

10623 Midway Executive Summary

Improving Math Problem Solving with Long Context LLMs

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1 Introduction

We explore how increasing context lengths in modern LLMs can improve mathematical reasoning through many-shot in-context learning. Recent work has shown that using hundreds of examples in prompts can significantly boost performance on math tasks. We aim to validate these findings using open-source LLMs and investigate whether synthetic examples can match human-annotated data. Our approach focuses on re-implementing and extending the many-shot prompting techniques from ? using models like Llama with 128k context windows. We evaluate on the MATH and GSM8K datasets, expecting to demonstrate that increasing the number of in-context examples improves performance regardless of example quality. Our preliminary results with baseline few-shot prompting show promise, and we plan to systematically compare supervised and unsupervised many-shot approaches.

2 Dataset & Task

We evaluate on two mathematical reasoning datasets - MATH and GSM8K. Our primary metric is exact match accuracy between model outputs and ground truth solutions.

2.1 MATH

The MATH dataset ? contains 12,500 high school-level math problems from competitive math events. Each problem requires producing a normalized final answer (e.g. $\frac{2}{3}$). Problems are categorized by difficulty (1-5) across seven mathematical domains. The dataset tests complex mathematical reasoning and step-by-step problem solving.

2.2 GSM8K

GSM8K ? comprises 8,500 grade school math word problems (7,500 train, 1,000 test). Problems require 2-8 solution steps, with human-written natural language solutions. While problems aren't categorized by topic, answers are exact for reliable evaluation.

3 Related Work

3.1 Many-Shot In-Context Learning

Recent work ? demonstrated significant gains using many-shot prompting with Gemini 1.5 Pro's long context. They explored both supervised and unsupervised approaches, showing 7.9-9

3.2 Long Context Benefits

Studies ? show performance scales with more examples, though with diminishing returns. Long-context models are less sensitive to example ordering compared to short-context ones.

3.3 RAG with Long Context

Research ? reveals initial benefits from increased context in retrieval-augmented generation, but performance plateaus with too many retrieved passages.

3.4 Information Positioning Effects

Analysis ? shows performance varies based on information location - stronger when relevant content appears at prompt start/end versus middle.

4 Approach

We are implementing a systematic evaluation of many-shot prompting techniques using open-source LLMs with 128k context windows. Our key components include:

- Baseline: Few-shot prompting with 3-5 examples
- Unsupervised many-shot: Up to 500 questions without answers
- Supervised many-shot: Questions with synthetic answers
- Efficient implementation using DsPY framework and prefix prompt caching

5 Experiments

We will conduct the following experimental evaluations:

5.1 Baseline Results

Current few-shot prompting results on our test sets: [Results to be added]

5.2 Scaling Analysis

We will evaluate performance vs number of examples (10 to 500): [Table/plot to be added showing accuracy vs. number of examples]

5.3 Example Quality Impact

Comparison of different example types: [Table comparing human-annotated vs synthetic data performance]

5.4 Model Size Effects

Performance across different model scales: [Table comparing results across model sizes]

6 Plan

Remaining project timeline:

- Week 1-2 (All members):
 - Complete baseline implementation
 - Initial experiments with few-shot prompting
- Week 3 (Anish, Rajeev):
 - Implement many-shot variations
 - Synthetic data generation
- Week 4 (Ajay, Rajeev):

- Run full experimental suite
- Analysis and documentation

References

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