

# Assignment 1

## Ncert Exemplar

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### I. QUESTION 10.13.2.10

I toss three coins together. The possible outcomes are no heads, 1 heads, 2 heads and 3 heads. So, I say that probability of no heads is  $1/4$ . What's wrong with this conclusion

#### **Solution:**

Let,  $p_X(X_i)$  be the sequence of independent Bernoulli random variables.

$$X_i = \begin{cases} 1, & \text{coin toss result in a Heads} \\ 0, & \text{result in Tails} \end{cases} \quad (1)$$

which means

$$p = p_X(X_i = 1) = 0.5 \quad (2)$$

$$q = p_X(X_i = 0) = 0.5 \quad (3)$$

For number of trials be  $n$  and the pmf of getting  $k$  heads is given by:

$$p_X(k) = {}^nC_k (p)^k (q)^{n-k} \quad (4)$$

$$= {}^nC_k (0.5)^k (0.5)^{n-k} \quad (5)$$

The cdf for pmf of  $n$  no. of trials is given by:

$$F_X(k) = \sum_{i=0}^k p_X(i) \quad (6)$$

$$= \sum_{k=0}^n {}^nC_k (0.5)^{n-k} (0.5)^k \quad (7)$$

Then cmf of getting no head after three toss is given by :

$$F_X(0) = p_X(0) = {}^3C_0 \times \left(\frac{1}{2}\right)^3 \times \left(\frac{1}{2}\right)^0 \quad (8)$$

$$= \frac{3!}{(3-0)! \times 0!} \times \frac{1}{2}^3 \quad (9)$$

$$= \frac{3!}{3! \times 1} \times \frac{1}{8} \quad (10)$$

$$= \frac{1}{8} \quad (11)$$

Hence, the given statement is wrong ( $\because \frac{1}{8} \neq \frac{1}{4}$ )