# New oxides of the filled-Ti<sub>2</sub>Ni type structure

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#### Abstract

The metal atom ordering and oxygen occupancy of four compounds of the filled-Ti<sub>2</sub>Ni type structure have been determined by single-crystal X-ray diffraction studies. Three additional phases have been identified and indexed from powder X-ray diffraction data. All the phases crystallize in space group  $Fd\bar{3}m$  with the following compositions:  $Zr_4Ni_2O$  (a=12.1970(9) Å),  $Zr_6Ni_4Ti_2O_{0.6}$  (a=12.0299(9) Å),  $Nb_6Ni_6O$  (a=11.2117(5) Å), and  $Nb_6Ni_4Ta_2O_2$  (a=11.5813(3) Å). Phases identified using powder data are  $Nb_4Ni_2O$  (a=11.5933(3) Å),  $Zr_4Cu_2O$  (a=12.2659(7) Å), and  $Zr_6Co_4Ti_2O$  (a=11.8649(9) Å). A comparison of the structures and oxygen occupancies is presented, as well as tentative explanations based on results of extended Hückel calculations. The role of interstitial oxygen as an electron acceptor and its effect on metal-metal bonding are considered.

#### 1. Introduction

The  $Ti_2Ni$ , the filled- $Ti_2Ni$ , and the related  $\eta$  carbide type structures have been known for some time [1]. Much of the earlier work revealed the variety of combinations of metals for which this structure forms. The simplicity of the formula conceals the subtleties and complexities in the chemistry of these phases. It is a frequently found structure of binary intermetallics of stoichiometry A<sub>2</sub>B [2]. Many of these binary intermetallics can incorporate light interstitial atoms. Many more phases form only in the presence of these interstitial atoms, commonly C [3–6], N [7–9], O [10–12], and even H [13]. A review of the literature and list of reported phases suggests that there is no general explanation for the variability in compositions and there is no known correlation of interstitial atom site occupancy and metal:metal ratio. Although much of the work was done a number of years ago, significant recent reports in the literature prompt further investigation of these phases [6, 9, 12-14]. Many reports are based on X-ray powder diffraction data, with the inherent difficulty in refining parameters for light interstitial elements. Some neutron diffraction work has been reported [6, 14, 15]. No single-crystal work has been previously reported for any of these interstitial stabilized phases. Presumably this is because of the difficulty in forming single crystals suitable for diffraction experiments. The crystals examined here were all very small, and the successful refinements were possible because of the high X-ray beam intensity from a diffractometer with a rotating anode X-ray generator.

The filled-Ti<sub>2</sub>Ni type structure crystallizes in space group  $Fd\bar{3}m$ , and the unit cell contains 96 metal atoms. Adopting the notation of Newsam et al. [6], the general formula for the oxides is written  $M_6^f M_4^e M_2^d O_5^e O_1^a$ . The superscript letters are those of the Wyckoff symbol for the crystallographic site occupied by the superscripted atoms. The subscripts are based on the unit cell formula with Z=8. For a ternary compound  $M^f$  and  $M^e$  are different transition metals, and Md may be the same as either M<sup>f</sup> or M<sup>e</sup>, depending on the system being considered. The transition metal M<sup>f</sup> is always to the left of the M<sup>e</sup> metal atom in the periodic table. When the f and d sites are occupied by the same metal the metal:metal ratio is 8:4, or 2:1. When the e and d sites are occupied by the same metal the metal:metal ratio is 6:6, or 1:1. No mixing on the M<sup>d</sup> site has been observed. Oxygen is reported to occupy either the 16c site, in which it fills distorted octahedra, or the 8a site, filling regular octahedra.

The structure of the large cubic unit cell has been described in the literature in two general schemes. In the first scheme, the cell is built up of alternating subunits, as depicted in Fig. 1. The octahedra of M<sup>c</sup> and tetrahedra of M<sup>c</sup> atoms are outlined. The oxygen atoms can be seen in Fig. 1(a) between the outlined octahedra. This is a distorted octahedral site, sharing opposite faces with the regular octahedra. The M<sup>d</sup> metal atoms can be seen in Fig. 1(b) capping the faces of the M<sup>c</sup> tetrahedra. The second scheme describes the structure in terms of two interpenetrating networks, as depicted in Fig. 2. Figure 2(a) illustrates a network of face-sharing octahedra which alternately share two and

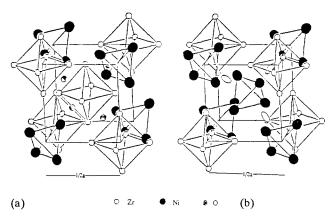


Fig. 1. View of individual subunits making up the unit cell of  $Zr_4Ni_2O$ : (a) Subunit centered by zirconium octahedron; (b) subunit centered by nickel tetrahedron.

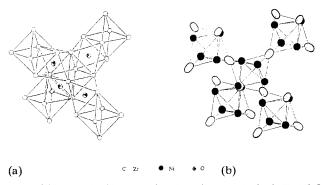


Fig. 2. (a) Network of face-sharing zirconium octahedra in  $Zr_4Ni_2O$ . Shaded octahedra are centered by oxygen, unshaded octahedra are empty. (b) Network of stellae quadrangulae in  $Zr_4Ni_2O$ . Nickel tetrahedra are shaded.

four faces. The octahedra shown are alternately centered by oxygen and empty. The face-sharing octahedra form rings made up of 12 octahedra. The void spaces within and between these rings are filled by an interpenetrating network of corner-sharing stellae quadrangulae (Fig. 2(b)) [16, 17].

## 2. Experimental details

All chemicals were used as they were received from the supplier, except as noted below: Zr (0.25 mm foil, Alfa Products, 99.9%); Zr (-20 to +60 mesh, Johnson Matthey, 99.9%); Ti (Ames Laboratory); ZrO<sub>2</sub> (Johnson Matthey Puratronic, 99.9975%); NiO (Johnson Matthey Puratronic, 99.998%); Nb (-325 mesh, Alfa Products, 99.8%); Ta (60 mesh, Johnson Matthey, 99.98%); Ni (foil, Inco, 99.99%); Ni (powder, Fisher Scientific, purified); Cu (ribbons, J.T. Baker Chemical Co., 99.98%); Co (pieces, Alfa, 99.5%); NaClO<sub>4</sub> (GFS Chemical Co., 99%). Ni received from Inco was arc melted under argon, and rolled into a foil. Analysis was carried out after this treatment. The foils were cleaned in acid solutions to remove surface oxides prior to their use.

Samples were prepared by two general techniques. The first technique consisted of arc melting the metals and the oxide of either zirconium or nickel. The samples were then annealed under vacuum in an induction furnace. This technique often resulted in a mixture of phases. ZrO<sub>2</sub> was always present as a minor phase in the zirconium compounds. Other minor phases present in various samples were Zr<sub>3</sub>NiO and the oxygen-stabilized cubic Laves phase, ZrNi<sub>2</sub>O<sub>x</sub> [18]. Apparently, the Laves phase has a low melting point (less than 1000 °C) and the presence of this phase masks the refractory nature of this family of compounds. Samples free of this phase remained solid when annealed at 1250-1275 °C. Samples containing niobium all had NbO as a minor phase, and some also had Nb<sub>7</sub>Ni<sub>6</sub> present. The desired phase was present on annealing at temperatures as low as 1000 °C, but most samples were annealed at 1250 °C. The melting point of Nb<sub>7</sub>Ni<sub>6</sub> is 1290 °C.

A second method was used successfully for the preparation of a nearly single-phase sample of Zr<sub>4</sub>Ni<sub>2</sub>O. Only the two strongest lines of ZrO<sub>2</sub> were barely visible in the powder X-ray diffraction pattern of this phase. A sample of Zr and Ni was arc melted, as before, and then ground to small pieces. The metal and an appropriate amount of oxidizing agent, NaClO<sub>4</sub>, were sealed in an evacuated fused silica tube. On heating to 600 °C for 4 days in a tube furnace the perchlorate decomposed, and crystals of NaCl formed at the cool end of the tube. The resulting oxide was crushed to a fine powder and pressed into a pellet before annealing as before.

X-ray powder diffraction techniques were used to identify the phases present, and to determine accurate lattice parameters. Powder diffraction films were obtained using a vacuum Guinier camera FR552 (Enraf-Nonius, Delft, the Netherlands) with Cu  $K\alpha_1$  radiation. Lattice parameters were determined by a least-squares refinement of indexed line positions calibrated by an internal silicon standard (NIST).

Single-crystal X-ray diffraction data collection was carried out on a Rigaku AFC6R diffractometer, with Mo K $\alpha$  radiation ( $\lambda$ =0.710 69 Å). The structures were solved by direct methods and refined using the shells [19] and Texsan [20] software packages. All crystals were refined in space group Fd3m. Details of crystal data are listed in Table 1.

A Quantum Design superconducting quantum interference device magnetometer was used to check for superconductivity and to measure magnetic behavior at a field of 3 T over the temperature range 6–298 K.

Elemental analysis of the zirconium nickel oxides by energy-dispersive spectroscopy (EDS) was performed on a JEOL JSM-840 electron microscope.

TABLE 1. Single-crystal data of new filled-Ti<sub>2</sub>Ni type phases

Formula	$Zr_4Ni_2O$	$Zr_6Ni_4Ti_2O_{0.6}$	$Nb_6Ni_6O$	$Nb_6Ni_4Ta_2O_2$
a (Å)	12.1970(9)	12.0299(9)	11.2117(5)	11.5813(3)
$V(\mathring{A}^3)$	1814.5(4)	1740.9(4)	1409.3(2)	1553.4(1)
Z	16	8	8	8
$d_{\rm calc}$ (g cm <sup>-3</sup> )	7.295	6.747	8.742	10.390
Crystal size ( $\mu$ m <sup>3</sup> )	$40\times50\times70$	$50 \times 50 \times 100$	$40 \times 40 \times 40$	$30\times40\times50$
$\mu(\text{Mo K}\alpha) \text{ (cm}^{-1})$	167	169	246	494
Data collection range $2\theta$ (deg)	0-60	055	0-55	0-60
Number of reflections measured	768	579	482	1253
Number of unique data, total with $F_0^2 > 3\sigma(F_0^2)$	112	87	79	101
Number of parameters refined	13	15	11	15
Transmission factor ratio (maximum:minimum)	1.116	1.168	1.146	1.179
R <sup>a</sup>	0.020	0.029	0.017	0.022
$R_{\mathbf{w}}^{\ b}$	0.024	0.031	0.023	0.029
GOF <sup>c</sup>	1.019	0.995	0.980	1.026
Largest peak (e Å <sup>-3</sup> )	1.59	1.20	0.88	1.54
Largest negative peak (e Å <sup>-3</sup> )	-1.17	- 1.31	-1.04	-3.19

 $<sup>{}^{</sup>a}R = \Sigma ||F_{o}| - |F_{c}||/\Sigma |F_{o}|.$ 

#### 3. Results

Interest in the Ti<sub>2</sub>Ni-type structures arose from a study of the interstitially stabilized intermetallic phases that form in the Zr-Ni system [21-23]. Two experimental results deserved attention. First, previous work on the Zr-Ni-O phase diagram in an intentional search for this cubic phase indicated that it does not exist in equilibrium at 950 °C [24]. It does exist, however, at 1275 °C, the annealing temperature used in these experiments. This is thus an example of a high temperature solid phase which decomposes at lower temperature, in this case probably to Zr<sub>3</sub>NiO and Ni. Second, there was a noticeable shift in lattice parameters for this phase in several of the samples, as observed in the films of the powder diffraction patterns taken on a Guinier camera. A single crystal was chosen from both a sample with the larger lattice parameter and a sample with the smaller lattice parameter. The results for the data refinement of the larger cell correspond to the data reported for Zr<sub>4</sub>Ni<sub>2</sub>O in Table 2. The preliminary solution for the smaller cell was also based on a Zr-Ni-O ternary system, and required Ni vacancies on the 16d site for a suitable refinement, giving a stoichiometry of Zr<sub>6</sub>Ni<sub>6-r</sub>O. This solution was corrected when elemental analysis by EDS revealed the presence of titanium, which could be detected in samples prepared with a zirconium starting material which unexpectedly contained significant amounts of titanium Placing Ti in the 16d site in the structure solution improved the refinement significantly, and the final refinement showed full occupancy on all the metal sites. The results for  $Zr_6Ni_4Ti_2O_{0.6}$  are also in Table 2. Efforts to synthesize a compound of stoichiometry  $Zr_6Ni_6O$ , without titanium, were unsuccessful.

A systematic check for a solid solution between Zr<sub>4</sub>Ni<sub>2</sub>O and Ti<sub>4</sub>Ni<sub>2</sub>O was not performed, but, for low concentrations of titanium, the titanium preferentially substitutes on the 16d site. Furthermore, the oxygen partially occupies both interstitial sites in the sample containing titanium, with total oxygen occupancy given by the formula Zr<sub>6</sub>Ni<sub>4</sub>Ti<sub>2</sub>O<sub>0.6</sub>. The refinement was carried out considering the following possible solutions: Zr<sub>6</sub>Ni<sub>4</sub>Ti (no oxygen), Zr<sub>6</sub>Ni<sub>4</sub>Ti<sub>2</sub>O<sub>1-x</sub> (variable oxygen occupancy on the 8a site only), Zr<sub>6</sub>Ni<sub>4</sub>Ti<sub>2</sub>O<sub>2-x</sub> (variable oxygen occupancy on the 16c site only), and Zr<sub>6</sub>Ni<sub>4</sub>Ti<sub>2</sub>O<sub>3-x</sub> (variable oxygen occupancy on both the 8a and the 16c sites). By careful comparison of each of the refinement solutions, according to Hamilton's test [26], the solution with both sites partially occupied is correct with a 95% level of confidence.

Conflicting reports exist for the  $Zr_4Co_2O$  phase. Nevitt and Downey [24] did not find this phase in determining the 950 °C isothermal section of this ternary system. Holleck and Thümmler [8] include  $Zr_4Co_2O$  (a=12.18 Å) in a list of phases observed. This phase did not form in samples annealed at 1100 °C. However, it was observed to form at this temperature in samples prepared with the titanium-contaminated zirconium. By analogy with the substitution of Ti in  $Zr_4Ni_2O$ , this is formulated as  $Zr_6Co_4Ti_2O$  (a=11.8649(9) Å), with undetermined oxygen occupancy.

 $<sup>{}^{</sup>b}R_{w} = [\Sigma w(|F_{o}| - |F_{c}|)^{2}/\Sigma w|F_{o}|^{2}]^{1/2}; \ w = 1/\sigma^{2}(|F_{o}|).$ 

<sup>&</sup>lt;sup>c</sup>GOF =  $(\Sigma(|F_o| - |F_c|)/\sigma_i)/(N_{\text{obs refl}} - N_{\text{parameters}})$ .

TABLE 2. Final atomic parameters from single-crystal refinement

Atom	Site	x	у	z	$B_{\rm eq}  (\mathring{\rm A}^2)^{ \rm a}$
$Zr_4Ni_2O$	)				
Zr1	48f	0.18517(8)	0.0	0.0	0.51(1)
Ni	32e	0.8396(1)	0.8396	0.8396	1.2716(5)
Zr2	16d	0.625	0.625	0.625	1.5990(5)
$O_{\mathfrak{p}}$	16c	0.125	0.125	0.125	0.562(2)
Zr <sub>6</sub> Ni <sub>4</sub> T	$i_2O_{0.6}$				
Zr	48 <b>f</b>	0.1901(1)	0.0	0.0	0.73(4)
Ni	32e	0.8326(2)	0.8326	0.8326	1.1795(7)
Ti	16d	0.625	0.625	0.625	1.430(1)
$O_c$	16c	0.125	0.125	0.125	1.17(3)
$O_{\mathfrak{c}}$	8a	0.0	0.0	0.0	0.98(3)
Nb <sub>6</sub> Ni <sub>6</sub>	9				
Nb	48f	0.1996(1)	0.0	0.0	0.47(2)
Ni1	32e	0.8317(1)	0.8317	0.8317	0.3289(4)
Ni2	16d	0.625	0.625	0.625	0.4602(6)
$O_{\mathfrak{p}}$	8a	0.0	0.0	0.0	0.497(4)
Nb <sub>6</sub> Ni₄	$Ta_2O_2$				
$Nb^d$	48 <b>f</b>	0.1867(1)	0.0	0.0	0.48(4)
Ni	32e	0.8311(1)	0.8311	0.8311	0.422(1)
Tae	16d	0:625	0.625	0.625	0.3491(6)
$O_{\mathfrak{p}}$	16c	0.125	0.125	0.125	1.154(5)
Idealize	d metal	positions <sup>f</sup>			
M1	48f	0.1875	0.0	0.0	
M2	32e	0.8250	0.8250	0.8250	

 $<sup>{}^{*}</sup>B_{eq} = \frac{8\pi^{2}}{3} \sum_{1}^{3} \sum_{1}^{3} U_{ij} a_{i}^{*} a_{j}^{*} \vec{a}_{i} \vec{a}_{j}.$ 

The results of electronic structure calculations on Zr<sub>4</sub>Ni<sub>2</sub>O indicated the presence of empty bonding orbitals. This suggested the possibility of adding electrons to the system by substituting copper for nickel or niobium for zirconium. The synthesis of both Zr<sub>4</sub>Cu<sub>2</sub>O and Zr<sub>6</sub>Cu<sub>6</sub>O was attempted at temperatures between 900 and 1100 °C. With the Zr:Cu starting ratio of 2:1, the powder pattern indicated the presence of the desired phase as well as binary Zr<sub>2</sub>Cu as a minor phase. When the starting Zr:Cu ratio was 1:1 the products were the cubic phase and the binary Zr<sub>3</sub>Cu<sub>8</sub>. The lattice parameters of the Ti<sub>2</sub>Ni-type phase differed only slightly in all the samples made. For the nearly single-phase sample made with a 2:1 starting metal ratio, a = 12.2659(7) Å. The smallest cell edge measured for the cubic phase with the 1:1 starting ratio was a = 12.2615(6) Å. This leads to the conclusion there is only the one phase, Zr<sub>4</sub>Cu<sub>2</sub>O, with perhaps a slightly varying oxygen content accounting for the differences in observed cell lengths. Characterization of these phases was performed by Xray powder diffraction photographs. The oxygen is assumed to occupy the 16c site. A significant shortening in the unit cell is observed when Ti is added to form  $Zr_6Cu_4Ti_2O$  (a = 12.16(2) Å).

The existence of the two distinct phases in the Nb-Ni-O system reported previously is confirmed [8]. This contrasts with the Nb-Ni-C system for which only the Nb<sub>4</sub>Ni<sub>2</sub>C phase is noted in the 1100 °C isotherm of the ternary phase diagram [27]. Single-crystal X-ray diffraction data for  $Nb_6Ni_6O$  (a = 11.2117(5) Å) were used to determine oxygen occupancy in this phase which had been reported as  $Nb_3Ni_3O$  (a = 11.20 Å)  $Nb_4Ni_2O$  has lattice parameter a = 11.5933(3) Å (pre viously reported with  $a = 11.58 \,\text{Å}$ ). Comparison of oxygen occupancies in the Nb-Ni-O samples is incomplete because single crystals of Nb<sub>4</sub>Ni<sub>2</sub>O have not been found. The difference in lattice parameters clearly indicates the existence of two distinct phases. Samples of the oxides have been prepared which contain both phases in an equilibrium mixture. The existence of the two distinct phases emphasizes that the 16d site is occupied entirely either by niobium or by nickel, but not by both in a solid solution on this metal site.

Ta<sub>4</sub>Ni<sub>2</sub>O is reported by Holleck and Thümmler [8]. Kotyk and Stadelmaier [7] find that this phase only exists with nitrogen present, as either Ta<sub>4</sub>Ni<sub>2</sub>N or the mixed Ta<sub>4</sub>Ni<sub>2</sub>(O,N), but not as the pure oxide. Efforts to synthesize both Ta<sub>4</sub>Ni<sub>2</sub>O and Ta<sub>6</sub>Ni<sub>6</sub>O, annealing at temperatures between 1430 and 1550 °C, resulted in mixtures of binary phases. However, noting the effect of titanium in the zirconium compounds, the synthesis of mixed Ta-Nb compounds was attempted. Both of the starting compositions Ta<sub>6</sub>Ni<sub>4</sub>Nb<sub>2</sub>O<sub>2</sub> and Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub> were tried. Only the latter formed the cubic phase, at 1550 °C, with (Ta,Nb)<sub>7</sub>Ni<sub>6</sub> present as a minor phase. A single crystal was selected for study by X-ray diffraction. A  $\psi$  scan suitable for absorption correction in the refinement process was not collected. As an empirical absorption correction (DIFABS) did not improve the refinement, no correction was applied in the final refinement. The Nb and Ta occupancies were allowed to vary in the final steps of the refineresulting in a final stoichiometry  $(Nb_{0.82}Ta_{0.18})_6Ni_4(Ta_{0.61}Nb_{0.39})_2O_2$ , or  $Nb_{5.7}Ni_4Ta_{2.3}O_2$ .

Crystal data for all the single-crystal refinements are listed in Table 1. Positional and thermal parameters for the four single-crystal refinements are listed in Table 2. Interatomic distances are shown in Table 3. Table 4 summarizes all of the phases identified in this study and corresponding lattice parameters. Anisotropic displacement parameters and structure factor tables are available in the supplementary material.

Zr<sub>4</sub>Ni<sub>2</sub>O, Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>, Nb<sub>4</sub>Ni<sub>2</sub>O, and Nb<sub>6</sub>Ni<sub>6</sub>O were checked for superconductivity down to 6 K. No transition was observed. Magnetic measurements of the Zr<sub>4</sub>Ni<sub>2</sub>O and Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub> phases from 6 to 298 K at a field

<sup>&</sup>lt;sup>b</sup>Refined with full oxygen occupancy.

<sup>&</sup>lt;sup>c</sup>Refinement of the oxygen occupancy gave results of the 16c site being 18(6)% occupied and the 8a site 24(6)% occupied. <sup>d</sup>Refined with mixed Nb–Ta occupancy: Nb, 82(2)%; Ta, 18(2)%. <sup>e</sup>Refined with mixed Ta–Nb occupancy: Ta, 61(3)%; Nb, 39(3)%. <sup>f</sup>From ref. 25.

TABLE 3. Interatomic distances in new filled-Ti<sub>2</sub>Ni type phases

	$Zr_4Ni_2O$	$Zr_6Ni_4Ti_2O$	Nb <sub>6</sub> Ni <sub>6</sub> O	Nb <sub>6</sub> Ti <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>
M1*-O1 ×1		2.287(2)	2.238(1)	
$O2 \times 2$	2.2776(7)	2.266(2)		2.162(1)
$Ni \times 2$	2.7832(9)	2.861(2)	2.691(1)	2.774(1)
$Ni \times 2$	3.152(1)	3.075(2)	2.773(1)	2.9912(6)
$M2 \times 2$	3.164(1)	3.078(1)	2.7920(8)	2.999(1)
$M1 \times 4$	3.194(1)	3.175(1)	2.915(1)	3.058(1)
$M1 \times 4$	3.248(1)	3.234(1)	3.165(1)	3.075(1)
Ni–M2 ×3	2.688(1)	2.600(1)	2.4170(6)	2.4928(6)
$Ni \times 3$	3.0910(9)	2.811(5)	2.591(1)	2.657(1)
$M1 \times 3$	2.7832(9)	2.861(2)	2.691(1)	2.774(1)
$M1 \times 3$	3.152(1)	3.075(2)	2.773(1)	2.999(1)
$O1 \times 1$	_	3.488(3)	3.268(2)	_
$O2 \times 3$	3.534(1)	3.590(2)	_	3.388(1)
$M2^b$ –Ni ×6	2.6878(8)	2.600(1)	2.4170(6)	2.4928(6)
$M1 \times 6$	3.164(1)	3.078(1)	2.7920(8)	2.9912(6)
$O1^c$ – $M1 \times 6$	_	2.287(2)	2.238(1)	_
$Ni \times 4$	_	3.488(3)	3.268(2)	***
$O2^{d}-M1 \times 6$	2.2776(7)	2.266(2)	_ `´	2.162(1)
Ni ×6	3.534(1)	3.590(2)		3.388(1)

 $<sup>^{</sup>a}M1 = Zr$  or Nb in 48f.

TABLE 4. Lattice parameters for all new filled-Ti<sub>2</sub>Ni type phases found

Composition	a (Å)	
Zr <sub>4</sub> Cu <sub>2</sub> O	12.2659(7)	
Zr <sub>4</sub> Ni <sub>2</sub> O	12.1970(9)	
$Zr_6Ni_4Ti_2O_{0.6}$	12.0299(9)	
Zr <sub>6</sub> Co <sub>4</sub> Ti <sub>2</sub> O	11.8649(9)	
Nb <sub>4</sub> Ni <sub>2</sub> O	11.5933(3)	
Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>	11.5813(3)	
Nb <sub>6</sub> Ni <sub>6</sub> O	11.2117(5)	

of 3 T show that they are both paramagnetic. The latter sample contained approximately 10% of an impurity phase of the Nb<sub>7</sub>Ni<sub>6</sub> type. No magnetic measurements of Nb<sub>7</sub>Ni<sub>6</sub> or Ta<sub>7</sub>Ni<sub>6</sub> have been reported, and it is possible this phase is paramagnetic also.

## 4. Electronic structure calculations

Electronic structure calculations were carried out on the  $Zr_4Ni_2O$  phase. Calculations were also performed on  $Nb_6Ni_6O$  in an attempt to correlate the oxygen ordering with the metal ratios. The calculations were of the extended Hückel type using the tight binding approximation. The atomic parameters used for the calculations are listed in Table 5. The valence state ionization potentials  $H_{ii}$  for the metals were obtained

TABLE 5. Atomic parameters used for extended Hückel cal-

Atom	Orbital	$H_{ii}$ (eV)	$\zeta_1^a$	$\zeta_2^{\mathfrak{u}}$	$c_1^b$	$c_2^{h}$
Zr	4d 5s 5p	-6.72 -7.06 -3.68	3.84 1.82 1.78	1.505	0.6213	0.5798
Ni	3d 4s 4p	-8.43 -6.76 -3.03	5.75 1.925 1.925	2.20	0.5817	0.5800
О	2s 2p	- 32.3 - 14.8	2.275 2.275			

<sup>&</sup>lt;sup>a</sup>Exponent in the double ζ function for d orbitals.

<sup>&</sup>lt;sup>b</sup>Coefficients to exponential terms.

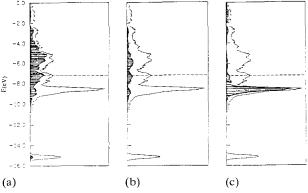


Fig. 3. Projection of individual atomic contributions on total DOS for  $Zr_4Ni_2O$ : (a) projection of Zr1 on total DOS; (b) projection of Zr2 on total DOS; (c) projection of Ni on total DOS.

from a charge iteration calculation on the binary Zr<sub>2</sub>Ni, Al<sub>2</sub>Cu-type structure. Other parameters were taken from previous work [28–32].

General features of the density of states (DOS) plots of Zr<sub>4</sub>Ni<sub>2</sub>O can be seen in Fig. 3, which shows the projection of the contribution of the metal atoms to the total DOS. Figure 3(a) shows the projection of the Zr1 atoms on the total DOS. These are the zirconium atoms which make up the network of face-sharing octahedra. The oxygen atoms center an alternating set of these octahedra, and the mixing of zirconium with the oxygen p band is seen at low energy. The broad band at higher energy has principally zirconium d character. Figure 3(b) similarly shows the broad d band of the zirconium atoms occupying the M<sup>d</sup> site. Figure 3(c) shows the narrow nickel d band, with nickel character extending up through the conduction band to higher energy. The Fermi level indicated by the broken line is in the middle of the conduction band. In all the calculations, the Zr1 atoms were placed on the "idealized" atom position [25], making all octahedral sites equal in size to avoid biasing the results and favoring a site for oxygen occupancy dependent on size

 $<sup>{}^{</sup>b}M2=Zr$ , Ti, Ni, or Ta in 16d.

 $<sup>^{</sup>c}O1 = O$  in 8a.

 $<sup>^{</sup>d}O2 = O$  in 16 c.

factors. The nickel position was shifted to be between the observed atom position and the "idealized" atom position.

Table 6 compares the effect on the Fermi energies and total energies of adding oxygen to the hypothetical cubic binary; first to the sixteenfold site, as observed in the single-crystal refinement, and then to the other possible octahedral site, an eightfold site. The bottom row of Table 6 is the total energy gain per oxygen atom added to the system. That is to say, the formation of Zr<sub>4</sub>Ni<sub>2</sub>O by adding oxygen to Zr<sub>4</sub>Ni<sub>2</sub> decreases the total energy of the system from -1225.62 eV to -1775.43 eV, or by -549.81 eV. There are four oxygen atoms in the primitive unit cell, so the energy change per oxygen atom is one-fourth the total change, or -137.45 eV. By comparing the change per oxygen atom, the results of adding different amounts of oxygen can be compared. The table shows the two results differ by only 0.31 eV per oxygen atom. The calculated preferred ordering is in favor of the observed result, but it is doubtful whether the difference is significant within the errors of the calculations associated with the approximations of the extended Hückel method.

The results of the single-crystal refinement of Nb<sub>6</sub>Ni<sub>6</sub>O show that the oxygen can occupy the eightfold site in the structure. Not only is the oxygen occupancy in this compound different from that in Zr<sub>4</sub>Ni<sub>2</sub>O, but the metal:metal ratio is also different. Calculations were performed on the compound Nb<sub>6</sub>Ni<sub>6</sub>O, using for niobium the zirconium parameters from the charge iteration. Table 7 lists the energies associated with each of these phases with different amounts of oxygen. The changes in energy per oxygen atom are such that the observed phase is again favored, but by only 0.15 eV. In addition to the uncertainty within the calculations, the calculations do not allow for non-stoichiometry, or partial filling of the sites. If only half of the sixteenfold sites are occupied by oxygen, the stoichiometry is the same as for the observed phase, Nb<sub>6</sub>Ni<sub>6</sub>O. For the calculation

TABLE 6. Fermi energy and total energy of calculated phases

	Zr <sub>4</sub> Ni <sub>2</sub>	Zr <sub>4</sub> Ni <sub>2</sub> O <sub>1/2</sub>	Zr <sub>4</sub> Ni <sub>2</sub> O
Fermi energy $E_{\rm F}$ (eV) Total energy $E_{\rm T}$ (eV) $\Delta E_{\rm T}$ (oxygen atom)	-7.242 -1225.62	- 7.212 - 1499.91 - 137.14	-7.205 -1775.43 -137.45

TABLE 7. Fermi energy and total energy of calculated phases

	Nb <sub>6</sub> Ni <sub>6</sub>	Nb <sub>6</sub> Ni <sub>6</sub> O	Nb <sub>6</sub> Ni <sub>6</sub> O <sub>2</sub>
Fermi energy $E_F$ (eV) Total energy $E_T$ (eV) $\Delta E_T$ (oxygen atom)	-7.087 -1515.37	- 7.027 - 1789.10 - 136.86	-6.817 -2062.22 -136.71

TABLE 8. Overlap populations for Zr<sub>4</sub>Ni<sub>2</sub>O

Atomic interaction	Overlap population	Interatomic distance (Å)
Zr2-Zr1	0.1646	3.12
Zr1-Ni	0.1347	2.76
Zr1-O	0.1089	2.27
Zr2-Ni	0.1014	2.67
Zr1-Zr1	0.0980	3.21
Zr1-Ni	0.0412	3.10

of this phase, then, two of the four oxygen sites were filled, and the other two were empty. The total energy for this phase was -1789.01 eV, resulting in a stabilization of -136.82 eV per oxygen atom. This is different by only 0.04 eV from the calculated energy for the observed structure. These results suggest that the important consideration may not be which site is occupied, but the amount of oxygen the system requires for maximum stabilization.

It should be noted that when O atoms are added to both binary intermetallics, the calculated Fermi energies rise. In general, the valence orbitals of main group interstitial atoms interact with bonding orbitals within early transition metal and rare earth clusters [33]. These levels occur at the bottom of the conduction band in intermetallic solids. The O interstitials, through their orbital interactions, push some of these cluster bonding levels to high energy, and we observe slight increases in the position of the Fermi level. In terms of chemical bonding ideas, these intermetallics gain electronic energy by forming metal-interstitial bonds at the expense of metal-metal bonds in the cluster.

Crystal orbital overlap population (COOP) curves were calculated for the interactions in  $Zr_4Ni_2O$ . The calculated overlap populations are tabulated in Table 8, appropriately weighted to reflect the number of each symmetry unique bond. Nickel-nickel overlap population was very low, ca. 0.001, and is not included in the table. Each of the COOP curves for metal-metal interactions shows empty bonding orbitals above the Fermi level. The only indication of antibonding character at the Fermi level was in the COOP curve for Zr1-O interactions. As mentioned previously the calculation of empty bonding levels was the motivation for the synthesis of more electron-rich compounds than  $Zr_4Ni_2O$ .

## 5. Discussion

The Ti<sub>2</sub>Ni-type structure has been described in terms of two interpenetrating three-dimensional networks made of idealized octahedra and tetrahedra [25]. With

the idealized parameters listed in Table 2, M1 is at (x, 0, 0) with x = 0.1875, and all the face-sharing octahedra are exactly the same size. When x deviates from this value the octahedral centred at an 8a site maintain ideal octahedral symmetry, but the other octahedra, centered at a 16c site, lose their fourfold symmetry, and become distorted octahedra, or, more precisely, trigonal antiprisms. The direction of the deviation of x from ideality appears to be related to the oxygen occupancy. The octahedra, regular or distorted, centered by oxygen are expanded. When oxygen occupies the 8a site, at the origin, the expansion of the regular octahedra corresponds to an increased value for x (compare  $Nb_6Ni_6O$ , with x = 0.1996, and x=0.1875). Occupancy of the 16c site causes expansion of the distorted octahedra, or trigonal antiprisms, and a corresponding decrease in x (compare x = 0.1852 in  $Zr_4Ni_2O$  and x=0.1867 in  $Nb_6Ti_4Ta_2O_2$ , with ideal x=0.1875). The expansion of the oxygen-centered octahedra can be interpreted as resulting from the filled antibonding metal-oxygen orbitals, as calculated in the COOP curves. There appears to be a correlation of metal atom position with interstitial site occupancy. This is a useful crystal-chemical correlation, given the inherent difficulty of refining light atom positions by X-ray diffraction techniques. For example, this suggests a reinvestigation of a recent report of Mo<sub>3</sub>Fe<sub>3</sub>N [9]. The positional parameters for the molybdenum suggest that the nitrogen occupies the 8a site, with the corresponding formula Mo<sub>6</sub>Fe<sub>6</sub>N.

Interpenetrating the octahedral network is another network made of corner-sharing stellae quadrangulae. In the compounds studied here the central tetrahedron is always made of Ni, on the 32e site, and the other atoms are the metals on the 16d site, which cap the faces of the Ni<sub>4</sub> tetrahedra. None of these tetrahedra is centered by interstitial atoms. Hyde and Andersson list the idealized position for the metal atom as x = 0.4250[25]. This has been converted to the alternate but equivalent value of 0.8250 for comparison with the refinement results. The refined Ni atom positions on the 32e site vary from x = 0.8311 to x = 0.8396. The effect of increasing the x parameter is to enlarge the central nickel tetrahedron. A look at the distances in Table 3 shows these units are far from regular stellae quadrangulae. In all cases the central Ni<sub>4</sub> tetrahedron is expanded  $(d_{N_i-N_i}>d_{N_i-M_2})$ .  $Zr_4Ni_2O$  exhibits the largest departure from ideality. For the ideal structural arrangement of this compound,  $d_{Ni-Ni} = 2.5873$  Å. The observed distance is much larger,  $d_{Ni-Ni} = 3.0910$  Å. In elemental nickel  $d_{N_i-N_i} = 2.4916 \text{ Å}$ . The distance between the tetrahedral nickel atoms and the zirconium atoms in the octahedral network consequently decreases considerably from the ideal. Compare the observed  $d_{Zr_1-N_1}=2.783$  Å in  $Zr_4Ni_2O$  with the

 $d_{\text{Zr1-Ni}}$  = 3.0224 Å. This expansion of the Ni<sub>4</sub> tetrahedron suggests that Ni-Ni interactions are weaker, relative to Zr-Ni interactions, than would be the case in the idealized structure. This suggests that the visual description of the structure in terms of two interpenetrating networks does not accurately portray the chemical interaction between the two networks. The icosahedral units around the M2 atoms at the 16d sites are exactly the bonding connections between the two networks [9, 34]. The interactions between the two interpenetrating networks are as important as the interactions within a network.

Periodic equipotential surfaces and periodic zero potential surfaces have been calculated for this space group [35]. The potential surfaces of appropriate coulombic fields are very similar in shape to minimal surfaces, but can be correlated to the spatial distribution of the electrons, and hence correlated to physical properties. For the Ti<sub>2</sub>Ni structure the potential surface resides between the two interpenetrating networks. One can assume that the most weakly bound electrons are located closest to the potential surface. In a metal, these are the conduction electrons. This view of potential surfaces in no way contradicts the finding here of significant interaction between the two structural networks.

It is interesting to note some structural similarities with other phases here. A two-dimensional analogue to the three-dimensional network of face-sharing zirconium octahedra is seen in both the  $\kappa$  phase [22] and the new  $Zr_6Ni_6TiSiO_{1.8}$  structure [23]. In each case, rings of twelve face-sharing zirconium octahedra form. In the case of all three of these structures, icosahedral units fill the void spaces and link the octahedral networks.

The results of this study can be rationalized in a system-by-system manner. In the Nb-Ni-O system the two phases Nb<sub>4</sub>Ni<sub>2</sub>O and Nb<sub>6</sub>Ni<sub>6</sub>O occur. This occurrence was not observed in the Zr-Ni-O system. The phase diagrams of the binary intermetallic Zr-Ni and Nb-Ni systems are very different. In the Nb-Ni binary system there are only two compounds, NbNi<sub>3</sub> and Nb<sub>7</sub>Ni<sub>6</sub>, which compete with formation of the ternary oxide. In neither case is the Nb:Ni ratio 1:1 or 2:1. The binary intermetallics in the Zr–Ni system, especially ZrNi, compete more favorably with the formation of the ternary oxide. One can consider the role of oxygen in stabilizing the Ti<sub>2</sub>Ni-type structure in the Zr<sub>4</sub>Ni<sub>2</sub>O phase. The oxygen is also necessary in the formation of the Hf<sub>4</sub>Ni<sub>2</sub>O phase [7], but is not necessary for Ti<sub>2</sub>Ni. A principal difference between titanium on the one hand, and zirconium and hafnium on the other, is the orbital expansion of the d orbitals for zirconium and hafnium and the corresponding increase in metal-metal bond strength. Compare, for example, the heats of

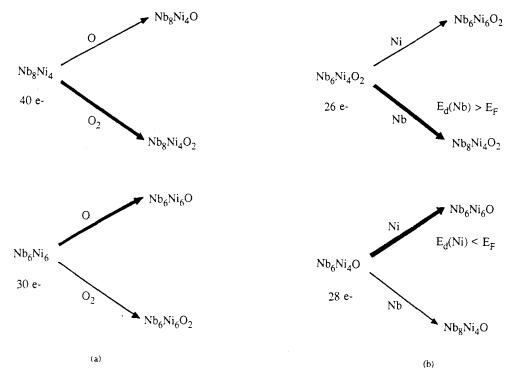


Fig. 4. (a) Addition of oxygen to hypothetical metal framework follows path shown by bold arrows. (b) Addition of capping metal atoms to core compounds follows path shown by bold arrows.

formation of the gaseous atoms at 0 K, which may be regarded as a measure of the cohesive energy of the metals. For Ti,  $\Delta H_f^{\,o}(0 \text{ K}) = 111.65 \text{ kcal mol}^{-1}$ , and the values for Zr and Hf are 145.19 kcal mol<sup>-1</sup> and 147.92 kcal mol<sup>-1</sup> respectively [36]. The phases in the Zr-Ni system are different from those in the Ti-Ni system because the bonding energies of zirconium and titanium differ. Specifically Zr<sub>2</sub>Ni and Ti<sub>2</sub>Ni crystallize with different structures. When oxygen is added to Zr<sub>2</sub>Ni, zirconium-oxygen bonds form at the expense of the zirconium-metal bonds. This decrease in metal-metal bonding makes Zr-Ni more like the Ti-Ni system, and the filled-Ti<sub>2</sub>Ni phase in the Zr-Ni-O system is stabilized with respect to the binary phases.

The oxygen occupancy in the Nb<sub>4</sub>Ni<sub>2</sub>O phase has not been determined experimentally, but is based on the assumption that the oxygen occupancy in this phase is the same as for Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>. The two phases Nb<sub>6</sub>Ni<sub>6</sub>O and Nb<sub>4</sub>Ni<sub>2</sub>O have different Nb:Ni ratios and different oxygen contents. The band calculations on Nb<sub>6</sub>Ni<sub>6</sub>O suggest the ordering of the oxygen may not be as important as the total amount of oxygen present. Figure 4(a) outlines the possibility of adding different amounts of oxygen to metal frameworks with different Nb:Ni ratios. With reference to the DOS curve in Fig. 3, the electrons in the sharp Ni d peak are strongly localized. The electrons occupying the Zr d, s and p bands, and Ni s and p bands, are more delocalized. The core metal framework with the greater number of delocalized

electrons in the conduction band will favor adding more oxygen, which acts as an electron sink, nominally forming O<sup>2-</sup>. Nb<sub>8</sub>Ni<sub>4</sub> contains 40 delocalized electrons per formula unit, and Nb<sub>6</sub>Ni<sub>6</sub> has 30 electrons. Thus Nb<sub>8</sub>Ni<sub>4</sub> will add more oxygen atoms per formula unit than Nb<sub>6</sub>Ni<sub>6</sub> to form Nb<sub>8</sub>Ni<sub>4</sub>O<sub>2</sub> and Nb<sub>6</sub>Ni<sub>6</sub>O respectively.

The same conclusion is reached if the oxygen ordering is assumed to determine the metal ratios, rather than the metal ratios determining the oxygen ordering as described above. In this case, the two core compounds with different oxygen contents, Nb<sub>6</sub>Ni<sub>4</sub>O and Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub>, can add either niobium or nickel to the 16d site (Fig. 4(b)). Nb<sub>6</sub>Ni<sub>4</sub>O has 28 delocalized electrons in its conduction band, and Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub> has 26. Since Nb<sub>6</sub>Ni<sub>4</sub>O is more electron rich it will more readily add nickel, for which atomic orbitals lie lower in energy than the Fermi level and will act as electron acceptors, than gain electrons by adding niobium to form Nb<sub>6</sub>Ni<sub>6</sub>O. Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub>, with fewer delocalized electrons, will favor the addition of niobium, for which the orbitals lie above the Fermi energy and will act as electron donors to form Nb<sub>8</sub>Ni<sub>4</sub>O<sub>2</sub>, or Nb<sub>4</sub>Ni<sub>2</sub>O. While this explanation is internally consistent in that the same conclusion is reached whether the oxygen content is considered to determine the metal occupancy, or the metal ratios determine the oxygen content, it does not explain the formation of phases such as Mo<sub>6</sub>Co<sub>6</sub>C and Mo<sub>6</sub>Co<sub>6</sub>C<sub>2</sub> where both possible orderings of interstitials are observed for a single metal ratio [6].

The formation of only Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>, and no other tantalum-containing compounds, can be explained on the basis of work on mixed niobium-tantalum sulfides performed previously in this laboratory [16, 17]. In these sulfides, the formation of certain phases depends on the relative strengths of metal-sulfur bonds and metal-metal bonds. The same interplay between metal-oxygen and metal-metal bonds exists in these oxide phases. Generally speaking, Ta-O bonds are stronger than Nb-O bonds, by electronegativity arguments. Also, Ta-M bonding among transition metals is generally stronger than Nb-M bonds in a given structure, because of greater d orbital extension and overlap of 5d transition metals. In the Ti<sub>2</sub>Ni-type structure one must consider the balance between the M-O and the M-M bonding. In Nb<sub>4</sub>Ni<sub>2</sub>O the oxygen is surrounded by niobium in the 48f site, forming Nb<sub>6</sub>O octahedra. The other niobium atom has only other metal atoms as neighbors; it is icosahedrally coordinated to six nickel and six niobium atoms. When tantalum replaces niobium in the 16d site, oxygen still is coordinated to only niobium, but now the presence of tantalum increases the metal-metal interactions in the structure. If, however, tantalum were to replace the other niobium atoms, the stronger Ta-O bonds would come at the expense of the Ta-M bond strength, shifting the balance of metal-oxygen vs. metal-metal bond strength, and the phase is unstable with respect to formation of the binary phases.

## 6. Conclusions

Structural determination of these new phases by single-crystal X-ray diffraction techniques gives evidence for three different orderings of the interstitial oxygen. Zr<sub>4</sub>Ni<sub>2</sub>O and Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub> contain oxygen in the 16c site. Nb<sub>6</sub>Ni<sub>6</sub>O contains oxygen in the 8a site. The oxygen in Zr<sub>6</sub>Ni<sub>4</sub>Ti<sub>2</sub>O<sub>0.6</sub> partially occupies both the 8a and the 16c sites. The octahedral site around oxygen is expanded, and this is noted in a shift of the positional parameter of the Zr or Nb atom on the 48f site. This correlation is very useful, as powder X-ray diffraction is better able to determine metal atom positions than to distinguish between possible interstitial site occupancies. The metal atoms in the quaternary compounds selectively occupy unique sites.

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## Supplementary material available

Anisotropic displacement parameters (1 page) and a listing of structure factor data (4 pages) are available from the authors.

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