

(14) Maximum Consecutive 1's in a Binary Array:

I/P → [1, 0, 1, 1, 1, 1, 0, 1, 1]

O/P → 4

[0, 0, 0]

0

[1, 1, 1]

3

Naive → $O(n^2)$

efficient → $O(n)$

```

int f(int a[], int n)
{
    int ms = 0, c = 0;
    for(int i = 0; i < n; i++)
    {
        if(a[i] == 0)
            c = 0;
        else
            c++;
        ms = max(ms, c);
    }
    return ms;
}
    
```

(15) Maximum Sum SubArray:

I/P → {-3, 8, -2, 4, -5, 6}

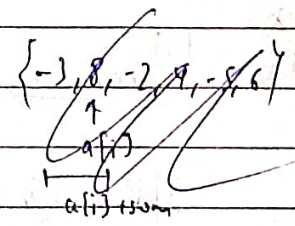
O/P → 11

- ✓ a) Kadane's Algo $O(n)$
- b) Naive $O(n^2)$
- ✓ c) efficient $O(n)$

```

int maxSum(int a[], int n)
{
    int ms = a[0], sum = a[0];
    for(int i = 1; i < n; i++)
    {
        sum = max(a[i], a[i] + sum);
        ms = max(ms, sum);
    }
    return ms;
}
    
```

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⑫ Maximum length Even-Odd Subarray :

→ pairs can be even-odd / odd-even both valid

→ I/P: {10, 12, 14, 3, 8} I/P: {3, 6, 13, 14} I/P: {4, 6, 8}

O/P: 3 O/P: 4 O/P: 1

Naive $\rightarrow O(n^2)$ \rightarrow break it and (hint)

efficient $\rightarrow O(n)$

```
int maxlength(int a[], int n)
{
```

```
    int res = 1, c = 1;
```

```
    for (int i = 1; i < n; i++)
    {
```

```
        if ((a[i] % 2 == 0 && a[i-1] % 2 != 0) ||
            (a[i] % 2 != 0 && a[i-1] % 2 == 0))
        {
```

```
            c++;
```

```
            res = max(res, c);
```

```
        }
        else
```

```
            c = 1;
```

```
    }
    return res;
}
```

⑬

Maximum Circular SubArray Sum :

I/P: {5, -2, 3, 4}

O/P: 12

{2, 3, -4}

5

{8, -4, 3, -5, 4}

12

{3, 4, 6, -2}

10

a) Naive Solution $O(N^2)$

$n=4$ 5, -2, 3, 4 \Rightarrow to again go to index 0 we do
 0 1 2 3
 i \rightarrow \rightarrow \rightarrow
 \leftarrow
 $(i \cdot n)$ $4 \cdot 4 = 0$

```
int f(int a[], int n)
{
```

```
    int ans = a[0];
```

```
    for (int i = 0; i < n; i++)
    {
```

```
        sum = a[i], ms = a[i];
```

```
        for (j = 1; j < n; j++)
```

```
            sum += a[(i+j) % n];
```

```
            ms = max(ms, sum);
```

```
        ans = max(ans, ms);
```

```
    }
    return ans;
}
```

```
for i = 0
```

5, -2, 3, 4

0 1 2 3
 \nearrow
 $i=0$

we go through 5 \rightarrow -2 \rightarrow 3 \rightarrow 4

```
for i = 1
```

we go -2 \rightarrow 3 \rightarrow 4 \rightarrow 5

```
for i = 2
```

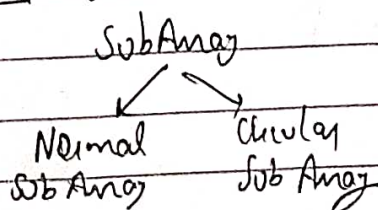
we go 3 \rightarrow 4 \rightarrow 5 \rightarrow -2

Similarly other

* For every i we do +1
 through j loop to
 access index in circular
 manner

b) efficient $O(n)$

Logic



- Step I We will find max SubArray Sum from Normal SubArray say $ms1$
 Step II Circular " say $ms2$
 Step III Then Do Max of results from Step I & Step II
 $ans = \max(ms1, ms2);$

One Concept for Step II Calculation

$$a[] = \{8, -4, 3, -5, 4\}$$

we know max (Circular SubArray Sum) = $8 + 4 = 12$

Remaining elements are the minimum SubArray Sum of Normal SubArray

→ So basically we find (Total sum of Array) - (minimum SubArray Sum)

proof

eg: To find MSS

Method (I)

$$a[] = \{8, -4, 3, -5, 4\} \Rightarrow \text{Multiply } -1 \Rightarrow \{-8, 4, -3, 5, -4\}$$

↓ Now find max SubArray Sum

$$\text{when } -6 \leftarrow 6$$

int sum = a[0], ans = a[0];

Method (II)

~~Kada~~ for(int a[], int n)
{
for(i = 0 to n-1)
sum += a[i];

ans = max(ans, sum);

if(sum > 0)

{

sum = 0;

}

when sum ans.


```
int CircularSum(int a[], int n)
```

```
{
```

```
    int ans1 = f(a, n);
```

```
    if (ans1 < 0)
```

```
        return ans1;
```

→ Normal SubArray Sum

→ when all elements are -ve

```
    int total = 0;
```

```
    for (int i = 0; i < n; i++)
```

```
    {
```

```
        total += a[i];
```

```
        a[i] = -a[i];
```

```
    }
```

```
    int ans2 = f(a, n);
```

→ 4 (Minimum SubArray Sum)

```
    ans2 = total + ans2;
```

```
    return max(ans1, ans2);
```

```
}
```

```
int f(int a[], int n)
```

```
{
```

```
    int sum = a[0], ms = a[0];
```

```
    for (int i = 1; i < n; i++)
```

```
    {
```

```
        sum = max(a[i], a[i] + sum);
```

```
        ms = max(ms, sum);
```

```
    }
```

```
    return ms;
```

```
}
```

(Moore's Voting Algo)

(18) Majority Element I

- Given array of size n find a majority element.
→ Only 1 solⁿ max^m possible. element that occurs ^{more than} $\lfloor \frac{n}{2} \rfloor$ values.

Naive $\rightarrow O(n^2)$ Brute force $O(n^2)$ / HashMap $O(n \log n)$, $SC \rightarrow O(n)$
efficient $\rightarrow O(n)$

I/P $\rightarrow [8, 3, 4, 8, 8]$	$\{3, 2, 4, 2, 2, 5\}$	$\{3, 4, 4\}$
O/P $\rightarrow 8$	-1	4

```
int MajorityElement(int a[], int n)
```

```
{  
    int c=0, num;  
    for(int i=0; i<n; i++)
```

```
    {  
        if(c==0)  
            num=a[i];  
        if(num==a[i])  
            c++;  
        else  
            c--;
```

```
    }  
    int c1=0;  
    for(int i=0; i<n; i++)  
    {  
        if(a[i]==num)  
            c1++;  
    }
```

```
    if(c1 > n/2)
```

```
        return num;
```

```
    return -1;  $\rightarrow$  when no ME present
```

Moore Voting Algo

\rightarrow num is our majority element, but only when there is ME exist.

\rightarrow counting num occurrence

here count(c) becomes zero and also num is assigned a new value

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eg: {7, 7, 5, 7, 5, 1} {5, 7} {5, 5, 7, 7} {5, 5, 5, 5}

$c = \emptyset \times \times \times \times \emptyset \times \emptyset \times \times \times \emptyset \times \times \times \times$
 $num = \times 8 \times 5$

whenever count becomes 0
then we assign new num (ME)
again start

for part at extra it starts

→ every time num value change we consider that element as our new ME.

{7, 7, 5, 7, 5, 1}

we consider 7 as our largest element (ME)
here (majority == minority) they cancel each other

19) Majority Element II:

- Given array find ME (element that occurs $> \lfloor \frac{n}{3} \rfloor$ times)
- Remember → at max only two solⁿ are possible.

Naive → $O(n^2)$ SC → $O(1)$ | Hashmap → $O(n \log n)$ SC → $O(n)$
efficient → $O(n)$

eg: {1, 4, 5} {1, 4, 5, 5, 5, 3, 4, 7} $n = 11$

$c1 = \emptyset \times \emptyset \times \times \times \times 1$

$c2 = \emptyset \times \emptyset \times \times \times 1$

$num1 = \times \times 5$

$num2 = \times 4$

in {1, 4, 5}

$n = 3/3 = 1$

no element occurs more than 1

5, 4 are needed ME

→ Using num1, num2 we keep track of two ME.

```
class Solution {
```

```
public:
```

```
vector<int> find(vector<int> &a)
```

```
{
```

```
    int c1=0, c2=0, num1=-1, num2=-1;
```

```
    for(int i=0; i<a.size(); i++)
```

```
    {
```

```
        if(a[i]==num1) c1++;
```

```
        else if(a[i]==num2) c2++;
```

```
        else if(c1==0)
```

```
        {
```

```
            num1=a[i]
```

```
            c1++; // or c1=1;
```

```
        }
```

```
        else if(c2==0)
```

```
        {
```

```
            num2=a[i]
```

```
            c2++; // or c2=1;
```

```
        } else
```

```
        {
```

```
            c1--; c2--;
```

```
        }
```

```
    }
```

```
    c1=c2=0;
```

```
    for(int i=0; i<a.size(); i++)
```

```
    {
```

```
        if(a[i]==num1)
```

```
            c1++;
```

```
        if(a[i]==num2)
```

```
            c2++;
```

```
    }
```

→ calculating occurrence
of num1 & num2


```

vector<int> v;
if (c1 > a.size()/3)
    v.push_back(num1);
if (c2 > a.size()/3)
    v.push_back(num2);

```

```

return v;
}

```

② Minimum Group flip to make Binary Array Same :

Brute force $\rightarrow O(n^2)$

efficient $O(n)$

I/P \rightarrow 0, 0, 1, 1, 0, 0, 1, 1, 0

0 1 2 3 4 5 6 7 8

O/P \rightarrow flip 2 to 3

flip 6 to 7

Concept

\rightarrow Group of 0 & 1 differ by at most 1. (either same or differ by one)

① Group differ by 1

1100011100 \rightarrow count of 1 group = 3 $(3-2) = 1$
 " " " " = 2

010100111100 \rightarrow count of 1 = 3 $(4-3) = 1$
 0 = 4

When $a[0]$ & $a[n-1]$ are same then group differ by 1

② Group counts same

00111000011 \rightarrow count of 0 = count of 1 = 2

10101100110 \rightarrow _____ = 4

When $a[0]$ & $a[n-1]$ are different then group count is same.

Remember we will solve by taking second different group ie say 1100010100111 for able to write code for both case.

```
void f(int a[], int n)
{
    for(int i=1; i<n; i++)
    {
        if(a[i] != a[i-1])
        {
            if(a[i] == a[0])
                cout << i-1 << endl;
            else
                cout << "from " << i << " to ";
        }
    }
    if(a[n-1] != a[0])
    {
        cout << n-1;
    }
}
```

when both grp count same
110001010000

Brute force:

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- Problems / Concept

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(21) Given an Array of integers and a number k , find the maximum sum of k consecutive elements?

Naive $\rightarrow O(nk)$

efficient $\rightarrow O(n)$

```
int f(int k, vector<int> &a, int n)
{
```

```
    int ms = 0;
```

```
    for(int i=0; i<n; i++)
```

```
        ms += a[i];
```

```
    int sum = ms;
```

```
    for(int i=k; i<n; i++)
    {
```

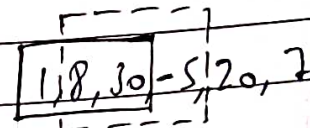
```
        sum += a[i] - a[i-k];
```

```
        ms = max(ms, sum);
```

```
    }
    return ms;
}
```

T/P: $\{1, 8, 30, -5, 20, 7\}, k=3$

O/P: 45



↑
window slides by 1.

(22)