Multiple Logistic Regression

```
In [1]: import pandas as pd
    import numpy as np
    import matplotlib as mpl
    import matplotlib.pyplot as plt
    import seaborn as sns

#input balance and income (Float)
#output default (Categorical data)
```

In [2]: tbl=pd.read_excel("Default1.xlsx")
tbl

Out[2]:

	Unnamed: 0	default	student	balance	income
0	1	No	Yes	729.526495	44361.625074
1	2	No	Yes	817.180407	12106.134700
2	3	No	No	1073.549164	31767.138947
3	4	No	No	529.250605	35704.493935
4	5	No	No	785.655883	38463.495879
9995	9996	No	No	711.555020	52992.378914
9996	9997	No	No	757.962918	19660.721768
9997	9998	No	No	845.411989	58636.156984
9998	9999	No	No	1569.009053	36669.112365
9999	10000	No	Yes	200.922183	16862.952321

10000 rows × 5 columns

In [3]: tbl.head()

Out[3]:

	Unnamed: 0	default	student	balance	income
0	1	No	Yes	729.526495	44361.625074
1	2	No	Yes	817.180407	12106.134700
2	3	No	No	1073.549164	31767.138947
3	4	No	No	529.250605	35704.493935
4	5	No	No	785.655883	38463.495879

In [4]: tbl.shape

Out[4]: (10000, 5)

```
In [5]: tbl.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 10000 entries, 0 to 9999
        Data columns (total 5 columns):
              Column
                          Non-Null Count Dtype
              _____
                          -----
         0
             Unnamed: 0 10000 non-null int64
          1
             default
                          10000 non-null object
          2
             student
                          10000 non-null object
          3
             balance
                          10000 non-null float64
         4
                          10000 non-null float64
              income
        dtypes: float64(2), int64(1), object(2)
        memory usage: 390.8+ KB
In [6]: tbl.describe()
Out[6]:
                Unnamed: 0
                               balance
                                           income
               10000.00000
                          10000.000000
                                      10000.000000
         count
          mean
                5000.50000
                            835.374886 33516.981876
           std
                2886.89568
                            483.714985 13336.639563
                              0.000000
           min
                   1.00000
                                        771.967729
          25%
                2500.75000
                            481.731105 21340.462903
          50%
                5000.50000
                            823.636973 34552.644802
          75%
                7500.25000
                            1166.308386 43807.729272
          max 10000.00000
                           2654.322576 73554.233495
In [7]: tbl.isnull().sum
Out[7]: <bound method NDFrame._add_numeric_operations.<locals>.sum of
                                                                               Unname
        d: 0 default student balance income
        0
                    False
                             False
                                      False
                                                False
                                                        False
        1
                    False
                             False
                                      False
                                                False
                                                        False
        2
                    False
                             False
                                      False
                                                False
                                                        False
        3
                    False
                             False
                                      False
                                                False
                                                        False
        4
                    False
                             False
                                      False
                                                False
                                                        False
        9995
                    False
                             False
                                      False
                                                False
                                                        False
        9996
                    False
                             False
                                      False
                                                False
                                                        False
        9997
                    False
                             False
                                      False
                                                False
                                                        False
        9998
                    False
                             False
                                      False
                                                False
                                                        False
                    False
        9999
                             False
                                      False
                                                False
                                                        False
```

Statistical Analysis

[10000 rows x 5 columns]>

```
In [8]: #unique => default value 2 that means Yes or No
    tbl.describe(include='all')
```

Out[8]:

	Unnamed: 0	default	student	balance	income
count	10000.00000	10000	10000	10000.000000	10000.000000
unique	NaN	2	2	NaN	NaN
top	NaN	No	No	NaN	NaN
freq	NaN	9667	7055	NaN	NaN
mean	5000.50000	NaN	NaN	835.374886	33516.981876
std	2886.89568	NaN	NaN	483.714985	13336.639563
min	1.00000	NaN	NaN	0.000000	771.967729
25%	2500.75000	NaN	NaN	481.731105	21340.462903
50%	5000.50000	NaN	NaN	823.636973	34552.644802
75%	7500.25000	NaN	NaN	1166.308386	43807.729272
max	10000.00000	NaN	NaN	2654.322576	73554.233495

Analysis of Zero Values in Predictors

```
In [9]: #499 rows of the balance variable contain is 0 value
     #499 default
     (tbl.balance==0).sum(axis=0)
Out[9]: 499
```

Categorical Variable Analysis

```
In [10]: tbl.student.value_counts()
Out[10]: student
    No     7055
    Yes    2945
    Name: count, dtype: int64
```

Response Variable Analysis

```
In [11]: tbl.default.value_counts()
Out[11]: default
    No    9667
    Yes    333
    Name: count, dtype: int64
```

Encode Categorical Variables

Out[12]:

	Unnamed: 0	default	student	balance	income	default2	student2
0	1	No	Yes	729.526495	44361.625074	0	0
1	2	No	Yes	817.180407	12106.134700	0	0
2	3	No	No	1073.549164	31767.138947	0	1

Graphical Representation

In [14]: tbl_df

Out[14]:

	Unnamed: 0	default	student	balance	income	default2	student2
6702	6703	No	No	512.513526	44178.840504	0	1
4875	4876	No	No	0.000000	37825.221415	0	1
7279	7280	No	No	1074.791401	25715.177454	0	1
758	759	No	Yes	638.691983	18148.301705	0	0
8434	8435	No	No	0.000000	48025.616855	0	1
9912	9913	Yes	No	2148.898454	44309.917173	1	1
9921	9922	Yes	Yes	1627.898323	17546.997016	1	0
9949	9950	Yes	No	1750.253150	51578.940163	1	1
9951	9952	Yes	No	1515.606239	48688.512086	1	1
9978	9979	Yes	No	2202.462395	47287.257108	1	1

1783 rows × 7 columns

```
fig=plt.figure(figsize=(12,5))
In [15]:
          gs=mpl.gridspec.GridSpec(1,4)
          ax1=plt.subplot(gs[0,:2])
          ax2=plt.subplot(gs[0,2:3])
          ax3=plt.subplot(gs[0,3:4])
          ax1.scatter(tbl_df[tbl_df.default=='Yes'].balance,
                        tbl_df[tbl_df.default=='Yes'].income,s=40,c='orange',marker='+
          ax1.scatter(tbl_df[tbl_df.default=='No'].balance,
                        tbl_df[tbl_df.default=='No'].income,s=40,marker='o',linewidths
                        edgecolors='lightblue',facecolors='white',alpha=.6)
          ax1.set_ylim(ymin=0)
          ax1.set_ylabel('Income')
          ax1.set_xlim(xmin=-100)
          ax1.set xlabel('Balance')
          c_palette={'No':'lightblue','Yes':'Orange'}
          sns.boxplot(x='default',y='balance',data=tbl,orient='v',ax=ax2,palette=c_pa
          sns.boxplot(x='default',y='income',data=tbl,orient='v',ax=ax3,palette=c_pal
          gs.tight_layout(plt.gcf())
            70000
                                                                         70000
                                                     2500
            60000
                                                                         60000
                                                     2000
            50000
                                                                         50000
                                                     1500
            40000
                                                                         40000
                                                                         30000
            30000
                                                     1000
            20000
                                                      500
            10000
                            1000
                                  1500
                                        2000
                                              2500
                                                                                  default
```

Logistic Regression Using sklearn

```
In [17]: X_train=tbl.balance.values.reshape(-1,1)
In [18]: y=tbl.default2
In [19]: X_test=np.arange(tbl.balance.min(),tbl.balance.max()).reshape(-1,1)
```

Logistic Regression Using sklearn

```
In [20]: import sklearn.linear_model as skl_lm
```

```
clf=skl_lm.LogisticRegression(solver='newton-cg')
In [21]:
In [22]:
          clf.fit(X_train,y)
Out[22]:
                       LogisticRegression
           LogisticRegression(solver='newton-cg')
In [23]:
          prob=clf.predict_proba(X_test)
In [24]: fig,(ax1,ax2)=plt.subplots(1,2,figsize=(12,5))
          sns.regplot(x=tbl.balance,
                       y=tbl.default2,
                        order=1, ci=None,
                        scatter_kws={'color':'orange'},
                        line_kws={'color':'lightblue','lw':2},
                        ax=ax1)
          ax2.scatter(X_train,y,color='orange')
          ax2.plot(X_test,prob[:,1],color='lightblue')
          for ax in fig.axes:
               ax.hlines(1,xmin=ax.xaxis.get_data_interval()[0],xmax=ax.xaxis.get_data
               ax.hlines(0,xmin=ax.xaxis.get_data_interval()[0],xmax=ax.xaxis.get_data
               ax.set_ylabel('Probability of default')
              ax.set_xlabel('Balance')
              ax.set_yticks([0,0.25,0.5,0.75,1.])
               ax.set_xlim(xmin=-100)
             1.00
                                                      1.00
             0.75
                                                      0.75
                                                    Probability of default
           Probability of default
            0.50
                                                      0.50
             0.25
                                                      0.25
             0.00
                                                      0.00
                      500
                            1000
                                  1500
                                        2000
                                              2500
                                                                500
                                                                     1000
                                                                            1500
                                                                                  2000
                                                                                       2500
                                                                         Balance
In [25]:
          #Print the values of coefficient predicted beta0, beta1 and array of distinc
In [26]:
          print(clf)
          LogisticRegression(solver='newton-cg')
In [27]: print('classes:',clf.classes_)
          classes: [0 1]
```

Logistic Regression (X=Balance) Using statsmodel

```
import statsmodels.api as sm
In [30]:
          import statsmodels.discrete.discrete_model as sms
In [31]: X_train=sm.add_constant(tbl.balance)
          est=sm.Logit(y.ravel(),X_train).fit()
          Optimization terminated successfully.
                    Current function value: 0.079823
                    Iterations 10
In [32]:
          est.summary2().tables[1]
Out[32]:
                       Coef.
                              Std.Err.
                                                        P>|z|
                                                                  [0.025]
                                                                           0.975]
             const -10.651331  0.361169  -29.491287  3.723665e-191  -11.359208
                                                                        -9.943453
                    0.005499 0.000220 24.952404 2.010855e-137
           balance
                                                               0.005067
                                                                         0.005931
```

Logistic Regression (Dummy Variable) Using statsmodel

```
In [34]:
     print(est.summary().tables[1].as_text())
      ______
                                    P>|z|
                coef std err
                                           [0.025
                                                   0.
      9751
      const
              -3.0996 0.091 -34.169 0.000
                                           -3.277
      2.922
              -0.4044 0.115 -3.516
                                    0.000
                                           -0.630
      student2
      0.179
```

Multiple Logistic Regression

Optimization terminated successfully.

Current function value: 0.078577

Iterations 10

```
In [36]: print(est.summary().tables[1])
      _____
                 coef std err
                              z P > |z| [0.025]
                                                    0.
             -11.5158 0.438 -26.299
                                     0.000 -12.374 -1
      const
      0.658
               0.0057
                      0.000
                             24.736
                                     0.000
      balance
                                            0.005
      0.006
            3.033e-06 8.2e-06
      income
                             0.370
                                     0.712 -1.3e-05 1.91
      e-05
               0.6468
                       0.236
                              2.738
                                     0.006
                                             0.184
      student2
```

1.110

```
In [ ]:
```