

1.1.6-21

EE24BTECH11028 - Jadhav Rajesh

Question: Show that points $A(a, b + c)$, $B(b, c + a)$, $C(c, a + b)$ are collinear.

Solution: : We know that points, A, B, C are collinear, if

$$\text{rank} \begin{pmatrix} B - A \\ C - A \end{pmatrix}^T = 1 \quad (0.1)$$

$$\text{rank} \begin{pmatrix} b - a & a - b \\ c - a & a - c \end{pmatrix}^T = 1 \quad (0.2)$$

$$\begin{pmatrix} b - a & c - a \\ a - b & a - c \end{pmatrix} \quad (0.3)$$

$$R_2 \rightarrow R_2 - R_1 \quad (0.4)$$

$$\begin{pmatrix} b - a & c - a \\ 0 & 0 \end{pmatrix} \quad (0.5)$$

Thus, the rank of matrix is 1 and the points are collinear.

Define the coordinates of points A, B, and C.

$$a, b, c = 1, 2, 3 \quad (0.6)$$

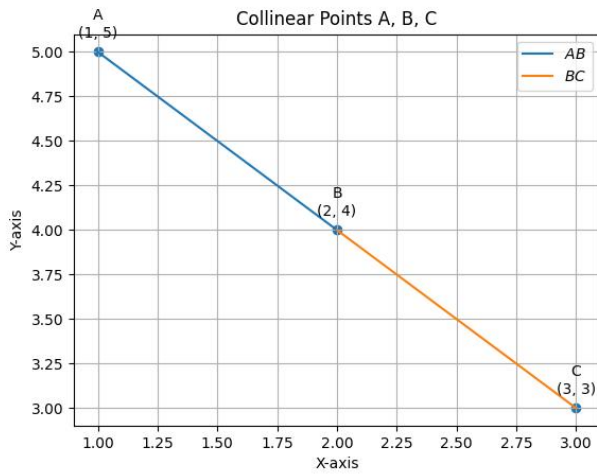


Fig. 0.1: Plot of points **A**, **B** and **P**