Outlier and Novelty Detection using Local Outlier Factor

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Package_import

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import scipy
import statsmodels as stm

from sklearn.datasets import load_breast_cancer, load_iris
from sklearn.neighbors import LocalOutlierFactor
from sklearn.ensemble import IsolationForest

%matplotlib inline
```

```
In [2]: pd.set_option('display.max_rows',151)
```

Dataset_import

```
In [3]: cancer_dataset, iris_dataset = load_breast_cancer(), load_iris()
```

1. Cancer Dataset

Segregating Features and Labels

Segregating Features and Labels

```
X_iris_df = pd.DataFrame(iris_dataset.data,columns=iris_dataset.feature_names)
 In [8]:
          y_iris_df = pd.DataFrame(iris_dataset.target,columns=['Label'])
 In [9]:
          X_iris_df.shape, X_iris_df.head()
         ((150, 4),
 Out[9]:
              sepal length (cm)
                                 sepal width (cm) petal length (cm) petal width (cm)
          0
                                               3.5
          1
                            4.9
                                               3.0
                                                                  1.4
                                                                                     0.2
          2
                            4.7
                                               3.2
                                                                  1.3
                                                                                     0.2
           3
                            4.6
                                               3.1
                                                                  1.5
                                                                                     0.2
          4
                                               3.6
                                                                  1.4
                                                                                     0.2)
In [10]:
          iris_dataset.target.shape, iris_dataset.target_names
Out[10]: ((150,), array(['setosa', 'versicolor', 'virginica'], dtype='<U10'))
          y_iris_df.shape, y_iris_df.value_counts()
Out[11]: ((150, 1),
          Label
                    50
          2
                    50
          1
                    50
          a
          dtype: int64)
```

Outlier_Detection

• We want to find the outliers in the given dataset or make the train dataset outliers free.

LOF totally relies on distance calculations and below are some points which we need to consider when we are working distance calculating algorithms:

- Does your features exist in different scales? For example f1 in kg and f2 in mm so on..
 - If yes and you are using Euclidean distance (most popular among data scientists), then without performing the features standard scaling(means all features are one mean centric) you will get the highly variant or skewed distances.
 - If no (means feature values are in same scale/unit) and you are using Eucildean distance then still you will be better off if perform the features standard scaling (means all features are one mean centric) else you will get higher distances of

global outliers and these will dominate your outlier detection distances and the local outliers will get impacted.

Here, I will use below distance metrics:

- Euclidean
- Manhattan
- Mahalanobis (if we want to consider the correlation b/w the features)

[12]:		<pre>from sklearn.preprocessing import StandardScaler ss = StandardScaler()</pre>										
[13]:	X_ir	ris_df_st = po	d.DataFrame(ss.	fit_transform(X_	_iris_df.copy(de	ep= True)),columns=i						
[14]:	<pre>X_iris_df_st.head()</pre>											
14]:	se	pal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)							
	0	-0.900681	1.019004	-1.340227	-1.315444							
	1	-1.143017	-0.131979	-1.340227	-1.315444							
	2	-1.385353	0.328414	-1.397064	-1.315444							
	3	-1.506521	0.098217	-1.283389	-1.315444							
	4	-1.021849	1.249201	-1.340227	-1.315444							

Using LOF to find outliers in IRIS Dataset

CASE-I

Neighbors = 20 & Contamination = 0.05 or 5% & Leaf_Size = 15 & Distance Metric = Manhattan

```
print(X_iris_df_st.shape)
In [15]:
          iris contam = 0.05
          print(X_iris_df_st.shape[0]*iris_contam)
         (150, 4)
         7.5
          lof_iris = LocalOutlierFactor(n_neighbors=20,algorithm='kd_tree',leaf_size=15,contam
In [16]:
                                         novelty=False, metric='minkowski', p=1)
          lof_iris_pred = lof_iris.fit_predict(X_iris_df_st)
In [17]:
          lof_iris_pred.shape
Out[17]: (150,)
In [18]:
          pred dict = {1:0, -1:1}
          lof_iris_pred = [pred_dict.get(val) for val in lof_iris_pred]
```

Here, LOF returns the results in the form of [1, -1] where 1's are considered as inliers and -1 are considered as Outliers.

```
In [19]: np.unique(lof_iris_pred), np.bincount(lof_iris_pred)
```

```
Out[19]: (array([0, 1]), array([142, 8], dtype=int64))
In [20]: lof_iris_vals = lof_iris.negative_outlier_factor_ ## -ve lof value
```

LOF will always returns the -ve factor score and the inliers generally have score close to 1 i.e. close to -1, whereas Outliers tends to have a larger score.

```
In [21]: lof_iris_offset = lof_iris.offset_ ## Threshold Value
lof_iris_offset
```

Out[21]: -1.4735496359340885

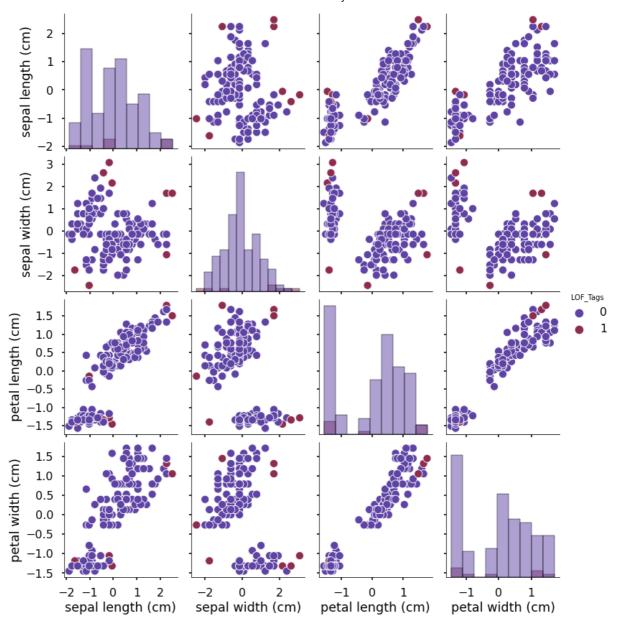
This is the negative threshold value generated by LOF if any value is greater than it then such a record will be considered as an Outlier.

In [23]: iris_lof_result[iris_lof_result['LOF_Values'] < lof_iris_offset]</pre>

Out[23]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	Label	LOF_Values	LOF_Tags
	14	-0.052506	2.169988	-1.453901	-1.315444	0	-1.511115	1
	15	-0.173674	3.090775	-1.283389	-1.052180	0	-1.910514	1
	33	-0.416010	2.630382	-1.340227	-1.315444	0	-1.506934	1
	41	-1.627688	-1.743357	-1.397064	-1.183812	0	-1.878636	1
	60	-1.021849	-2.433947	-0.146641	-0.262387	1	-1.496300	1
	117	2.249683	1.709595	1.672157	1.317199	2	-1.667270	1
	118	2.249683	-1.052767	1.785832	1.448832	2	-1.626788	1
	131	2.492019	1.709595	1.501645	1.053935	2	-1.736445	1

Now, if we see the -ve scores then they are not so highly away or larger than the offset value but if we compare these values with -1 then yes the above records are a bit away from the generally considered inliers.

- Here, the dataset was not having any labels for the outliers, so this is completely driven based on distance calculation
- Plotting the records with above generated score will tell the better story



As, the plot is self-explanatory because the data points which are away(separated from others) from the clusters or at the edges/boundaries of it are labelled as Outliers. This is exactly the way LOF behaves.

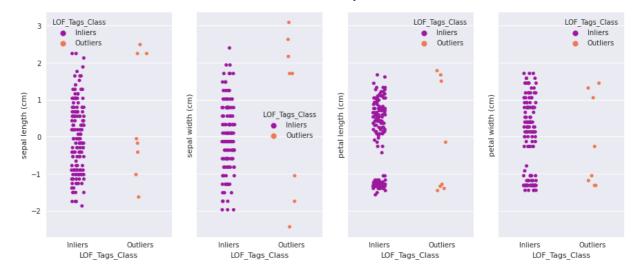
More analysis

```
In [25]:
         iris_lof_result.columns
dtype='object')
In [26]:
         def lbl(val):
            if val == 1:
                return 'Outliers'
            else:
                return 'Inliers'
         iris_lof_result['LOF_Tags_Class'] = iris_lof_result['LOF_Tags'].apply(lambda val: lb
In [27]:
         fig, ax = plt.subplots(1,4,sharex=True,sharey=True,squeeze=True,figsize=(15,6))
In [28]:
         sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue='LOF_T
         sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='LOF_Ta
         sns.boxplot(data=iris lof result,x='LOF Tags Class',y='petal length (cm)',hue='LOF T
```

```
sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='LOF_Ta
             plt.show()
                  LOF_Tags_Class
                                                                                    LOF_Tags_Class
                                                                                                               LOF_Tags_Class
                     Inliers
                                                                                       Inliers
                                                                                                                  Inliers
                    Outliers
                                                                                      Outliers
                                                                                                                  Outliers
               2
            (cm)
               1
                                                                      Ē
                                          width (cm)
                                                                                                 Œ
                                                        LOF_Tags_Class
                                                                      length (
            sepal length
                                                                                                 width
                                                           Inliers
                                                          Outliers
               0
                                                                                                 petal
                                                                      petal
              -1
              -2
                     Inliers
                               Outliers
                                                Inliers
                                                           Outliers
                                                                                      Outliers
                                                                                                       Inliers
                                                                                                                  Outliers
                       LOF_Tags_Class
                                                   LOF_Tags_Class
                                                                              LOF Tags Class
                                                                                                          LOF Tags Class
In [29]:
             iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)
Out[29]:
                              sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF_Tags_Class
                     Inliers
                                      -1.870024
                                                          -1.973554
                                                                              -1.567576
                                                                                                 -1.447076
                    Outliers
                                      -1.627688
                                                          -2.433947
                                                                              -1.453901
                                                                                                 -1.315444
In [30]:
             iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)'
Out[30]:
                              sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF_Tags_Class
                                                                               0.364896
                                                                                                  0.132510
                     Inliers
                                      -0.052506
                                                          -0.131979
                    Outliers
                                      -0.113090
                                                           1.709595
                                                                              -0.715015
                                                                                                 -0.657283
             iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)'
In [31]:
Out[31]:
                              sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF Tags Class
                     Inliers
                                       2.249683
                                                           2.400185
                                                                               1.672157
                                                                                                  1.712096
                    Outliers
                                       2.492019
                                                           3.090775
                                                                               1.785832
                                                                                                  1.448832
```

So, all the features have good point variation in the 5 number summary of Inliers and Outliers.

```
with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
```



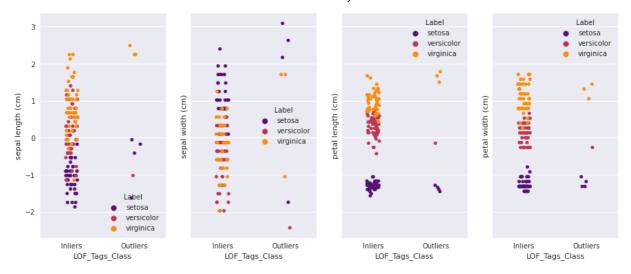
If we look at the outliers then they are clearly the extreme points which are either at the edges or boundaries of the clusters.



Some gaps are quite evident in the above plots and point to mention here is that majority of the outliers are from the extreme values of features.

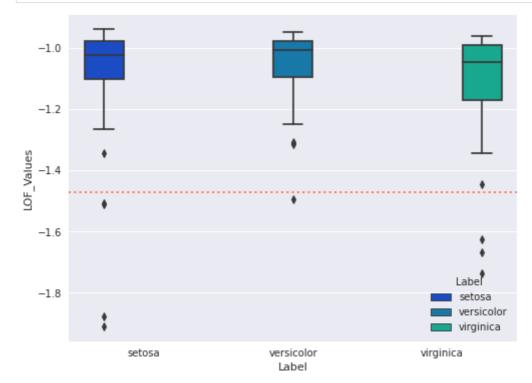
```
In [34]: iris_classes = {0:'setosa',1:'versicolor',2:'virginica'}
iris_lof_result['Label'] = iris_lof_result['Label'].apply(lambda val : iris_classes.

In [35]: with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
```



In this case with contamination == 0.05 and 20 NN, based on that LOF looks to work good in capturing the local and overall outliers.

```
In [36]: with plt.style.context('seaborn'):
    plt.figure(figsize=(8,6))
    sns.boxplot(data=iris_lof_result,x='Label',y='LOF_Values',hue='Label',palette='w
    plt.axhline(lof_iris_offset,color='coral',linestyle=':',linewidth=2)
```



Above showing the outliers captured on the basis of the Manhattan Distance used by LOF, out of these only one point belongs to Versicolor class.

CASE-II

Neighbors = 20 & Contamination = 0.05 or 5% & Leaf_Size = 15 & Distance Metric = Euclidean

```
In [37]: print(X_iris_df_st.shape)
    iris_contam = 0.05
    print(X_iris_df.shape[0]*iris_contam)
```

```
(150, 4)
7.5
```

Here, LOF returns the results in the form of [1, -1] where 1's are considered as inliers and -1 are considered as Outliers.

```
In [41]: np.unique(lof_iris_pred), np.bincount(lof_iris_pred)
Out[41]: (array([0, 1]), array([142, 8], dtype=int64))
In [42]: lof_iris_vals = lof_iris.negative_outlier_factor_ ## -ve lof value
```

LOF will always returns the -ve factor score and the inliers generally have score close to 1 i.e. close to -1, whereas Outliers tends to have a larger score.

This is the negative threshold value generated by LOF if any value is greater than it then such a record will be considered as an Outlier.

```
In [45]: iris_lof_result[iris_lof_result['LOF_Values'] < lof_iris_offset]</pre>
```

ut[45]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	Label	LOF_Values	LOF_Tags
	14	-0.052506	2.169988	-1.453901	-1.315444	0	-1.495164	1
	15	-0.173674	3.090775	-1.283389	-1.052180	0	-2.068567	1
	32	-0.779513	2.400185	-1.283389	-1.447076	0	-1.456299	1
	33	-0.416010	2.630382	-1.340227	-1.315444	0	-1.637883	1
	41	-1.627688	-1.743357	-1.397064	-1.183812	0	-1.912040	1
	117	2.249683	1.709595	1.672157	1.317199	2	-1.822850	1
	118	2.249683	-1.052767	1.785832	1.448832	2	-1.602136	1
	131	2.492019	1.709595	1.501645	1.053935	2	-1.883861	1

Now, if we see the -ve scores then they are not so highly away or larger than the offset value but if we compare these values with -1 then yes the

above records are a bit away from the generally considered inliers.

- Here, the dataset was not having any labels for the outliers, so this is completely driven based on distance calculation
- Plotting the records with above generated score will tell the better story

```
In [46]:
             with plt.style.context('seaborn-poster'):
                   g = sns.pairplot(data=iris_lof_result[['sepal length (cm)','sepal width (cm)','p
                                    hue='LOF_Tags',palette='inferno',height=3,aspect=0.9,diag_kind='his
              sepal length (cm)
                   2
                   1
                   0
                   -1
                  -2
                   3
              sepal width (cm)
                   2
                   1
                   0
                  -1
                  -2
                                                                                                                      LOF Tags
                 1.5
            petal length (cm)
                 1.0
                 0.5
                 0.0
               -0.5
                -1.0
                -1.5
                 1.5
            petal width (cm)
                 1.0
                 0.5
                 0.0
                -0.5
                -1.0
```

As, the plot is self-explanatory because the data points which are away(separated from others) from the clusters or at the edges/boundaries of it are labelled as Outliers. This is exactly the way LOF behaves.

petal length (cm)

sepal width (cm)

-1

petal width (cm)

More analysis

-1.5

-1 0

1

sepal length (cm)

```
fig, ax = plt.subplots(1,4,sharex=True,sharey=True,squeeze=True,figsize=(15,6))
In [49]:
            sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue='LOF_T
            sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='LOF_Ta
            sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue='LOF_T
            sns.boxplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='LOF_Ta
            plt.show()
                 LOF_Tags_Class
                                           LOF_Tags_Class
                                                                               LOF_Tags_Class
                                                                                                         LOF_Tags_Class
                    Inliers
                                              Inliers
                                                                                  Inliers
                                                                                                            Inliers
                   Outliers
                                             Outliers
                                                                                  Outliers
                                                                                                            Outliers
              2
           sepal length (cm)
              1
                                                                  length (cm)
                                        Ē
                                        width (
                                                                                            width
              0
                                        Sepal 1
                                                                  petal
                                                                                            petal
             -1
             -2
                                                        Outliers
                                                                                  Outliers
                   Inliers
                              Outliers
                                             Inliers
                                                                                                 Inliers
                                                                                                            Outliers
                      LOF_Tags_Class
                                                LOF_Tags_Class
                                                                          LOF_Tags_Class
                                                                                                    LOF_Tags_Class
In [50]:
            iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)'
Out[50]:
                             sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF Tags Class
                    Inliers
                                    -1.870024
                                                                          -1.567576
                                                       -2.433947
                                                                                            -1.447076
                   Outliers
                                    -1.627688
                                                       -1.743357
                                                                          -1.453901
                                                                                            -1.447076
In [51]:
            iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)'
Out[51]:
                            sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF_Tags_Class
                    Inliers
                                    -0.052506
                                                       -0.131979
                                                                          0.364896
                                                                                             0.132510
                   Outliers
                                    -0.113090
                                                       1.939791
                                                                          -1.283389
                                                                                            -1.117996
In [52]:
            iris_lof_result.groupby(['LOF_Tags_Class'])[['sepal length (cm)', 'sepal width (cm)'
Out[52]:
                             sepal length (cm) sepal width (cm) petal length (cm) petal width (cm)
            LOF_Tags_Class
                    Inliers
                                     2.249683
                                                       1.939791
                                                                           1.672157
                                                                                             1.712096
                   Outliers
                                     2.492019
                                                       3.090775
                                                                           1.785832
                                                                                             1.448832
```

So, all the features have good point variations in the 5 number summary of Inliers and Outliers.

```
In [53]: with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
```



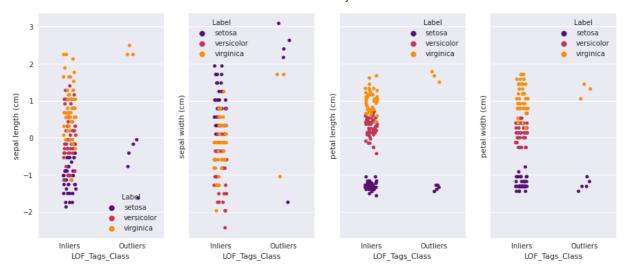
If we look at the outliers then they are clearly the extreme points which are either at the edges or boundaries of the clusters.



Some gaps are quite evident in the above plots and point to mention here is that majority of the outliers are from the extreme values of features.

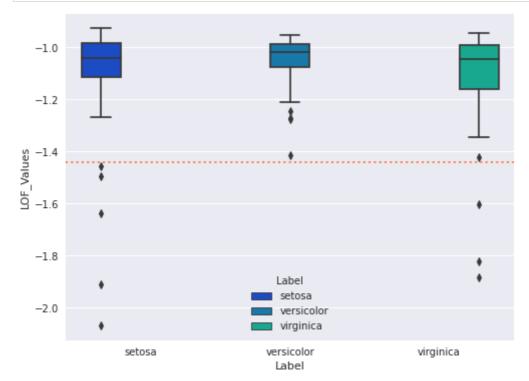
```
In [55]: iris_classes = {0:'setosa',1:'versicolor',2:'virginica'}
iris_lof_result['Label'] = iris_lof_result['Label'].apply(lambda val : iris_classes.

In [56]: with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue=
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
```



In this case with contamination == 0.05 and 20 NN, based on that LOF looks to work good in capturing the local and overall outliers.

```
In [57]: with plt.style.context('seaborn'):
    plt.figure(figsize=(8,6))
    sns.boxplot(data=iris_lof_result,x='Label',y='LOF_Values',hue='Label',palette='w
    plt.axhline(lof_iris_offset,color='coral',linestyle=':',linewidth=2)
```



Above showing the outliers captured on the basis of the Manhattan Distance used by LOF, out of these no point belongs to Versicolor class.

CASE-III

Neighbors = 20 & Contamination = 0.05 or 5% & Leaf Size = 15 & Distance Metric = Precomputed Mahalanobis
Distance Metric with shape nxn where n is the number of observations in the dataset

NOTE :: MAHALANOBIS is scale-invariant

Out[

Out

In [58]: X_iris_df.head()

[58]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)
	0	5.1	3.5	1.4	0.2
	1	4.9	3.0	1.4	0.2
	2	4.7	3.2	1.3	0.2
	3	4.6	3.1	1.5	0.2
	4	5.0	3.6	1.4	0.2

Generating Co-variance Symmetric Matrix of the given dataset

In [59]: X_iris_df_st.head()

t[59]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)
	0	-0.900681	1.019004	-1.340227	-1.315444
	1	-1.143017	-0.131979	-1.340227	-1.315444
	2	-1.385353	0.328414	-1.397064	-1.315444
	3	-1.506521	0.098217	-1.283389	-1.315444
	4	-1.021849	1.249201	-1.340227	-1.315444

Biased Co-variance Symmetric Matrix

In [60]: pd.DataFrame((1/X_iris_df_st.shape[0]) * (X_iris_df_st.T @ X_iris_df_st))

 Out[60]:
 sepal length (cm)
 sepal width (cm)
 petal length (cm)
 petal width (cm)

 sepal length (cm)
 1.000000
 -0.117570
 0.871754
 0.817941

 sepal width (cm)
 -0.117570
 1.000000
 -0.428440
 -0.366126

petal width (cm) 0.817941 -0.366126 0.962865 1.000000

-0.428440

1.000000

0.962865

In [61]: pd.DataFrame(np.cov(X_iris_df_st,rowvar=False,bias=True))

0.871754

2 Out[61]: 1 3 0 1.000000 -0.117570 0.871754 0.817941 -0.117570 1.000000 -0.428440 -0.366126 0.871754 -0.428440 0.962865 1.000000 0.817941 -0.366126 0.962865 1.000000

petal length (cm)

Un-Biased Co-variance Symmetric Matrix

In [62]: pd.DataFrame((1/(X_iris_df_st.shape[0]-1)) * (X_iris_df_st.T @ X_iris_df_st))

 Out[62]:
 sepal length (cm)
 sepal width (cm)
 petal length (cm)
 petal width (cm)

 sepal length (cm)
 1.006711
 -0.118359
 0.877604
 0.823431

	sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)
sepal width (cm)	-0.118359	1.006711	-0.431316	-0.368583
petal length (cm)	0.877604	-0.431316	1.006711	0.969328
petal width (cm)	0.823431	-0.368583	0.969328	1.006711

```
In [63]: pd.DataFrame(np.cov(X_iris_df_st,rowvar=False,bias=False))
```

```
2
                                                      3
Out[63]:
                      0
                                 1
               1.006711
                         -0.118359
                                     0.877604
                                                0.823431
              -0.118359
                          1.006711
                                              -0.368583
                                    -0.431316
               0.877604 -0.431316
                                     1.006711
                                                0.969328
               0.823431 -0.368583
                                     0.969328
                                                1.006711
```

Computing Mahalanobis Distance Metric

Out[64]:		0	1	2	3	4	5	6	7	8	9
	0	4.555953	2.479101	2.685287	1.704051	4.512709	5.574929	2.484211	3.555688	1.126132	2.598991
	1	2.479101	8.117477	3.979952	2.545627	1.032946	0.136103	0.963860	2.065696	4.442087	4.395718
	2	2.685287	3.979952	4.331971	4.039356	2.684836	1.285841	3.997162	2.735031	5.289667	3.246306
	3	1.704051	2.545627	4.039356	6.014176	2.476593	0.426890	4.863778	2.642637	7.430052	3.933751
	4	4.512709	1.032946	2.684836	2.476593	6.062205	7.434547	4.496747	4.024086	1.384612	2.216339

5 rows × 150 columns

```
precomp_dist_sq.shape
In [65]:
Out[65]: (150, 150)
            lof_precomp_iris = LocalOutlierFactor(n_neighbors=20,leaf_size=15,contamination=iris
In [66]:
                                                         metric='precomputed',algorithm='auto',n_jobs=N
In [67]:
            lof_precomp_iris.fit_predict(precomp_dist_sq)
Out[67]: array([ 1,
                                       -1,
                                                               1,
                                                                         1,
                         1,
                                   1,
                                                           1,
                                                               1,
                                                                         1,
                                       1,
                                                 1,
                                                                              1,
                                                                                       1,
                                                                                                 1,
                              1,
                                            1,
                                                     -1,
                                                                    1,
                         1,
                     1,
                              1,
                                        1,
                                            1,
                                                 1,
                                                      1,
                                                           1,
                                                                         1,
                                   1,
                                                               1,
                                                                              1,
                                                                                                 1,
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                                                      1,
                                                           1,
                                                                              1,
                                                                                       1,
                                                                    1,
                                                                                           -1,
                                                               1,
                         1,
                              1,
                                   1,
                                            1,
                                                 1,
                                                      1,
                                                           1,
                                                                         1,
                                                                              1,
                                                                                       1,
                                                                                           -1,
                    1,
                                      -1,
                                                                    1,
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```

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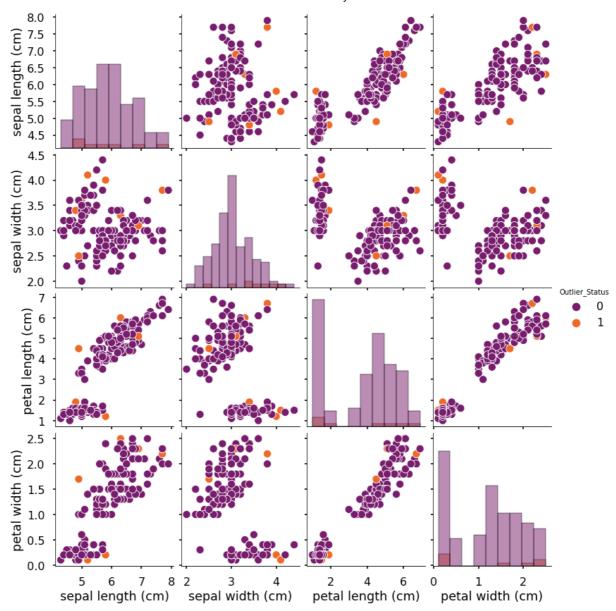
1,

1,

```
LOF Outliers & Novelty Detection
           lof_precomp_iris.offset_
In [68]:
           -1.407113636384807
Out[68]:
           X_mahala_results = pd.concat([X_iris_df.copy(deep=True),y_iris_df],axis=1)
In [69]:
            X_mahala_results.head()
Out[69]:
              sepal length (cm) sepal width (cm) petal length (cm) petal width (cm) Label
           0
                           5.1
                                            3.5
                                                              1.4
                                                                               0.2
                                                                                        0
           1
                           4.9
                                                                               0.2
                                                                                       0
                                            3.0
                                                              1.4
           2
                           4.7
                                            3.2
                                                              1.3
                                                                               0.2
                                                                                        0
                                            3.1
           3
                           4.6
                                                              1.5
                                                                               0.2
                                                                                       0
                           5.0
                                            3.6
                                                              1.4
                                                                               0.2
                                                                                        0
In [70]:
           X_mahala_results['LOF_Values'] = lof_precomp_iris.negative_outlier_factor_
            X_mahala_results['Outlier_Status'] = lof_precomp_iris.fit_predict(precomp_dist_sq)
            X_mahala_results['Outlier_Status'] = X_mahala_results['Outlier_Status'].apply(lambda
           X_mahala_results.head()
In [71]:
Out[71]:
                sepal length
                               sepal width
                                             petal length
                                                            petal width
                                                                         Label LOF_Values Outlier_Status
                       (cm)
                                     (cm)
                                                                   (cm)
                                                                                 -1.090641
                                                                                                       0
           0
                        5.1
                                       3.5
                                                                    0.2
                                                                             0
                                                      1.4
           1
                        4.9
                                       3.0
                                                      1.4
                                                                    0.2
                                                                                 -1.151355
                                                                                                       0
           2
                                       3.2
                        4.7
                                                      1.3
                                                                    0.2
                                                                             0
                                                                                 -1.047989
                                                                                                       0
           3
                        4.6
                                       3.1
                                                      1.5
                                                                    0.2
                                                                             0
                                                                                 -0.957528
                                                                                                       0
           4
                        5.0
                                       3.6
                                                                    0.2
                                                                             0
                                                                                 -1.423120
                                                      1.4
                                                                                                       1
           X_mahala_results[X_mahala_results['LOF_Values'] < lof_precomp_iris.offset_]</pre>
In [72]:
0
```

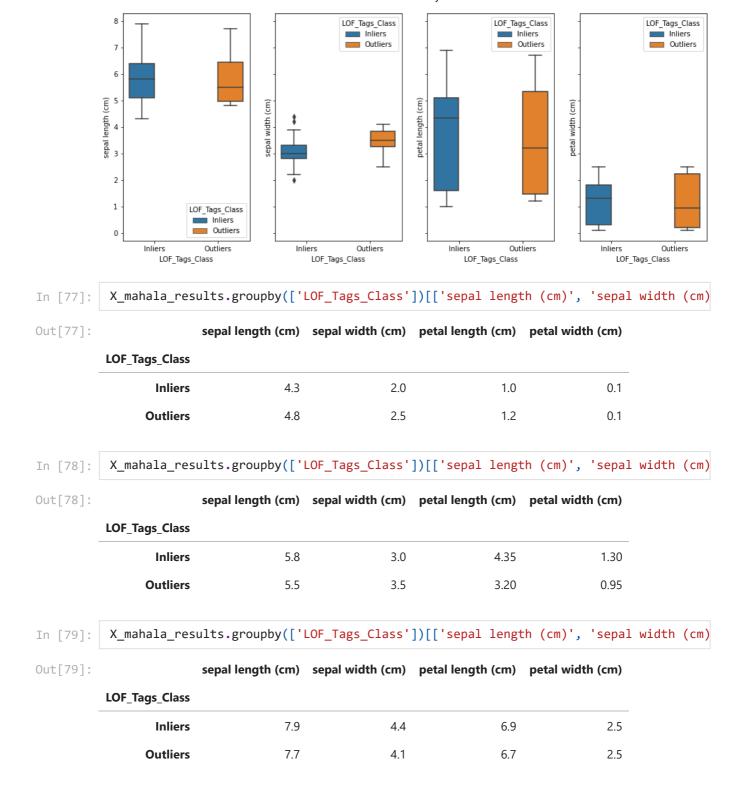
Out[72]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	Label	LOF_Values	Outlier_Status
	4	5.0	3.6	1.4	0.2	0	-1.423120	1
	14	5.8	4.0	1.2	0.2	0	-1.440691	1
	24	4.8	3.4	1.9	0.2	0	-1.457974	1
	32	5.2	4.1	1.5	0.1	0	-1.750358	1
	100	6.3	3.3	6.0	2.5	2	-1.450683	1
	106	4.9	2.5	4.5	1.7	2	-1.778370	1
	117	7.7	3.8	6.7	2.2	2	-1.938577	1
	141	6.9	3.1	5.1	2.3	2	-1.883941	1

```
with plt.style.context('seaborn-poster'):
In [73]:
              g = sns.pairplot(data=X_mahala_results[['sepal length (cm)','sepal width (cm)','
                           hue='Outlier Status',palette='inferno',height=3,aspect=0.9,diag kin
```



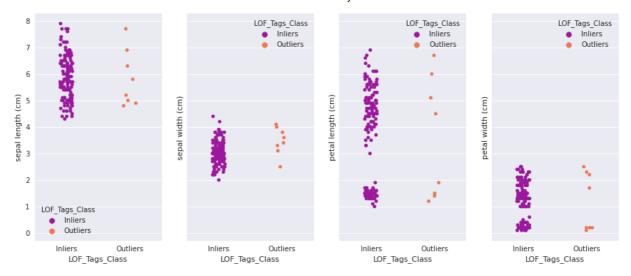
With Mahalanobis, I have observed quite a bit different results as compared to Euclidean and Manhattan. Some of points in above plot are surrounded by inliers but still they are labelled as 1(means outliers).

More analysis

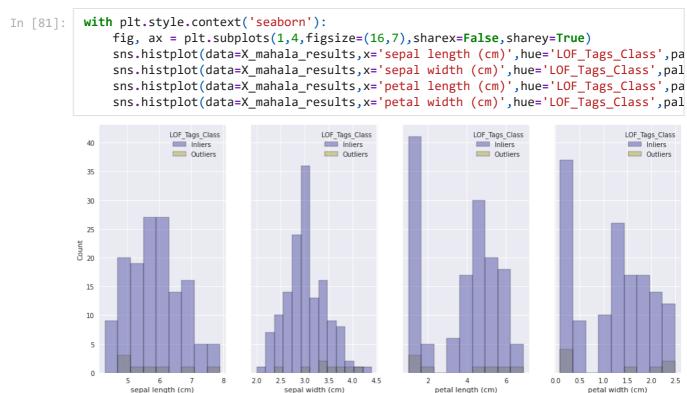


So, all the features have good point variations in the 5 number summary of Inliers and Outliers.

```
In [80]: with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='sepal length (cm)',hue
    sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='sepal width (cm)',hue
    sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='petal length (cm)',hue
    sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='petal width (cm)',hue=
```



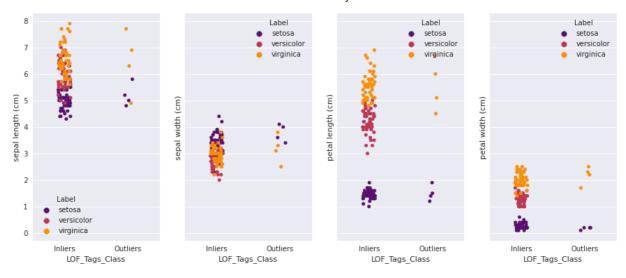
If we look at the outliers then some of the oultiers are even from the area where we have good amount of inliers.



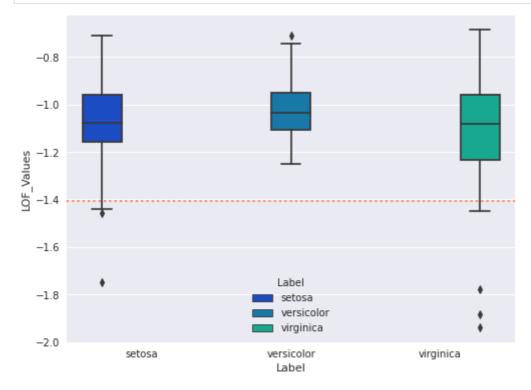
Here, the results are quite different as compared to Euclidean and Manhattan. Outliers here are not the extreme points of the dataset whereas some of them are even from the area where we have good amount of inliers.**

```
In [82]: iris_classes = {0:'setosa',1:'versicolor',2:'virginica'}
   X_mahala_results['Label'] = X_mahala_results['Label'].apply(lambda val : iris_classe

In [83]: with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
        sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='sepal length (cm)',hue
        sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='sepal width (cm)',hue
        sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='petal length (cm)',hue
        sns.stripplot(data=X_mahala_results,x='LOF_Tags_Class',y='petal width (cm)',hue
```



```
In [84]: with plt.style.context('seaborn'):
    plt.figure(figsize=(8,6))
    sns.boxplot(data=X_mahala_results,x='Label',y='LOF_Values',hue='Label',palette='
    plt.axhline(lof_precomp_iris.offset_,color='coral',linestyle=':',linewidth=2)
```



Above showing the outliers captured on the basis of the Mahalanobis Distance used by LOF, out of these no point belongs to Versicolor class.

CASE-IV

Neighbors = 20 & Contamination = 0.1 or 1% & Leaf_Size = 15 & Euclidean as Distance Metric

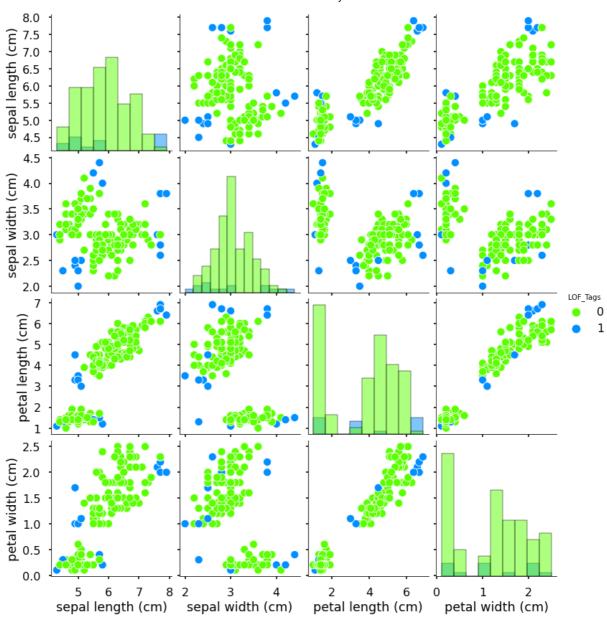
```
In [85]: iris_contam = 0.1
    lof_iris = LocalOutlierFactor(n_neighbors=20,algorithm='kd_tree',leaf_size=15,contam
In [86]: lof_iris_pred = lof_iris.fit_predict(X_iris_df)
    lof_iris_pred.shape
Out[86]: (150,)
```

Out[90]: -1.3060565525969516

The new offset value with higher percentage of contamination has increased quite significantly.

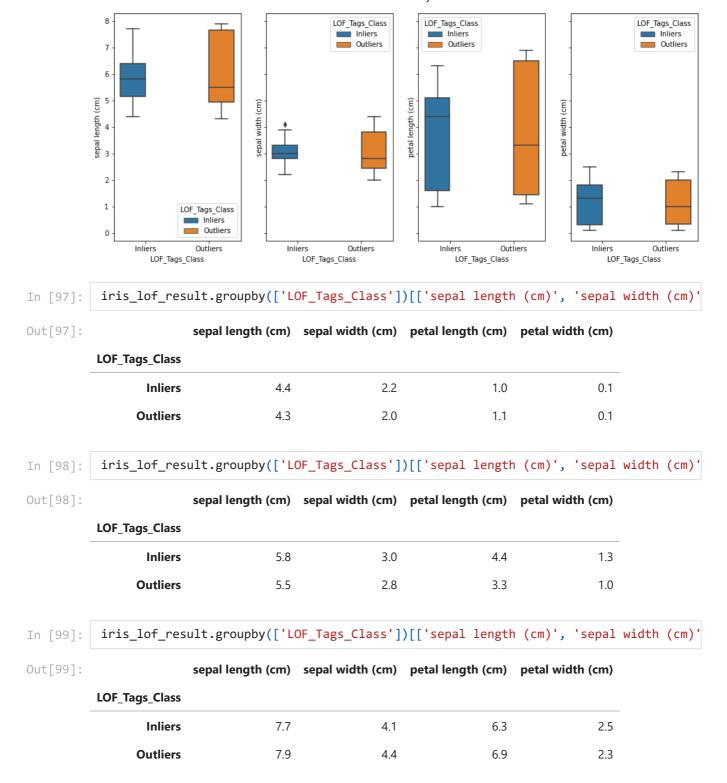
In [92]: iris_lof_result[iris_lof_result['LOF_Values'] < lof_iris_offset]</pre>

Out[92]:		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	Label	LOF_Values	LOF_Tags
	13	4.3	3.0	1.1	0.1	0	-1.325687	1
	14	5.8	4.0	1.2	0.2	0	-1.480203	1
	15	5.7	4.4	1.5	0.4	0	-1.671872	1
	33	5.5	4.2	1.4	0.2	0	-1.365882	1
	41	4.5	2.3	1.3	0.3	0	-1.777582	1
	57	4.9	2.4	3.3	1.0	1	-1.432891	1
	60	5.0	2.0	3.5	1.0	1	-1.395791	1
	93	5.0	2.3	3.3	1.0	1	-1.401342	1
	98	5.1	2.5	3.0	1.1	1	-1.511868	1
	105	7.6	3.0	6.6	2.1	2	-1.399554	1
	106	4.9	2.5	4.5	1.7	2	-1.373468	1
	117	7.7	3.8	6.7	2.2	2	-1.572990	1
	118	7.7	2.6	6.9	2.3	2	-1.624653	1
	122	7.7	2.8	6.7	2.0	2	-1.491365	1
	131	7.9	3.8	6.4	2.0	2	-1.547288	1



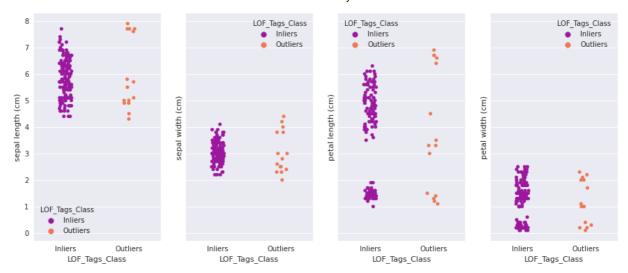
Outliers marking has become a bit aggressive in this case as some of the points near to the clusters are also marked as outliers.

More analysis



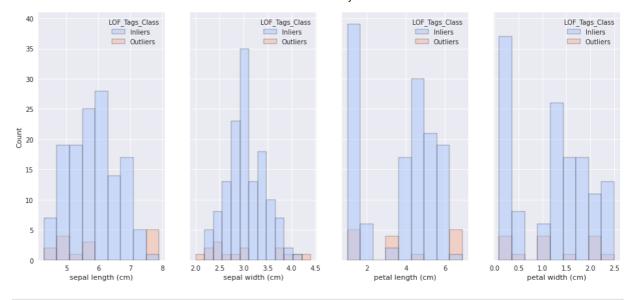
Above boxplots shows us some good amount of variations in features other than Petal Width.

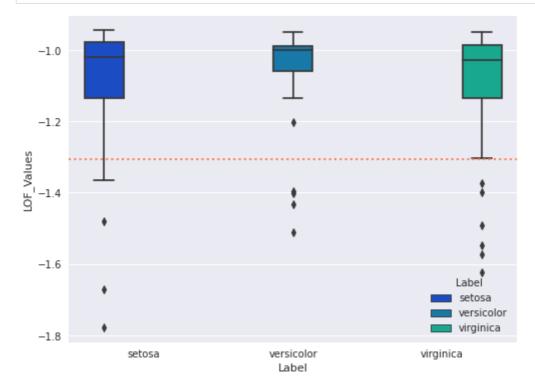
```
with plt.style.context('seaborn'):
    fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue='
    sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
```



One thing to mention here is that as seen in the plots with contamination == 0.05, the outliers are picked from the same or nearby region with contamination == 0.1

```
iris_classes = {0:'setosa',1:'versicolor',2:'virginica'}
In [101...
             iris_lof_result['Label'] = iris_lof_result['Label'].apply(lambda val : iris_classes.
In [102...
             with plt.style.context('seaborn'):
                  fig, ax = plt.subplots(1,4,figsize=(15,6),sharex=True,sharey=True)
                  sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal length (cm)',hue=
                  sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='sepal width (cm)',hue='
sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal length (cm)',hue=
                  sns.stripplot(data=iris_lof_result,x='LOF_Tags_Class',y='petal width (cm)',hue='
                                                                         Label
                                                         setosa
                                                                         setosa
                                                                                                               setosa
                                                         versicolor
                                                                         versicolor
                                                                                                               versicolor
                                                         virginica
                                                                         virginica
                                                                                                               virginica
           length (cm)
                                                                   length (cm)
                                                                                             width (cm)
                                        sepal width (cm)
                                                                                              petal
             2
                   Label
             1
                   setosa
                    versicolo
                   virginica
             0
                             Outliers
                                                        Outliers
                                                                                                              Outliers
                   Inliers
                                             Inliers
                                                                        Inliers
                                                                                   Outliers
                                                                                                   Inliers
                     LOF_Tags_Class
                                                LOF Tags Class
                                                                           LOF Tags Class
                                                                                                     LOF Tags Class
            with plt.style.context('seaborn'):
In [103...
                  fig, ax = plt.subplots(1,4,figsize=(16,7),sharex=False,sharey=True)
                  sns.histplot(data=iris_lof_result,x='sepal length (cm)',hue='LOF_Tags_Class',pal
                  sns.histplot(data=iris_lof_result,x='sepal width (cm)',hue='LOF_Tags_Class',pale
                  sns.histplot(data=iris_lof_result,x='petal length (cm)',hue='LOF_Tags_Class',pal
                  sns.histplot(data=iris_lof_result,x='petal width (cm)',hue='LOF_Tags_Class',pale
```





As, we can see here the offset value shifted a bit upwards thus few of the data points of Versicolor are also been labelled as Outliers.

Results_Analysis

In the above analysis across all 4 cases, I have observed that LOF is good in capturing the local and global outliers, however there are few things which we need to take into account before using it:

 As it relies on distances between the points so we need to be sure with the distance metric that we are using

- For example, when I used Mahalanobis Distance then I observed some of points which were surrounded by others points labelled as Outliers, however, this behavior is not observed with E.D and M.D.
- Another example, if dataset has categorical variables then these should be handled before and converted into numerical values
- Similarly, the scale has to be same across features otherwise distances will gets skewed
- With a small dataset this can be a good approach but if we have a high dimensional data then it suffers with all the drawbacks of KNN.

Novelty_Detection

There is a slight difference between the Outlier and Novelty Detection.

• Outliers are also known as Novelty, in outlier detection we provide the dataset features in the LOF then based on it we identify the potential outliers. However, in the Novelty Detection we train the model on Outliers free dataset then fed the unseen data into it to find the outliers in the provided unseen dataset.

```
In [132...
          X = iris_lof_result[iris_lof_result['LOF_Tags'] == 0][['sepal length (cm)','sepal wi
          y = iris_lof_result[iris_lof_result['LOF_Tags'] == 0][['Label']].copy(deep=True)
In [133...
         X.shape, y.shape
Out[133... ((135, 4), (135, 1))
In [134...
         X_test = iris_lof_result[iris_lof_result['LOF_Tags'] == 1][['sepal length (cm)','sep
          y_test = iris_lof_result[iris_lof_result['LOF_Tags'] == 1][['Label']].copy(deep=True
In [135... | X_test.shape, y_test.shape
Out[135... ((15, 4), (15, 1))
In [136...
         novl_lof = LocalOutlierFactor(n_neighbors=25,algorithm='kd_tree',novelty=True,contam
In [137... novl_lof.fit(X)
Out[137... LocalOutlierFactor(algorithm='kd_tree', contamination=0.1, leaf_size=15,
                             n_neighbors=25, novelty=True)
```

I have used the dataset cleaned in the above Outlier Detection, so I'm using the outliers free features as a train data and the observations which were declared Outliers in the above steps as a test set.

```
In [138... nov1_lof.offset_
Out[138... -1.1395064780485147
```

When novelty is set to True be aware that you must only use predict, decision_function and score_samples on new unseen data and not on the

training samples as this would lead to wrong results.

```
In [139... novl_lof.decision_function(X_test.iloc[0:2,:])
Out[139... array([-0.21279232, -0.39126247])
In [140... novl_lof.decision_function(X_test.iloc[:,:])
Out[140... array([-0.21279232, -0.39126247, -0.62380956, -0.25358871, -0.67333104, -0.40624575, -0.37870996, -0.37254652, -0.52122239, -0.39445628, -0.13998717, -0.64729715, -0.69816836, -0.5362388 , -0.62497454])
```

For the majority of test records the shifted opposite LOF scores are away from 0 and all are negatives thus all are classified as Outliers. If the shifted opposite score is a large and positive number then it is an inlier.

```
In [142... novl_lof.decision_function([[1.33717756, 1.00979142, 1.16971425, 1.05217993]])
Out[142... array([-6.18355273])
In [143... novl_lof.predict([[1.33717756, 1.00979142, 1.16971425, 1.05217993]])
Out[143... array([-1])
```

The shifted opposite LOF score is +ve thus Random Test Input is labelled as Inlier.

This is the opposite of LOF score returned by score_samples the higher this score means obervation is an inlier. In our case, all the scores are -ve thus all are labelled as Outliers.

• The offset from training data is -1.16 and the opposite LOF score for the test data is greater than the offset value thus all are marked as Outliers.

```
In [145... novl_lof.score_samples([[1.33717756, 1.00979142, 1.16971425, 1.05217993]])
Out[145... array([-7.32305921])
```

• The opposite LOF score of the random test input is less than -1.16 thus it is marked as Inlier.

```
In [146... X['-ve_lof'] = novl_lof.negative_outlier_factor_
In [147... X[X['-ve_lof'] <= novl_lof.offset_].shape
```

Out[147... (14, 5)

```
In [148... X[X['-ve_lof'] <= novl_lof.offset_]</pre>
```

Out[148		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	-ve_lof
	5	5.4	3.9	1.7	0.4	-1.152862
	8	4.4	2.9	1.4	0.2	-1.221901
	18	5.7	3.8	1.7	0.3	-1.290834
	22	4.6	3.6	1.0	0.2	-1.209243
	32	5.2	4.1	1.5	0.1	-1.219220
	38	4.4	3.0	1.3	0.2	-1.193754
	50	7.0	3.2	4.7	1.4	-1.170177
	79	5.7	2.6	3.5	1.0	-1.157464
	81	5.5	2.4	3.7	1.0	-1.140011
	107	7.3	2.9	6.3	1.8	-1.305762
	109	7.2	3.6	6.1	2.5	-1.266638
	125	7.2	3.2	6.0	1.8	-1.157932
	130	7.4	2.8	6.1	1.9	-1.272495
	135	7.7	3.0	6.1	2.3	-1.402265

In [149... X_test['Oppo_LOF_score'] = novl_lof.score_samples(X_test)
 X_test['shif_opp_LOF_score'] = novl_lof.decision_function(X_test.iloc[:,0:-1])

In [150... X_test[X_test['Oppo_LOF_score'] < novl_lof.offset_]</pre>

Out[150		sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)	Oppo_LOF_score	shif_opp_LOF_score
	13	4.3	3.0	1.1	0.1	-1.352299	-0.212792
	14	5.8	4.0	1.2	0.2	-1.530769	-0.391262
	15	5.7	4.4	1.5	0.4	-1.763316	-0.623810
	33	5.5	4.2	1.4	0.2	-1.393095	-0.253589
	41	4.5	2.3	1.3	0.3	-1.812838	-0.673331
	57	4.9	2.4	3.3	1.0	-1.545752	-0.406246
	60	5.0	2.0	3.5	1.0	-1.518216	-0.378710
	93	5.0	2.3	3.3	1.0	-1.512053	-0.372547
	98	5.1	2.5	3.0	1.1	-1.660729	-0.521222
	105	7.6	3.0	6.6	2.1	-1.533963	-0.394456
	106	4.9	2.5	4.5	1.7	-1.279494	-0.139987
	117	7.7	3.8	6.7	2.2	-1.786804	-0.647297
	118	7.7	2.6	6.9	2.3	-1.837675	-0.698168
	122	7.7	2.8	6.7	2.0	-1.675745	-0.536239

petal width

(cm)

Oppo_LOF_score shif_opp_LOF_score

	131	7.9	3.8	6.4	2.0	-1.764481	-0.624975
In [151	X_te	est['Oppo_LOF_s	core'] - X_t	est['shif_op	p_LOF_scor	e']	
Out[151	13	-1.139506					
000[202	14	-1.139506					
	15	-1.139506					
	33	-1.139506					
	41	-1.139506					
	57	-1.139506					
	60	-1.139506					
	93	-1.139506					
	98	-1.139506					
	105	-1.139506					
	106	-1.139506					
	117	-1.139506					
	118	-1.139506					
	122	-1.139506					
	131	-1.139506					
	dtype	e: float64					

petal length

(cm)

```
In [159... novl_lof.offset_
```

Out[159... -1.1395064780485147

sepal length

(cm)

sepal width

(cm)

```
In [158... np.round(np.unique(X_test['Oppo_LOF_score'] - X_test['shif_opp_LOF_score'])[0],4) ==
```

Out[158... True

Relationship_bw_DF_SC_and_OFF

This means Decision_Function values = Score_Samples values - Offset

Points_to_remember_when_doing_novelty_detection

In my analysis I found that LOF works good with a small dimensional dataset to find the local and global outliers. Few points we need to consider while working with NOVELTY DETECTION using LOF:

- SciKit-Learn implements two "modes" for LocalOutlierFactor, where one is unsupervised(NOVELTY=FALSE) and one is semi-supervised(NOVELTY=True).
- Novelty: boolean, default False By default, LocalOutlierFactor is only meant to be used for outlier detection (novelty=False). Set novelty to True if you want to use LocalOutlierFactor for novelty detection. In this case be aware that that you should only use predict, decision_function and score_samples on new unseen data and not on the training set.