

DISCRETE 1-1.5-8

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Question

Find the ratio in which $P(4, 5)$ divides the line segment joining $A(2, 3)$ and $B(7, 8)$

Solution: Table

points	description	formula
$A(2, 3)$	one end of line segment	—
$B(7, 8)$	another end of line segment	—
$P(4, 5)$	divides A and B in the ratio $k : 1$	$P = \frac{A+kB}{k+1}$

Table: Variables Used

$$P = \frac{\mathbf{A}}{k+1} + \frac{k\mathbf{B}}{k+1} \quad (1)$$

$$\Rightarrow p = (\mathbf{A} \quad \mathbf{B}) \begin{pmatrix} \frac{1}{k+1} \\ \frac{k}{k+1} \end{pmatrix} \quad (2)$$

$$\text{from (2)} \quad (3)$$

$$\Rightarrow \begin{pmatrix} 4 \\ 5 \end{pmatrix} = \begin{pmatrix} 2 & 7 \\ 3 & 8 \end{pmatrix} \begin{pmatrix} \frac{1}{k+1} \\ \frac{k}{k+1} \end{pmatrix} \quad (4)$$

$$\Rightarrow \begin{pmatrix} 4 \\ 5 \end{pmatrix} = \begin{pmatrix} \frac{2}{k+1} + \frac{7k}{k+1} \\ \frac{3}{k+1} + \frac{8k}{k+1} \end{pmatrix} \quad (5)$$

$$\Rightarrow 4 = \frac{2 + 7k}{k + 1} \quad (6)$$

$$\Rightarrow 4k + 4 = 2 + 7k \quad (7)$$

$$3k = 2 \quad (8)$$

$$k = \frac{2}{3} \quad (9)$$

$$(10)$$

$$k:1 = \frac{2}{3}:1 \quad (11)$$

2 : 3

Python Code

Python Code

Python Code

Python Code

Figure

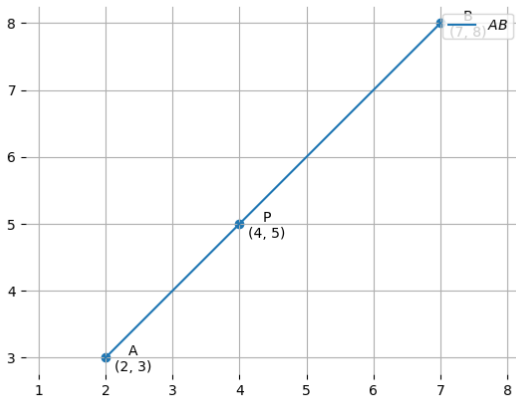


Figure: P divides A and B in the ratio 2 : 3