9-9.3-12

EE24BTECH11028 - Jadhav Rajesh

Question: If area between the curve $x = y^2$ and x = 4 is diveded into two equalparts by the line x = a, then find the value of a.

Solution: : The given parameters are

$$V = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, u = \frac{-1}{2}e_1 f = 0 \tag{0.1}$$

the parameters of the lines are

$$q_2 = \begin{pmatrix} a \\ 0 \end{pmatrix}, m_2 = e_2 \tag{0.2}$$

$$\mu_i = \frac{1}{m^T V m} ((-m^T (V h + u) \pm \sqrt{(m^T (V h + u))^2} - g(h) (m^T V m))$$
(0.3)

subtituting the above values in (0.3)

$$\mu_i = a, -a \tag{0.4}$$

yeilding the points of intersection as

$$a_0 = \begin{pmatrix} a \\ a \end{pmatrix}, a_1 = \begin{pmatrix} a \\ -a \end{pmatrix} \tag{0.5}$$

simailar, for the line x - 4 = 0,

$$q_1 = \begin{pmatrix} 4 \\ 0 \end{pmatrix}, m_1 = e_2 \tag{0.6}$$

yeilding

$$\mu_i = 2, -2 \tag{0.7}$$

and

$$a_3 = \begin{pmatrix} 4 \\ 2 \end{pmatrix}, a_2 = \begin{pmatrix} 4 \\ -2 \end{pmatrix} \tag{0.8}$$

Area between parabola and the line x = 4 is divided equally by the line x = a. Thus,

$$A_1 = \int_0^a \sqrt{x} dx \tag{0.9}$$

$$A_2 = \int_a 4\sqrt{x} dx \tag{0.10}$$

$$and A_1 = A_2 \tag{0.11}$$

$$\Rightarrow a = 4^{\frac{2}{3}} \tag{0.12}$$

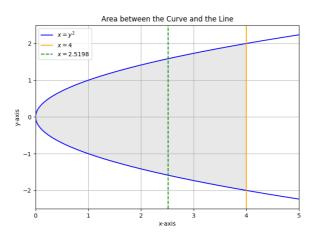


Fig. 0.1