

Q.6) Consider the 2 relations R & S where  $R \rightarrow (5 \times 6)$   $S \rightarrow (6 \times 3)$ , establish

a)

i) max\_min,

ii) min\_max,

iii) max\_product,

iv) max\_avg on composite relationship of R & s, considering the values of R & S randomly between 0-1.

b) Plot the graph of derived 4 principles.

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
# Generate random matrices R (5x6) and S (6x3) with values between 0 and 1
```

```
np.random.seed(42) #Setting seed for reproducibility
```

```
R = np.random.rand(5, 6) #R (5x6)
```

```
S = np.random.rand(6, 3) #S (6x3)
```

```
#a)
```

```
#i)
```

```
# Function for max-min composition
```

```
def max_min_composition(R, S):
```

```
    result = np.zeros((R.shape[0], S.shape[1])) #result=resultant mat ; R.shape = (5, 6) S.shape = (6, 3)
    => (R.shape[0], S.shape[1]) = (5, 3) ; np.zeros function in NumPy is used to create a new array filled
    with zeros.
```

```
    for i in range(R.shape[0]):
```

```
        for j in range(S.shape[1]):
```

```
            result[i, j] = np.max(np.minimum(R[i, :], S[:, j])) #R-> ith row, all cols(:) ; S-> jth col, all rows(:)
```

```
    return result
```

```
#ii)
```

# Function for min-max composition

```
def min_max_composition(R, S):  
    result = np.zeros((R.shape[0], S.shape[1]))  
    for i in range(R.shape[0]):  
        for j in range(S.shape[1]):  
            result[i, j] = np.min(np.maximum(R[i, :], S[:, j]))  
    return result
```

#iii)

# Function for max-product composition

```
def max_product_composition(R, S):  
    result = np.zeros((R.shape[0], S.shape[1]))  
    for i in range(R.shape[0]):  
        for j in range(S.shape[1]):  
            result[i, j] = np.max(R[i, :] * S[:, j])  
    return result
```

#iv)

# Function for max-avg composition

```
def max_avg_composition(R, S):  
    result = np.zeros((R.shape[0], S.shape[1]))  
    for i in range(R.shape[0]):  
        for j in range(S.shape[1]):  
            result[i, j] = np.max((R[i, :] + S[:, j]) / 2)  
    return result
```

# Calculate the compositions

```
max_min_result = max_min_composition(R, S)  
min_max_result = min_max_composition(R, S)  
max_product_result = max_product_composition(R, S)  
max_avg_result = max_avg_composition(R, S)
```

```

# Print the results

print("R:\n", R)

print("\nS:\n", S)

print("\nMax-Min Composition:\n", max_min_result)

print("\nMin-Max Composition:\n", min_max_result)

print("\nMax-Product Composition:\n", max_product_result)

print("\nMax-Avg Composition:\n", max_avg_result)

```

#b)

# Plot the results separately

def plot\_matrix(matrix, title): #matrix: The matrix (a 2D NumPy array) that you want to visualize,  
title: A string that will be used as the title of the plot.

```

    plt.figure(figsize=(6, 5))

```

plt.imshow(matrix, cmap='viridis', aspect='auto') #plt.imshow() is used to display the matrix as an image, cmap='viridis' Specifies the colormap to use. viridis is a popular color map , aspect='auto': Automatically adjusts the aspect ratio of the plot to fit the figure.

```

    plt.title(title)

```

```

    plt.colorbar() #Adds a colorbar to the side of the plot

```

```

    plt.show()

```

```

plot_matrix(max_min_result, "Max-Min Composition")

```

```

plot_matrix(min_max_result, "Min-Max Composition")

```

```

plot_matrix(max_product_result, "Max-Product Composition")

```

```

plot_matrix(max_avg_result, "Max-Avg Composition")

```

R:

```
[[0.37454012 0.95071431 0.73199394 0.59865848 0.15601864 0.15599452]
 [0.05808361 0.86617615 0.60111501 0.70807258 0.02058449 0.96990985]
 [0.83244264 0.21233911 0.18182497 0.18340451 0.30424224 0.52475643]
 [0.43194502 0.29122914 0.61185289 0.13949386 0.29214465 0.36636184]
 [0.45606998 0.78517596 0.19967378 0.51423444 0.59241457 0.04645041]]
```

S:

```
[[0.60754485 0.17052412 0.06505159]
 [0.94888554 0.96563203 0.80839735]
 [0.30461377 0.09767211 0.68423303]
 [0.44015249 0.12203823 0.49517691]
 [0.03438852 0.9093204 0.25877998]
 [0.66252228 0.31171108 0.52006802]]
```

Max-Min Composition:

```
[[0.94888554 0.95071431 0.80839735]
 [0.86617615 0.86617615 0.80839735]
 [0.60754485 0.31171108 0.52006802]
 [0.43194502 0.31171108 0.61185289]
 [0.78517596 0.78517596 0.78517596]]
```

Min-Max Composition:

```
[[0.15601864 0.31171108 0.25877998]
 [0.03438852 0.17052412 0.06505159]
 [0.30424224 0.18182497 0.30424224]
 [0.29214465 0.13949386 0.29214465]
 [0.30461377 0.19967378 0.45606998]]
```

Max-Product Composition:

```
[[0.90211906 0.91804019 0.76855492]
 [0.82190202 0.83640743 0.7002145 ]
 [0.50574624 0.27665368 0.27290904]
 [0.27634312 0.28122019 0.41864996]
 [0.74504211 0.75819106 0.63473416]]
```

Max-Avg Composition:

```
[[0.94979992 0.95817317 0.87955583]
 [0.90753084 0.91590409 0.83728675]
 [0.71999375 0.60678132 0.52241223]
 [0.62005734 0.62843059 0.64804296]
 [0.86703075 0.875404 0.79678665]]
```

