

# 01-07-2020 SHIFT-1-1-15

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- 1) The area of the region, enclosed by the circle  $x^2 + y^2 = 2$  which is not common to the region bounded by the parabola  $y^2 = x$  and straight line  $y = x$ , is
  - a)  $\left(\frac{1}{3}\right)(12\pi - 1)$
  - b)  $\left(\frac{1}{6}\right)(12\pi - 1)$
  - c)  $\left(\frac{1}{3}\right)(6\pi - 1)$
  - d)  $\left(\frac{1}{6}\right)(24\pi - 1)$
- 2) Total number of six-digit numbers in which only and all five digits 1, 3, 5, 7 and 9 appear, is
  - a)  $5^6$
  - b)  $\left(\frac{1}{2}\right)(6!)$
  - c)  $6!$
  - d)  $\left(\frac{5}{2}\right)6!$
- 3) An unbiased coin is tossed 5 times. Suppose that a variable  $X$  is assigned the value  $k$  when  $k$  consecutive heads are obtained for  $k = 3, 4, 5$ , otherwise  $X$  takes the value  $-1$ . The expected value of  $X$ , is
  - a)  $\frac{1}{8}$
  - b)  $\frac{3}{16}$
  - c)  $\frac{16}{8}$
  - d)  $\frac{3}{16}$
- 4) If  $\operatorname{Re} \left( \frac{z-1}{(2z+i)} \right) = 1$ , where  $z = x + iy$ , then the point  $(x, y)$  lies on a
  - a) circle whose centre is at  $\left(\frac{-1}{2}, \frac{-3}{2}\right)$
  - b) straight line whose slope is  $\frac{3}{2}$
  - c) circle whose diameter is  $\frac{\sqrt{5}}{2}$
  - d) straight line whose slope is  $\frac{-2}{3}$
- 5) If  $f(a + b + 1 - x) = f(x) \forall x$ , where  $a$  and  $b$  are fixed positive real numbers, then  $\frac{1}{(a+b)} \int_a^b x(f(x) + f(x+1)) dx$  is equal to
  - a)  $\int_{a-1}^{b-1} f(x) dx$
  - b)  $\int_{a+1}^{b+1} f(x+1) dx$
  - c)  $\int_{a-1}^{b-1} f(x+1) dx$
  - d)  $\int_{a+1}^{b+1} f(x) dx$
- 6) If the distance between the foci of an ellipse is 6 and the distance between its directrices is 12, then the length of its latus rectum is
  - a)  $2\sqrt{3}$
  - b)  $\sqrt{3}$
  - c)  $\frac{3}{\sqrt{2}}$
  - d)  $3\sqrt{2}$
- 7) The logical statement  $(p \implies q) \wedge (q \implies \sim p)$  is equivalent to
  - a)  $\sim p$
  - b)  $p$
  - c)  $q$
  - d)  $\sim q$
- 8) The greatest positive integer  $k$ , for which  $49^k + 1$  is a factor of the sum  $49^{125} + 49^{124} + \dots + 49^2 + 49 + 1$ , is
  - a) 32
  - b) 60
  - c) 65
  - d) 63
- 9) A vector  $\mathbf{a} = \alpha \hat{i} + 2\hat{j} + \beta \hat{k}$  ( $\alpha, \beta \in \mathbf{R}$ ) lies in the plane of the vectors,  $\mathbf{b} = \hat{i} + \hat{j}$  and  $\mathbf{c} = \hat{i} - \hat{j} + 4\hat{k}$ . If  $\mathbf{a}$  bisects the angle between  $\mathbf{b}$  and  $\mathbf{c}$ , then
  - a)  $\alpha \hat{i} + 3 = 0$
  - b)  $\alpha \hat{k} + 4 = 0$
  - c)  $\alpha \hat{i} + 1 = 0$
  - d)  $\alpha \hat{k} + 2 = 0$
- 10) If  $y(\alpha) = \sqrt{2 \left( \frac{\tan \alpha + \cot \alpha}{1 + \tan^2 \alpha} \right) + \frac{1}{\sin^2 \alpha}}$  where  $\alpha \in \left(\frac{3\pi}{4}, \pi\right)$  then  $\frac{dy}{d\alpha}$  at  $\alpha = \frac{5\pi}{6}$  is
  - a)  $-\frac{1}{4}$
  - b)  $\frac{4}{3}$
  - c) 4
  - d) -4

- 11)  $y = mx + 4$  is a tangent to both the parabolas,  $y^2 = 4x$  and  $x^2 = 2by$ , then  $b$  is equal to
- 64
  - 128
  - 128
  - 32
- 12) Let  $\alpha$  be a root of the equation  $x^2 + x + 1 = 0$  and the matrix  $A = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 1 & 1 \\ 1 & \alpha & \alpha^2 \\ 1 & \alpha^2 & \alpha^4 \end{pmatrix}$  then the matrix  $A^{31}$  is equal to
- $A$
  - $A^2$
  - $A^3$
  - $I_3$
- 13) If  $g(x) = x^2 + x - 1$  and  $(g \circ f)(x) = 4x^2 - 10x + 5$ , then  $f\left(\frac{5}{4}\right)$  is equal to
- $\frac{-3}{2}$
  - $\frac{-1}{2}$
  - $\frac{1}{2}$
  - $\frac{3}{2}$
- 14) let  $\alpha$  and  $\beta$  are two real roots of the equation  $(k+1)\tan^2 x - \sqrt{2}\lambda \tan x = 1 - k$ , where  $(k \neq -1)$  and are real numbers. If  $\tan^2(\alpha + \beta) = 50$ , then value of  $\lambda$  is
- $5\sqrt{2}$
  - $10\sqrt{2}$
  - 10
  - 5
- 15) Let  $P$  be a plane passing through the points  $(2, 1, 0)$ ,  $(4, 1, 1)$  and  $(5, 0, 1)$  and  $R$  be any point  $(2, 1, 6)$ . Then the image of  $R$  in the plane  $P$  is:
- $(6, 5, 2)$
  - $(6, 5, -2)$
  - $(4, 3, 2)$
  - $(3, 4, -2)$