## Tutorial 4

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91) 
$$T(n) = 3T (n/2) + n^2$$
  
 $T(n) = aT(n/6) + f(n^2)$   
 $a > 1, b > 1$   
On compairing  
 $a = 3, b = 2, f(n) = n^2$   
Now,  $C = lag = lag = 2 = 1.584$   
 $n^2 = n^{1.584} \le n^2$   
 $f(n) > n^2$   
 $f(n) > n^2$   
 $f(n) > n^2$   
 $f(n) = 0(n^2)$ 

93) 
$$T(n): T(n/2) + 2^n$$
 $A = 1$ 
 $b = 2$ 
 $f(n): 2^n$ 
 $c \cdot \log a \cdot \log c = 0$ 
 $h^c : h^c = 1$ 
 $f(n) > h^c$ 
 $T(n): \theta(2^n)$ 

95) 
$$T(n) = 16T(n/4) + n$$
 $A = 16, b = 4$ 
 $f(n) = n$ 
 $C = \log 16 = \log (4)^2 = 2\log 4$ 
 $= 2^{16} = n^2$ 
 $f(n) < n = n^2$ 

$$T(n)=2T(n/2)+n \log n$$

$$\rightarrow a=2, b=2$$

$$f(n)=n \log n$$

$$C=\log 2=1$$

$$n'=n'=n$$

$$n \log n > n$$

$$f(n) > n^{c}$$

$$T(n) > n^{c}$$

$$T(n) = 0 (n \log n)$$

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97) T(n): 2T(n/2) + n/lagn
 → a=2, b:2, f(m): n/legn
   C. lag 2 . 1
   ncinis n
 <u>n</u> < n
· + (n) < n°
 · · T(n) = 8(n)
98) T(n)=2T(n/4)+ n000
→ a.2, b.4, f(n): no.51
    C = leg a = leg 2 = 0.5
  nos < no.81
    f(n)>nc
   .. T(n) = 0 (nº 51)
39) T(n)2 0.5 T(n/2)+1/n
- a=0.5, b=2
   a 1/1 but here a is 0.5
 so me cannet apply Master's
 Theorem.
g10) T(n)= 16T(n/4)+n!
-> a=16, b=4, f(n)=n!
 · · · C = lag a z lag 16 2 2
     n^c = n^2
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As n/ > n2

·. T(n) = 0(n!)

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911) 4T(n/2) + lag n
-, a=4, b=e, f(n)=lagn
    C = laga · laga · 2

ne · ne
    {(n). lagn
: lagn < n=
        *(m)<n°
      T(n): 0(nc)
            * 0 (n2)
Q12) T(n) = Agrt (n) T(n/2) + logn
  , a: In, b:2
  C: lago a · lago Tu · 1 lagon
· - 1 leg_n < leg (n)
· + (n)>nc
   T(n)= 0 (f(n))
         = 0 (/leg (n))
(13) T(n)=3T(n/2)+n
 ) a=3; b=2; f(n)=n
  C = lag a = lag 3 = 1.5849
     n< n1.5842
ラ f(n) くno
     T(n)= 0 (n 1.5841)
Q14) T(n) = 3T(n/3) + sqrt(n)
\rightarrow a=3, b=3
  C = leg a = leg 3 = 1
    n^{c} = n^{2} = n
 A sgut (n) < n
     f(n) < nc
     T(n) = 0 (n)
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\$15) 
$$T(n) : 4T(n/2) + n$$
 $\rightarrow \quad 0 : 4, b : 2$ 
 $C : lag a = lag : 2$ 
 $h^{c} = n^{2}$ 
 $n < n^{2}$  (for any constant)

 $f(n) < n^{c}$ 
 $f(n) = 0 (n^{2})$ 

916) 
$$T(n)=3T(n/4)+n \log n$$
  
 $\rightarrow a=3,b=4, f(n)=n \log n$   
 $C=\log_b a=\log_4 3=0.792$   
 $n^c \cdot n^{0.792}$   
 $n^{0.792} < n \log n$   
 $T(n)=0 (n \log n)$ 

$$g_{17}$$
)  $T(n)=3T(n/3)+n/2$   
 $\rightarrow a=3;b=3$   
 $c=laga-lag_3=1$   
 $f(n)=n/2$   
 $n^c=n'=n$   
 $A=n/2  
 $f(n)$$ 

:. T(n)=0(n)

$$g_{18}$$
)  $T(n) = GT(n/3) + n^{2} lagn$   
 $\rightarrow a = G; b = 3$   
 $C = lag_{b}a = lag_{5}G = 1.6309$ 

$$n^{c} = n^{1.6301}$$
  
As  $n^{1.6301} \le n^{2} \log n$   
 $\therefore T(n) \ge 0 (n^{2} \log n)$ 

$$g_{19}$$
)  $T(n)=4T(n)$   $\frac{1}{n}$   $\frac$ 

$$\begin{array}{l}
g20) T(n) = 64 T(n/8) - n^{2} lagn \\
\longrightarrow 0 = 64 b \cdot 8 \\
C = laga = lag 64 = lag (8)^{2} \\
C = 2 \\
N^{c} = n^{2} \\
\therefore n^{2} lagn > n^{2} \\
T(n) = 0 (n^{2} lagn)
\end{array}$$

$$\begin{array}{c} g_{21} \\ T(n) = 7T(n/3) + n^2 \\ \rightarrow a = 7; b = 3; f(n) = n^2 \\ C = lag_b a = lag_3 7 = 1.7712 \\ n^c = n^{1.7712} \\ n^{1.7712} < n^2 \\ T(n) = 0(n^2) \end{array}$$

$$\frac{g_{22}}{\Delta = 1, b \cdot 2} + n (2-(asn))$$

$$\frac{c}{\Delta = 1, b \cdot 2}$$

$$\frac$$