

## Arrays

### Definition:

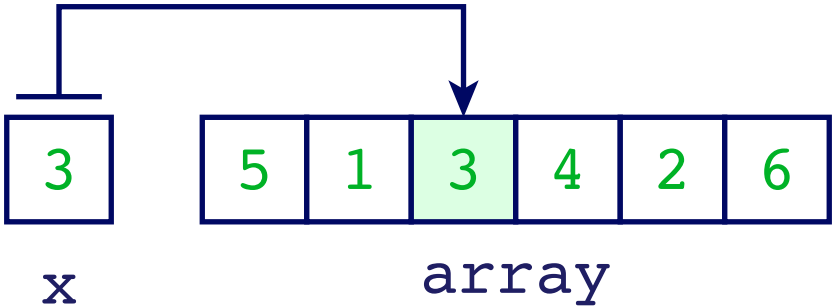
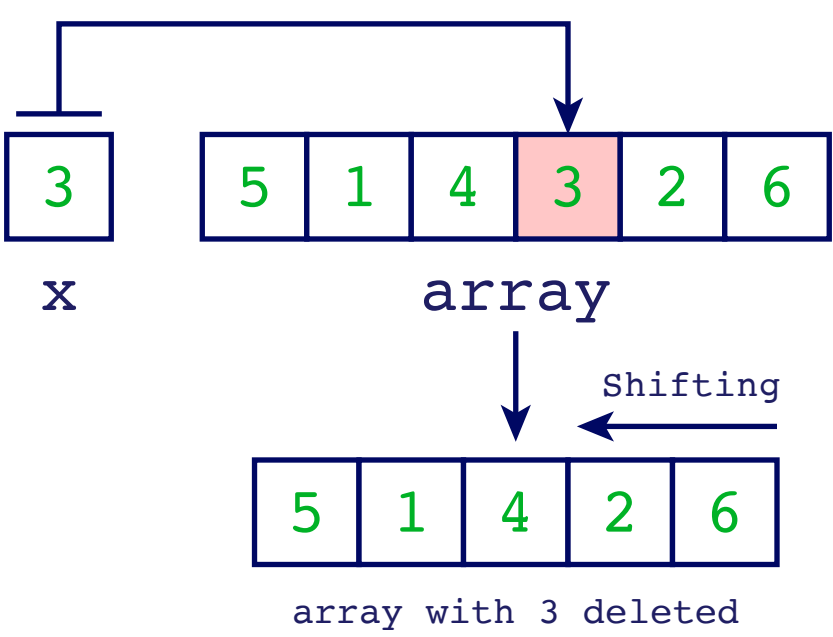
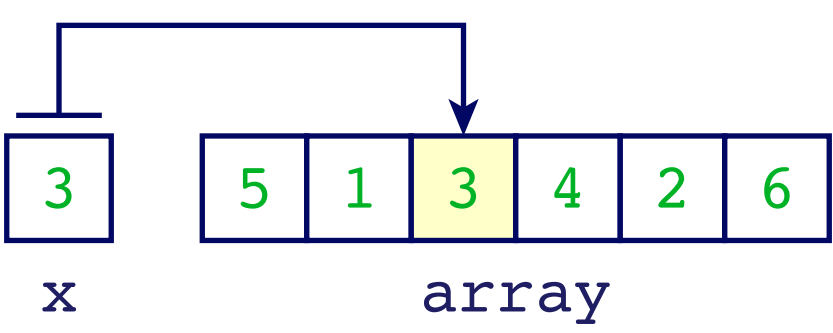
It is a data structure consisting of a collection of elements at contiguous memory locations, each identified by an index.

Elements	5	1	4	2	6
Indexes	0	1	2	3	4

### Key concepts:

- **Indexing:** Elements can be accessed using their index
- **Memory allocation:** Contiguous block of memory

### Common operations:

Operation	Example	Time Complexity (worst-case)
Insertion		O(n)
Deletion		O(n)
Search		O(n)

### Application:

- **Dynamic Programming**—Store intermediate results to avoid redundant calculations, improving efficiency

### Pros:

- **Quick access:** O(1) time complexity for accessing elements by index
- **Predictable memory use:** Fixed size makes memory management easy

### Cons:

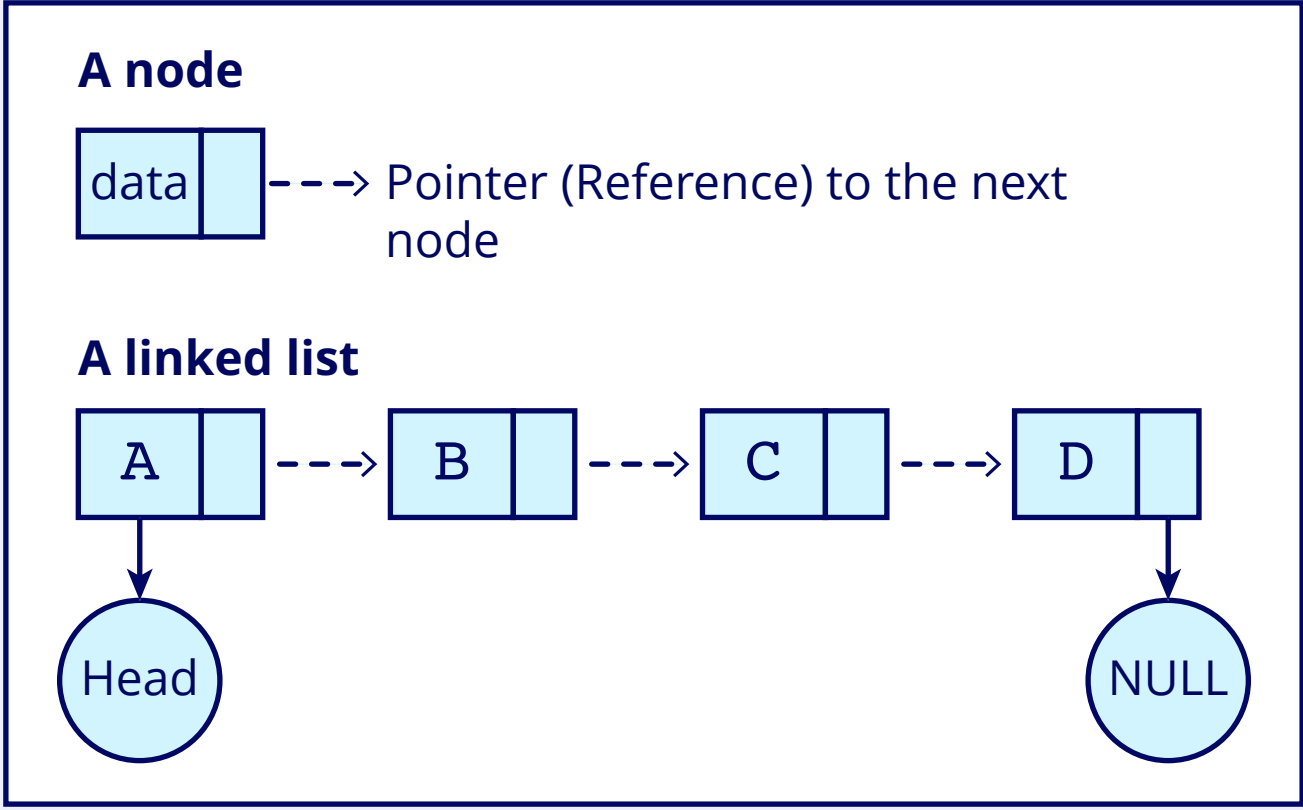
- **Fixed size:** Specifying size at the time of creation leads to potentially wasted or insufficient space
- **Expensive insertion/deletion:** Inserting or deleting elements (except at the end) requires shifting elements, resulting in O(n) time complexity

## Linked List (Singly, Doubly)

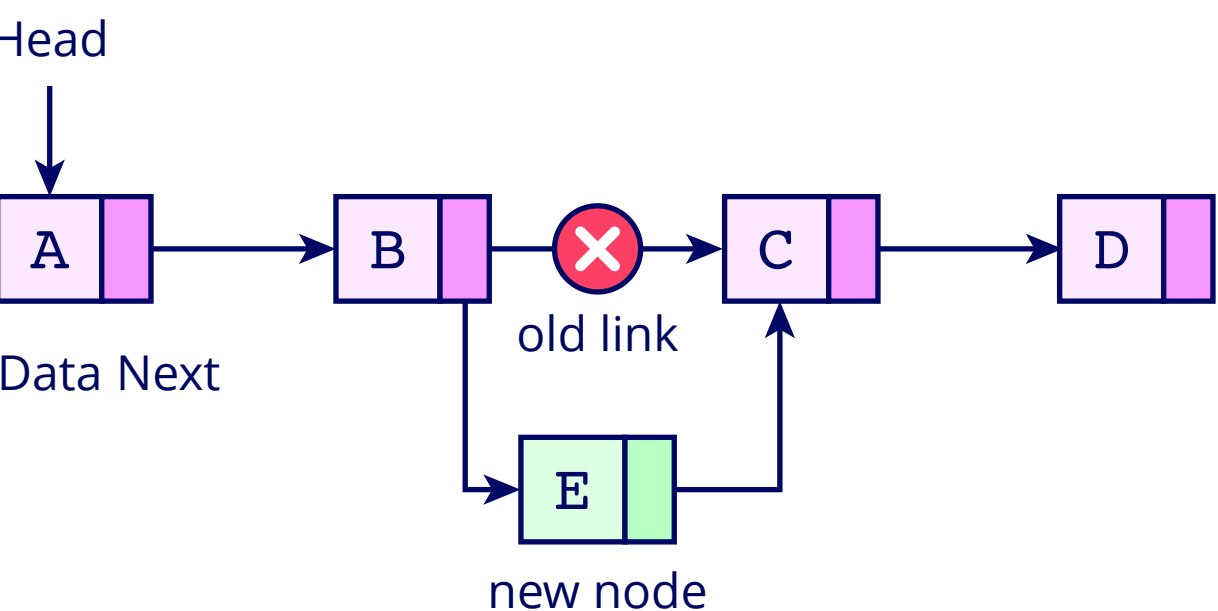
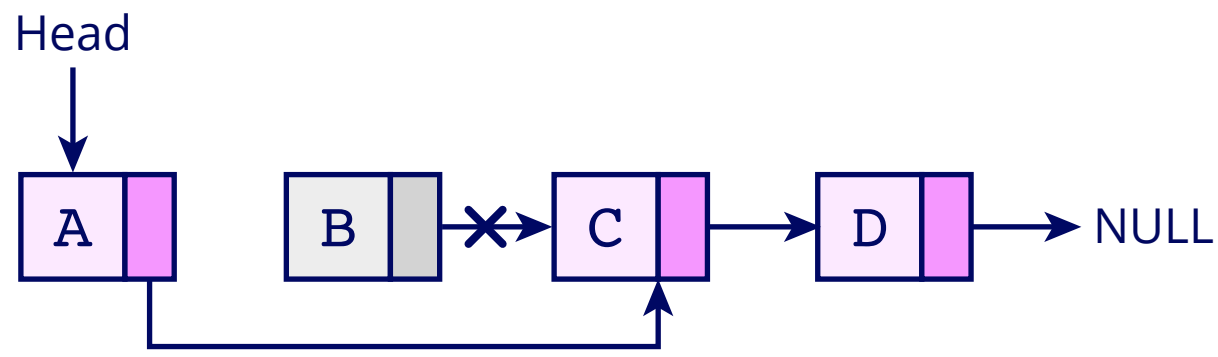
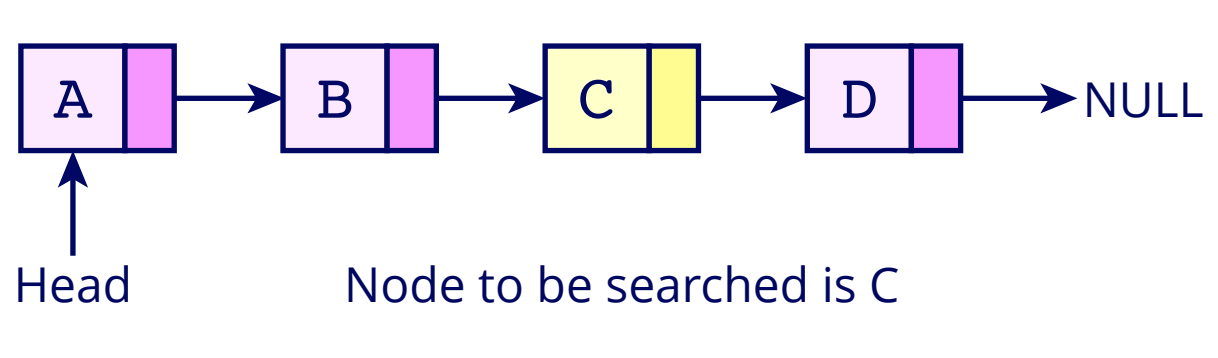
### Singly Linked List

### Definition:

It's a data structure consisting of nodes containing data and a reference (or link) to the immediate next node.



Common operations:

Operation	Example	Time Complexity (worst-case)
Insertion		O(n)
Deletion		O(n)
Search		O(n)

Traversal:

- Forward: Only in the forward direction

Application:

- Implementing stacks and queues

Pros:

- **Dynamic size:** Grow or shrink as needed
- **No contiguous memory requirement:** Does not require a large block of contiguous memory

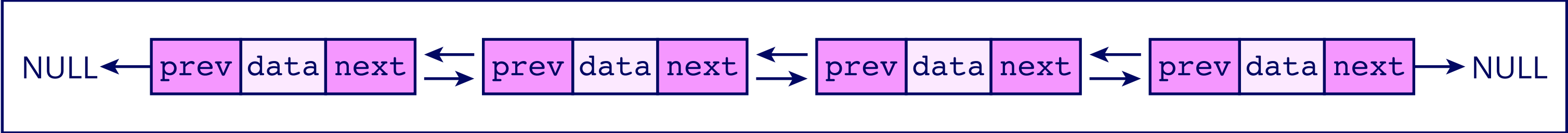
Cons:

- **Extra memory overhead:** Requires additional memory for storing pointers
- **Sequential access:** Traverse nodes sequentially to access an element

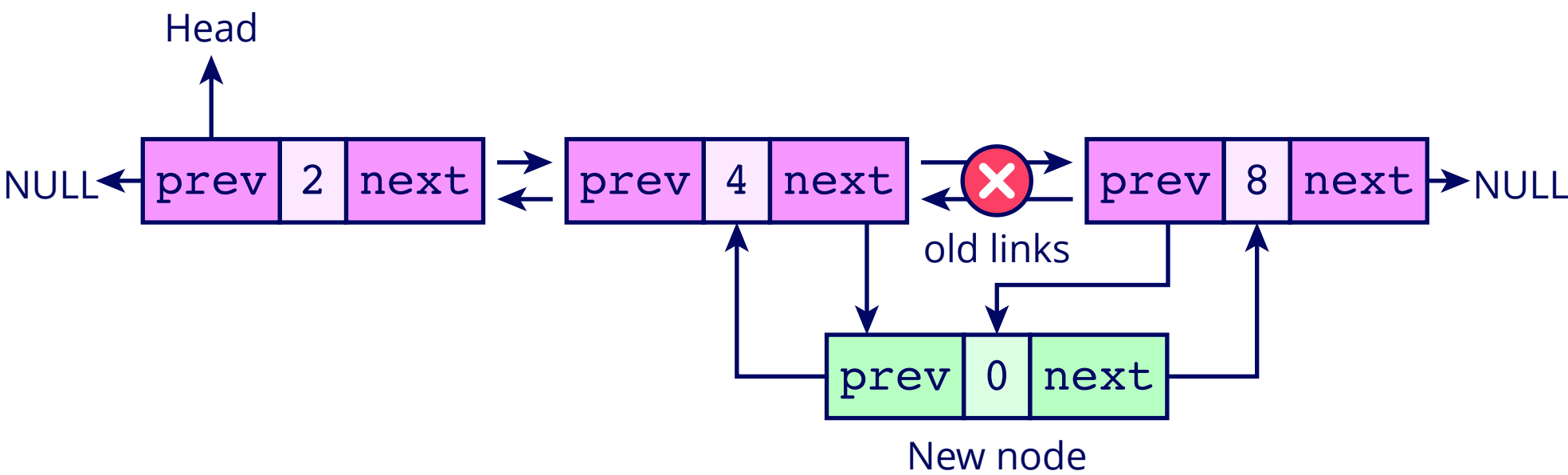
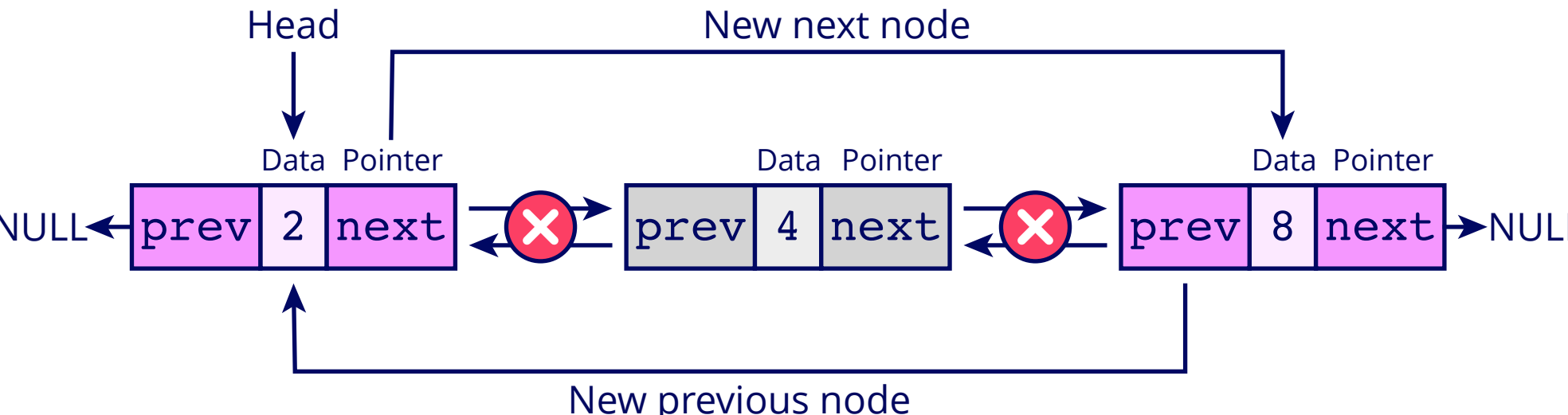
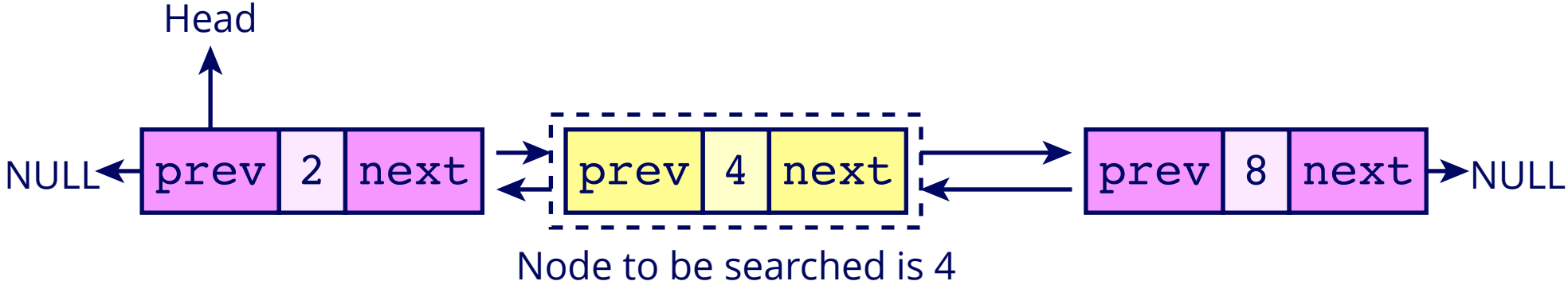
Doubly Linked List

Definition:

It’s a data structure consisting of nodes containing data and references (or links) to both the immediate next and previous nodes.



Common operations:

Operation	Example	Time Complexity (worst-case)
Insertion		O(n)
Deletion		O(n)
Search		O(n)

Traversal:

- **Forward and backward:** Traversal is in both directions (forward and backward)

Application:

- Implementing complex data structures like Fibonacci heaps

Pros:

- **Bidirectional traversal:** Traverse the list in both directions
- **Dynamic Size:** Grow or shrink as needed

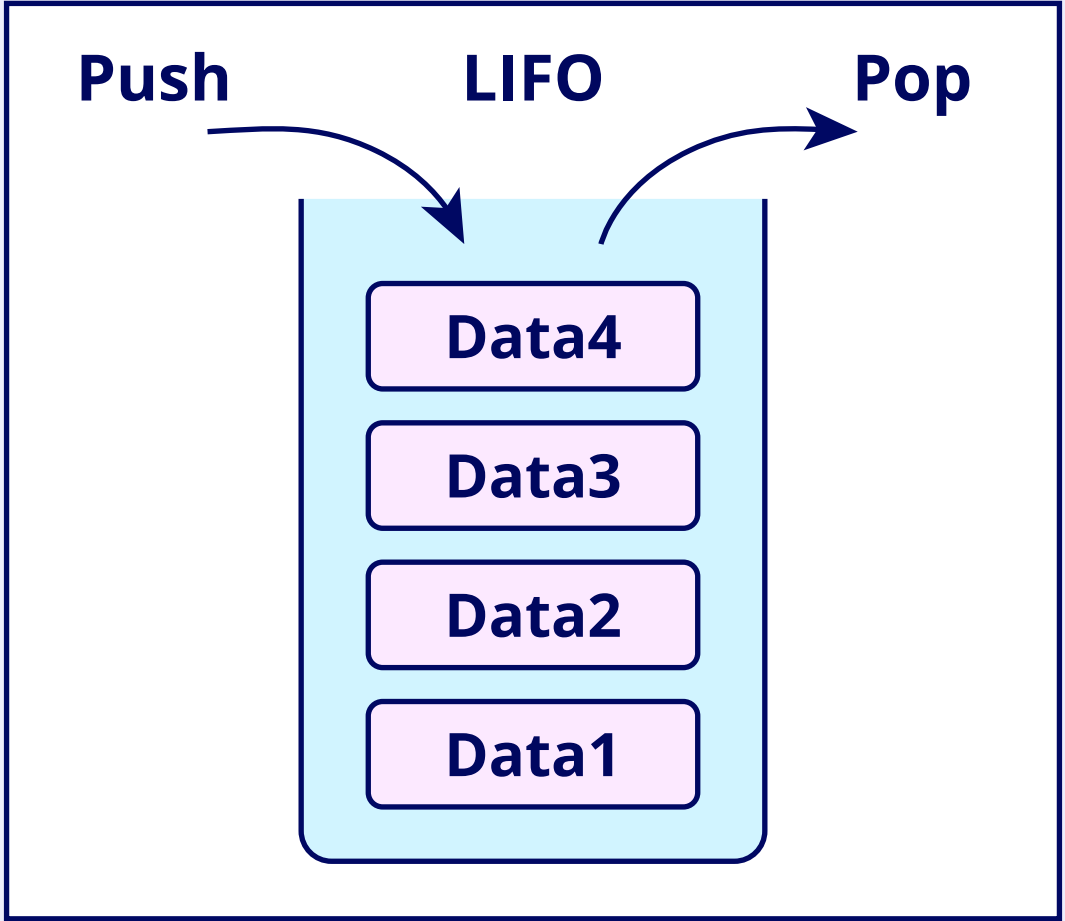
Cons:

- **Extra memory overhead:** Requires additional memory to store two pointers per node
- **Complex implementation:** More complex than singly linked lists

Stacks

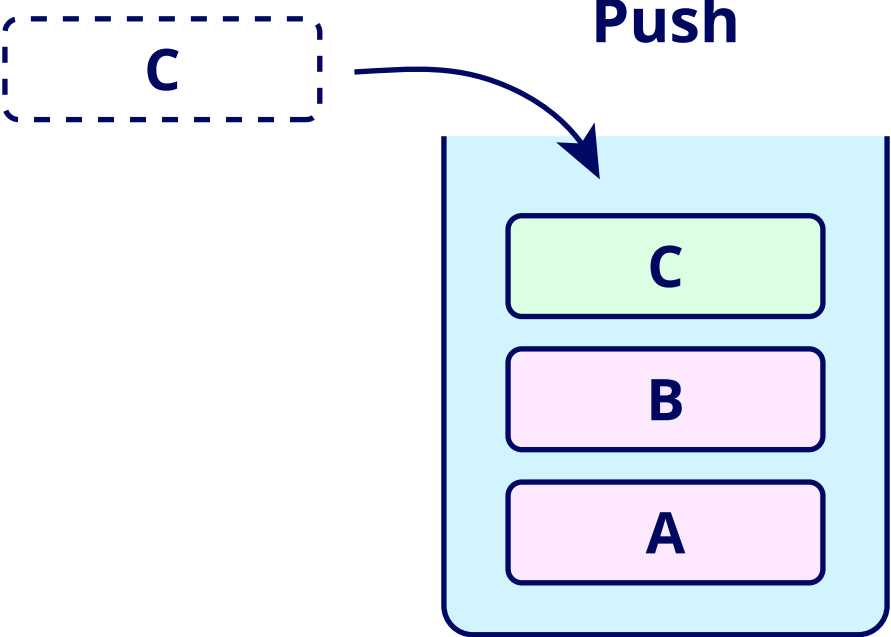
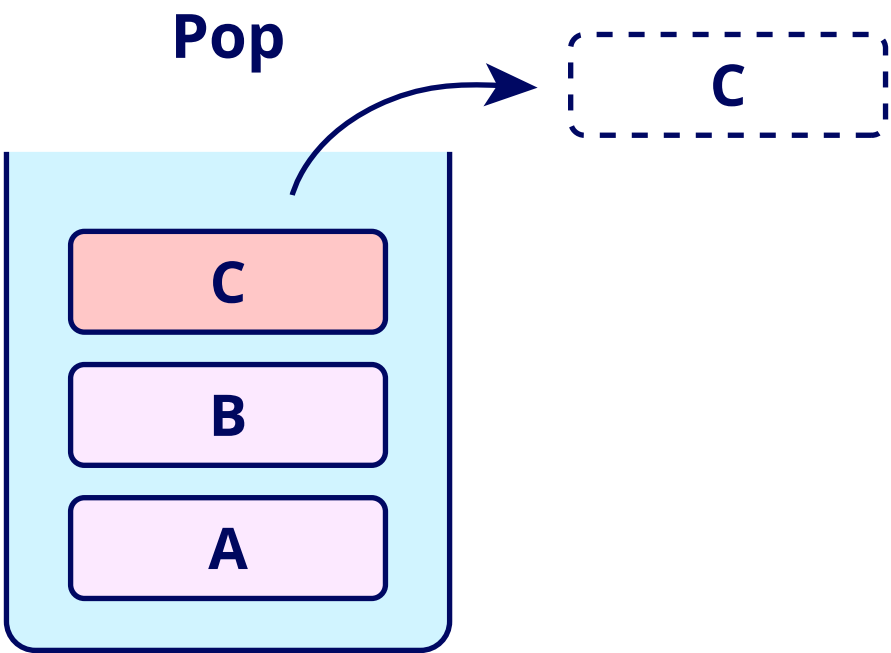
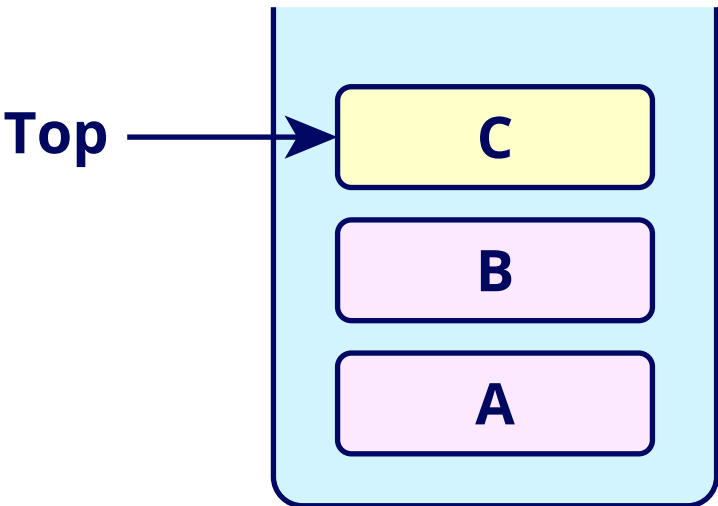
Definition:

It’s a collection of elements following the Last In, First Out (LIFO) principle, where the most recently added element is the first to be removed.



### Common operations:

- **Push:**  $O(1)$  — Adds an element to the top of the stack

Operation	Example	Time Complexity (worst-case)
Push		$O(1)$
Pop		$O(1)$
Top		$O(1)$

### Application:

- Expression evaluation and syntax parsing (e.g., converting infix expressions to postfix or evaluating postfix expressions)

### Pros:

- **Efficient operations:**  $O(1)$  time complexity for push and pop operations

### Cons:

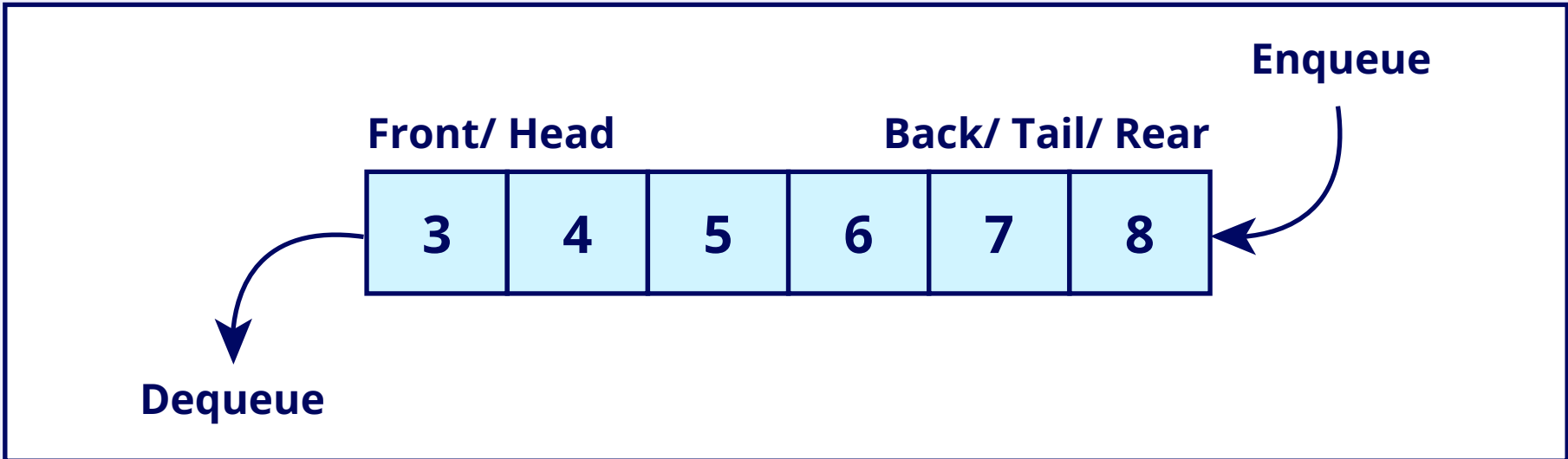
- **Sequential access:** Elements are accessed in a LIFO order

\*Note: It can be implemented using arrays or linked lists.

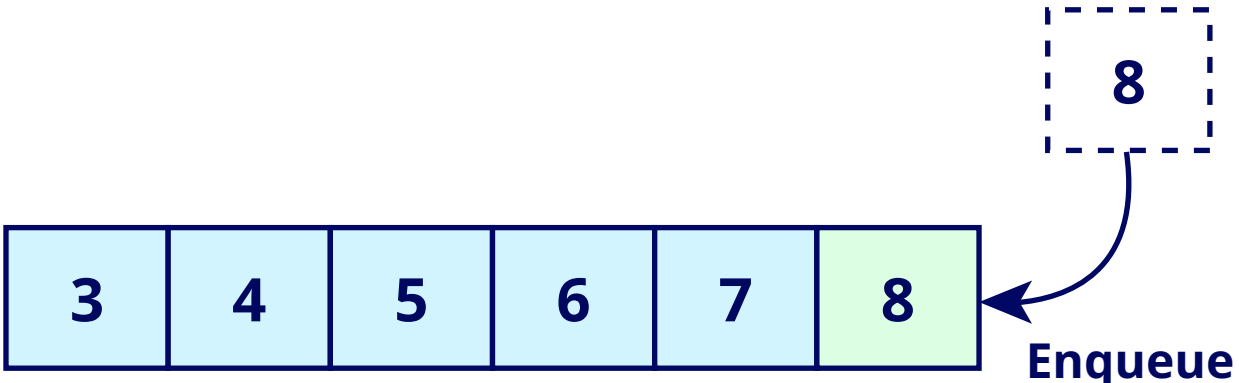
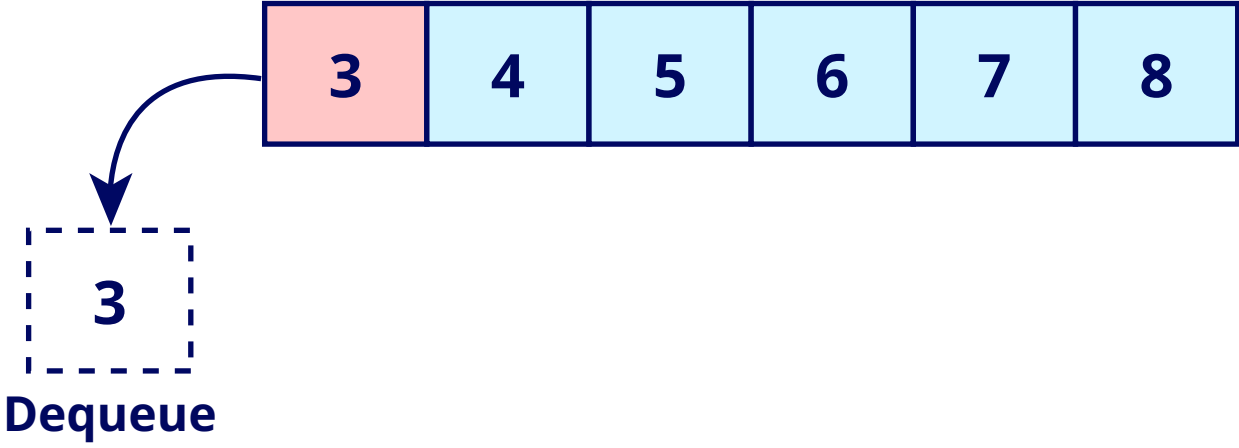
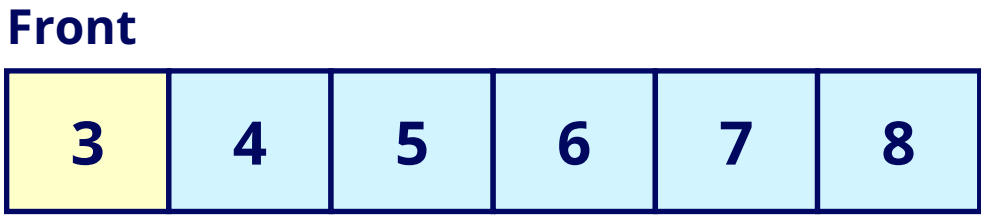
## Queues

### Definition:

It’s a collection of elements following the First In, First Out (FIFO) principle, where the first element added is the first to be removed.



## Common operations:

Operation	Example	Time Complexity (worst-case)
Enqueue		O(1)
Dequeue		O(1)
Front		O(1)

## Application:

- Task management (e.g., printer queue)

## Pros:

- Efficient operations: O(1) time complexity for enqueue and dequeue operations

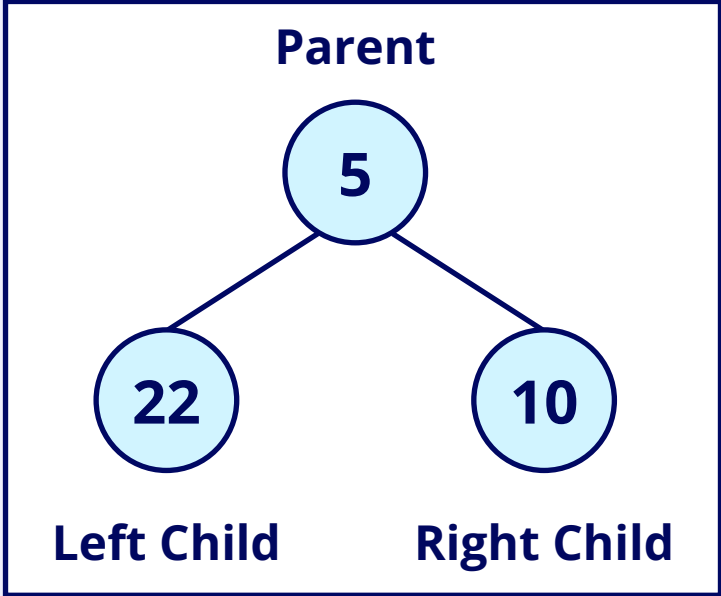
## Cons:

- Sequential access: Elements are accessed in a FIFO order
- \*Note: It can be implemented using arrays or linked lists.

# Binary Trees

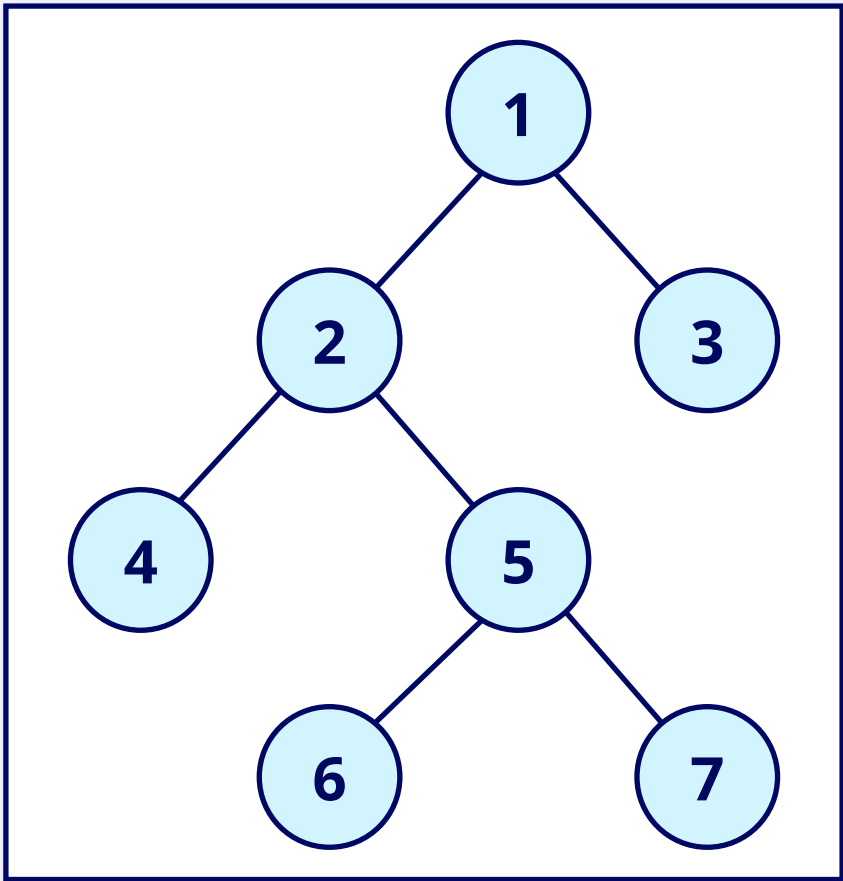
## Definition:

It's a data structure in which each node has at most two children, referred to as the left and right children.



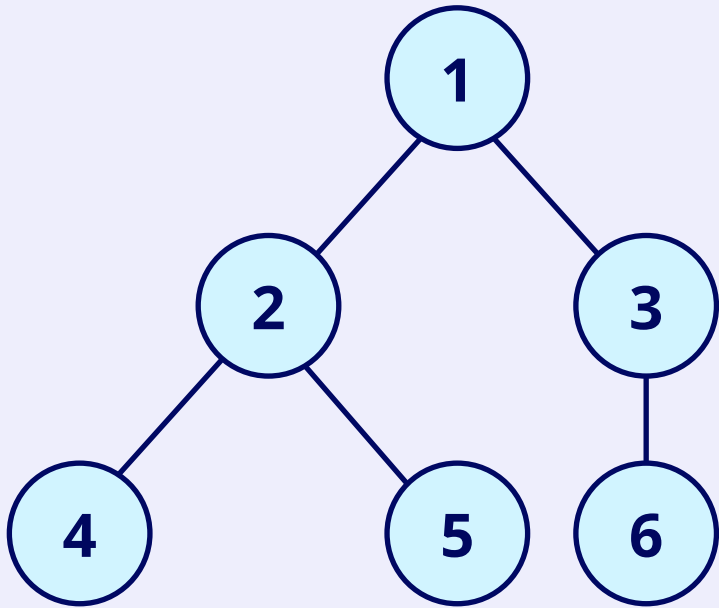
## Types:

1. Full binary tree: Every node has 0 or 2 children.

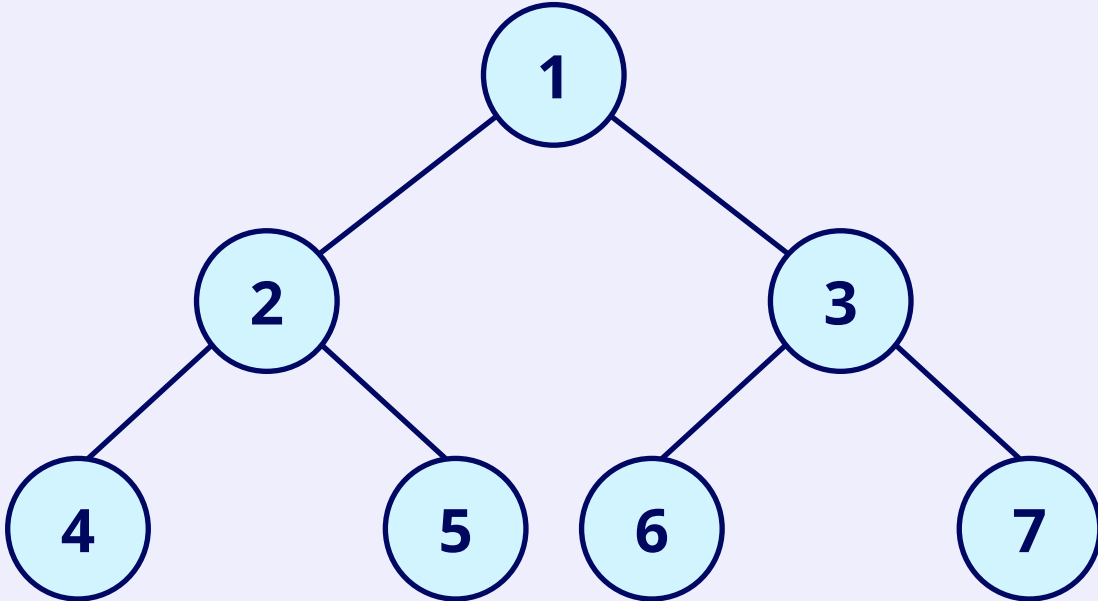




2. **Complete binary tree:** All levels are completely filled except possibly the last level, filled from left to right.

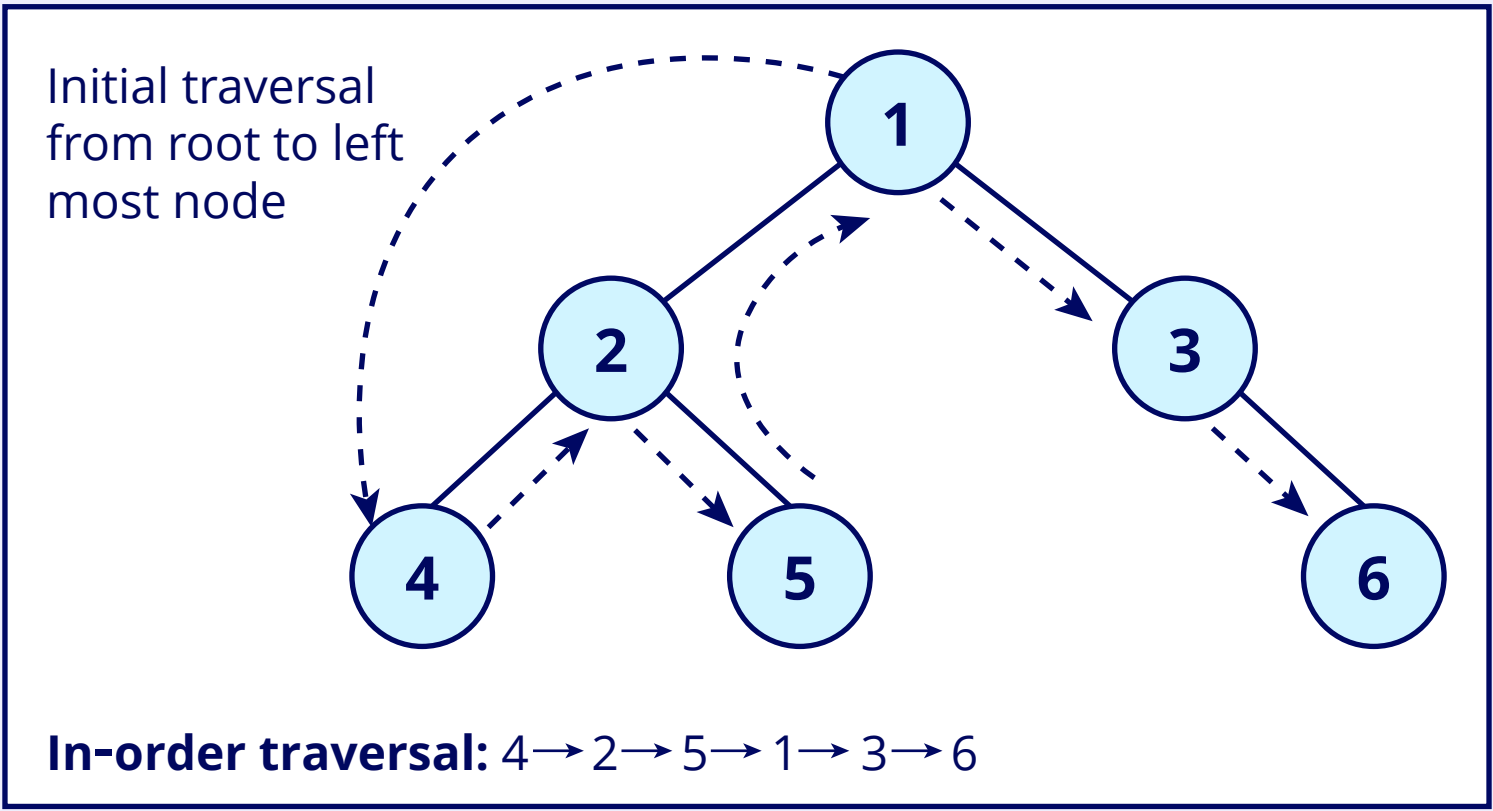


3. **Perfect binary tree:** All internal nodes have two children, and all leaves are at the same level.

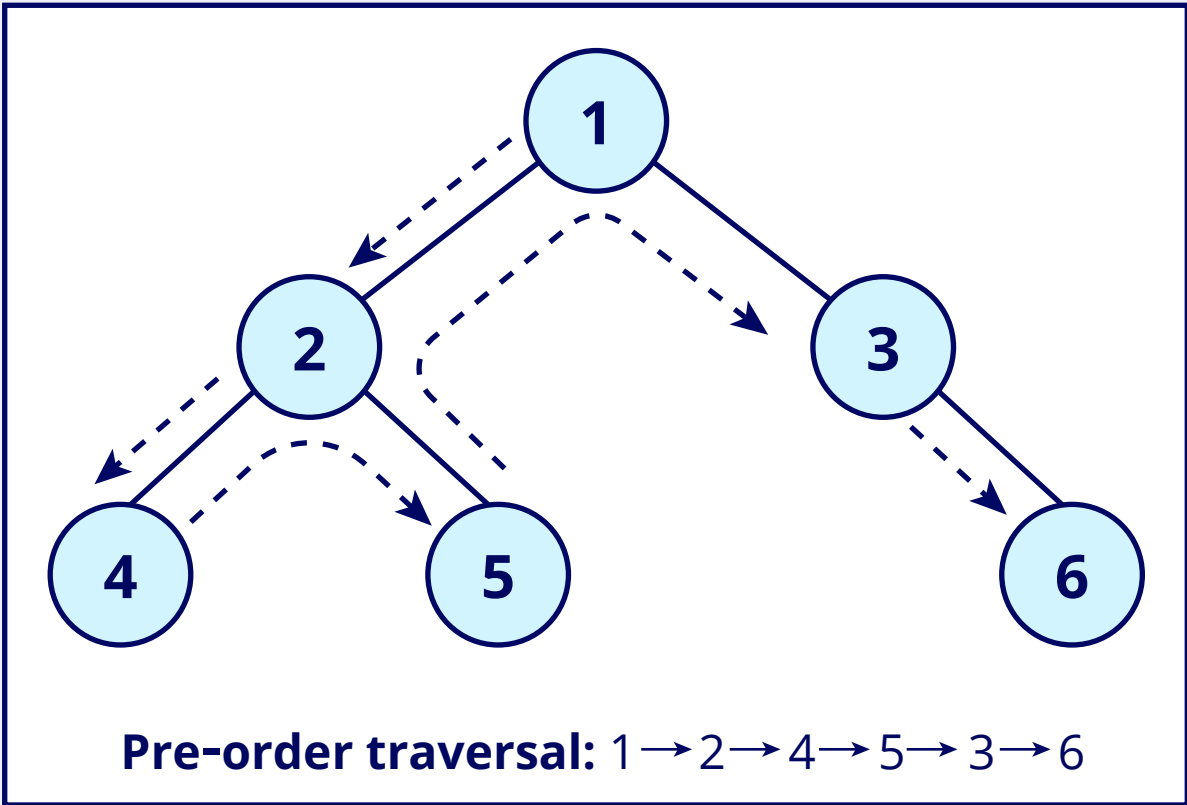


3. Traversals:

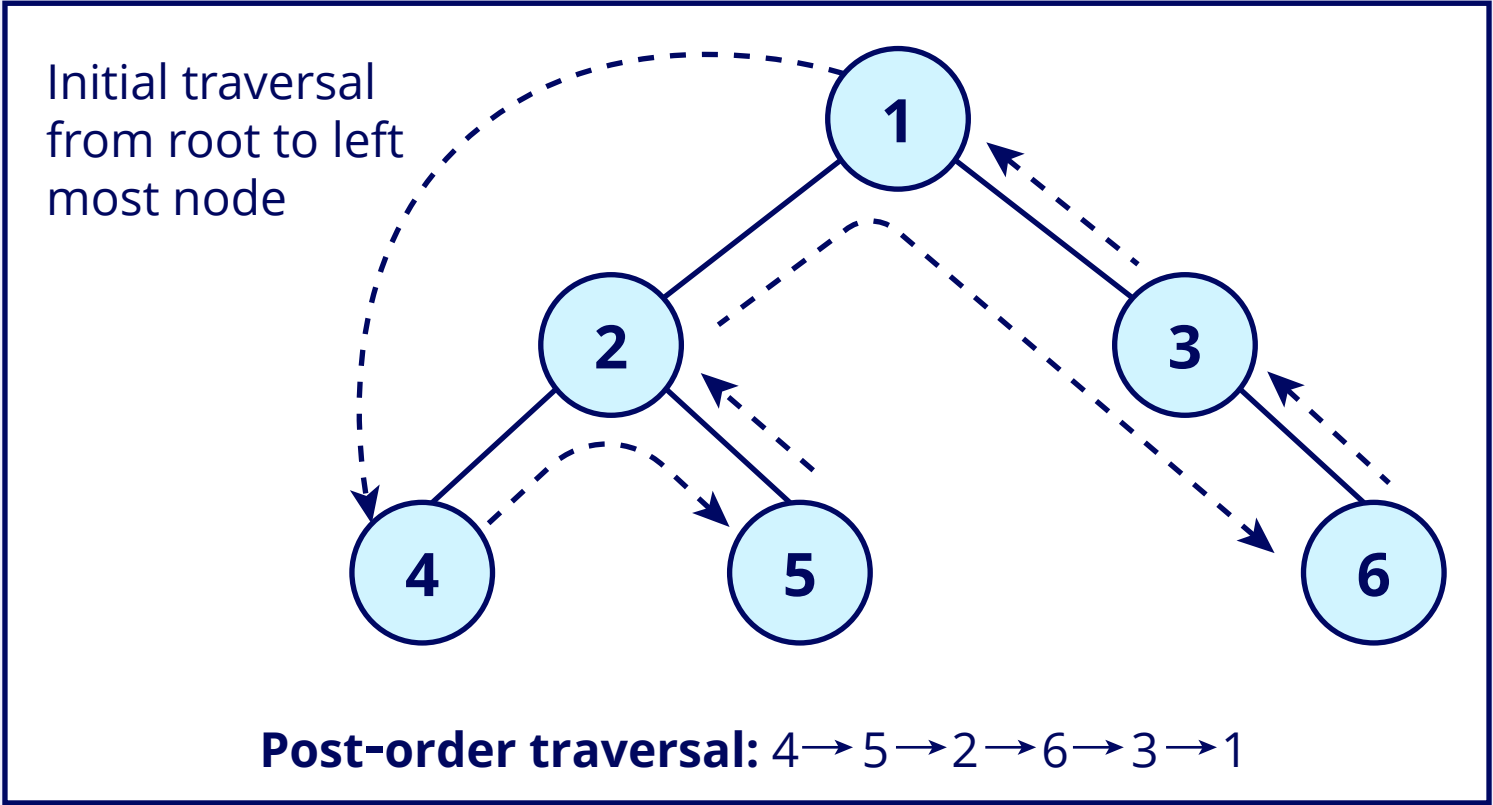
- **In-order (LNR):** Visit the left subtree, node, and the right subtree.



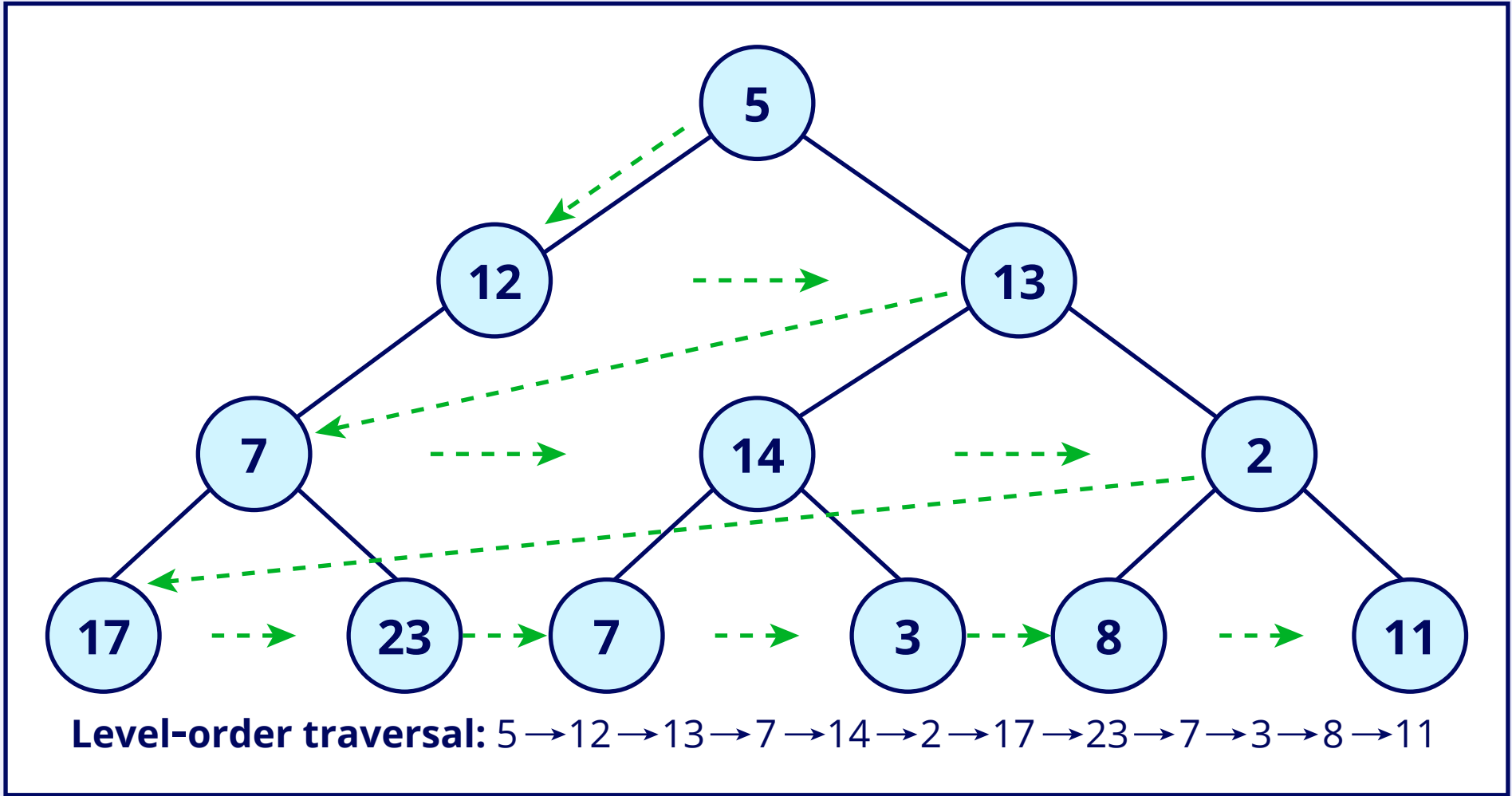
- **Pre-order (NLR):** Visit the node, left subtree, and right subtree.



- **Post-order (LRN):** Visit the left subtree, right subtree, and node.

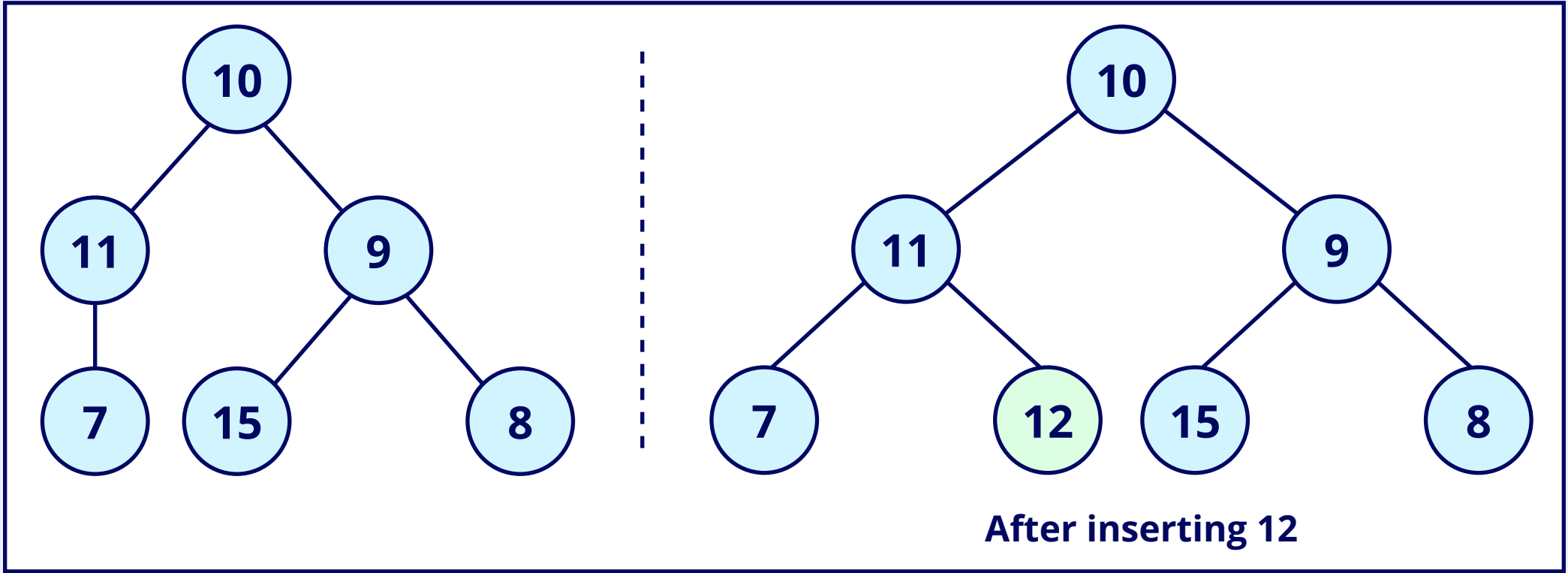


- **Level-order:** Visit nodes level by level.

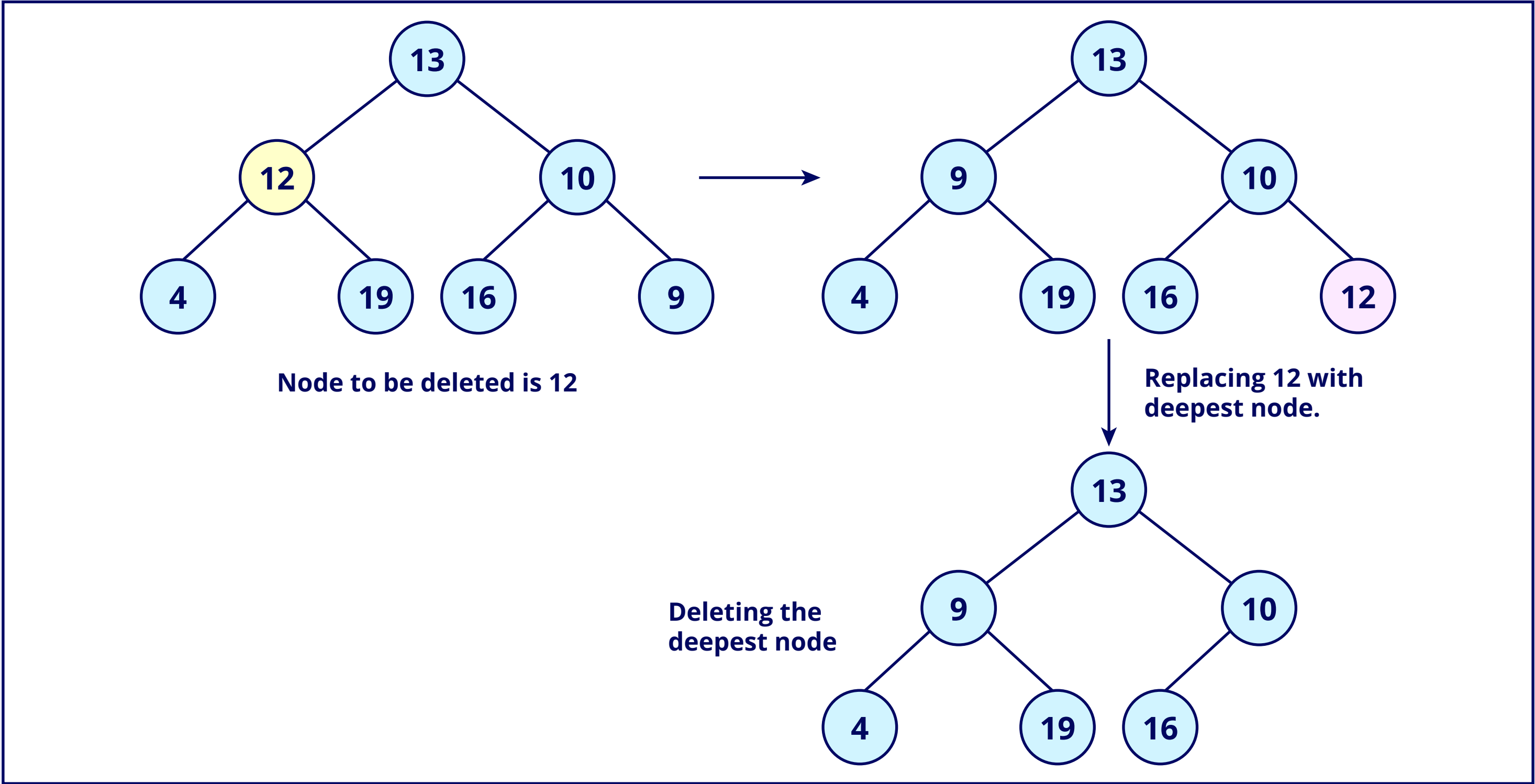


4. Common operations:

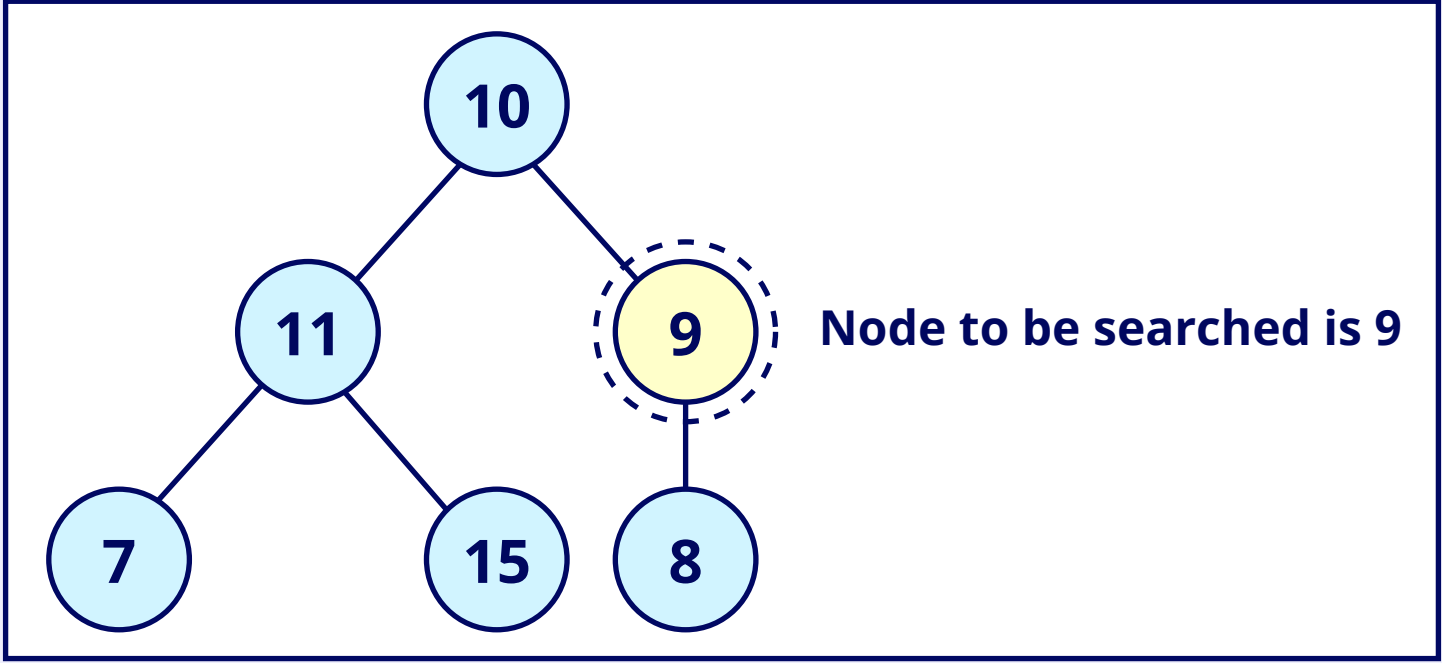
- **Insertion:**  $O(n)$



- **Deletion:**  $O(n)$



- **Search:**  $O(n)$



Application:

- Hierarchical data representation (e.g., file systems, databases)

Pros:

- Hierarchical structure: Ideal for representing hierarchical data
- Multiple traversals: Provides various traversal methods for different use cases

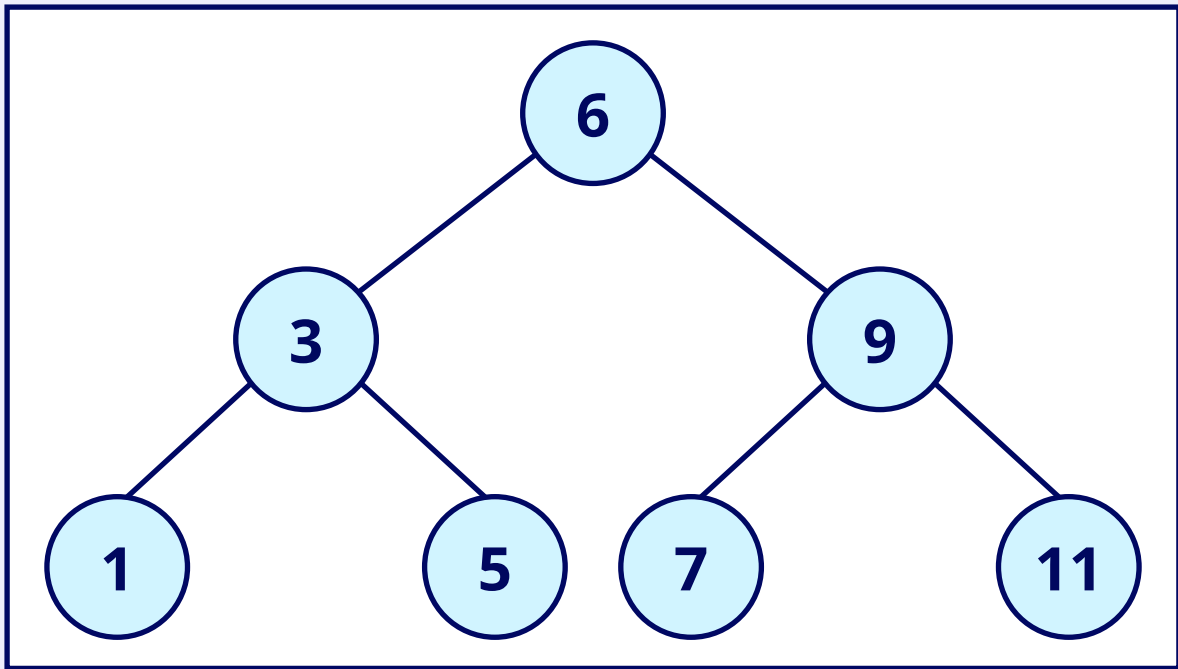
Cons:

- Inefficient operations:  $O(n)$  time complexity for insertion, deletion, and searching
- Memory overhead: Requires memory for storing pointers for each node

Binary Search Trees (BST):

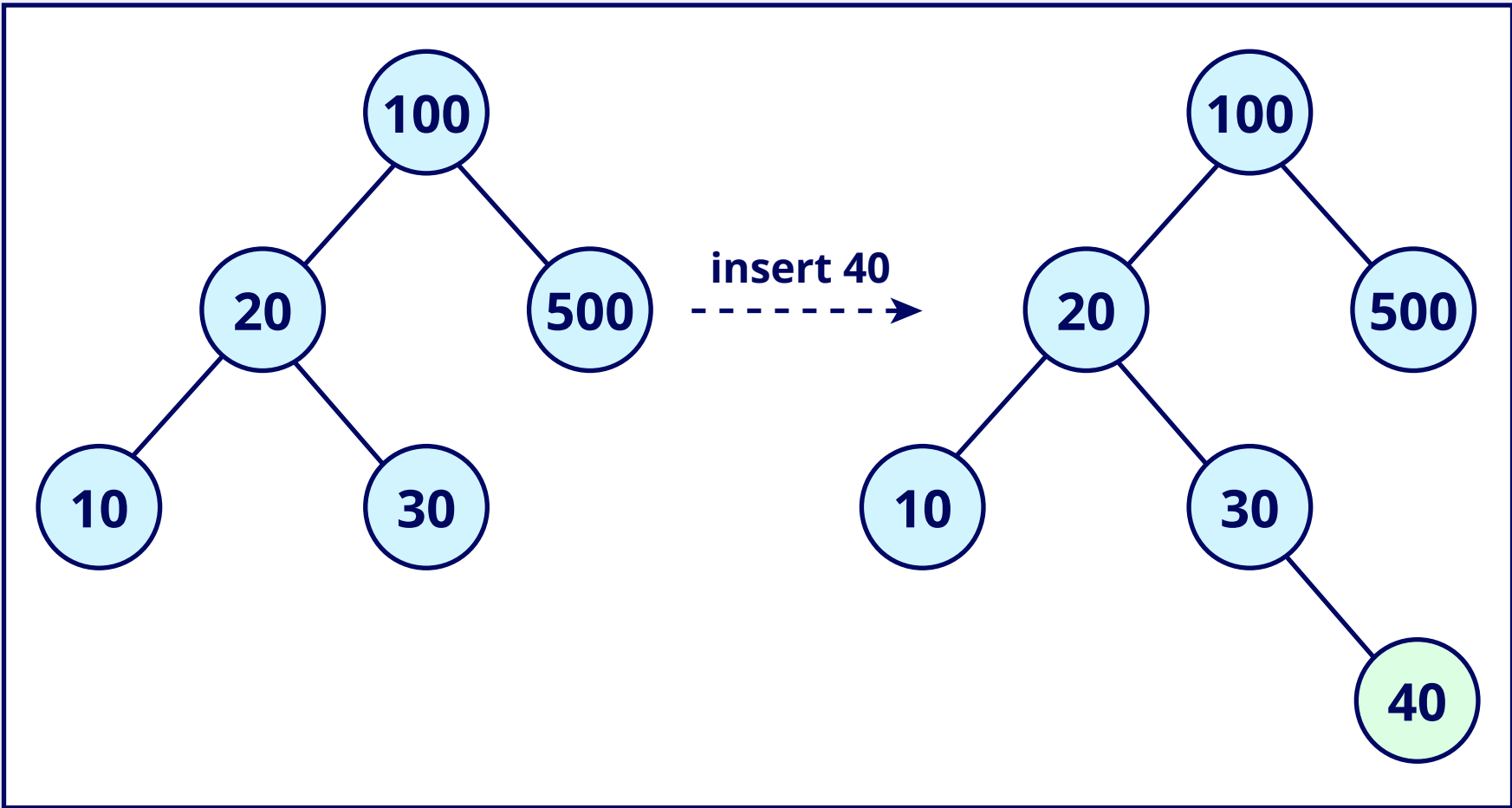
Definition:

It's a binary tree where the left child has a value less than its parent node, and the right child has a value greater than its parent node.

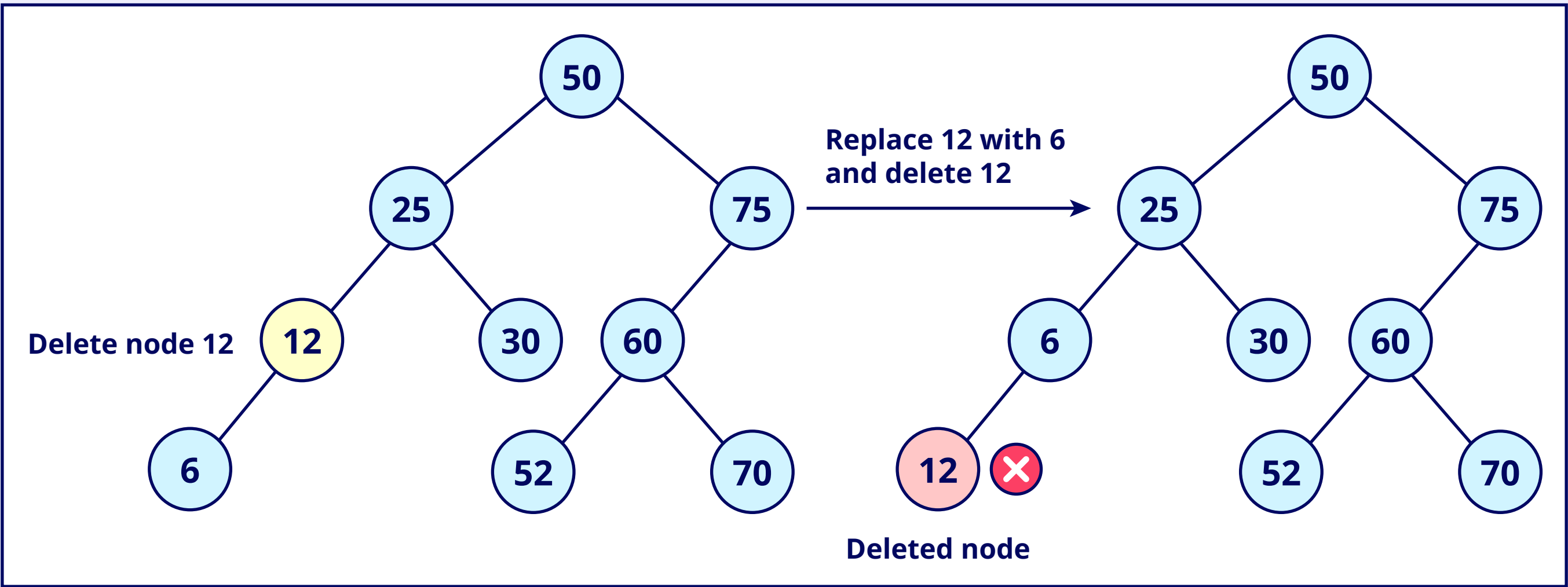


Common operations:

- Insertion:  $O(h)$  ( $h$  = height)

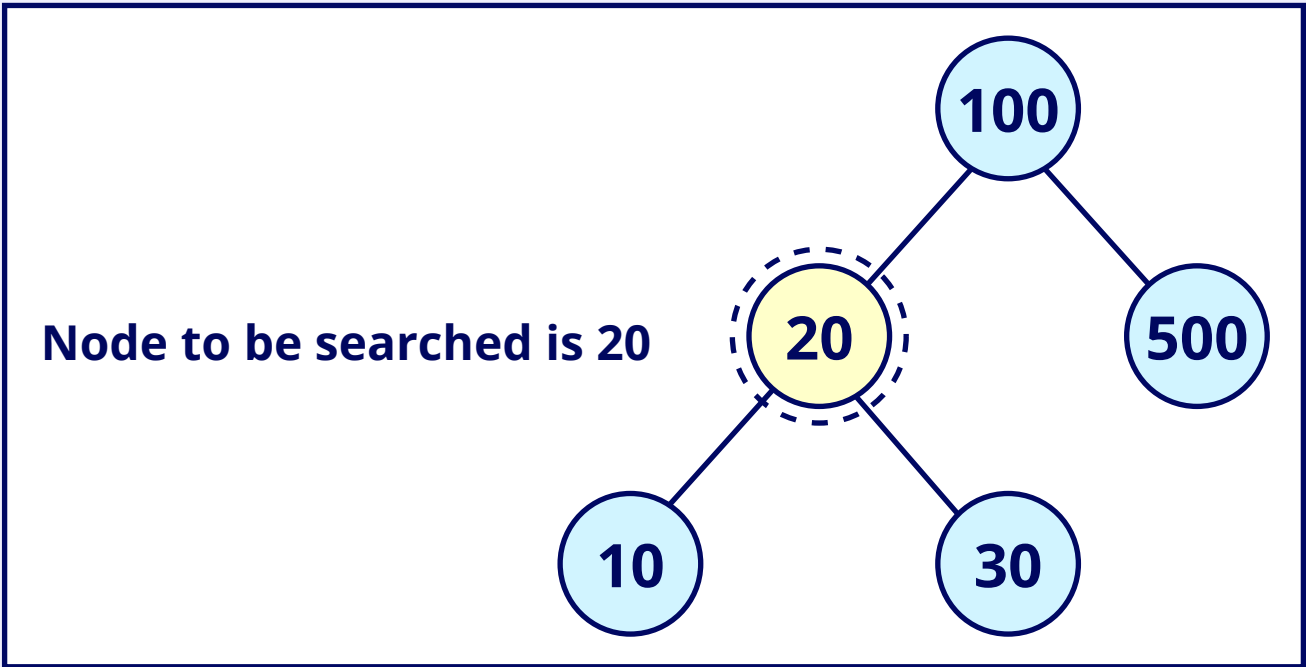


- Deletion:  $O(h)$  ( $h$  = height)





- Search:  $O(h)$  ( $h$  = height)



Application:

- Implementing associative arrays and priority queues

Pros:

- **Efficient searching/sorting:**  $O(h)$  time complexity for searching, insertion, and deletion
- **Maintains order:** Keeps elements in a sorted order

Cons:

- **Height-dependent:** Performance depends on the height of the tree; in the worst case (skewed tree), it can degrade to  $O(n)$
  - **Duplicate handling:** Typically, duplicates are discarded, which may not be suitable for all use cases
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