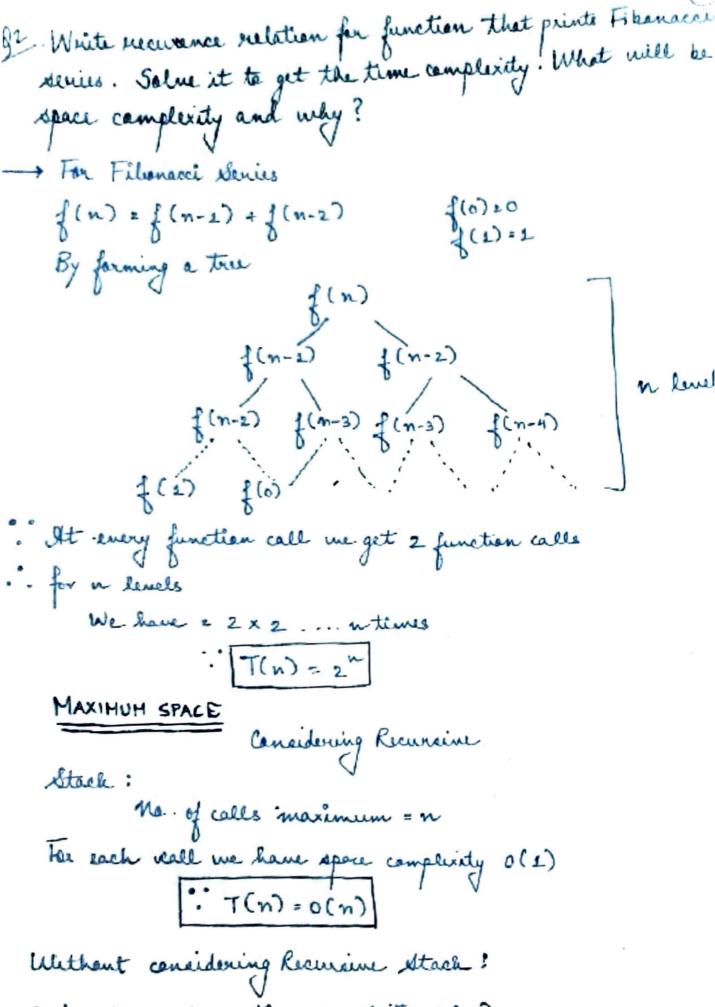
Tutorial 2

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Void fun ( int n)
   int j=1, i=0; while (i(n) {
  i+=j;
j++;
for (i)
 · m (m+1) <n
      m & Jn
        => 1+1+...+ In times
         T(n) = In - Ans
```



each call me have time complexity O(1)

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93.
  Write pregrams which have complexity:
   n (lag n), n', lag (lag n)
 1) negn - Juich sant
        Vaid quickant (int aur (), int law, int high)
              if ( law < high)
                ant pi = partition (avr, low, high);
queckeant (arr, low, pi-1);
               ginckent ( av, pi + 1, high);
    int partition (int arr [], int law, int high)
              int pinet = avr[high];
               int i = ( law - 1);
         for ( int j = lane; j (= high -1; j++)
                 of (arr(i) < pinet)
                     sur ( davr [i], davr [j]);
            suap (& are [i+1], & are [high]);
                 return (i+1);
2) n3 -> Multiplication of 2 square matrix
         for (i=0; i<n1; i++) {
            for (j=0; j < c=; j++)
                   for ( h = 0; h < c1; h++)
                          MECLICITY = a CITCH] * bCK] (j);
```

gh. Salue the following recurrence relation $T(n) = T(n/4) + T(n/2) + cn^2$

$$T(n/a) \qquad T(n/2 \rightarrow 1$$

$$T(n/s) \qquad T(n/a) \qquad T(n/s) \rightarrow 2$$

At level

$$0 \to Cn^{2}$$

$$1 \to \frac{n^{2}}{4^{2}} + \frac{n^{2}}{2^{2}} = \frac{C5n^{2}}{16}$$

$$2 \to \frac{n^{2}}{8^{2}} + \frac{n^{2}}{16^{2}} + \frac{n^{2}}{4^{2}} + \frac{n^{2}}{8^{2}} = \left(\frac{5}{16}\right)^{2}n^{2}C$$

$$\vdots$$

$$\max \text{ level} = \frac{n}{2^{k}} = 1$$

$$T(n) = c \left(\frac{n^2 + \left(\frac{5}{16} \right) n^2 + \left(\frac{5}{16} \right)^2 n^2 + \dots + \left(\frac{5}{16} \right)^2 \log n}{n^2} \right)$$

$$T(n) = C n^2 \left[1 + \left(\frac{5}{16} \right) + \left(\frac{5}{16} \right)^2 + \dots + \left(\frac{5}{16} \right)^2 \log n}{1 + \left(\frac{5}{16} \right)^4 \log n} \right]$$

$$T(n) = C n^2 \times 1 \times \left(\frac{1 - \left(\frac{5}{16} \right)^4 \log^4 n}{1 - \left(\frac{5}{16} \right)^6} \right)$$

```
of What is the time complexity of following funt??
                 int fun (int n) {
                  for Cint Los; i con; L++) [
                    for ( int j = 1; j < n ; j ++1) {
                      11 Some O(L) task
               3 33
                                                          j= (n-1)/i-times
          £ (n-1)
       T(n) = (\frac{n-1}{1}) + (\frac{n-1}{2}) + (\frac{n-1}{2}) + \cdots + (\frac{n-1}{n})
      T(n) = n[1+1/2+1/3+...+1/n] - 1×[1+1/2+1/3+..+/n]
               2 n lagn-lagn
                   T(n)=O(nlagn) -> Ohs.
go What should be time camplexity of
for ( int i=2, i <= n; i = pow(i, k))
                    11 Some 0(1)
        where he is a constant

i

2<sup>1</sup>

2<sup>k</sup>

2<sup>k</sup>

2<sup>k</sup>

2<sup>k</sup>

2<sup>k</sup>

2<sup>k</sup>
                                         2 km < = n
                                          km z legzn
                                            m = lag h lag n
                 · £ 1
```

T(n) = O (lag x lag n) -Ans.

It Write a recurrence relation when quick sort repeatedly divide array into 2 parts of 99% and 1%. Denice time complexity in this case. Show the recurrence true while deriving time complexity Ef find difference in heighte of both extreme points. What do you understand by this analysis? " (given algorithm divides away in 99%, and 1%, part $T(n) = \{T(n-1) + o(1)\}$ n-1 2 "n" work is done at each level T(n) = (T (n-1) + T (n-2) + + T(1) + O(1) xn T(n) = 0 (n2) highest height = 2 difference = n-2 n/1 The given algorithm produces linear result

a) n and following in increasing order of nate of granth: a) n, n1, lagn, laylagn, meet (n), lag(n!), n lagn, lag2(n), 2, 22, 4, n2, 100 100 < lag lag n < lag n < (lag n) 2 < Jn < n < n lag n < lag (n!) < n² < b) 2 (2 n), 4 n, 2 n, 1, leg (n), leg (leg (n)), They (n), leg 2 n, 2 leg (n), n leg (n), n!, ne, nleg (n) 2 < lag lagn < Jlagn < lagn < lag 2 n < 2 lag n < n lag n < n lag n < lag n < n lag c) g²n, leg_(n), nleg_(n), nleg_2(n), leg(n!), n!, leg_s(n), 94, 812, $796 < lag_{1}n < lag_{2}n < 5n < n lag_{6}n) < n lag_{2}n < lag_{1}) < .8n^{2}$ $7n^{3} < n! < 8^{2}n$