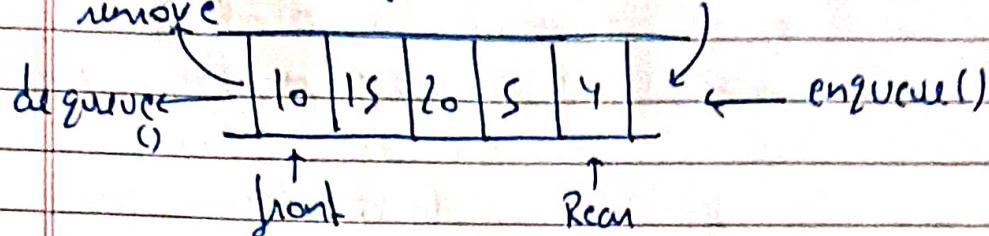


Date _____
Page _____

- FIFO (First in First out) add
remove



- Removal operation done from front is called dequeue()
- Addition ————— Rear ————— enqueue()
- getFront() - to get front item
- getRear() ————— rear —————
- size() - Queue size return
- isEmpty() - return bool value, 1 if empty, 0 if empty.
- isFull() -

e.g) Queue q

begin	q.enqueue(10)	<table border="1"><tr><td>10</td></tr></table>	10			
10						
Independent code	q.enqueue(20)	<table border="1"><tr><td>10</td><td>20</td></tr></table>	10	20		
10	20					
	q.enqueue(30)	<table border="1"><tr><td>10</td><td>20</td><td>30</td></tr></table>	10	20	30	
10	20	30				
	q.enqueue(40)	<table border="1"><tr><td>10</td><td>20</td><td>30</td><td>40</td></tr></table>	10	20	30	40
10	20	30	40			
	print(q.dequeue())	<table border="1"><tr><td>20</td><td>30</td><td>40</td></tr></table> 10	20	30	40	
20	30	40				
	print(q.dequeue())	<table border="1"><tr><td>30</td><td>40</td></tr></table> 20	30	40		
30	40					
	print(q.getFront())	30				
	print(q.getRear())	40				

We make Queue of Tickets

→ Application of Queue :

- ① Single Resource and Multiple Consumers (e.g. Ticket in a Queue at counter, ATM, ticket counter get ticket) in combination also that from scheduling algorithm can just serve

- * Multiple Consumers till at Queue (Waiting until you get service a little bit by time)
- * Synchronization of Queue of slow & fast devices

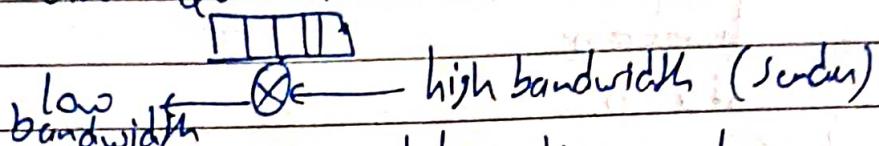
② Synchronization between slow & fast devices.

e.g. (Keyboard & monitor work in synchronizing way)

slow devic^s fast

Character entered are stored in Queue to be processed by one who takes a job & process data quickly.

* In Raster also Queue is used



here Queue stores some data b/w sender sends data fast & Receiver consumes slow : Queue stores data.

③ In OS (Semaphore) (there are sleeping processes waiting in a Queue when resource become available one of them wakes up and uses the resource), FCFS (First come First serve), Spooling (used in printer b/w printer serves one page at a time), buffer for devices like Keyboard.

④ In Mail Queue (mail server), in CN what get server don't get Queue until until consumer take

⑤ Variation - Dqueue, Priority Queue, Doubly Ended Priority Queue

We are about Array concept

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Date _____

Page _____

→ Any Implementation of Queue: → all O(1)

short Queue

```
{ int +an;  
int front, cap, size;  
Queue(int c)  
{ an = new int[c];  
cap = c;  
front = 0;  
size = 0;  
}
```

```
& bool isFull() { return (cap == size); }  
bool isEmpty() { return (size == 0); }
```

```
int getFront()  
{ if (isEmpty())  
    return -1;  
else  
    return front;
```

```
int getRear()  
{ if (isEmpty())  
    return -1;  
else  
    return (front + size - 1) % cap;
```

```
void enqueue(int x)  
{ if (isFull()) return;  
int rear = getRear();  
rear = (rear + 1) % cap;  
an[rear] = x;  
size++;
```

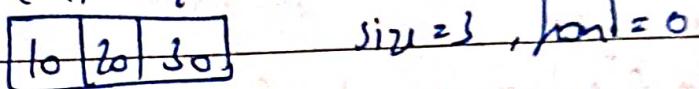
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Date _____
Page _____

```

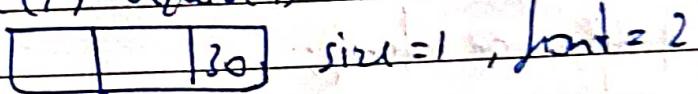
void dequeue()
{
    if (!IsEmpty())
        when;
    front = (front + 1) % cap;
    size--;
}

```

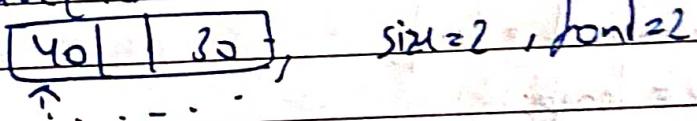
eg) $cap=3$, $size=0$, $front=0$
 $enqueue(10)$, $enqueue(20)$, $enqueue(30)$



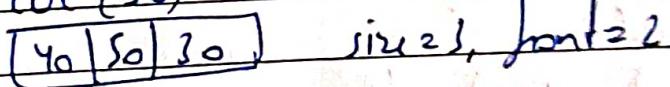
$dequeue()$, $dequeue()$



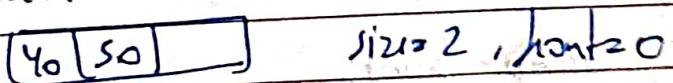
$enqueue(40)$



$enqueue(50)$



$dequeue()$



→ linked list implementation of Queue :

```

struct Node
{
    int data;
    Node *next;
    Node(int x)
    {
        data=x;
        next=NULL;
    }
};

```



short Queue

{ Node *front, *rear;

int size;

Queue()

{ front=NULL;

rear=NULL; size=0; }

void enqueue(int x)

{

Node *temp = new Node(x); size++;

if (front == NULL)

{ front=rear=temp;

return;

}

rear->next = temp;

rear = temp;

}

void dequeue()

{ if (front == NULL) return;

size--;

Node *temp = front;

front = front->next;

if (front == NULL)

rear=NULL;

delete(temp);

}

int void getSize() { return size; }

void int getFront { return front->data; } edge case

int int getRear { return rear->data; } null state

(current state:

30

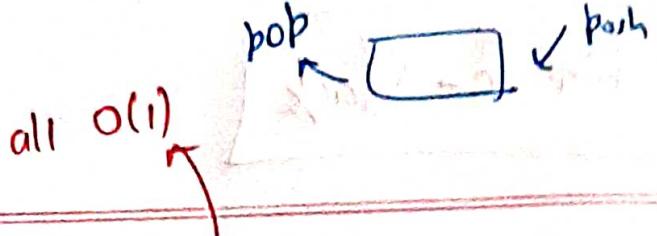
front rear → front=rear=NULL

dequeue()

enqueue(10)

rear front=rear=NULL

front 10 rear



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Date _____

Page _____

→ Queue in STL :

- * ① q.push(x) : add element x at the end of queue
- ② q.pop() : delete last " of the queue
- ③ q.size() : return size of queue
- ④ q.empty() : return 1 if q empty or 0.
- ⑤ q.front() : return reference to the first element of the q
- ⑥ q.back() : _____ last

- ⑦ q.swap() : exchange content of 2 different queue (q1.swap(q2)).
- ⑧ q.emplace() : new element is added to the end of queue

queue<int> q;

q.push(10);

q.push(20), q.push(30)

10	20	30
----	----	----

cout << q.front() << " " << q.back() << endl; 10 30

q.pop(); [20 30]

Traversing a Queue (We remove element from Queue)

while(q.empty() = false)

```
{ cout << q.front() << " "; }      10 20 30
q.pop(); }
```

→ Queue is implemented using Dequeue.

→ Queue is also contains adapter.

Reverse करना 4 - Stack

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Date _____

Page _____

I) Reverse a Queue:

Input {10, 5, 9, 13} Output {13, 9, 5, 10}

a) Iterative (Using Stack)

```
void f(queue<int> q)
{
    stack<int> st;
    while(!q.empty())
    {
        st.push(q.top());
        q.pop();
    }
    while(!st.empty())
    {
        q.push(st.top());
        st.pop();
    }
}
```

q.pop()

b) Recursive

```
void reverse(queue<int> &q)
```

```
{
    if(q.empty())
        return;
    int x = q.top();
    q.pop();
    reverse(q);
    q.push(x);
}
```



↑ q.pop()

↑ q.top()

II) Gas Station

- There are n gas stations in circular route.
- $gas[i]$ - gas at i^{th} station
- $cost[i]$ - cost to travel from i^{th} sta. to $(i+1)^{th}$ station of gas
- return index from which you can travel whole circle min

int l(vector<int> &g, vector<int> &c)

{ int total = 0, fuel = 0, ans = 0;

for(int i=0 ; i < g.size() ; i++)

 fuel += g[i] - c[i];

 if(fuel < 0)

 fuel = 0;

 ans = i+1; // new answer may be

-1 if total < 0
total sum of profit/gas
less than distance/rate

 total += g[i] - c[i];

when (total < 0 ? -1 : ans);

e.g. [1, 2, 3, 4, 5] → g o/p - index > 9

& [3, 4, 5, 1, 2] → c

i=0 fuel = -2

fuel < 0

fuel = 0

ans = 1

total = -2

i=1 fuel = -2

(-2 < 0) fuel < 0

fuel = 0

ans = 2

total = -2 + (-2) = -4

i=2 (-2 < 0) fuel < 0

fuel = 0

ans = 3

total = -4 + (-2)

= -6

i=3

fuel = 3

total = -6 + 3

= -3

i=4

fuel = 6

total = -3 + 3

= 0

total < 0 X when ans > 4

e.g. [

--- [] ---]

let say ans = 3 is answer but

first with fuel < 0 is

lets say 4 & index 4, ans = 4 is

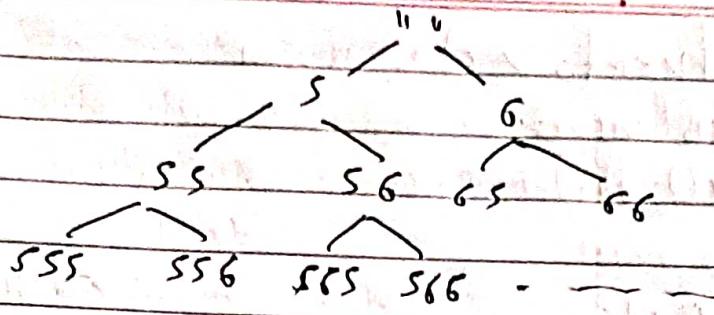
not the correct answer

Q: Generate numbers with given digits :

Given a no. n, print n no. in increasing order such that all these numbers have digits in set {5, 6}.

e.g. n=10

o/p 5, 6, 55, 56, 555, 556, 565, 566, 5555, 5556



`vector<string> f(int n)`

{ `vector<string> ans;`

`queue<string> q;`

`q.push("5");`

`q.push("6");`

`for (int i=0; i < n; i++)`

 {

`string run = q.top();`

`ans.push_back(run);`

`q.pop();`

`q.push(run + "5");`

`q.push(run + "6");`

 }

`n=4 i=0 [S|6] ← 2 [S] ← ,`

`[6|ss|s6]`

`i=1 [6|ss|s6] [S|6] ← ,`

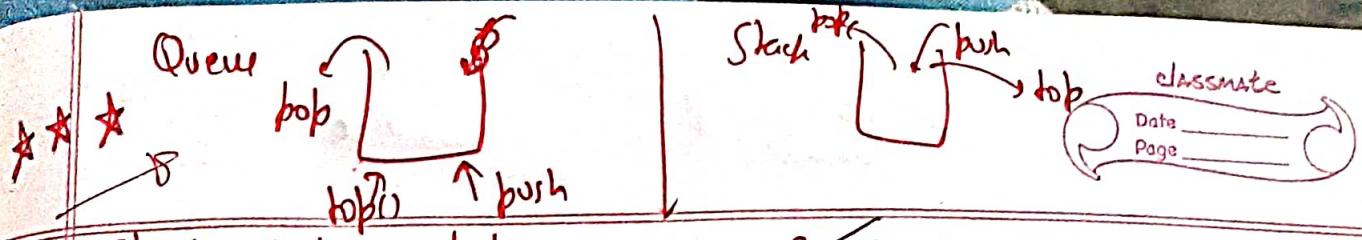
`ss|sc|6s|66`

`i=2 [ss|s6|6s|66] [S|6|ss] ← ,`

`s6|6s|66|sss|ss6`

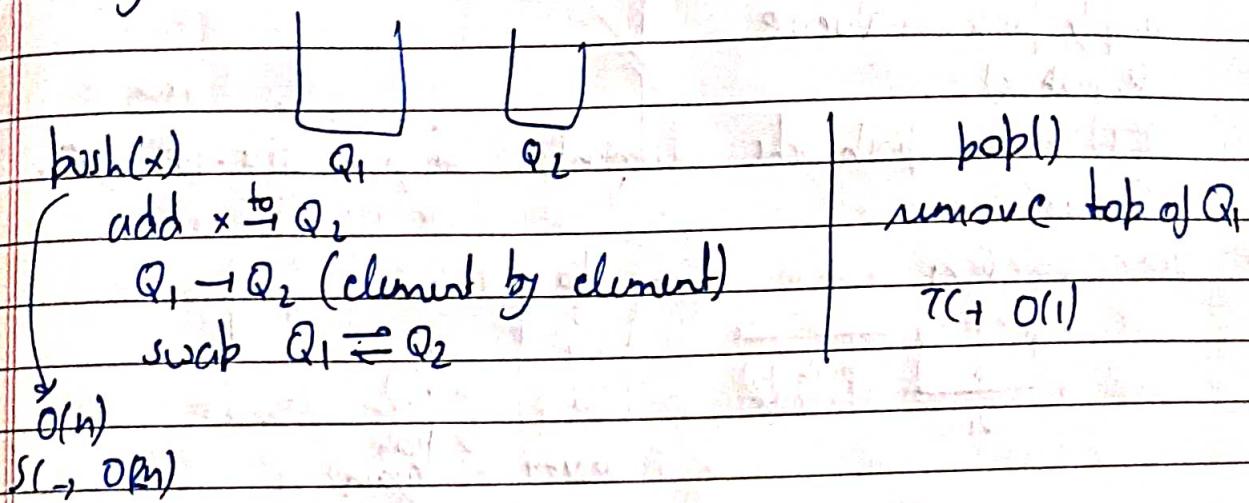
`i=3 [ss|cs|cs|ss|sss|ss6] [S|6|ss|ss] ← ,`

`cs|cs|ss|sc|ss|sc`

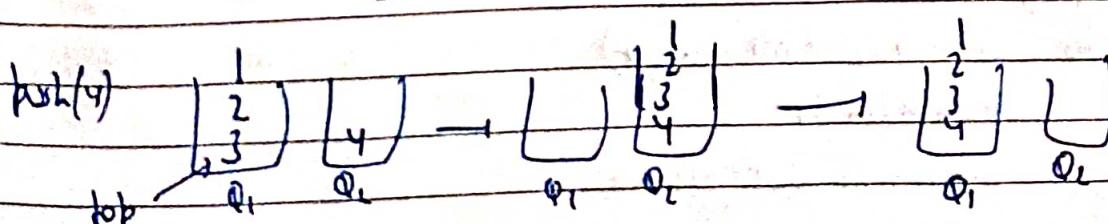
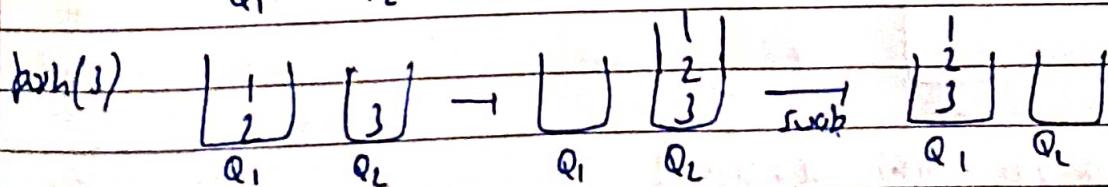
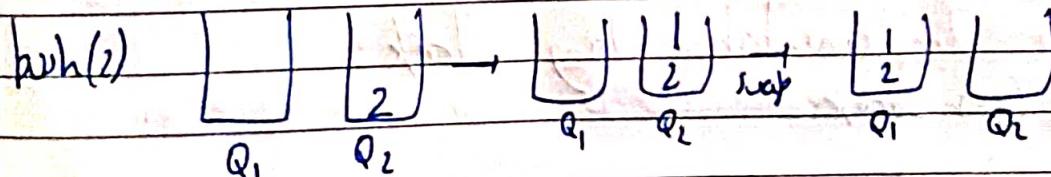
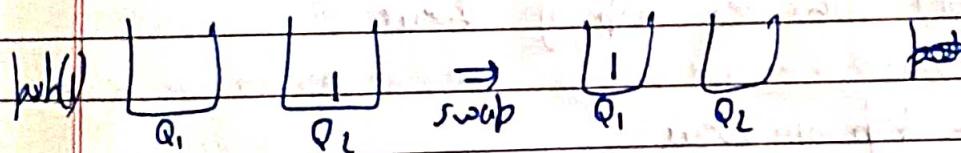


→ Stack Implementation using a Single Queue:

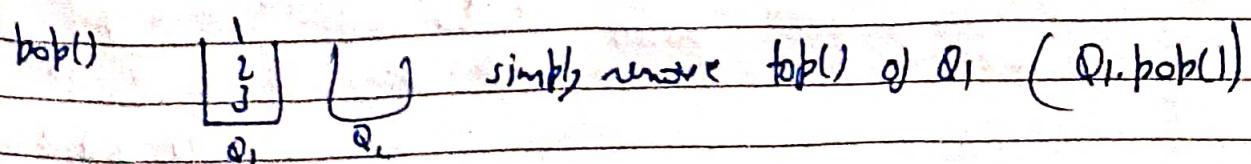
a) Using Two Queue



e.g. push(1), push(2), pop(), push(4), pop(), top()

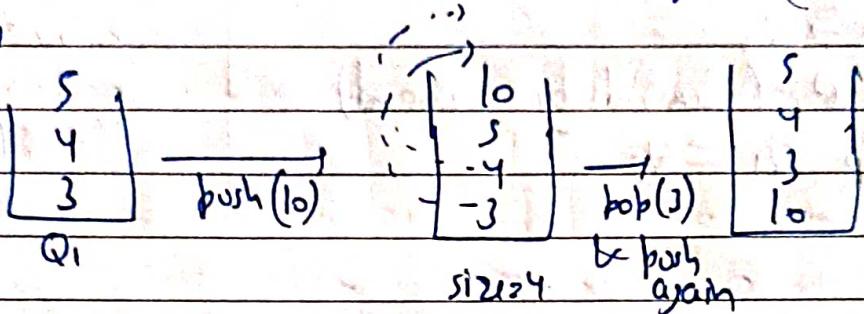


~~top()~~ ~~push(4)~~ when $Q_1.\text{top}() \rightarrow 4$

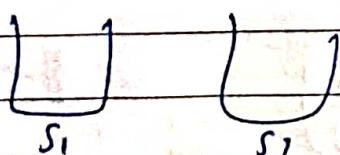
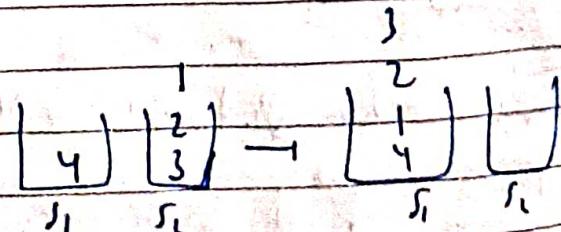
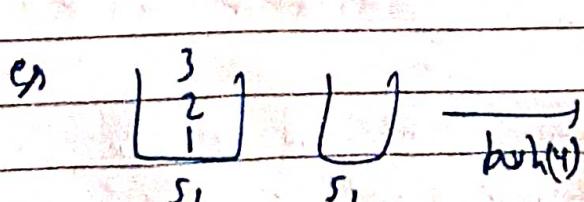


b) Using One Queue $\text{push}(x)$ $O(n)$ $SC = O(n)$

simply push in Queue

 $Q.\text{push}(x)$ ~~at~~ then push the elements from $(size - 1)$ again in Queue $O(1)$ $\rightarrow \text{pop}()$ simply $Q.\text{pop}()$ removes top of Queue $\text{top}()$ $Q.\text{top}()$ when top of QueueQueue Implementation Using Stack:

a) Using Two Stack.

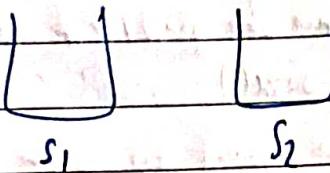
 $\text{push}(x)$ $O(n)$ $SC = O(2n)$ do $S_1 \rightarrow S_2$ (all element) $\text{push}(x)$ in S_1 $S_2 \rightarrow S_1$ (all element)

$O(1)$

\bullet $\text{pop}()$
 $s_1.\text{pop}()$

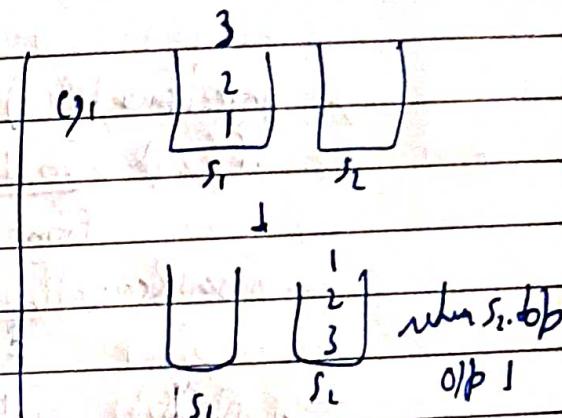
\bullet $\text{top}()$
 $s_1.\text{top}()$

- b) $\text{push}(x)$ Using two stack only code & operation is less
 $\text{push}(x)$
simply push to s_1 , $O(1)$



$\text{pop}()$
 $\text{top}() \Rightarrow \text{empty}$

- If $s_2 == \text{empty}$
 $\text{push } s_1 \text{ in } s_2 \text{ then return } s_2.\text{top}()$
- If $s_2 != \text{empty}$
return $s_2.\text{top}()$



$\text{pop}()$

- If $s_2 == \text{empty}$
 $\text{push } s_1 \text{ in } s_2 \text{ then do } s_2.\text{pop}()$
- If $s_2 != \text{empty}$
simply $s_2.\text{pop}()$

* $\text{top}()$ & $\text{pop}()$ are $O(1)$ amortized complexity (means maximum
at $O(1)$ but ~~at $O(n)$~~)