3/27/2021 Feature_Selection

Best Practices: Feature Selection

The objective for creating this notebook is to understand below topics:

- Different types of Feature Selection Techniques
- Which technique to be applied on which kind of dataset
- How these techniques work and different from each other?
- Examples
- 1. Understanding Feature Selection
- 2. Regression problem

```
A. Case-1: Selecting only top 4 features: SelectKBest f_regression
```

- a. Case-1.2: Selecting only top 4 features with SelectPercentile
- B. Case-2: Selecting top 8 features instead of 4
- 3. Classification Problem
 - A. Case-1: Selecting top 5 features: f_classif
 - B. Case-2: Only Categorical Explanatory Variables:: Selecting only top 5 features
 - a. Difference between Sklearn Label and Ordinal Encoder
 - b. Mutual_info_classif
 - C. Case-3: Categorical Explanatory & Target Variables
 - a. Case-3.1: With Chi-Squared Scoring Function
 - b. Case-3.2: With Mutual Information Scoring Function
- 4. Feature Forward Selection
- 5. Backward Elimination
- 6. Bi-Directional Elimination
- 7. Lasso Regularization using **SelectFromModel**
- 8. Ridge Regularization using **SelectFromModel**
- 9. Permutation Importance

```
In [1]: import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt
    import seaborn as sns
    import scipy
```

Background

Feature Selection

- It is the process of selecting the most relevant subset of input features from the dataset. Below are some feature selection techniques.
- 1. Unsupervised: This type of feature selection techniques doesn't use the target variable
 - For example, such methods uses the correlation in the input features and remove the redundant variables
 - Low Variance Threshold and KNN based Laplacian Score
- 2. **Supervised**: This type of feature selection techniques uses the target variable

localhost:8888/lab 1/41

3/27/2021 Feature Selection

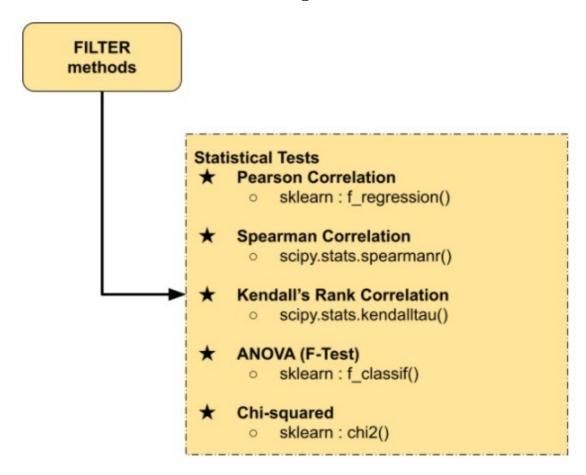
- For example, input features which are not explaining the variations in target variable are considereed as irrelevant variables thus got removed
- 2.1. Wrapper: Search for well-performing subsets of features on a machine learning model.
 - Forward Feature Selection(FFS), Backword Elimination(BE), Bi-Directional Elimination(RFE)
- 2.2. **Filter**: Select subsets of features based on their relationship with the target.
 - Statistical Methods like ANOVA, CHI, Kendall's, PCC and SPC
- 2.3 Embedded:
 - Information Therory: Algorithms that perform automatic feature selection during training.
 - Decision Trees and its extensions

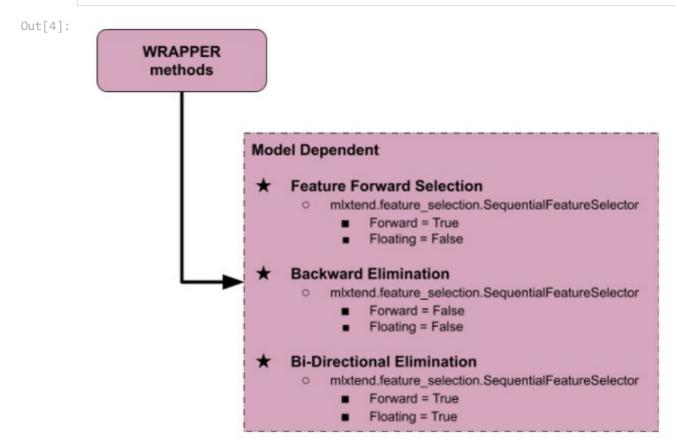
Out[1]: L2 Regn L1 Regn Permutation Model Importance Interpretability **Feature Selection** Feature Importance Low-variance threshold Supervised Unsupervised Laplacian score (KNN based) **EMBEDDED** WRAPPER methods **FILTER** methods methods Information Theory **Statistical Tests Model Dependent** Trees based models Pearson Correlation Feature Forward Selection **Decision Trees** Spearman Correlation **Backward Elimination** Random Forest Kendall's Rank Correlation Bi-Directional Elimination **Mutual Information** ANOVA (F-Test) mutual_info_classif() Chi Square Test mutual_info_regression()

Out[3]:

localhost:8888/lab 2/41

3/27/2021 Feature Selection





localhost:8888/lab 3/41

In [5]: from IPython.display import Image

path = 'E:\STUDY\PROJECTS\AAIC_Practice\MODULES\Module_3\Mod_3_Feature_Encoding\Feat
Image(filename = path + "1_4_Embedded_Methods.jpg", width=650, height=650)

Information Theory -- Mutual Information / Entropy
Rate

Models in-built (Tree based models)

CART

Sklearn: model.feature_importances_

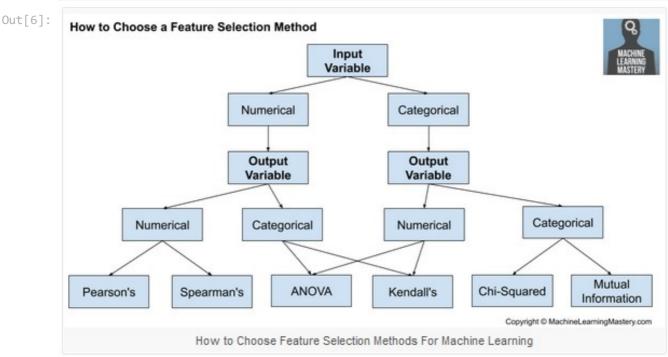
Random Forest
Sklearn: model.feature_importances_

Mutual Information (Features level)

sklearn: mutual_info_classif()
sklearn: mutual_info_regression()

In [6]: from IPython.display import Image

Thanks to Machine Learning Mastery (Jason Brownlee)
path = 'E:\STUDY\PROJECTS\AAIC_Practice\MODULES\Module_3\Mod_3_Feature_Encoding\Feat
Image(filename = path + "1_5_How_to_choose_Feature_Selection_Tech.jpg", width=750, h



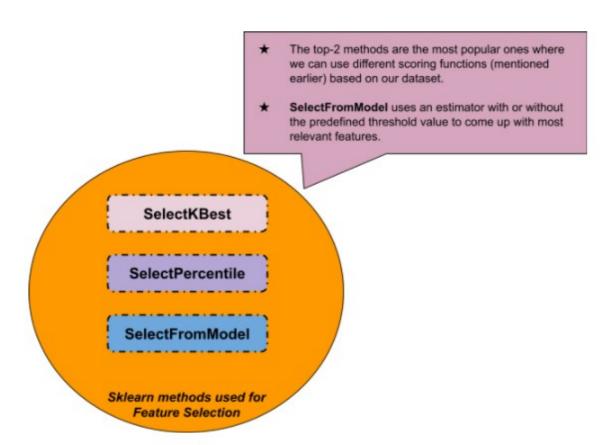
In [7]: from IPython.display import Image

localhost:8888/lab 4/41

3/27/2021 Feature Selection

path = 'E:\STUDY\PROJECTS\AAIC_Practice\MODULES\Module_3\Mod_3_Feature_Encoding\Feat
Image(filename = path + "1_6_Sklearn_selection_methods.jpg", width=800, height=800)

Out[7]:



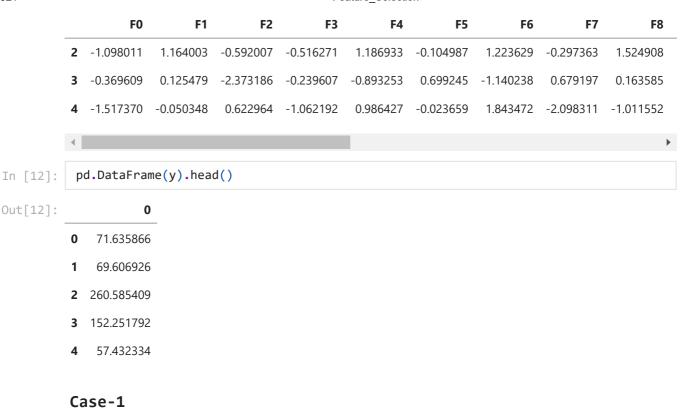
SelectKBest removes all but the highest scoring features

SelectPercentile removes all but a user-specified highest scoring percentage of features

Regression_Problem

```
In [8]:
           from sklearn.datasets import make_regression
           from sklearn.feature_selection import SelectKBest, SelectPercentile
           from sklearn.feature_selection import f_regression
           X, y = make_regression(n_samples=200,n_features=20,n_informative=10,n_targets=1,nois
 In [9]:
In [10]:
           col_names = ['F'+str(val) for val in range(20)]
           print(col names)
           X = pd.DataFrame(X,columns=col_names)
           print(X.shape, y.shape)
          ['F0', 'F1', 'F2', 'F3', 'F4', 'F5', 'F6', 'F7', 'F8', 'F9', 'F10', 'F11', 'F12', 'F13', 'F14', 'F15', 'F16', 'F17', 'F18', 'F19']
          (200, 20) (200,)
In [11]:
          X.head()
                                       F2
                                                  F3
                                                            F4
                                                                                                    F8
Out[11]:
                             F1
                                                                      F5
                                                                                F6
                                                                                          F7
             0.315769 0.750800 -1.159184
                                            0.819769
                                                      1.606124
                                                                0.446812
                                                                          2.038095
                                                                                     1.743551
                                                                                               0.792619
          1 -0.143725 -1.241941
                                  0.966777
                                            0.949195
                                                      0.964779
                                                                0.511315 -1.242663
                                                                                    -0.014709
                                                                                               0.546720
```

localhost:8888/lab 5/41



Selecting only top 4 features

```
In [13]: fs = SelectKBest(score_func=f_regression,k=4)
```

F_Regression

Univariate linear regression tests.

Linear model for testing the individual effect of each of many regressors. This is a scoring function to be used in a feature selection procedure, not a free standing feature selection procedure.

This is done in 2 steps:

```
- The correlation between each regressor and the target is computed, that is, ((X[:,i] - mean(X[:,i])) * (y - mean_y)) / (std(X[:,i]) * std(y)).
```

- It is converted to an F score then to a p-value.

```
fs.fit(X,y)
In [14]:
Out[14]: SelectKBest(k=4, score_func=<function f_regression at 0x0000019B05909C80>)
          fs selected features = pd.DataFrame(fs.transform(X))
In [15]:
           fs_selected_features.head()
Out[15]:
                   0
                             1
                                       2
                                                3
             0.446812
                       0.284038 -1.105044 0.052869
             0.511315
                       0.930303 -0.325833 0.722508
            -0.104987
                       2.203024 -0.858813 0.773638
```

localhost:8888/lab 6/41

```
0
                                        2
          3
              0.699245
                       -0.260664
                                -0.034045 0.552747
            -0.023659
                       0.688407
                                 1.017710 1.441373
           p_vals = np.round(pd.DataFrame(fs.pvalues_).T,5)
In [16]:
           p_vals.columns = col_names
           p_vals
                 F0
                                                                                         F10
Out[16]:
                         F1
                                 F2
                                        F3
                                                F4
                                                    F5
                                                            F6
                                                                     F7
                                                                             F8
                                                                                     F9
                                                                                                 F11
            0.37115 0.00002 0.23515 0.115 0.94458 0.0 0.00803 0.45473 0.00203 0.21641
                                                                                         0.0
           loc = 1.0
In [17]:
           alpha = 1 - loc
           manual_selected_cols = []
           for feature in col_names:
               if p_vals[feature].values == alpha:
                   manual_selected_cols.append(feature)
           manual_selected_cols
Out[17]: ['F5', 'F10', 'F15', 'F19']
```

In the above cell, I have selected the Level of Confidence as 100% for testing purpose but we can select any threshold value. The only point here is that the higher this value the more relevant features are selected.

The SelectKBest works on the basis of selecting the top-k features with minimum p-vals or maximum F-statistic.

```
## F-value or F-statstic calculated based on the linear regression test
In [18]:
          np.round(fs.scores_,1)
         array([ 0.8, 19.7, 1.4, 2.5, 0., 41.2, 7.2, 0.6, 9.8, 1.5, 88.2,
                 0., 4.1, 13.3, 0.1, 22., 0., 0.3, 7.4, 64.5])
          f_stats, p_vals = fs.score_func(X,y)
          pd.DataFrame(np.round(f stats,3)).T
In [20]:
Out[20]:
                                                                    9
                                                                         10
               0
                           2
                                 3
                                              5
                                                   6
                                                        7
                                                                               11
                                                                                     12
                                                                                            13
         0 0.803 19.691 1.418 2.506 0.005 41.221 7.17 0.561 9.781 1.538 88.241 0.032 4.056 13.323
```

Here, if we see the test statistic value of features (F5, F10, F15 and F19) are extremely high as compared to others. Thus, we can say that these are the top 4 features who are rejecting the null hypothesis i.e. no linear relation exists.

```
In [21]: pd.DataFrame(np.round(p_vals,5)).T
Out[21]: 0 1 2 3 4 5 6 7 8 9 10 11
```

localhost:8888/lab 7/41

3/27/2021

```
0
                                          5
                                                  6
                                                                            10
                                                                                      11
                              3
0 0.37115 0.00002 0.23515 0.115 0.94458 0.0 0.00803 0.45473 0.00203 0.21641 0.0 0.85823 (
```

P-values of features(F5, F10, F15 and F19) are also highly significant, also looking at the p-value of feature F1 suggests that it can be potentially the

```
5th best feature in this dataset.
          ## Manually selected top-4 features based on self provided alpha value
In [22]:
           X[manual_selected_cols].head()
                           F10
                                              F19
Out[22]:
                   F5
                                     F15
          0
             0.446812
                       0.284038
                                -1.105044 0.052869
             0.511315
                       0.930303
                                -0.325833 0.722508
          2
             -0.104987
                       2.203024
                                -0.858813 0.773638
             0.699245 -0.260664
                                -0.034045 0.552747
             -0.023659
                       0.688407
                                 1.017710 1.441373
          ## Features returned by SelectKBest
In [23]:
           fs_selected_features.head()
Out[23]:
                    0
                             1
                                       2
                                                3
                               -1.105044 0.052869
             0.446812
                       0.284038
             0.511315
                       0.930303 -0.325833 0.722508
             -0.104987
                       2.203024
                                -0.858813 0.773638
             0.699245
                      -0.260664
                                -0.034045 0.552747
                       0.688407
            -0.023659
                                 1.017710 1.441373
          for i in range(len(fs.scores_)):
In [24]:
               print('Feature %d: %f' % (i, fs.scores_[i]))
          Feature 0: 0.803444
          Feature 1: 19.690933
          Feature 2: 1.418082
          Feature 3: 2.506152
          Feature 4: 0.004845
          Feature 5: 41.220732
          Feature 6: 7.170474
          Feature 7: 0.561033
          Feature 8: 9.781180
          Feature 9: 1.537810
          Feature 10: 88.240872
          Feature 11: 0.031991
          Feature 12: 4.055694
          Feature 13: 13.322614
          Feature 14: 0.132082
          Feature 15: 22.042628
          Feature 16: 0.002107
          Feature 17: 0.339627
          Feature 18: 7.379732
          Feature 19: 64.500395
          x1,y1 = [i for i in range(len(fs.scores_))], fs.scores_
In [25]:
           data = pd.DataFrame({'x':x1,'y':y1})
```

localhost:8888/lab 8/41

```
with plt.style.context('seaborn'):
   plt.figure(figsize=(12,6))
   sns.barplot(data=data,x=x1,y=y1,palette='inferno')
   plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
   plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
    plt.xticks(style='oblique',size=10)
   plt.yticks(style='oblique',size=10)
   plt.show()
```



So, good here as everything matched and doubts are solved!!

Case-1.2

Selecting only top 4 features with SelectPercentile

```
# Total number of features in the dataset is 20; I'm selecting top 20% of relevant f
In [26]:
          fs_p = SelectPercentile(score_func=f_regression,percentile=20)
          fs_p.fit(X,y)
In [27]:
         SelectPercentile(percentile=20,
                            score_func=<function f_regression at 0x0000019B05909C80>)
          fs_selected_features = pd.DataFrame(fs_p.transform(X))
In [28]:
          fs_selected_features.head()
Out[28]:
                                                3
             0.446812
                       0.284038
                               -1.105044 0.052869
          1
             0.511315
                       0.930303 -0.325833 0.722508
            -0.104987
                       2.203024 -0.858813 0.773638
             0.699245
                      -0.260664
                               -0.034045 0.552747
          3
            -0.023659
                       0.688407
                                1.017710 1.441373
          p vals = np.round(pd.DataFrame(fs p.pvalues ).T,5)
In [29]:
          p vals.columns = col names
          p_vals
```

localhost:8888/lab 9/41

3/27/2021 Feature_Selection

```
F10
                                                                                                         F11
Out[29]:
                   F0
                            F1
                                     F2
                                           F3
                                                        F5
                                                                 F6
                                                                          F7
                                                                                   F8
                                                                                            F9
           0 0.37115 0.00002 0.23515 0.115 0.94458
                                                        0.0 0.00803 0.45473 0.00203 0.21641
                                                                                                     0.85823
                                                                                                 0.0
            X.head()
In [30]:
Out[30]:
                    F0
                               F1
                                          F2
                                                     F3
                                                               F4
                                                                          F5
                                                                                     F6
                                                                                               F7
                                                                                                          F8
                                   -1.159184
                                               0.819769
                                                          1.606124
                                                                    0.446812
                                                                               2.038095
               0.315769
                          0.750800
                                                                                          1.743551
                                                                                                    0.792619
              -0.143725
                         -1.241941
                                    0.966777
                                               0.949195
                                                         0.964779
                                                                    0.511315
                                                                              -1.242663
                                                                                         -0.014709
                                                                                                    0.546720
              -1.098011
                          1.164003
                                   -0.592007
                                              -0.516271
                                                          1.186933
                                                                   -0.104987
                                                                               1.223629
                                                                                         -0.297363
                                                                                                    1.524908
              -0.369609
                         0.125479
                                   -2.373186
                                              -0.239607
                                                         -0.893253
                                                                              -1.140238
                                                                                         0.679197
                                                                                                    0.163585
                                                                    0.699245
              -1.517370
                         -0.050348
                                    0.622964
                                              -1.062192
                                                         0.986427
                                                                   -0.023659
                                                                               1.843472 -2.098311
                                                                                                   -1.011552
            loc = 1.0
In [31]:
            alpha = 1 - loc
            manual_selected_cols = []
            for feature in col_names:
                 if p_vals[feature].values == alpha:
                     manual_selected_cols.append(feature)
            manual selected cols
Out[31]: ['F5', 'F10', 'F15', 'F19']
```

In the above cell, I have selected the Level of Confidence as 100% for testing purpose but we can select any threshold value. The only point here is that the higher this value the more relevant features are selected.

The SelectKBest works on the basis of selecting the top-k features with minimum p-vals or maximum F-statistic.

```
## F-value or F-statstic calculated based on the linear regression test
In [32]:
          np.round(fs_p.scores_,1)
         array([ 0.8, 19.7, 1.4, 2.5, 0., 41.2,
                                                     7.2,
                                                           0.6, 9.8,
Out[32]:
                 0., 4.1, 13.3, 0.1, 22., 0.,
                                                     0.3,
                                                           7.4, 64.51
          f_stats, p_vals = fs_p.score_func(X,y)
In [33]:
In [34]:
          pd.DataFrame(np.round(f_stats,3)).T
                                                        7
                                                                    9
                                                                          10
                                                                               11
Out[34]:
                                                   6
                                                                                     12
                                                                                            13
           0.803 19.691 1.418 2.506 0.005 41.221 7.17 0.561 9.781 1.538
                                                                      88.241
                                                                             0.032
                                                                                   4.056 13.323
```

Here, if we see the test statistic value of features (F5, F10, F15 and F19) are extremely high as compared to others. Thus, we can say that these are the top 4 features who are rejecting the null hypothesis i.e. no linear relation exists.

```
In [35]: pd.DataFrame(np.round(p_vals,5)).T
```

localhost:8888/lab 10/41

3/27/2021

Out[35]: 5 6 10 11 2 3 **0** 0.37115 0.00002 0.23515 0.115 0.94458 0.0 0.00803 0.45473 0.00203 0.21641 0.0 0.85823 (

P-values of features(F5, F10, F15 and F19) are also highly significant, also looking at the p-value of feature F1 suggests that it can be potentially the 5th best feature in this dataset.

```
## Manually selected top-4 features based on self provided alpha value
In [36]:
          X[manual_selected_cols].head()
```

```
F10
                                                   F19
Out[36]:
                    F5
                                         F15
           0
               0.446812
                          0.284038
                                   -1.105044 0.052869
               0.511315
                         0.930303
                                   -0.325833 0.722508
           2
              -0.104987
                          2.203024
                                   -0.858813 0.773638
               0.699245 -0.260664
                                   -0.034045 0.552747
           3
              -0.023659
                         0.688407
                                    1.017710 1.441373
```

```
## Features returned by SelectKBest
In [37]:
          fs_selected_features.head()
```

```
Out[37]:
                      0
                                 1
                                           2
                                                     3
                          0.284038
                                   -1.105044 0.052869
               0.446812
               0.511315
                         0.930303 -0.325833 0.722508
              -0.104987
                          2.203024
                                   -0.858813 0.773638
               0.699245
                         -0.260664
                                    -0.034045 0.552747
                         0.688407
              -0.023659
                                    1.017710 1.441373
```

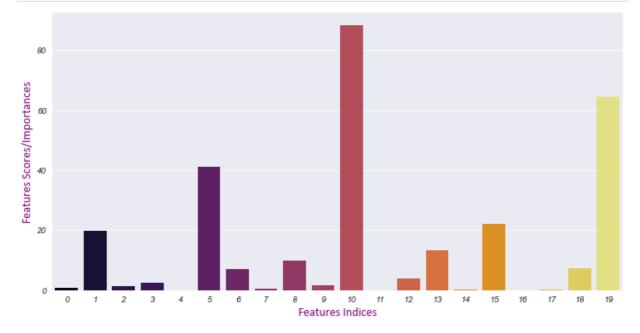
```
for i in range(len(fs_p.scores_)):
In [38]:
              print('Feature %d: %f' % (i, fs_p.scores_[i]))
```

Feature 0: 0.803444 Feature 1: 19.690933 Feature 2: 1.418082 Feature 3: 2.506152 Feature 4: 0.004845 Feature 5: 41.220732 Feature 6: 7.170474 Feature 7: 0.561033 Feature 8: 9.781180 Feature 9: 1.537810 Feature 10: 88.240872 Feature 11: 0.031991 Feature 12: 4.055694 Feature 13: 13.322614 Feature 14: 0.132082 Feature 15: 22.042628 Feature 16: 0.002107 Feature 17: 0.339627 Feature 18: 7.379732 Feature 19: 64.500395

```
x1,y1 = [i for i in range(len(fs_p.scores_))], fs_p.scores_
In [39]:
          data = pd.DataFrame({'x':x1,'y':y1})
```

localhost:8888/lab 11/41

```
with plt.style.context('seaborn'):
    plt.figure(figsize=(12,6))
    sns.barplot(data=data,x=x1,y=y1,palette='inferno')
    plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
    plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
        plt.xticks(style='oblique',size=10)
    plt.yticks(style='oblique',size=10)
    plt.show()
```



So, good here as every thing matched and doubts are solved!!

Case-2

Selecting top 8 features instead of 4

```
In [40]:
           fs = SelectKBest(score_func=f_regression,k=8)
In [41]:
           fs.fit(X,y)
          SelectKBest(k=8, score func=<function f regression at 0x0000019B05909C80>)
Out[41]:
           fs selected features = pd.DataFrame(fs.transform(X))
In [42]:
           fs selected features.head()
Out[42]:
                                         2
                                                   3
                                                             4
                                                                       5
                                                                                 6
                                                                                          7
                               1
                                                      -0.730733 -1.105044
              0.750800
                        0.446812
                                  0.792619
                                            0.284038
                                                                           0.036702 0.052869
             -1.241941
                        0.511315
                                  0.546720
                                            0.930303
                                                      -0.778257 -0.325833
                                                                          -0.095713 0.722508
              1.164003
                       -0.104987
                                  1.524908
                                            2.203024
                                                                -0.858813
                                                                                    0.773638
                                                       0.236323
                                                                           0.460964
              0.125479
                        0.699245
                                                                           0.197593 0.552747
          3
                                  0.163585
                                            -0.260664
                                                       1.669772
                                                                -0.034045
             -0.050348
                      -0.023659
                                 -1.011552
                                            0.688407
                                                     -1.175474
                                                                1.017710 -0.741902 1.441373
           p_vals = np.round(pd.DataFrame(fs.pvalues_).T,5)
In [43]:
           p_vals.columns = col_names
           p_vals
```

Out[43]:

3/27/2021 Feature Selection

```
F0
                         F1
                                                   F5
                                                                                        F10
                                                                                                F11
                                 F2
                                                            F6
                                                                    F7
                                                                                    F9
          0 0.37115 0.00002 0.23515 0.115 0.94458 0.0 0.00803 0.45473 0.00203 0.21641
                                                                                        0.0 0.85823
In [44]:
          loc = 0.99
           alpha = 1 - loc
           manual_selected_cols = []
           for feature in col names:
               if p vals[feature].values < alpha:</pre>
                   manual selected cols.append(feature)
           manual selected cols
Out[44]: ['F1', 'F5', 'F6', 'F8', 'F10', 'F13', 'F15', 'F18', 'F19']
```

In the above cell, I have selected the Level of Confidence as 99% instead of 100% because I'm increasing the number of relevant features.

The SelectKBest works on the basis of selecting the top-k features with minimum p-vals or maximum F-statistic.

```
## F-value or F-statstic calculated based on the linear regression test
In [45]:
           fs.scores
Out[45]: array([8.03444130e-01, 1.96909331e+01, 1.41808170e+00, 2.50615240e+00,
                  4.84485790e-03, 4.12207323e+01, 7.17047427e+00, 5.61033056e-01,
                  9.78117974e+00, 1.53780952e+00, 8.82408724e+01, 3.19905479e-02,
                  4.05569406e+00, 1.33226136e+01, 1.32082232e-01, 2.20426284e+01, 2.10745892e-03, 3.39626752e-01, 7.37973153e+00, 6.45003951e+01])
           f_stats, p_vals = fs.score_func(X,y)
In [46]:
In [47]:
           pd.DataFrame(np.round(f_stats,3)).T
Out[47]:
                                                         6
                                                                             9
                                                                                    10
                                                                                          11
                                                                                                 12
                                                                                                        13
           0 0.803 19.691 1.418 2.506 0.005 41.221 7.17 0.561 9.781 1.538
                                                                                88.241
                                                                                       0.032 4.056 13.323
```

Here, if we see the test statistic values of features (F1, F5, F6, F8, F10, F13, F15, F18 and F19) are high as compared to others. Thus, we can say that these are the top 8 features who are rejecting the null hypothesis i.e. no linear relation exists.

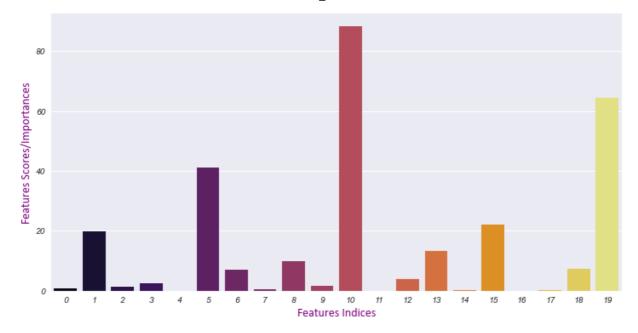
P-values of features(F1, F5, F6, F8, F10, F13, F15, F18 and F19) are also highly significant.

```
In [49]: ## Manually selected top-4 features based on self provided alpha value
    X[manual_selected_cols].head()
```

localhost:8888/lab 13/41

```
Out[49]:
                   F1
                             F5
                                                          F10
                                                                    F13
                                                                              F15
                                                                                        F18
                                                                                                 F19
                                       F6
                                                 F8
              0.750800
                        0.446812
                                  2.038095
                                            0.792619
                                                      0.284038
                                                              -0.730733 -1.105044
                                                                                    0.036702 0.052869
          0
             -1.241941
                        0.511315
                                 -1.242663
                                            0.546720
                                                      0.930303
                                                               -0.778257
                                                                        -0.325833
                                                                                   -0.095713 0.722508
          2
              1.164003
                       -0.104987
                                  1.223629
                                            1.524908
                                                      2.203024
                                                                0.236323
                                                                         -0.858813
                                                                                    0.460964 0.773638
          3
              0.125479
                        0.699245
                                 -1.140238
                                            0.163585
                                                     -0.260664
                                                                1.669772
                                                                         -0.034045
                                                                                    0.197593 0.552747
             -0.050348 -0.023659
                                  1.843472 -1.011552
                                                      0.688407 -1.175474
                                                                         1.017710 -0.741902 1.441373
           ## Features returned by SelectKBest
In [50]:
           fs_selected_features.head()
                                        2
                                                  3
                                                                      5
Out[50]:
                    0
                              1
                                                            4
                                                                                6
                                                                                         7
              0.750800
                        0.446812
                                  0.792619
                                            0.284038
                                                     -0.730733 -1.105044
                                                                          0.036702 0.052869
             -1.241941
                        0.511315
                                  0.546720
                                            0.930303
                                                     -0.778257 -0.325833
                                                                         -0.095713 0.722508
              1.164003
                       -0.104987
                                                      0.236323 -0.858813
          2
                                  1.524908
                                            2.203024
                                                                          0.460964 0.773638
              0.125479
                        0.699245
                                  0.163585
                                           -0.260664
                                                      1.669772
                                                               -0.034045
                                                                          0.197593 0.552747
             -0.050348 -0.023659 -1.011552
                                           0.688407 -1.175474
                                                               1.017710 -0.741902 1.441373
In [51]:
           for i in range(len(fs.scores_)):
               print('Feature %d: %f' % (i, fs.scores_[i]))
          Feature 0: 0.803444
          Feature 1: 19.690933
          Feature 2: 1.418082
          Feature 3: 2.506152
          Feature 4: 0.004845
          Feature 5: 41.220732
          Feature 6: 7.170474
          Feature 7: 0.561033
          Feature 8: 9.781180
          Feature 9: 1.537810
          Feature 10: 88.240872
          Feature 11: 0.031991
          Feature 12: 4.055694
          Feature 13: 13.322614
          Feature 14: 0.132082
          Feature 15: 22.042628
          Feature 16: 0.002107
          Feature 17: 0.339627
          Feature 18: 7.379732
          Feature 19: 64.500395
In [52]:
           x1,y1 = [i for i in range(len(fs.scores ))], fs.scores
           data = pd.DataFrame({'x':x1,'y':y1})
           with plt.style.context('seaborn'):
               plt.figure(figsize=(12,6))
               sns.barplot(data=data,x=x1,y=y1,palette='inferno')
               plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
               plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
               plt.xticks(style='oblique', size=10)
               plt.yticks(style='oblique', size=10)
               plt.show()
```

localhost:8888/lab 14/41



So, good here as everything matched and doubts are solved!!

The point to remember here is that SelectKBest runs a statistical test(passed as an input parameter) or a scoring_function at the backend and based on p-values or test statistics it filters the top dataset representing features.

Classification_Problem

```
from sklearn.datasets import make_classification
In [53]:
           from sklearn.feature_selection import f_classif, chi2, mutual_info_classif, mutual_i
           X, y = make_classification(n_samples=200,n_features=15,n_informative=6,n_classes=3)
In [54]:
           X.shape, y.shape
In [55]:
          ((200, 15), (200,))
Out[55]:
In [56]:
           col_names = ['F'+str(val) for val in range(15)]
           print(col_names)
           X = pd.DataFrame(X,columns=col names)
           print(X.shape, y.shape)
          ['F0', 'F1', 'F2', 'F3', 'F4', 'F5', 'F6', 'F7', 'F8', 'F9', 'F10', 'F11', 'F12', 'F
          13', 'F14']
          (200, 15) (200,)
In [57]:
           X.head()
                                                  F3
                                                             F4
                                                                       F5
Out[57]:
                    F0
                              F1
                                        F2
                                                                                 F6
                                                                                           F7
                                                                                                     F8
          0
              0.617210
                        0.077013
                                  -0.894102
                                            -0.781200
                                                       1.433713
                                                                 -0.656310
                                                                            1.233136
                                                                                      0.889938
                                                                                                2.348430
             -0.550493
                        -0.635994
                                  -0.315456
                                            -2.021173
                                                      -3.234403
                                                                 1.008197
                                                                            3.562111
                                                                                      0.252936
                                                                                                0.113089
          2
              0.737995
                        -1.563568
                                  -3.159686
                                            -0.559418
                                                       0.963973
                                                                 1.843948
                                                                            1.642310
                                                                                     -0.432715
                                                                                               -0.293203
              1.189695
                        -0.675657
                                  -1.026329
                                                                           -0.150608
                                                                                     -0.240283
          3
                                            -1.739962
                                                       1.326861
                                                                 0.250127
                                                                                                1.222818
                       -1.938871
                                                                                      2.207218
                                                                                                0.070794
              0.831337
                                   0.438057
                                             1.947839
                                                       1.245345
                                                                 0.525033
                                                                            0.623199
```

localhost:8888/lab 15/41

3/27/2021 Feature Selection

In [58]:

np.unique(y), np.bincount(y), pd.DataFrame(y).head()

```
(array([0, 1, 2]),
Out[58]:
           array([67, 67, 66], dtype=int64),
           0
              0
           1
              0
           2
             0
           3
              1
              2)
          Case:1
         Selecting only top 5 features
          fs = SelectKBest(score_func=f_classif,k=5)
In [59]:
         F Classif
         Compute the ANOVA F-value for the provided sample.
          fs.fit(X,y)
In [60]:
Out[60]: SelectKBest(k=5)
           fs_selected_features = pd.DataFrame(fs.transform(X))
In [61]:
           fs_selected_features.head()
Out[61]:
                             1
                                                 3
                                                          4
            -0.781200
                       1.433713
                                 0.889938
                                           2.307657
                                                    3.410207
          1 -2.021173 -3.234403
                                 0.252936 -2.619302 -0.167694
            -0.559418
                      0.963973 -0.432715
                                          3.295914
                                                    2.142418
            -1.739962
                       1.326861 -0.240283 -0.825527 -1.019253
             1.947839
                       1.245345
                                 2.207218
                                          0.021330
                                                    3.189145
In [62]:
           p_vals = np.round(pd.DataFrame(fs.pvalues_).T,5)
           p_vals.columns = col_names
           p_vals
                 F0
                                                                                    F10
                         F1
                                                  F5
                                                          F6
                                                                  F7
                                                                          F8
                                                                                 F9
                                                                                             F11
Out[62]:
                                 F2 F3
                                         F4
          0 0.38543 0.93467 0.00293 0.0 0.0 0.87692 0.01381 0.00015 0.71355 0.2917
                                                                                     0.0 0.62029 0.2!
           loc = 0.99
In [63]:
           alpha = 1 - loc
           manual_selected_cols = []
           for feature in col names:
               if p vals[feature].values < alpha:</pre>
                   manual_selected_cols.append(feature)
           manual_selected_cols
Out[63]: ['F2', 'F3', 'F4', 'F7', 'F10', 'F13', 'F14']
```

localhost:8888/lab 16/41

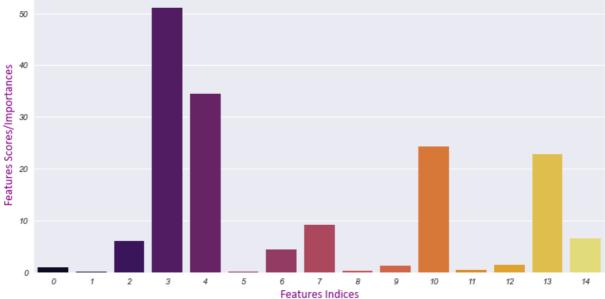
3/27/2021 Feature Selection

In the above cell, I have selected the Level of Confidence as 99% and based on it top-5 features are printed.

```
## F-value or F-statstic calculated based on the linear regression test
In [64]:
           fs.scores_
Out[64]: array([ 0.95801214,
                                0.06758588,
                                              6.00767971, 51.04637477, 34.4121281,
                                              9.20382652, 0.33808061, 1.23977527, 1.38023315, 22.86703697, 6.50653816])
                  0.13142818,
                                4.37647881,
                 24.25573132,
                                0.47872054,
           f_stats, p_vals = fs.score_func(X,y)
In [65]:
           pd.DataFrame(np.round(f_stats,3)).T
In [66]:
Out[66]:
                                                       6
                                                                    8
                                                                         9
                                                                               10
                                                                                     11
                                                                                          12
                                                                                                  13
             1.24
                                                                           24.256 0.479
                                                                                         1.38
                                                                                              22.867
         Here, if we see the test statistic values of features (F3, F4, F10, F7 and F13)
         are high as compared to others. Thus, we can say that these are the top 5
         features who are rejecting the null hypothesis i.e. no linear relation exists.
           pd.DataFrame(np.round(p_vals,5)).T
In [67]:
Out[67]:
                                   2
                                                   5
                                                                                   9
                                                                                      10
                                                                                              11
             0.38543 0.93467 0.00293 0.0 0.0 0.87692 0.01381 0.00015 0.71355 0.2917 0.0 0.62029 0.25
         P-values of features(F3, F4, F10, F7 and F13) are also highly significant.
In [68]:
           ## Manually selected top-4 features based on self provided alpha value
           X[manual_selected_cols].head()
                   F2
                             F3
                                      F4
                                                F7
                                                         F10
                                                                   F13
                                                                             F14
Out[68]:
            -0.894102
                      -0.781200
                                 1.433713
                                           0.889938
                                                     2.307657
                                                               3.410207
                                                                         1.551725
                       -2.021173
             -0.315456
                                -3.234403
                                           0.252936
                                                    -2.619302
                                                              -0.167694
                                                                         0.934084
             -3.159686
                       -0.559418
                                 0.963973
                                          -0.432715
                                                     3.295914
                                                               2.142418
                                                                         0.438327
             -1.026329
                       -1.739962
                                 1.326861
                                          -0.240283
                                                    -0.825527
                                                              -1.019253
                                                                        -1.158147
              0.438057
                       1.947839
                                 1.245345
                                           2.207218
                                                     0.021330
                                                               3.189145 -1.346295
           ## Features returned by SelectKBest
In [69]:
           fs selected features.head()
Out[69]:
                                        2
                                                 3
                                                           4
            -0.781200
                       1.433713
                                 0.889938
                                           2.307657
                                                     3.410207
             -2.021173
                       -3.234403
                                 0.252936
                                          -2.619302
                                                    -0.167694
             -0.559418
                       0.963973
                                 -0.432715
                                           3.295914
                                                     2.142418
          3
             -1.739962
                       1.326861
                                 -0.240283
                                          -0.825527
                                                    -1.019253
              1.947839
                       1.245345
                                 2.207218
                                           0.021330
                                                     3.189145
```

localhost:8888/lab 17/41

```
3/27/2021
    In [70]: | for i in range(len(fs.scores_)):
                   print('Feature %d: %f' % (i, fs.scores_[i]))
              Feature 0: 0.958012
              Feature 1: 0.067586
              Feature 2: 6.007680
              Feature 3: 51.046375
              Feature 4: 34.412128
              Feature 5: 0.131428
              Feature 6: 4.376479
              Feature 7: 9.203827
              Feature 8: 0.338081
              Feature 9: 1.239775
              Feature 10: 24.255731
              Feature 11: 0.478721
              Feature 12: 1.380233
              Feature 13: 22.867037
              Feature 14: 6.506538
              x1,y1 = [i for i in range(len(fs.scores_))], fs.scores_
    In [71]:
               data = pd.DataFrame({'x':x1,'y':y1})
               with plt.style.context('seaborn'):
                   plt.figure(figsize=(12,6))
                   sns.barplot(data=data,x=x1,y=y1,palette='inferno')
                   plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
                   plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
                   plt.xticks(style='oblique',size=10)
                   plt.yticks(style='oblique',size=10)
                   plt.show()
                50
```



So, good here as everything matched and doubts are solved!!

Case:2

Only Categorical Explanatory Variables :: Selecting only top 5 features

```
import scipy.io.arff as arff
In [72]:
          import os
In [73]:
          path = os.getcwd()
          file = path + '\\Autism-Child-Data.arff'
          print(file)
```

E:\STUDY\PROJECTS\AAIC Practice\MODULES\Module 3\Mod 3 Feature Encoding\Autism-Child

18/41 localhost:8888/lab

-Data.arff

```
In [74]:
              arff.loadarff(file)[1]
Out[74]: Dataset: child
                         A1 Score's type is nominal, range is ('0', '1')
                         A2 Score's type is nominal, range is ('0',
                         A3_Score's type is nominal, range is ('0', '1')
                         A4_Score's type is nominal, range is ('0', '1')
                         A5_Score's type is nominal, range is ('0', '1')
                         A6_Score's type is nominal, range is ('0', '1')
                         A7_Score's type is nominal, range is ('0', '1')
                         A8_Score's type is nominal, range is ('0', '1')
                         A9_Score's type is nominal, range is ('0', '1')
                         A10_Score's type is nominal, range is ('0', '1')
                         age's type is numeric
             gender's type is nominal, range is ('m', 'f')
ethnicity's type is nominal, range is ('Others', 'Middle Eastern ', 'White-E
uropean', 'Black', 'South Asian', 'Asian', 'Pasifika', 'Hispanic', 'Turkish', 'Latin
             o')
                         jundice's type is nominal, range is ('no', 'yes')
                         austim's type is nominal, range is ('no', 'yes')
             austim's type is nominal, range is ('no', 'yes')
contry_of_res's type is nominal, range is ('Jordan', 'United States', 'Egyp
t', 'United Kingdom', 'Bahrain', 'Austria', 'Kuwait', 'United Arab Emirates', 'Europ
e', 'Malta', 'Bulgaria', 'South Africa', 'India', 'Afghanistan', 'Georgia', 'New Zea
land', 'Syria', 'Iraq', 'Australia', 'Saudi Arabia', 'Armenia', 'Turkey', 'Pakista
n', 'Canada', 'Oman', 'Brazil', 'South Korea', 'Costa Rica', 'Sweden', 'Philippine
s', 'Malaysia', 'Argentina', 'Japan', 'Bangladesh', 'Qatar', 'Ireland', 'Romania',
'Netherlands', 'Lebanon', 'Germany', 'Latvia', 'Russia', 'Italy', 'China', 'Nigeri
a', 'U.S. Outlying Islands', 'Nepal', 'Mexico', 'Isle of Man', 'Libya', 'Ghana', 'Bh
             utan')
                         used_app_before's type is nominal, range is ('no', 'yes')
                         result's type is numeric
                         age_desc's type is nominal, range is ('4-11 years',)
                         relation's type is nominal, range is ('Parent', 'Self', 'Relative', 'Health
              care professional', 'self')
                         Class/ASD's type is nominal, range is ('NO', 'YES')
In [75]:
               def apply_decode(df_name):
                     Description: Function created for changing the character encoding
                     Input: It accepts one parameter:
                           df name : `Pandas DataFrame`
                     Return: `utf-8` encoded DataFrame
                     for col in df name.columns:
                           if df name[col].dtype != 'float64':
                                 df name[col] = df name[col].apply(lambda val : val.decode('utf-8'))
                     pd.set option('display.max columns',50)
                     return df name
In [76]:
               autism dataset = pd.DataFrame(arff.loadarff(file)[0])
               autism dataset.head()
Out[76]:
                  A1_Score A2_Score A3_Score A4_Score A5_Score A6_Score A7_Score A8_Score A9_Score A
              0
                                                                             b'1'
                                                                                                                    b'1'
                                                                                                                                  b'0'
                        b'1'
                                      b'1'
                                                   b'0'
                                                                b'0'
                                                                                          b'1'
                                                                                                        b'0'
              1
                        b'1'
                                      b'1'
                                                   b'0'
                                                                b'0'
                                                                             b'1'
                                                                                          b'1'
                                                                                                        b'0'
                                                                                                                    b'1'
                                                                                                                                  b'0'
              2
                        b'1'
                                      b'1'
                                                   b'0'
                                                                b'0'
                                                                             b'0'
                                                                                          b'1'
                                                                                                        b'1'
                                                                                                                    b'1'
                                                                                                                                  b'0'
```

localhost:8888/lab 19/41

b'0'

A1_Score A2_Score A3_Score A4_Score A5_Score A6_Score A7_Score A8_Score A9_Score A

b'1'

b'1'

b'0'

b'0'

b'0'

3

b'0'

b'1'

b'0'

	4	b'1'	b'1'	b'1'	b'1'	b'1'	b'1'	b'1'	b'1'	b'1'	
	5 rows ×	21 colun	nns								
	4										•
In [77]:	<pre>autism_df = apply_decode(autism_dataset)</pre>										
In [78]:	<pre>autism_df.head()</pre>										
Out[78]:	A1_S	core A2_	Score A3	_Score	A4_Score	A5_Score	A6_Score	A7_Score	A8_Score	A9_Score	A
	0	1	1	0	0	1	1	0	1	0	
	1	1	1	0	0	1	1	0	1	0	
	2	1	1	0	0	0	1	1	1	0	
	3	0	1	0	0	1	1	0	0	0	
	4	1	1	1	1	1	1	1	1	1	
	4										•
In [79]:	<pre>X_category_data = autism_df[['ethnicity', 'contry_of_res', 'relation']].copy(deep=Tr X_category_data.head()</pre>										
Out[79]:	ethnicity contry_of_res relation										
	0	Others	Jo	rdan	Parent						
	1 Midd	le Eastern	Jo	rdan	Parent						
	2	?	Jo	rdan	?						
	3	?	Jo	rdan	?						
	4	Others	United St	ates	Parent						
In [80]:	<pre>X_category_data = X_category_data.applymap(lambda val: None if val == '?' else val)</pre>										
In [81]:	X_category_data.isnull().sum()										
Out[81]:	ethnici contry_ relation dtype:	of_res	43 0 43								
In [82]:	<pre>X_category_data['ethnicity'].value_counts()</pre>										
Out[82]:	Asian	European Eastern Asian	108 46 27 21								

localhost:8888/lab 20/41

```
Others
                                14
          Black
                                14
          Latino
                                 8
                                 7
          Hispanic
          Pasifika
                                 2
          Turkish
                                 2
          Name: ethnicity, dtype: int64
In [83]:
          X_category_data['relation'].value_counts()
                                         214
          Parent
Out[83]:
                                          17
          Relative
                                          13
          Health care professional
          Self
                                           4
                                           1
          self
          Name: relation, dtype: int64
           X_category_data['ethnicity'].fillna(value='White-European',axis=0,inplace=True)
In [84]:
           X_category_data['relation'].fillna(value='Parent',axis=0,inplace=True)
In [85]:
           X_category_data.isnull().sum()
          ethnicity
                             0
Out[85]:
          contry_of_res
                            0
          relation
                             0
          dtype: int64
In [86]:
           X_category_data.head()
Out[86]:
                   ethnicity contry of res relation
          0
                     Others
                                  Jordan
                                           Parent
              Middle Eastern
                                  Jordan
          1
                                           Parent
             White-European
                                  Jordan
                                           Parent
             White-European
                                  Jordan
                                           Parent
                     Others
                             United States
                                           Parent
```

Diff_b/w_LE_and_OE

- 1. Both of these techniques performs the same function, as they do the numerical encoding on categorical data. Point to note that Ordinal Encoder sounds like it performs Ordinal numerical encoding on the data but it also fails to perform the semantic ordinal encoding.
 - For example; hot, cold, warm are labelled as cold, hot, warm by both the techniques whereas these should be labelled as cold < warm < hot.
 - We need to provide the explicit linking in order to perfrom semantic ordinal encoding.
- 1. Scikit learn has these 2 implementations for same task because Label Encoder is created for applying encoding of Target Variable and Ordinal Encoder for features.
 - Because,
 - LabelEncoder learns classes_
 - OrdinalEncoder learns categories_
 - And,
 - LabelEncoder expects 1D array i.e. Target Variable

from sklearn.preprocessing import LabelEncoder, OrdinalEncoder

OrdinalEncoder expects 2D array i.e. Features

localhost:8888/lab 21/41

```
Feature Selection
In [88]:
            le = LabelEncoder()
            oe = OrdinalEncoder()
In [89]:
            le.fit(X category data['ethnicity'])
          LabelEncoder()
Out[89]:
In [90]:
            le.classes
Out[90]: array(['Asian', 'Black', 'Hispanic', 'Latino', 'Middle Eastern ', 'Others', 'Pasifika', 'South Asian', 'Turkish', 'White-European'],
                  dtype=object)
          The above list of various categories are in the sequence of lables assigned
          to each category.
            • For example, 'Asian' -- 0, 'Black -- 1, 'Hispanic' -- 2 .... so on.
           X_category_data['ethnicity'] = le.transform(X_category_data['ethnicity'])
In [91]:
            X_category_data.head()
Out[91]:
              ethnicity contry_of_res relation
           0
                     5
                              Jordan
                                        Parent
           1
                     4
                              Jordan
                                        Parent
           2
                     9
                              Jordan
                                        Parent
           3
                     9
                              Jordan
                                        Parent
```

```
cntry_le = LabelEncoder()
In [92]:
          cntry_le.fit(X_category_data['contry_of_res'])
```

Out[92]: LabelEncoder()

5

United States

Parent

```
cntry_le.classes_
In [93]:
```

```
Out[93]: array(['Afghanistan', 'Argentina', 'Armenia', 'Australia', 'Austria',
                                   'Bahrain', 'Bangladesh', 'Bhutan', 'Brazil', 'Bulgaria', 'Canada', 'China', 'Costa Rica', 'Egypt', 'Europe', 'Georgia', 'Germany', 'Ghana', 'India', 'Iraq', 'Ireland', 'Isle of Man', 'Italy',
                                  'China', 'Costa Rica', 'Egypt', 'Europe', 'Georgia, Germa', 'India', 'Iraq', 'Ireland', 'Isle of Man', 'Italy 'Japan', 'Jordan', 'Kuwait', 'Latvia', 'Lebanon', 'Libya', 'Malaysia', 'Malta', 'Mexico', 'Nepal', 'Netherlands',
                                   'New Zealand', 'Nigeria', 'Oman', 'Pakistan', 'Philippines', 'Qatar', 'Romania', 'Russia', 'Saudi Arabia', 'South Africa',
                                   'South Korea', 'Sweden', 'Syria', 'Turkey', 'U.S. Outlying Islands', 'United Arab Emirates', 'United Kingdom',
                                   'United States'], dtype=object)
```

```
X_category_data['contry_of_res'] = cntry_le.transform(X_category_data['contry_of_res')
In [94]:
          X_category_data.head()
```

```
Out[94]:
               ethnicity contry_of_res relation
            0
                       5
                                     24
                                           Parent
            1
                      4
                                     24
                                           Parent
            2
                      9
                                     24
                                           Parent
            3
                       9
                                     24
                                           Parent
```

22/41 localhost:8888/lab

```
X category data['relation'] = X category data['relation'].apply(lambda val: str(val)
In [95]:
          X_category_data['relation'].value_counts()
         Parent
                                       257
Out[95]:
          Relative
                                        17
         Health care professional
                                        13
          Name: relation, dtype: int64
          oe.fit(X_category_data[['relation']])
In [96]:
Out[96]: OrdinalEncoder()
In [97]:
          oe.categories_
         [array(['Health care professional', 'Parent', 'Relative', 'Self'],
                 dtype=object)]
In [98]:
          X_category_data['relation'] = pd.DataFrame(oe.transform(X_category_data[['relation']
          X_category_data.head()
Out[98]:
             ethnicity contry_of_res relation
          0
                   5
                               24
                                       1.0
          1
                   4
                               24
                                       1.0
          2
                   9
                               24
                                       1.0
          3
                   9
                               24
                                       1.0
          4
                               51
                                       1.0
          pred_dict = {'NO':0,'YES':1}
In [99]:
          y_cat_data = autism_df['Class/ASD']
          y_cat_data = y_cat_data.apply(lambda val: pred_dict.get(val))
In [100...
          X_category_data.shape, y_cat_data.shape
Out[100... ((292, 3), (292,))
```

Mutual_info_classif

In [101...

ethnicity contry_of_res relation

51

Parent

5

4

• Estimate mutual information for a discrete target variable.

fs = SelectKBest(score_func=mutual_info_classif,k=1)

- Mutual information (MI) between two random variables is a non-negative value, which measures the dependency between the variables. It is equal to zero if and only if two random variables are independent, and higher values mean higher dependency.
- The term "discrete features" is used instead of naming them "categorical", because it describes the essence more accurately. For example, pixel intensities of an image are discrete features (but hardly categorical) and you will get better results if mark them as

localhost:8888/lab 23/41

3/27/2021 Feature Selection

such. Also note, that treating a continuous variable as discrete and vice versa will usually give incorrect results, so be attentive about that.

• True mutual information can't be negative. If its estimate turns out to be negative, it is replaced by zero.

```
fs.fit(X_category_data,y_cat_data)
In [102...
         SelectKBest(k=1,
Out[102...
                      score_func=<function mutual_info_classif at 0x0000019B05C91048>)
In [103...
          fs.scores_
         array([0.01284735, 0.03797437, 0.
                                                    ])
Out[103...
In [104...
          fs.score_func(X_category_data,y_cat_data)
Out[104... array([0.017547 , 0.06310153, 0.
                                                    1)
          pd.DataFrame(fs.transform(X_category_data)).head()
In [105...
               0
Out[105...
          0 24.0
          1 24.0
          2 24.0
          3 24.0
          4 51.0
In [106...
          for i in range(len(fs.scores_)):
               print('Feature %d: %f' % (i, fs.scores_[i]))
          Feature 0: 0.012847
          Feature 1: 0.037974
          Feature 2: 0.000000
In [107...
          x1,y1 = [i for i in range(len(fs.scores_))], fs.scores_
          data = pd.DataFrame({'x':x1,'y':y1})
          with plt.style.context('seaborn'):
               plt.figure(figsize=(12,6))
               sns.barplot(data=data,x=x1,y=y1,palette='inferno')
               plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
               plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
               plt.xticks(style='oblique', size=10)
               plt.yticks(style='oblique', size=10)
               plt.show()
```

localhost:8888/lab 24/41



Feature with maximum MI score is selected as the relevant feature. Now, looking at the scores we can say that these features have very slight dependency on the target variable.

Case: 3
Categorical Explanatory & Target Variables

```
In [108...
           from sklearn.model_selection import train_test_split
           from sklearn.impute import SimpleImputer
In [109...
           cat_data = pd.read_csv('https://raw.githubusercontent.com/jbrownlee/Datasets/master/
           X = cat_data.iloc[:,0:-1].copy(deep=True)
In [110...
           y = cat_data.iloc[:,-1].copy(deep=True)
In [111...
           X.shape, y.shape
Out[111... ((286, 9), (286,))
           X.isnull().sum()
In [112...
               0
Out[112...
          1
               0
          2
               0
          3
               0
               8
               0
          6
               0
          7
               1
          dtype: int64
           si = SimpleImputer(strategy='most_frequent')
In [113...
           X[4] = pd.DataFrame(si.fit_transform(X[[4]]))
In [114...
           X[7] = pd.DataFrame(si.fit_transform(X[[7]]))
In [115...
           X.head(), y.head()
In [116...
```

localhost:8888/lab 25/41

```
Out[116... (
                     a
                                                                                             8
                                                      'yes'
              '40-49'
                                    '15-19'
                                                             '3'
                                                                             'left_up'
                                              '0-2'
                                                                   'right'
                                                                                          'no'
           a
                        'premeno'
                            'ge40'
                                    '15-19'
                                                             '1'
              '50-59'
                                              '0-2'
                                                       'no'
                                                                   'right'
           1
                                                                             'central'
                                                                                          'no'
                            'ge40'
              '50-59'
                                                             '2'
                                                                   'left'
                                    '35-39'
                                              '0-2'
                                                      'no'
                                                                            'left_low'
                                                                                          'no'
           2
                                                      'yes'
              '40-49'
                                    '35-39'
                                              '0-2'
                                                             '3'
                                                                  'right'
                                                                            'left_low'
           3
                        'premeno'
                                                                                          'yes'
                                              '3-5'
           4
              '40-49'
                                    '30-34'
                                                     'yes'
                                                             '2'
                                                                   'left'
                                                                            'right_up'
                        'premeno'
                                                                                          'no',
           0
                    'recurrence-events'
           1
                'no-recurrence-events'
           2
                    'recurrence-events'
           3
                 'no-recurrence-events'
                    'recurrence-events'
           Name: 9, dtype: object)
           X_train, X_test, y_train, y_test = train_test_split(X,y,test_size=0.35,random_state=
In [117...
          X_train.shape, X_test.shape, y_train.shape, y_test.shape
In [118...
Out[118... ((185, 9), (101, 9), (185,), (101,))
In [119...
           oe = OrdinalEncoder()
           le = LabelEncoder()
In [120...
           oe.fit(X_train)
           le.fit(y_train)
Out[120... LabelEncoder()
In [121...
           X_train = oe.transform(X_train)
           X_test = oe.transform(X_test)
           y_train = le.transform(y_train)
           y_test = le.transform(y_test)
          X_train.shape, X_test.shape, y_train.shape, y_test.shape
In [122...
Out[122... ((185, 9), (101, 9), (185,), (101,))
```

Case:3.1

With Chi-Squared Scoring Function

```
In [123... fs = SelectKBest(score_func=chi2,k='all')
```

Chi-Squared

- Compute chi-squared stats between each non-negative feature and class.
- This score can be used to select the n_features features with the highest values for the
 test chi-squared statistic from X, which must contain only non-negative features such
 as booleans or frequencies (e.g., term counts in document classification), relative to
 the classes.

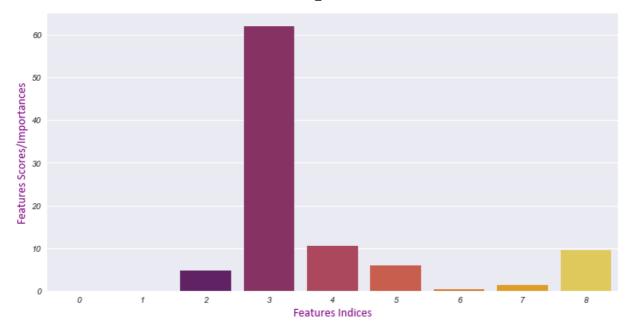
Recall that the chi-square test measures dependence between stochastic variables, so using this function "weeds out" the features that are the most likely to be independent of class and therefore irrelevant for classification.

```
In [124... fs.fit(X_train,y_train)
Out[124... SelectKBest(k='all', score_func=<function chi2 at 0x0000019B05909AE8>)
```

localhost:8888/lab 26/41

```
pd.DataFrame(fs.transform(X_train)).head()
In [125...
Out[125...
              0
                      2
                          3
                                   5
                                       6
                                           7
            3.0 0.0 7.0 0.0 0.0 1.0 0.0
                                              0.0
                                         1.0
            2.0 0.0 3.0 0.0 0.0 2.0 0.0
                                         1.0
                                              0.0
                2.0 5.0 0.0 0.0 2.0 0.0
            3.0
                                         1.0
                                              0.0
            3.0 0.0 4.0 0.0 0.0 2.0
                                     0.0
                                         4.0
                                              0.0
          4 2.0 2.0 3.0 0.0 0.0 1.0 0.0 1.0 0.0
          pd.DataFrame(fs.transform(X_test)).head()
In [126...
Out[126...
                      2
                          3
                                   5
                                       6
                                           7
                                               8
                  1
          0
            3.0 0.0 5.0 0.0 0.0 0.0 0.0
                                         2.0
                                              0.0
            3.0 1.0 3.0 0.0 0.0 0.0 0.0
                                         2.0 0.0
            2.0 2.0 4.0 0.0
                            0.0
                                 2.0 0.0
                                         4.0
                                              0.0
            2.0 2.0 6.0 6.0
                            1.0 1.0
                                     1.0
                                         4.0
                                             1.0
            3.0 2.0 4.0 0.0 0.0 0.0 1.0 2.0 0.0
In [127...
          for i in range(len(fs.scores_)):
               print('Feature %d: %f' % (i, fs.scores_[i]))
          Feature 0: 0.004460
          Feature 1: 0.043274
          Feature 2: 4.807863
          Feature 3: 61.981838
          Feature 4: 10.479021
          Feature 5: 6.011364
          Feature 6: 0.294110
          Feature 7: 1.365009
          Feature 8: 9.455277
          x1,y1 = [i for i in range(len(fs.scores_))], fs.scores_
In [128...
          data = pd.DataFrame({'x':x1,'y':y1})
           with plt.style.context('seaborn'):
               plt.figure(figsize=(12,6))
               sns.barplot(data=data,x=x1,y=y1,palette='inferno')
               plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
               plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
               plt.xticks(style='oblique',size=10)
               plt.yticks(style='oblique', size=10)
               plt.show()
```

localhost:8888/lab 27/41



Case:3.2

With Mutual Information Scoring Function

```
In [129...
           fs = SelectKBest(score_func=mutual_info_classif,k='all')
In [130...
           fs.fit(X_train,y_train)
          SelectKBest(k='all',
Out[130...
                       score_func=<function mutual_info_classif at 0x0000019B05C91048>)
In [131...
           pd.DataFrame(fs.transform(X_train)).head()
Out[131...
                       2
                           3
                                    5
                                        6
                                            7
                                                8
                 0.0 7.0 0.0
                              0.0 1.0
                                      0.0
                                           1.0
             2.0 0.0 3.0 0.0 0.0
                                  2.0 0.0
                                           1.0
                                               0.0
             3.0
                 2.0 5.0 0.0
                              0.0
                                  2.0
                                      0.0
                                           1.0
             3.0 0.0 4.0 0.0
                                  2.0
                              0.0
                                      0.0
                                           4.0
                                               0.0
          4 2.0 2.0 3.0 0.0 0.0 1.0 0.0
                                          1.0 0.0
In [132...
           pd.DataFrame(fs.transform(X_test)).head()
Out[132...
                       2
                           3
                                    5
            3.0 0.0
                    5.0 0.0
                              0.0 0.0
                                      0.0
                                           2.0
                                              0.0
             3.0
                 1.0
                     3.0
                         0.0
                              0.0
                                  0.0
                                      0.0
                                           2.0
            2.0 2.0 4.0 0.0 0.0 2.0 0.0
                                          4.0
                                               0.0
             2.0
                 2.0 6.0
                          6.0
                              1.0
                                  1.0
                                      1.0
                                          4.0
          4 3.0 2.0 4.0 0.0 0.0 0.0 1.0 2.0 0.0
In [133...
           for i in range(len(fs.scores_)):
               print('Feature %d: %f' % (i, fs.scores_[i]))
```

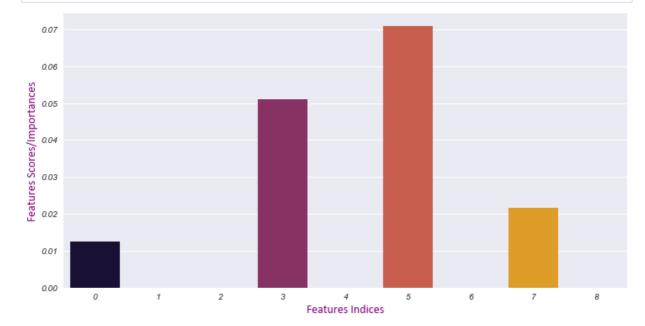
Feature 1: 0.000000

Feature 0: 0.012467

```
Feature 2: 0.000000
Feature 3: 0.050990
Feature 4: 0.000000
Feature 5: 0.070850
Feature 6: 0.000000
Feature 7: 0.021693
Feature 8: 0.000000
```

```
In [134... x1,y1 = [i for i in range(len(fs.scores_))], fs.scores_
data = pd.DataFrame({'x':x1,'y':y1})

with plt.style.context('seaborn'):
    plt.figure(figsize=(12,6))
    sns.barplot(data=data,x=x1,y=y1,palette='inferno')
    plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
    plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
        plt.xticks(style='oblique',size=10)
    plt.yticks(style='oblique',size=10)
    plt.show()
```



Chi-squared Function has given the weightage on 4th feature whereas Mutual_Info_Classif we have got some features with a score of 0 thus we can removed such features.

Feature_Forward_Selection

3 3.0 0.0 4.0 0.0 0.0 2.0 0.0 4.0 0.0

```
from mlxtend.feature_selection import SequentialFeatureSelector as SFS
In [135...
           from sklearn.tree import DecisionTreeClassifier
In [136...
           X_train.shape, y_train.shape
Out[136... ((185, 9), (185,))
           pd.DataFrame(X_train).head()
In [144...
Out[144...
               0
                        2
                                              7
                                                  8
                            3
                                     5
                                         6
             3.0
                      7.0
                          0.0
                                       0.0
                                            1.0
                 0.0
                               0.0
                                   1.0
                                                 0.0
             2.0
                  0.0
                      3.0
                          0.0
                               0.0
                                   2.0
                                        0.0
                                            1.0
                                                 0.0
             3.0
                  2.0
                      5.0 0.0
                               0.0
                                   2.0 0.0
                                            1.0
                                                 0.0
```

localhost:8888/lab 29/41

```
0 1 2 3 4 5 6 7 8
4 2.0 2.0 3.0 0.0 0.0 1.0 0.0 1.0 0.0
```

```
In [137... dt = DecisionTreeClassifier()
In [138... ffs = SFS(estimator=dt,k_features=4,verbose=1,scoring='accuracy',cv=10)
```

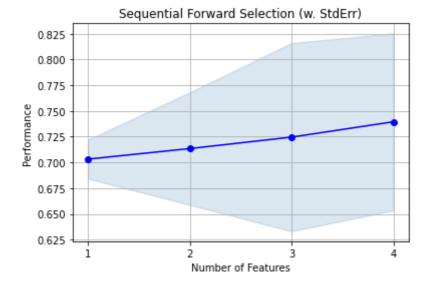
I have selected default DecisionTreeClassifier as the model for selecting top 4 features with cv as 10 and measuring accuracy; keeping verbose as want to see the logs

```
In [139... | ffs.fit(X_train,y_train)
         [Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n_jobs=1)]: Done
                                      9 out of 9 | elapsed:
                                                                 0.2s finished
         Features: 1/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
         workers.
                                      8 out of 8 | elapsed:
         [Parallel(n_jobs=1)]: Done
                                                                 0.2s finished
         Features: 2/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
         workers.
         [Parallel(n_jobs=1)]: Done
                                      7 out of 7 | elapsed:
                                                                 0.1s finished
         Features: 3/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
         workers.
         [Parallel(n_jobs=1)]: Done 6 out of 6 | elapsed:
                                                                 0.1s finished
         Features: 4/4
Out[139... SequentialFeatureSelector(cv=10, estimator=DecisionTreeClassifier(),
                                   k_features=4, scoring='accuracy', verbose=1)
In [140...
          ffs.k_feature_names_, ffs.k_feature_idx_, ffs.k_features, ffs.k_score_, ffs.subsets_
Out[140... (('0', '3', '4', '5'),
          (0, 3, 4, 5),
          4,
          0.7394736842105264,
          {1: {'feature_idx': (0,),
             'cv_scores': array([0.68421053, 0.68421053, 0.68421053, 0.68421053, 0.68421053,
                   0.72222222, 0.72222222, 0.72222222, 0.72222222),
            'avg_score': 0.703216374269006,
            'feature_names': ('0',)},
           2: {'feature_idx': (0, 4),
             cv_scores': array([0.73684211, 0.68421053, 0.68421053, 0.78947368, 0.68421053,
                   0.72222222, 0.77777778, 0.61111111, 0.77777778, 0.66666667]),
            'avg score': 0.7134502923976609,
            'feature_names': ('0', '4')},
           3: {'feature idx': (0, 4, 5),
             'cv_scores': array([0.73684211, 0.57894737, 0.78947368, 0.78947368, 0.68421053,
                   0.61111111, 0.77777778, 0.83333333, 0.83333333, 0.61111111]),
            'avg score': 0.724561403508772,
            'feature_names': ('0', '4', '5')},
           4: {'feature_idx': (0, 3, 4, 5),
             'cv scores': array([0.78947368, 0.63157895, 0.84210526, 0.84210526, 0.78947368,
                   0.611111111, 0.77777778, 0.77777778, 0.72222222, 0.61111111]),
             'avg score': 0.7394736842105264,
             'feature_names': ('0', '3', '4', '5')}})
          ffs.get_metric_dict()
In [141...
Out[141... {1: {'feature_idx': (0,),
            'cv_scores': array([0.68421053, 0.68421053, 0.68421053, 0.68421053, 0.68421053,
                  0.72222222, 0.72222222, 0.72222222, 0.72222222]),
            'avg_score': 0.703216374269006,
            'feature_names': ('0',),
            'ci_bound': 0.014115889413033223,
            'std_dev': 0.01900584795321636,
```

localhost:8888/lab 30/41

```
'std err': 0.006335282651072119},
2: {'feature_idx': (0, 4),
 'cv_scores': array([0.73684211, 0.68421053, 0.68421053, 0.78947368, 0.68421053,
        0.72222222, 0.77777778, 0.61111111, 0.77777778, 0.66666667]),
 'avg_score': 0.7134502923976609,
 'feature_names': ('0', '4'),
 'ci_bound': 0.0406167147817032,
 'std_dev': 0.054686961828098415,
 'std_err': 0.018228987276032803},
3: {'feature_idx': (0, 4, 5),
 'cv_scores': array([0.73684211, 0.57894737, 0.78947368, 0.78947368, 0.68421053,
        0.61111111, 0.77777778, 0.83333333, 0.83333333, 0.61111111]),
 'avg_score': 0.724561403508772,
 'feature names': ('0', '4', '5'),
 'ci bound': 0.06792728161477092,
 'std dev': 0.09145832391217575,
 'std err': 0.03048610797072525},
4: {'feature_idx': (0, 3, 4, 5),
 'cv_scores': array([0.78947368, 0.63157895, 0.84210526, 0.84210526, 0.78947368,
        0.61111111, 0.77777778, 0.77777778, 0.72222222, 0.61111111]),
 'avg score': 0.7394736842105264,
 'feature_names': ('0', '3', '4', '5'),
 'ci bound': 0.06384466827271998,
 'std_dev': 0.08596143128568985,
 'std err': 0.028653810428563284}}
```

In [142...
from mlxtend.plotting import plot_sequential_feature_selection as plot_sfs
import matplotlib.pyplot as plt
fig1 = plot_sfs(ffs.get_metric_dict(), kind='std_dev')
plt.title('Sequential Forward Selection (w. StdErr)')
plt.grid()
plt.show()



With 1 feature we have 70% accuracy and with 4 features we have less than 75% so, not much of a rise.

Backward Elimination

localhost:8888/lab 31/41

3/27/2021 Feature Selection

In [148... be = SFS(estimator=dt,k_features=4,verbose=1,scoring='accuracy',cv=10,forward=False,

I have selected default DecisionTreeClassifier as the model for selecting top 4 features with cv as 10 and measuring accuracy; keeping verbose as want to see the logs

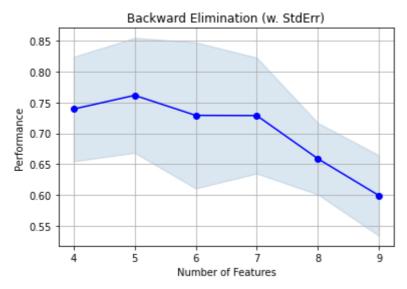
```
In [149... | be.fit(X_train,y train)
          [Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
          [Parallel(n_jobs=1)]: Done 9 out of 9 | elapsed:
                                                                     0.3s finished
          Features: 8/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
          [Parallel(n_jobs=1)]: Done
                                        8 out of 8 | elapsed:
                                                                      0.2s finished
          Features: 7/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
          workers.
                                        7 out of
                                                   7 | elapsed:
          [Parallel(n_jobs=1)]: Done
                                                                     0.2s finished
          Features: 6/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
          [Parallel(n_jobs=1)]: Done
                                        6 out of 6 | elapsed:
                                                                      0.2s finished
          Features: 5/4[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent
          [Parallel(n_jobs=1)]: Done
                                         5 out of 5 | elapsed:
                                                                     0.1s finished
          Features: 4/4
Out[149... SequentialFeatureSelector(cv=10, estimator=DecisionTreeClassifier(),
                                     forward=False, k_features=4, scoring='accuracy',
                                     verbose=1)
          be.k_feature_names_, be.k_feature_idx_, be.k_features, be.k_score_, be.subsets_
In [150...
          (('3', '4', '6', '7'),
Out[150...
           (3, 4, 6, 7),
           4,
           0.7391812865497076,
           {9: {'feature_idx': (0, 1, 2, 3, 4, 5, 6, 7, 8),
              cv_scores': array([0.57894737, 0.57894737, 0.63157895, 0.68421053, 0.68421053,
                                            , 0.66666667, 0.61111111, 0.5
                    0.55555556, 0.5
                                                                                  ]),
             'avg_score': 0.5991228070175438,
             'feature_names': ('0', '1', '2', '3', '4', '5', '6', '7', '8')},
            8: {'feature_idx': (0, 1, 3, 4, 5, 6, 7, 8),
             'cv_scores': array([0.73684211, 0.68421053, 0.73684211, 0.63157895, 0.63157895,
                    0.66666667, 0.61111111, 0.611111111, 0.72222222, 0.55555556]),
             'avg score': 0.6587719298245613,
            'feature_names': ('0', '1', '3', '4', '5', '6', '7', '8')},
7: {'feature_idx': (1, 3, 4, 5, 6, 7, 8),
             'cv scores': array([0.84210526, 0.78947368, 0.84210526, 0.68421053, 0.68421053,
                    0.5555556, 0.83333333, 0.72222222, 0.72222222, 0.61111111]),
             'avg score': 0.728654970760234,
            'feature_names': ('1', '3', '4', '5', '6', '7', '8')},
6: {'feature_idx': (3, 4, 5, 6, 7, 8),
              cv_scores': array([0.84210526, 0.68421053, 0.89473684, 0.73684211, 0.63157895,
                               , 0.83333333, 0.83333333, 0.72222222, 0.61111111]),
             'avg score': 0.7289473684210528,
            'feature_names': ('3', '4', '5', '6', '7', '8')},
5: {'feature_idx': (3, 4, 5, 6, 7),
              cv_scores': array([0.84210526, 0.78947368, 0.84210526, 0.84210526, 0.63157895,
                    0.61111111, 0.77777778, 0.88888889, 0.66666667, 0.72222222]),
             'avg_score': 0.7614035087719299,
            'feature_names': ('3', '4', '5', '6', '7')},
4: {'feature_idx': (3, 4, 6, 7),
              cv_scores': array([0.73684211, 0.78947368, 0.78947368, 0.84210526, 0.78947368,
                    0.55555556, 0.72222222, 0.83333333, 0.666666667, 0.666666667]),
             'avg_score': 0.7391812865497076,
             'feature_names': ('3', '4', '6', '7')}})
          be.get_metric_dict()
In [144...
Out[144... {9: {'feature idx': (0, 1, 2, 3, 4, 5, 6, 7, 8),
```

localhost:8888/lab 32/41

```
'cv_scores': array([0.57894737, 0.42105263, 0.52631579, 0.57894737, 0.63157895,
                  0.5555556, 0.61111111, 0.66666667, 0.61111111, 0.5
           'avg_score': 0.5681286549707603,
           'feature_names': ('0', '1', '2', '3', '4', '5', '6', '7', '8'),
           'ci_bound': 0.05028776628006419,
           'std_dev': 0.06770821248736365,
           'std_err': 0.02256940416245455},
          8: {'feature_idx': (0, 1, 3, 4, 5, 6, 7, 8),
           'cv_scores': array([0.78947368, 0.63157895, 0.73684211, 0.63157895, 0.63157895,
                  0.61111111, 0.66666667, 0.55555556, 0.72222222, 0.5
           'avg_score': 0.6476608187134503,
           'feature_names': ('0', '1', '3', '4', '5', '6', '7', '8'),
           'ci_bound': 0.060513411565051994,
           'std dev': 0.08147617664628949,
           'std err': 0.02715872554876316},
          7: {'feature_idx': (1, 3, 4, 5, 6, 7, 8),
           'cv_scores': array([0.84210526, 0.73684211, 0.94736842, 0.68421053, 0.63157895,
                  0.55555556, 0.83333333, 0.77777778, 0.66666667, 0.61111111]),
           'avg score': 0.728654970760234,
           'feature_names': ('1', '3', '4', '5', '6', '7', '8'),
           'ci bound': 0.085707195306951,
           'std_dev': 0.11539746981841105,
           'std err': 0.03846582327280368},
          6: {'feature_idx': (1, 3, 4, 6, 7, 8),
           'cv_scores': array([0.84210526, 0.73684211, 0.89473684, 0.73684211, 0.78947368,
                  0.611111111, 0.72222222, 0.72222222, 0.611111111, 0.66666667]),
           'feature_names': ('1', '3', '4', '6', '7', '8'),
           'ci_bound': 0.06458899678273299,
           'std_dev': 0.08696360649935293,
           'std err': 0.028987868833117648},
          5: {'feature_idx': (1, 3, 4, 6, 7),
           'cv_scores': array([0.84210526, 0.78947368, 0.73684211, 0.73684211, 0.78947368,
                  0.61111111, 0.72222222, 0.77777778, 0.61111111, 0.77777778]),
           'avg score': 0.7394736842105263,
           'feature_names': ('1', '3', '4', '6', '7'),
           'ci bound': 0.053420122368816804,
           'std_dev': 0.07192566431177344,
           'std_err': 0.02397522143725781},
          4: {'feature_idx': (1, 3, 4, 6),
           'cv_scores': array([0.89473684, 0.73684211, 0.84210526, 0.84210526, 0.73684211,
                  0.61111111, 0.66666667, 0.83333333, 0.72222222, 0.72222222]),
           'avg score': 0.7608187134502924,
           'feature_names': ('1', '3', '4', '6'),
           'ci bound': 0.06293963110438984,
           'std dev': 0.08474287549299496,
           'std err': 0.02824762516433165}}
         from mlxtend.plotting import plot sequential feature selection as plot sfs
In [151...
          import matplotlib.pyplot as plt
          fig1 = plot sfs(be.get metric dict(), kind='std dev')
          plt.title('Backward Elimination (w. StdErr)')
          plt.grid()
          plt.show()
```

localhost:8888/lab 33/41

3/27/2021 Feature_Selection



So, clearly with all the features we are getting the least accuracy and by dropping 4 feature we got the significant amount of increase in the accuracy.

Bi-Directional_Elimination

Also known as Step-wise Selection

```
In [152... from mlxtend.feature_selection import SequentialFeatureSelector as SFS
from sklearn.tree import DecisionTreeClassifier

In [153... X_train.shape, y_train.shape

Out[153... ((185, 9), (185,))

In [154... dt = DecisionTreeClassifier()

In [155... bde = SFS(estimator=dt,k_features=4,verbose=1,scoring='accuracy',cv=10,forward=True,
```

I have selected default DecisionTreeClassifier as the model for selecting top 4 features with cv as 10 and measuring accuracy; keeping verbose as want to see the logs

```
In [156...
          bde.fit(X_train,y_train)
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n jobs=1)]: Done
                                      9 out of
                                                  9 | elapsed:
                                                                  0.2s finished
         Features: 1/4[Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent
         workers.
         [Parallel(n jobs=1)]: Done
                                       8 out of
                                                  8 | elapsed:
                                                                  0.2s finished
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n jobs=1)]: Done
                                       1 out of
                                                  1 | elapsed:
                                                                  0.0s finished
         Features: 2/4[Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent
         workers.
         [Parallel(n jobs=1)]: Done
                                       7 out of
                                                  7 | elapsed:
                                                                  0.1s finished
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n jobs=1)]: Done
                                       2 out of
                                                  2 | elapsed:
                                                                  0.0s finished
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n jobs=1)]: Done
                                       1 out of
                                                  1 | elapsed:
                                                                  0.0s finished
         Features: 2/4[Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent
         [Parallel(n jobs=1)]: Done
                                       7 out of
                                                  7 | elapsed:
                                                                  0.1s finished
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n jobs=1)]: Done
                                       2 out of
                                                  2 | elapsed:
                                                                  0.0s finished
```

Features: 3/4[Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent

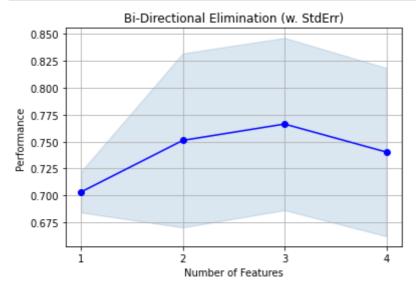
localhost:8888/lab 34/41

```
workers.
         [Parallel(n_jobs=1)]: Done 6 out of
                                                  6 | elapsed:
                                                                  0.1s finished
         [Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
         [Parallel(n_jobs=1)]: Done  3 out of
                                                 3 | elapsed:
                                                                  0.0s finished
         Features: 4/4
Out[156... SequentialFeatureSelector(cv=10, estimator=DecisionTreeClassifier(),
                                    floating=True, k features=4, scoring='accuracy',
                                    verbose=1)
          bde.k_feature_names_, bde.k_feature_idx_, bde.k_features, bde.k_score_, bde.subsets_
In [157...
Out[157... (('1', '3', '4', '5'),
          (1, 3, 4, 5),
          4,
          0.7403508771929824,
          {1: {'feature_idx': (0,),
             'cv_scores': array([0.68421053, 0.68421053, 0.68421053, 0.68421053, 0.68421053,
                   0.72222222, 0.72222222, 0.72222222, 0.72222222),
            'avg_score': 0.703216374269006,
            'feature_names': ('0',)},
           2: {'feature_idx': (4, 5),
             'cv_scores': array([0.84210526, 0.68421053, 0.78947368, 0.84210526, 0.63157895,
                   0.66666667, 0.72222222, 0.83333333, 0.83333333, 0.66666667]),
            'avg_score': 0.7511695906432749,
            'feature_names': ('4', '5')},
           3: {'feature_idx': (3, 4, 5),
             'cv_scores': array([0.89473684, 0.73684211, 0.84210526, 0.84210526, 0.73684211,
                   0.66666667, 0.77777778, 0.83333333, 0.666666667, 0.66666667]),
            'avg score': 0.766374269005848,
            'feature_names': ('3', '4', '5')},
           4: {'feature_idx': (1, 3, 4, 5),
             'cv_scores': array([0.89473684, 0.68421053, 0.84210526, 0.63157895, 0.68421053.
                   0.66666667, 0.77777778, 0.72222222, 0.77777778, 0.72222222]),
            'avg score': 0.7403508771929824,
             'feature_names': ('1', '3', '4', '5')}})
          bde.get_metric_dict()
In [158...
Out[158... {1: {'feature_idx': (0,),
            'cv_scores': array([0.68421053, 0.68421053, 0.68421053, 0.68421053, 0.68421053,
                  0.72222222,\ 0.722222222,\ 0.722222222,\ 0.722222222),
            'avg_score': 0.703216374269006,
            'feature_names': ('0',),
            'ci_bound': 0.014115889413033223,
           'std_dev': 0.01900584795321636,
           'std_err': 0.006335282651072119},
          2: {'feature_idx': (4, 5),
            'cv_scores': array([0.84210526, 0.68421053, 0.78947368, 0.84210526, 0.63157895,
                  0.66666667, 0.72222222, 0.83333333, 0.83333333, 0.666666667]),
            'avg_score': 0.7511695906432749,
            'feature_names': ('4', '5'),
            'ci bound': 0.06006910393311974,
           'std dev': 0.08087795410076846,
           'std err': 0.026959318033589485},
          3: {'feature idx': (3, 4, 5),
            'cv_scores': array([0.89473684, 0.73684211, 0.84210526, 0.84210526, 0.73684211,
                  0.66666667, 0.77777778, 0.83333333, 0.666666667, 0.66666667]),
            'avg score': 0.766374269005848,
            'feature_names': ('3', '4', '5'),
            'ci bound': 0.05947734563318215,
           'std dev': 0.08008120173578583,
           'std err': 0.026693733911928606},
          4: {'feature_idx': (1, 3, 4, 5),
            'cv_scores': array([0.89473684, 0.68421053, 0.84210526, 0.63157895, 0.68421053,
                  0.66666667, 0.77777778, 0.72222222, 0.77777778, 0.72222222]),
            'avg score': 0.7403508771929824,
            'feature_names': ('1', '3', '4', '5'),
            'ci bound': 0.05810844722714184,
```

localhost:8888/lab 35/41

```
'std_dev': 0.07823809612569363,
'std_err': 0.02607936537523121}}
```

```
In [159... from mlxtend.plotting import plot_sequential_feature_selection as plot_sfs
import matplotlib.pyplot as plt
fig1 = plot_sfs(bde.get_metric_dict(), kind='std_dev')
plt.title('Bi-Directional Elimination (w. StdErr)')
plt.grid()
plt.show()
```



From all the 3 wrapper methods features with index 3, 4 and 5 found to be important and more relevant.

Lasso Regularization

```
In [161...
          from sklearn.preprocessing import StandardScaler
          from sklearn.datasets import load_breast_cancer
          from sklearn.tree import DecisionTreeClassifier
          from sklearn.linear model import LogisticRegression
In [162...
          lbc = load_breast_cancer()
          X = pd.DataFrame(lbc.data,columns=lbc.feature_names)
          y = lbc.target
In [163...
          X.shape, y.shape
Out[163... ((569, 30), (569,))
          X_train, X_test, y_train, y_test = train_test_split(X,y,test_size=0.33,stratify=y,ra
In [164...
In [165...
          X train.shape, X test.shape, y train.shape, y test.shape
Out[165... ((381, 30), (188, 30), (381,), (188,))
In [166...
          ss = StandardScaler()
          ss.fit(X train)
          X train = pd.DataFrame(ss.transform(X train),columns=lbc.feature names)
          X test = pd.DataFrame(ss.transform(X test),columns=lbc.feature names)
In [199...
          log_reg=LogisticRegression(C=0.1, penalty='l1', solver='saga', max_iter=1000)
In [200...
          fs_model = SelectFromModel(estimator=log_reg, max_features=None)
```

localhost:8888/lab 36/41

True represents the important and non-zero features whereas False represents the not important features which are reduced to zero.

```
In [228... selected_feat = X_train.columns[(fs_model.get_support())]
    print('Total # of features : {}'.format((X_train.shape[1])))
    print('Selected # of features : {}'.format(len(selected_feat)))
    print('Features with coefficients reduced to zero : {}'.format(np.sum(fs_model.estim)))
    Total # of features : 30
    Selected # of features : 8
    Features with coefficients reduced to zero : 22
```

So, out of 30 features 22 have coefficients reduced to zero.

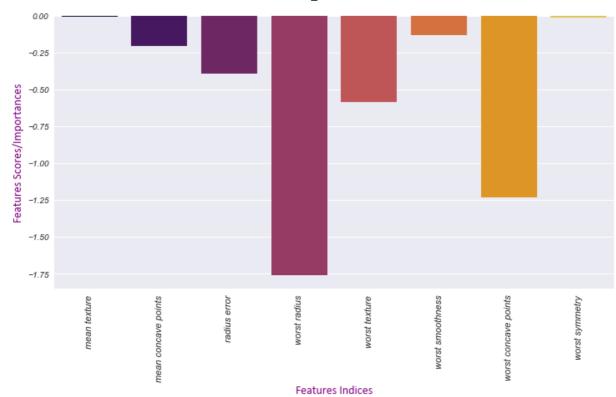
```
In [204... | fs_model.estimator_.coef_
Out[204... array([[ 0.
                          , -0.00592324, 0.
                                                    0.
                                                                0.
                          , 0. , -0.20294899, 0.
                 0.
                                                                0.
                                     , 0.
                -0.39338429, 0.
                                                    0.
                                                                0.
                                      , 0.
                0.
                      , 0.
                                                    0.
                                                               0.
                -1.76305377, -0.58572198, 0.
                                                               -0.13330742,
                                                    0.
                                , -1.2335202 , -0.01267504, 0.
                                                                          ]])
```

None, of the features are contributing to the positive class as all the coefficients values are negative.

```
In [225... x1 = list(X_train.columns[fs_model.get_support()])
    y1 = [val for val in np.ravel(fs_model.estimator_.coef_) if val != 0]
    data = pd.DataFrame({'x':x1,'y':y1})

with plt.style.context('seaborn'):
    plt.figure(figsize=(12,6))
    sns.barplot(data=data,x=x1,y=y1,palette='inferno')
    plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri', plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri', plt.xticks(style='oblique',size=11,rotation=90)
    plt.yticks(style='oblique',size=10)
    plt.show()
```

localhost:8888/lab 37/41



Ridge_Regularization

```
log_reg=LogisticRegression(C=0.1,penalty='12',solver='liblinear',max_iter=1000)
In [231...
In [232...
          fs_model = SelectFromModel(estimator=log_reg, max_features=None)
          fs_model.fit(X_train,y_train)
In [233...
         SelectFromModel(estimator=LogisticRegression(C=0.1, max_iter=1000,
                                                     solver='liblinear'))
          fs_model.get_support()
In [234...
Out[234... array([ True,
                       True, True,
                                    True, False, False, True, True, False,
                False,
                       True, False, True, True, False, False, False,
                                     True, True, True, False, True,
                False, False, True,
                      True, False])
```

True represents the important and non-zero features whereas False represents the non important features whose coefficients are not reduced to zero.

```
In [235... selected_feat = X_train.columns[(fs_model.get_support())]
    print('Total # of features : {}'.format((X_train.shape[1])))
    print('Selected # of features : {}'.format(len(selected_feat)))
    print('Features with coefficients reduced to zero : {}'.format(np.sum(fs_model.estim)))
    Total # of features : 30
    Selected # of features : 17
    Features with coefficients reduced to zero : 0
```

So, out of 30 features 17 are the selected ones and non of these have coefficients as zero.

```
In [241... print(list(selected_feat))
['mean radius', 'mean texture', 'mean perimeter', 'mean area', 'mean concavity', 'mean concavit
```

an concave points', 'radius error', 'perimeter error', 'area error', 'worst radius',

localhost:8888/lab 38/41

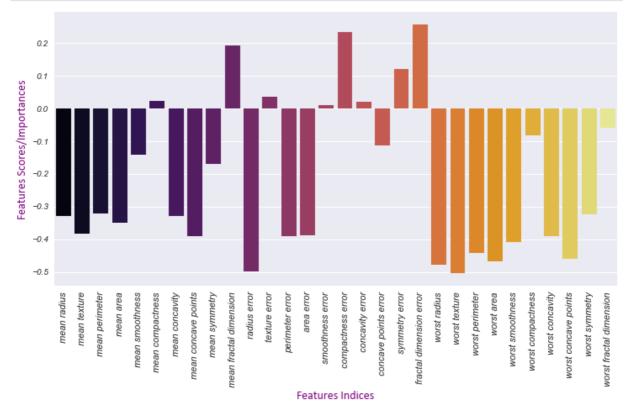
3/27/2021 Feature_Selection

Out[244... 0.2770428874008997

None, of the features from selectd ones are contributing to the positive class as all the coefficients values are negative.

```
In [238... x1 = X_train.columns
    y1 = [val for val in np.ravel(fs_model.estimator_.coef_)]
    data = pd.DataFrame({'x':x1,'y':y1})

with plt.style.context('seaborn'):
    plt.figure(figsize=(12,6))
    sns.barplot(data=data,x=x1,y=y1,palette='inferno')
    plt.xlabel("Features Indices",fontdict={'size':14,'family':'calibri','color':'pu
    plt.ylabel("Features Scores/Importances",fontdict={'size':14,'family':'calibri',
    plt.xticks(style='oblique',size=11,rotation=90)
    plt.yticks(style='oblique',size=10)
    plt.show()
```



As compared to Lasso Regression some of the features here are contributing for +ve class as well.

Permutation_Importance

How important this feature is for a particular model?

localhost:8888/lab 39/41

- Permutation feature importance is a model inspection technique that can be used for any fitted estimator when the data is tabular.
- This is especially useful for non-linear or opaque estimators.
- The permutation feature importance is defined to bring the decrease in a model score when a single feature value is randomly shuffled.
- This procedure breaks the relationship between the feature and the target, which means the drop in the model score is indicative of how much the model depends on the feature.
- This technique benefits from being model agnostic (means model independent) and can be calculated many times with different permutations of the feature.
- The permutation_importance function calculates the feature importance of estimators for a given dataset. The n_repeats parameter sets the number of times a feature is randomly shuffled and returns a sample of feature importances.

https://scikit-learn.org/stable/modules/permutation_importance.html

https://scikit-

learn.org/stable/auto_examples/inspection/plot_permutation_importance_multicollinear.html#sphx-glr-auto-examples-inspection-plot-permutation-importance-multicollinear-py

https://scikit-

learn.org/stable/auto_examples/inspection/plot_permutation_importance.html#sphx-glr-auto-examples-inspection-plot-permutation-importance-py

Permutation importances can be computed either on the training set or on a held-out testing or validation set. Using a held-out set makes it possible to highlight which features contribute the most to the generalization power of the inspected model. Features that are important on the training set but not on the held-out set might cause the model to overfit.

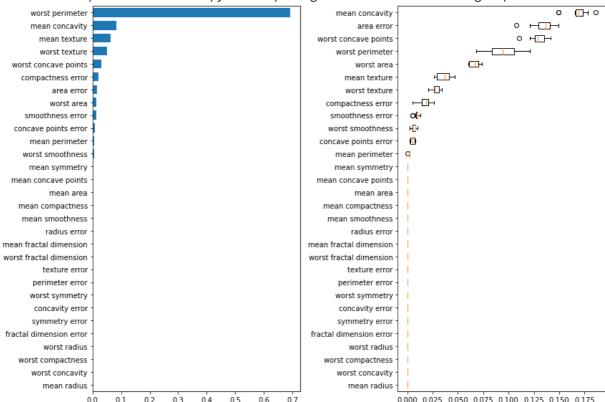
Features that are deemed of low importance for a bad model (low cross-validation score) could be very important for a good model. Therefore it is always important to evaluate the predictive power of a model using a held-out set (or better with cross-validation) prior to computing importances. Permutation importance does not reflect to the intrinsic predictive value of a feature by itself but how important this feature is for a particular model.

localhost:8888/lab 40/41

```
In [268...
          result.importances mean
                                                              , 0.
Out[268... array([0.
                          , 0.03622047, 0.0023622 , 0.
                                                              , 0.
                          , 0.16824147, 0. , 0.
                0.
                          , 0.
                                     , 0.
                0.
                                                  , 0.13385827, 0.00971129,
                0.01732283, 0.
                                                              , 0.
                                      , 0.00524934, 0.
                0.
                          , 0.02834646, 0.09448819, 0.06614173, 0.00656168,
                          , 0.
                0.
                                      , 0.12913386, 0.
                                                                           ])
          fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 8))
In [266...
          ax1.barh(tree indices,clf.feature importances [tree importance sorted idx], height=0
          ax1.set_yticklabels(lbc.feature_names[tree_importance_sorted_idx])
          ax1.set_yticks(tree_indices)
          ax1.set_ylim((0, len(clf.feature_importances_)))
          ax2.boxplot(result.importances[perm_sorted_idx].T,vert=False,labels=lbc.feature_name
          fig.tight_layout()
          plt.show()
```

c:\users\rajsh\appdata\local\programs\python\python36\lib\site-packages\ipykernel_la
uncher.py:3: UserWarning: FixedFormatter should only be used together with FixedLoca
tor





So, here it has become very clear that none of the features are really important the model because the maximum drop in the accuracy we have witnessed is only 0.175.

https://christophm.github.io/interpretable-ml-book/feature-importance.html

localhost:8888/lab 41/41