## $\begin{array}{c} {\rm UMC~202} \\ {\rm PROBLEM~SET~7} \end{array}$

(1) Use two step Adam-Bashforth explicit method to approximate the solutions of the following initial value problems. Compute the value of the solution at the end point of the interval and find the error

$$y' = y - t^2 + 1$$
,  $0 \le t \le 2$ ,  $y(0) = 0.5$ , exact solution  $y(t) = (t+1)^2 - 0.5 e^t$ .

- (2) Redo problem 1 by the two step Adams Moulton implicit method. Compare the results with Adam-Bashforth explicit method.
- (3) Redo problem 1 by the three step Adams Bashforth explicit method and three step Adams Moulton implicit method. Compare the results.
- (4) Apply the Adams fourth order predictor corrector method with h=0.2 and starting values are obtained from the Runge Kutta fourth order method to the initial value problem

$$y' = y - t^2 + 1$$
,  $0 \le t \le 2$ ,  $y(0) = 0.5$ .

(5) Transform the second order initial value problem

$$y'' - 2y' + 2y = e^{2t}$$
 sint for  $0 \le t \le 1$   
with  $y(0) = -0.4$ ,  $y'(0) = -0.6$ 

into a system of first order initial value problems, and use the Runge Kutta method with h=0.1 to approximate the solution.