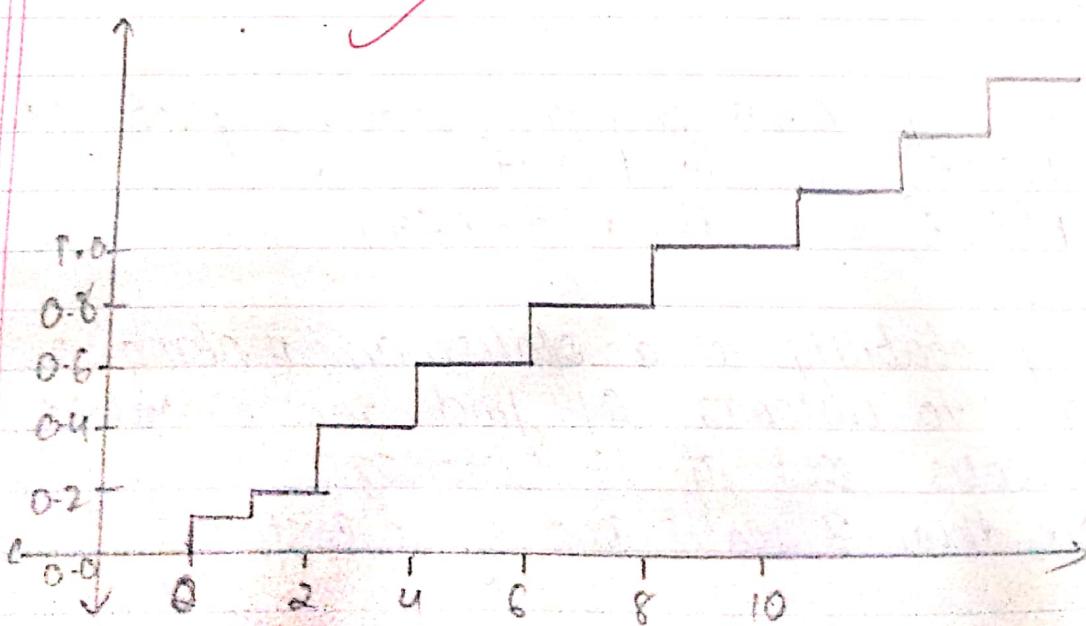
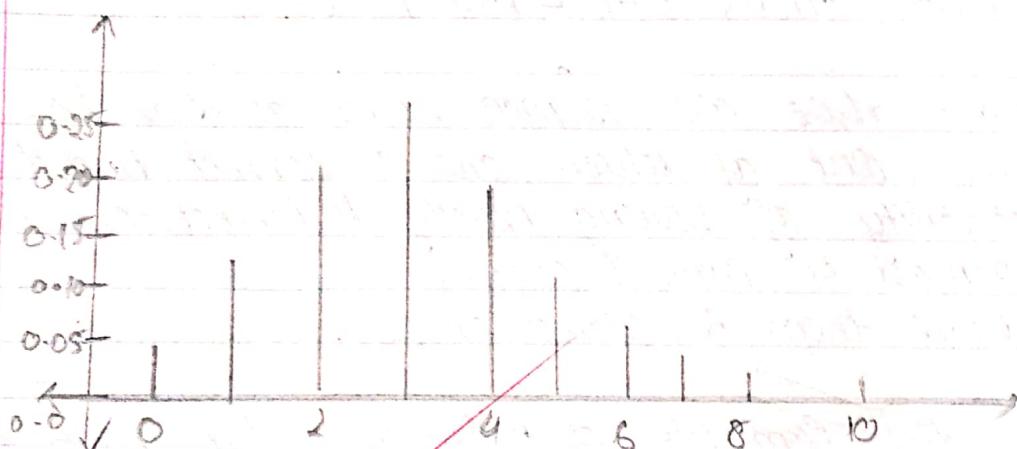
iv) $P(5 < X < 7)$

vii) The probability of a salesman making a sale to customer 0.15 find the probability of no sales out of 10 customer

viii) more than 3 sales out of 10 customer.

Q) A salesman has 80% probability of making a sale to customers out of 30 customers. What minimum number of sales he can make with 88% of probability.

7) X follows binomial distribution with $n=10$, $p=0.3$. Plot the graph of p.m.f and C.d.F.



> dbinom(0, 10, 0.15)
[1] 0.1968744

46

> 1 - pbisnom(3, 20, 0.15)
[1] 0.3522748

> abinom(0.88, 30, 0.2)
[1] 9

> n = 10

> p = 0.3

> x = 0:n

> prob = dbinom(x, n, p)

> cumprob = pbisnom(x, n, p).

> d = data.frame("x Values" = x, "Probability" = prob)
> print(d)

	x values	Probability
1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.0001
11	10	0.0000

G
S

Practical - 4

47

Aim : Normal Distribution.

i) $p(x = x) = dnorm(x, \mu, \sigma)$

ii) $p(x \leq x) = pnorm(x, \mu, \sigma)$

iii) $p(x > x) = 1 - pnorm(x, \mu, \sigma)$

iv) To generate random numbers from a normal distribution (n random numbers) the R code is $rnorm(n, \mu, \sigma)$

A random variable x follows normal distribution with mean $= \mu = 12$ and s.d $= \sigma = 3$. Find

i. $P(x \leq 15)$ ii. $P(10 \leq x \leq 13)$ iii. $P(x > 14)$

iv Generate 5 observations (random numbers)

Code :

> p1 = ~~pnorm~~(15, 12, 3)

> p1

[1] 0.8413447

> cat ("P(x \leq 15) = ", p1)

$P(x \leq 15) = 0.8413447$

> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)

> p2

[1] 0.3780661

> cat ("P(10 \leq x \leq 13) = ", p2)

$P(10 \leq x \leq 13) = 0.3780661$

> p3 = 1 - pnorm(14, 12, 3)

> p3

[1] 0.2524925

Q. A.

Q. 3

> cat ("P(X > 14) = ", p3)

P(X > 14) = 0.2524025

> p4 = rnorm(5, 12, 3)

> p4

[1] 15.2547983 16.548505 11.280515 6.419944
12.272460

2. X follows normal distribution with $\mu = 10, \sigma = 2$.
Find i) $P(X \leq 7)$ ii) $P(5 < X < 12)$ iii) $P(X > 12)$
iv) Generates 10 observations v) find K such
that $P(X < K) = 0.4$.

Code:

> a1 = pnorm(7, 10, 2)

> a1

[1] 0.668092

> a2 = pnorm(5, 10, 2) - pnorm(12, 10, 2)

> a2

[1] -0.8351351

> a3 = 1 - pnorm(12, 10, 2)

> a3

[1] 0.1586553

> a4 = rnorm(10, 10, 2)

> a4

[1] 11.608931 9.920417 12.637741 8.078354
8.721380 9.193726 9.366824 11.707106
9.537584 10.915006

> a5 = qnorm(0.4, 10, 2)

> a5

[1] 9.493306

B Generate 5 random numbers from a normal distribution $\mu=15, \sigma=4$ Find sample mean, Median, S.D and print it.

Code:

> rnorm(5, 15, 4)

[1] 10.7649 7.793249 9.953444 13.345904
[2] 17.509668

> am = mean(x)

> am

[1] 11.87345

> cat("Sample mean is =", am)

Sample mean is = 11.87345

> me = median(x)

> me

[1] 10.76499

> cat("Median is =", me)

Median is = 10.76499

> n = 5

> v = (n - 1) * var(x) / n

> v

[1] 11.09965

> sd = sqrt(v)

> sd

[1] 3.33163

> cat("S.D is =", sd)

S.D is = 3.331613

Q4 $X \sim N(30, 100)$, $\sigma = 10$

i $P(X \leq 40)$

ii $P(X > 35)$

iii $P(25 < X < 35)$

iv Find k such that $P(X < k) = 0.6$

> $f_1 = \text{pnorm}(40, 30, 10)$

> f_1

[I] 0.8413447

> $f_2 = 1 - \text{pnorm}(35, 30, 10)$

> f_2

[I] 0.3085375

> $f_3 = \text{pnorm}(25, 30, 10) - \text{pnorm}(35, 30, 10)$

> f_3

[I] -0.3829249

> $f_4 = qnorm(0.6, 30, 10)$

> f_4

[I] 32.53347

Q5 plot the standard normal graph

> $x = \text{seq}(-3, 3, by=0.1)$

> $y = \text{dnorm}(x)$

> $\text{plot}(x, y, xlab = "x values", ylab = "probability", main = "standard normal graph")$

(S)

Practical 5

TOPIC: Normal and t-test.

1. $H_0: \mu = 15 \quad H_1: \mu \neq 15$

Test the hypothesis

Random sample of size 400 is drawn and it is calculated. The sample mean is 14 And S.D is 3 test the hypothesis at 5% level of significance.

$0.05 >$ Accept the value

$0.05 <$ less than Reject.

$\geq m_0 = 15$

$\geq m_x = 14$

$\geq n = 400$

$\geq S_d = 3$

$\geq z_{\text{cal}} = (m_x - m_0) / (S_d / \sqrt{n})$

$\geq z_{\text{cal}}$

≥ -6.66667

~~> Cal C "Calculated value of z is \pm ", z_{cal}~~

~~Calculated value of z is $= -6.66667$~~

$\geq p\text{value} = 2 \times (1 - \text{pnorm}(|z_{\text{cal}}|))$

$\geq p\text{value}$

$[1] 2.616796e-11$

\therefore The value is less than 0.05 we will reject the value of $H_0: \mu = 15$

2) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$

A random sample size of 400 is drawn with sample mean = 10.2 and $S_D = 2.25$

Test the hypothesis at

$\geq m_0 = 10$

$\geq n = 400$

$$m_x = 10.2$$

$$sd = 2.25$$

$$z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$$

50

$$z_{\text{cal}}$$

$$11.7778$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\text{pvalue} *$$

$$0.07544036$$

The value p value is greater than 0.05

∴ The value is accepted.

Test the hypothesis H_0 : proportional of smokers in college is 0.2. A sample is collected and calculated the sample proportional as 0.125 test the hypothesis at 5% level of significance (sample size is 400).

$$p = 0.2$$

$$p = 0.125$$

$$n = 400$$

$$q = 1 - p$$

$$z_{\text{cal}} = (p - p) / (\sqrt{p * q / n})$$

cat ("Calculated value of z is =", zcal)

Calculated value of z is = -3.75

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\text{pvalue}$$

$$0.0001768341 \text{ (Reject)}$$

4) last year farmers lost 20% of their crops. A random sample of 60 fields are selected and it is found that a field crops are insect polluted. Test the hypothesis at 1% level of significance.

$$> p = 0.2$$

$$> P = 0/60$$

$$> n = 60$$

$$> z_{\text{cal}} = (p - P) / (\sqrt{P * Q/n})$$

$$[1] -0.9682458$$

$$> p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p_{\text{value}}$$

$$[1] 0.332216$$

→ The value is 0.1 so value is accepted.

5) Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance

$$> x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$$

$$> n = \text{length}(x)$$

$$> n$$

$$[1] 10$$

$$> mx = \text{mean}(x)$$

$$> mx$$

$$[1] 12.107$$

$$\text{variance} = (n-1) \times \text{var}(\bar{x})/n$$

? variance

? 0.019521

? sd = sqrt(Variance)

? sd

? 0.1397176

? mo = 12.5

$$t = (\bar{x} - mo) / (sd / \sqrt{n})$$

? t

? -8.8949049

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$$

? pvalue

? 0

? The value is less than 0.05 the value is
to accepted.

6

✓

Practical-6

Aim: Large sample test.

1. Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected to test the hypothesis that the population mean is 250 or not on 5% level of significance.
2. In a random sample of 1000 students it is found that 780 use blue pen. Test the hypothesis that the population is 0.8 at 1% level of significance.

1. Solution:

$$H_0 = \mu = 250$$

$$H_1 = \mu \neq 250$$

$$S_d = 30$$

$$n = 100$$

$$Z_{cal} = (M_n - \mu_0) / (S_d / (\sqrt{n}))$$

At calculated value of Z is $= 1, Z_{cal}$

[II] calculated value of Z is $= 8.3333333$

$$P\text{value} = 2 * (1 - \text{norm}(Z_{abs}(Z_{cal})))$$

Pvalue

10

The value is less than 0.05 we will reject the value of $H_0 = H_1 = 250$.

$$\hat{P} = 0.8$$

$$\hat{Q} = 1 - \hat{P}$$

$$\hat{P} = 750 / 1000$$

$$\hat{n} = 1000$$

$$\hat{z}_{\text{real}} = (\hat{P} - p) / (\sqrt{\hat{P} \cdot \hat{Q} / \hat{n}})$$

\hat{z}_{cal} ("Calculated value of z is:", z_{real})

[1] Calculated value of z is: -3.952847

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{real}})))$$

[2] pvalue

$$[3] 7.72268e-05$$

The value is less than 0.01 we reject!

3. To random sample of size 1000 & 2000 are drawn from two population with same SD 2.5 the sample means are 67.5 and 68 Test the hypothesis $H_0: \mu_1 = \mu_2$ at 5% level of significance.

4. A study of noise level in 2 hospital is given below test the claim that 2 hospital have same level of noise at 1% level of significance.

HOS.A

84

61.2

7.9

~~HOS.B~~

34

59.4

7.5

5. In a sample of 600 students it is found 400 used blue ink. In other city from a sample of 900 students 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in two colleges are equal or not at 1% level of significance.

3. do 11

> n1 = 1000 ;

> n2 = 2000

> mx1 = 67.5

> mx2 = 68

> sd1 = 2.5

> sd2 = 2.5

> zcal = $(mx1 - mx2) / \sqrt{((sd1^2/n1) + (sd2^2/n2))}$

> zcal

[1] -5.163778

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 2.417564e-07 \rightarrow Rejected.

4-

> n1 = 84

> n2 = 34

> mx1 = 61.2

> mx2 = 59.4

> sd1 = 7.0

> sd2 = 7.5

> zcal = $(mx1 - mx2) / \sqrt{((sd1^2/n1) + (sd2^2/n2))}$

> zcal

[1] 1.162528

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.2480211

\therefore The value is greater than 0.01 we accept the value.

$H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

> $n_1 = 600$

> $n_2 = 900$

> $P_1 = 400 / 600$

> $P_2 = 450 / 900$

> $p = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$

> p

[1] 0.566067

> $q = 1 - p$

> q

[1] 0.4333333

> $z_{\text{cal}} = (P_1 - P_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

> z_{cal}

[1] p 6.881534

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> $p\text{value}$

[1] $1.75322e^{-10}$

as value is less than 0.01 the value is rejected.

F.2

6 $H_0: p_1 = p_2$ as $H_1: p_1 \neq p_2$

> $n_1 = 200$

> $n_2 = 200$

> $p_1 = 44/200$

> $p_2 = 30/200$

> $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> p

[1] 0.185

> $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * (1 - p) * (1/n_1 + 1/n_2)}$

> z_{cal}

[1] 1.80274

> $P\text{value} = 2 * \text{pnorm}(\text{abs}(z_{\text{cal}}))$

> $P\text{value}$

[1] 0.0714288

∴ Accept : greater than 0.05



Practical - 7

Aim: One Sample test.

1. The marks of 10 students are given by 66, 68, 66, 69, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from the population with average 66.

$$H_0: \bar{M} = 66$$

$\gtreqless x = c(66, 68, 66, 69, 68, 69, 70, 70, 71)$

$\gtreqless t\text{-test}(x)$

One sample - test

data: x

$$t = 68.319, df = 9, p\text{value} = 1.538e^{-13}$$

alternative hypothesis:

True mean is not equal to 0.981 confidence

interval

65.65191

70.14829

Sample estimates

mean of x

67.9

If the p value is less than 0.05 we reject the hypothesis at 5% level of significance.

- Q. Two groups of students scored the following marks. Test the hypothesis that there is no significant difference b/w the 2 groups.

GR1 - 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

GR2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H_0 : There is no difference b/w the 2 groups.

$\gt x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

$\gt y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

$\gt t.test(x, y)$

Watch Two sample t-test.

data : x and y

$t = 2.2593 \quad df = 16.376 \quad p\text{-value} = 0.03798$

alternative hypothesis :

True difference in means is not equal to

0 as percent confidence interval:

0.1628205 5.0371995

sample estimate :

mean of x mean of y .

20.1 17.5

$\gt p\text{-value} = 0.03798$

$\gt \text{if } (\text{pvalue} > 0.05) \& (\text{cat } ("accept h0")) \}$

else $\& (\text{cat } ("reject h0")) \}$

reject H_0 .

(PAIRED = t.test)

The sales data of 6 shops before & after a special campaign are given below:

56

Before : 53, 28, 31, 48, 50, 42

After : 58, 29, 30, 55, 56, 48

Test the hypothesis that the campaign is effective or not.

H_0 : There is no significant difference of sales before & after campaign

$\gt x = c(\text{Before})$

$\gt y = c(\text{After})$

$\gt t\text{-test}(x, y, \text{paired} = T, \text{alternative} = \text{"greater"})$
paired t-test.

data : $x \& y$
 $t = -2.7815$, $df = 5$, $p\text{value} = 0.9806$

Alternative hypothesis

True difference in means is greater than 0
as percent confidence interval :

- 6.085547 inf

sample estimate

mean of the difference

- 3.5

\therefore P value is greater than 0.05, we accept the hypothesis at 5% level of significance.

4) Following are the weights before & after the diet program. Is the diet program effective?

Before : 120, 125, 115, 130, 123, 119.

After : 100, 114, 95, 90, 115, 99

Solⁿ: H_0 : There is no significant difference.

> $x = c(\text{Before})$

> $y = c(\text{After})$

> $t\text{-test}(x, y, \text{paired}=T, \text{alternative} = \text{"less"})$

Paired t-test.

Data : $x \& y$

$t = 4.3458$, $df = 5$, $p\text{value} = 0.9963$

alternative hypothesis : true difference
in means is less than 0

95 percent confidence interval:

- inf & 9.0295

sample estimates :

mean of the differences

19.83333

∴ P value is greater than 0.05 we
accept the hypothesis at 5% level of
significance.

2 medians are applied to two groups of patient respectively.

GR1: 10, 12, 13, 11, 14

GR2: 8, 9, 12, 14, 15, 10, 9

Is there any significance difference b/w 2 medicines?

H_0 : There is no significance difference.

$> x = c(\text{grp1})$

$> y = c(\text{grp2})$

$> t.tst(x, y)$

data : $x \& y$

$t = 0.80384$, $df = 9.7394$, p-value = 0.4406

alternative hypothesis : true difference in means is not equal to 0

95 percent confidence interval

- 0.9698853 4.2981886

~~sample estimates:~~

mean of x

12.0000

mean of y

10.33833

∴ p-value is greater than 0.05 we accept the null hypothesis at 5% level of significance.

88

Practical - 8

Aim: Large and small test.

Questions.

1. The arithmetic mean of a sample of 100 items from a large population is 52. If the standard is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

$$\text{Soln: } H_0: \mu = 55 \quad H_1: \mu \neq 55$$

$$> n = 100$$

$$> m_x = 52$$

$$> m_0 = 55$$

$$> S_d = 7$$

$$z_{\text{cal}} = (m_x - m_0) / (S_d / \sqrt{n})$$

$$> z_{\text{cal}}$$

$$[7] -4.285714$$

$$> p\text{value} = 2 * \text{pnorm}(|z_{\text{cal}}|)$$

$$> p\text{value}$$

$$[7] 1.82153e-05$$

~~∴ The value is less than 0.05 we will reject the value $H_0: \mu = 55$~~

Q2 In a to be exact Tu

$$SOL^n:$$

$$> Q = 1$$

$$> P = 3$$

$$> n = 7$$

$$> z_{\text{cal}}$$

$$[7] 0$$

$$> p\text{value}$$

$$> p\text{value}$$

$$[7] 1$$

∴ The accept

Q3 Thous

2. You find the

$$SOL^n:$$

$$> n_1 =$$

$$> n_2 =$$

$$> p_1 =$$

$$> p_2 =$$

$$> p =$$

$$> p$$

Q2 In a big city 350 out of 700 males are found to be smokers - does the information supports that exactly half of the males in the city are smokers. Test at 1% LOS

$$\text{Soln: } p = 0.5 \quad H_0 : p = 0.5$$

$$> Q = 1 - p$$

$$> p = 350/700$$

$$> n = 700$$

$$z_{\text{cal}} = (p - p) / \sqrt{(p(1-p)/n)}$$

$$> z_{\text{cal}}$$

$$[1] 0$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> pvalue$$

$$[1]$$

∴ The value of 1 is greater than 0.01 we accept the hypothesis.

Q3 Thousand articles from a factory A are found to have 2% defectives, 1500 articles from a 2nd factory B are found to have 1% defective. Test at 5% LOS that the two factories are similar or not.

$$\text{Soln: } H_0 : p_1 = p_2 \text{ as } H_1 : p_1 \neq p_2$$

$$> n_1 = 1000$$

$$> n_2 = 1500$$

$$> p_1 = 0.02$$

$$> p_2 = 0.01$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$[1] 0.014$$

$$> \beta = 1 - p$$

$$> g$$

[7] 0.986

$$> z_{\text{cal}} = (\bar{p}_1 - \bar{p}_2) / \sqrt{\frac{(\bar{p} \times (1 - \bar{p}))}{n_1 + n_2}}$$

$$z_{\text{cal}}$$

[7] 2.084842

$$> p\text{value} = 2 \times (1 - \text{pnorm}(|z_{\text{cal}}|))$$

> pvalue

[7] 0.03708264

∴ pvalue is less than 0.05 we reject the hypothesis.

Q4 A sample of size 400 was drawn at a sample mean 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

$$\rightarrow H_0: \mu = 100$$

$$> m_x = 99$$

$$> m_0 = 100$$

$$> s_d = 8$$

$$> n = 400$$

$$> z_{\text{cal}} = (\bar{m}_x - m_0) / (s_d / \sqrt{n})$$

$$> z_{\text{cal}}$$

[7] -2.5

$$> p\text{value} = 2 \times (1 - \text{pnorm}(|z_{\text{cal}}|))$$

> pvalue

[7] 0.01241923 (reject).

The flower item are selected and the heights are found to (cm) 63, 63, 68, 69, 71, 71, 72, test the hypothesis that the mean height is 66 or not at 1% level.

$$\rightarrow H_0 : \mu = 66$$

$$\rightarrow x = c(63, 63, 68, 69, 71, 71, 72)$$

t -test (n)

One sample t-test.

data : x

$t = 47.94$, df = 6, Pvalue = 5.522e-04

alternative hypothesis : true mean is not equal to 0

as percent confidence interval :

64.66479 71.62092

sample estimates :

means of x

68.14286

∴ Pvalue is ' 0.05 ' less than we reject the hypothesis.

Q. Two random samples were drawn from a normal population and their values are.
A. 66, 67, 75, 76, 82, 84, 88, 90, 92 B- 34, 66,
~~74, 78, 82, 85, 87, 92, 93, 88~~
B- 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97.
Test whether the population have the same variance at 5% los



$$> x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$$
$$> y = c(64, 66, 74, 78, 82, 85, 92, 93, 95, 97)$$

$$H_0: \sigma_1^2 = \sigma_2^2$$

$$> \text{var.test}(x, y)$$

t-test to compare two variance

$$\text{data: } x \& y$$

$$F = 0.63833$$

$$\text{num df} = 8$$

$$\text{denom df} = 9$$

$$\text{Pvalue} = 0.5383$$

alternative hypothesis: True ratio of variance
is not equal to 1:

95 percent confidence interval:
0.1558172 2.781878

sample estimates:

ratio of variance:

$$0.6383349$$

∴ P value is 0.05 we accept the value.

Q7 A company producing light bulbs finds that mean life span of the population of bulb is 1200 hours with SD 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

$$\text{Soln } H_0: \mu = 1200$$

$$\rightarrow \bar{x} = 1150$$

$$\rightarrow \sigma_0 = 1200$$

$$\rightarrow \sigma_d = 125$$

$$\rightarrow n = 100$$

$$\rightarrow z_{\text{cal}} = (\bar{x} - \mu_0) / (\sigma_d / \sqrt{n})$$

$$\rightarrow z_{\text{cal}}$$

$$[1]-11$$

$$\rightarrow p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\rightarrow p\text{value} *$$

$$[1] 63.34288e-05$$

\therefore P value is less than we reject the hypothesis.

Q8 From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% level?

	sample size	No. of bad apples
Consignment 1	200	44
Consignment 2	200	36

Soln $H_0: p_1 = p_2$

$$n_1 = 200$$

$$n_2 = 300$$

$$p_1 = 44/200$$

$$p_2 = 56/300$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$p$$

$$0.2$$

$$q = 1 - p$$

$$z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z_{\text{cal}}$$

$$0.9128709$$

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$p_{\text{value}}$$

$$0.3513104$$

\therefore p-value is less than 0.05 we reject the hypothesis.

Q

18 Practical - 9

Aim: Non-parametric testing of Hypothesis using R-environment.

1. The following data represent earnings (in dollars) for a random sample of five common stocks listed on the New York Stock Exchange. Test whether median earnings is 4 dollars.

Data : 1.68, 3.35, 2.50, 6.23, 3.24

```
> n <- c(1.68, 3.35, 2.50, 6.23, 3.24)
```

```
> n <- length(n);
```

```
> n
```

```
> x > 4;
```

[1] FALSE FALSE FALSE TRUE TRUE

```
> s <- sum(x > 4); s;
```

[1] 1

> binom.test(s, n, p = 0.5, alternative = "greater");
Exact binomial test

Data : s and n

number of success = 1, number of trials = 5,

p-value Alternative hypothesis : true probability of

success = 0.9888 is greater than 0.5,

95 percent confidence interval:

0.01020622 1.000000

Sample estimates :

Probability of success

0.2

2. Tukey after Test

Stu

Scor

Scor

code:

> b <- c(

> a <- c(

> D <- b

> wibor

contin

V =

alter,
the
wa

In

c.

P

The scores of 8 students in reading before and after lesson are as follows:

Test whether there is effect of reading 62

Student NO	1	2	3	4	5	6	7	8
Score before	10	15	16	12	09	07	11	12
Score after	13	16	18	13	09	10	13	10

$\mu_0 < \mu_1$ ($10, 15, 16, 12, 09, 07, 11, 12$)

$\mu_2 < \mu_3$ ($13, 16, 18, 13, 08, 10, 13, 10$)

$H_0 \leftarrow H_0 - a$;

Wilcoxon - Test (H_0 , alternative = "greater")

Wilcoxon signed rank list with continuity correct data: 0

$V = 10.5$, p-value = 0.8722

alternative hypothesis: true location is greater than 0

warning message:

In Wilcoxon. test. default (H_0 , alternative = "greater");

cannot compute exact p-value with ties.

p-value is greater than 0.05 we accept it.

3. The diameter of a ball bearing was measured by 5 inspectors each using two different kinds of calipers. The results were. Test whether average ball bearing for.

Inspector	1	2	3	4	5	6
Caliper 1	0.265	0.268	0.266	0.267	0.269	0.264
Caliper 2	0.263	0.262	0.270	0.261	0.271	0.260

Caliper 1 and caliper 2 are same

Code:

```
>x <- c(0.265, 0.268, 0.266, 0.267, 0.269, 0.264)  
>y <- c(0.263, 0.262, 0.270, 0.261, 0.271, 0.260)  
> wilcox.test(x, y, alternative = 'greater')
```

Wilcoxon rank sum test.

Data: x and y

W = 24, P = 0.197

alternative hypothesis: true location shift is greater than 0

• P-value is greater than 0.05 we accept it.

A office has three electric typewriters A, B and C. In a study of machine usage from time kept record of machine usage rate of seven weeks. Machine C was out of service for two weeks. It is of interest to find out which machine has better usage rate. Analyze the following data on usage rates and determine if there is a significant difference in coverage.

A	B	C
12.3	15.7	32.4
13.4	16.8	41.2
10.3	49.0	35.1
08.0	19.3	28.0
14.6	8.2	03.2
✓	20.1	18.4
26.3		32.5

88

Code:

```
> x <- c(12.8, 15.4, 10.3, 8.0, 14.6);  
> n1 <- length(x)  
> n1  
[1] 5  
> y <- c(15.7, 10.8, 45.0, 12.3, 8.2, 20.1, 26.3);  
> n2 <- length(y).  
> n2  
[1] 7  
> z <- c(32.4, 41.2, 35.1, 25.0, 8.2, 18.4, 32.5).  
> n3 <- length(z)  
> n3  
[1] 7  
> x <- c(x,y,z)  
> g <- c(rep(1,n1), rep(2,n2), rep(3,n3));  
> kruskal.test(x,g)
```

Kruskall-Wallis rank sum test

data : x and g

Kruskall-Wallis Chi-squared = 5.217, df = 2,
p-value = 0.07365.

(8)

∴ P-value is greater than 0.05 we accept it.

Practical-10

Ques: Chi square test & ANOVA

(Analysis of Variance)

61

Use the following data to test whether the condition of child are independent or not.

cond. child	cond. Home	
	clean	dirty
clean	70	50
Fairly clean	80	20
dirty	35	45

H₀: condition of Home & child are independent.

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

	[1,1]	[1,2]
[1,1]	70	50
[2,1]	80	20
[3,1]	35	45

> pv = chisq.test(y)

> pV

Pearson's Chi-squared test

Data

$$\chi^2 = 25.646$$

$$df = 2$$

$$p\text{-value} = 2.698 \times 10^{-6}$$

If they are independent

If p-value is less than 0.05 we reject the hypothesis at 5% level of significance

a) Test the hypothesis that vaccination & disease are independent or not.

Vaccine

Disease	Affected	Not affected
Affected	70	46
Non-affected	35	37

H_0 : Disease & Vaccine are independent

$$> x = c(70, 35, 46, 37)$$

$$> m = 2$$

$$> n = 2$$

$$> y = matrix(x, nrow = m, ncol = n)$$

$$> y$$

	[1]	[2]
[1]	70	46
[2]	35	37

> $p_{\text{v}} = \text{chisq.test}(y)$

> p_{v}
Pearson's chi-squared test with Yate's continuity correction

data: y

χ^2 -square = 2.0275

df = 1

p-value = 0.1845

∴ p-value is more than 0.05 we accept the hypothesis at 5% level of significance.

3) Perform a ANOVA for the following data

TYPE	OBSERVATIONS
A	50, 52
B	53, 55, 53
C	60, 53, 57, 56
D	52, 54, 54, 55

H_0 : The means are equal for A, B, C, D

> $x_1 = c(50, 52)$

> $x_2 = c(53, 55, 53)$

> $x_3 = c(60, 53, 57, 56)$

> $x_4 = c(52, 54, 54, 55)$

> $d = \text{stack}(\text{list}(b1 = x_1, b2 = x_2, b3 = x_3, b4 = x_4))$

> $\text{names}(d)$

[1] "values" "ind"

> $\text{oneway.test}(\text{values} \sim \text{ind}, \text{data} = d, \text{root.equal} = \text{TRUE})$

One-way analysis of means

data: values and ind

$F = 11.785$ df = 3, denom df = 9,

78

7th na,
0J7th OR

$$p\text{value} = 0.00183$$

\because p value is less than 0.05 we reject the hypothesis.

$> \text{anova} = \text{aov}(\text{values} \sim \text{ind_data} - d)$

$> \text{summary(anova)}$

	DF	Sum Sq	Mean Sq	F value	Pr(>F)
ind	3	71.08	23.688	11.73	0.00183*
Residuals	6	18.17	3.029		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*'
 $0.05 \cdot 0.1 \cdot 1$

4 following data gives a life of tire of 4 brands

Type	Life
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

H_0 : The means of A, B, C, D are equal

$> x_1 = C(20, 23, 18, 17, 18, 22, 24)$

$> x_2 = C(B)$

$> x_3 = C(C)$

$> x_4 = C(D)$

$> d = \text{stack}(list(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$

values (d)
"values" "ind"

one-way-test (values ~ ind, data=d, var.equal=T)
one-way analysis of variance

data: values ~ ind.

F = 6.8445 num df = 3 denom df = 20

p-value = 6.002849

: pvalue is less than 0.05 we reject the hypothesis

anova = aov (values ~ ind, data=d)

summary (anova)

	DF	sum Sq	mean Sq	F value	p(C(F))
ind	3	91.44	30.444	6.845	6.002849 **
Residual	20	89.06	4.453		

signif codes : 0 *** 1 .0.001 1 ** 0.01 * 0.05

x = read.csv("C:/Users/Padmaja/Desktop/marksheet.csv")

	Stats	Maths
1	40	60
2	45	68
3	42	47
4	15	20
5	37	25
6	36	27
7	49	57
8	39	58
9	20	25
10	27	27

38
> am = mean (x & stats)

> am

[IJ] 37

> am1 = mean (x & maths)

> am1

[IJ] 39.4

> m1 = median (x & maths)

> m1

[IJ] 38.5

> m2 = median (x & maths)

[IJ] 37

> n = length (x & stats)

> n

[IJ] 10

