

# DIFFERENTIAL EQUATIONS

## OBJECTIVES

1. The degree of the differential equation  $\frac{d^2y}{dx^2} + \sqrt{1 + \left(\frac{dy}{dx}\right)^3} = 0$  is
  - (a) 1
  - (b) 2
  - (c) 3
  - (d) 6
2. The order and degree of the differential equation  $\left[4 + \left(\frac{dy}{dx}\right)^2\right]^{2/3} = \frac{d^2y}{dx^2}$  are
  - (a) 2, 2
  - (b) 3, 3
  - (c) 2, 3
  - (d) 3, 2
3. The order of the differential equation  $y\left(\frac{dy}{dx}\right) = x\left/\frac{dy}{dx} + \left(\frac{dy}{dx}\right)^3\right.$  is
  - (a) 1
  - (b) 2
  - (c) 3
  - (d) 4
4. The order and degree of the differential equation  $\rho = \frac{\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{3/2}}{d^2y/dx^2}$  are respectively
  - (a) 2, 2
  - (b) 2, 3
  - (c) 2, 1
  - (d) None of these
- 5 The order and degree of the differential equation  $\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^4 - xy = 0$  are respectively
  - (a) 2 and 4
  - (b) 3 and 2
  - (c) 4 and 5
  - (d) 2 and 3
6. The degree of the differential equation  $\left(1 + \left(\frac{dy}{dx}\right)^2\right)^{3/4} = \left(\frac{d^2y}{dx^2}\right)^{1/3}$  is
  - (a)  $\frac{1}{3}$
  - (b) 4
  - (c) 9
  - (d)  $\frac{3}{4}$

**7 The degree of the differential equation**  $y(x) = 1 + \frac{dy}{dx} + \frac{1}{1.2} \left( \frac{dy}{dx} \right)^2 + \frac{1}{1.2.3} \left( \frac{dy}{dx} \right)^3 + \dots$  **is**

- (a) 2 (b) 3  
(c) 1 (d) None of these

**8 Which of the following differential equations has the same order and degree**

- (a)  $\frac{d^4 y}{dx^4} + 8 \left( \frac{dy}{dx} \right)^6 + 5y = e^x$   
(b)  $5 \left( \frac{d^3 y}{dx^3} \right)^4 + 8 \left( 1 + \frac{dy}{dx} \right)^2 + 5y = x^8$   
(c)  $\left[ 1 + \left( \frac{dy}{dx} \right)^3 \right]^{2/3} = 4 \frac{d^3 y}{dx^3}$   
(d)  $y = x^2 \frac{dy}{dx} + \sqrt{1 + \left( \frac{dy}{dx} \right)^2}$

**9. The order of the differential equation of a family of curves represented by an equation containing four arbitrary constants, will be**

- (a) 2 (b) 4  
(c) 6 (d) None of these

**10. Order and degree of differential equation**  $\frac{d^2 y}{dx^2} = \left\{ y + \left( \frac{dy}{dx} \right)^2 \right\}^{1/4}$  **are**

- (a) 4 and 2 (b) 1 and 2  
(c) 1 and 4 (d) 2 and 4

**11. Order of the differential equation of the family of all concentric circles centered at  $(h, k)$  is**

- (a) 1 (b) 2  
(c) 3 (d) 4

**12. Family  $y = Ax + A^3$  of curve represented by the differential equation of degree**

- (a) Three (b) Two  
(c) One (d) None of these

13. The degree and order of the differential equation of the family of all parabolas whose axis is  $x$ -axis, are respectively

- (a) 2, 1 (b) 1, 2 (c) 3, 2 (d) 2, 3

14. The order of the differential equation whose solution is  $x^2 + y^2 + 2gx + 2fy + c = 0$ , is

- (a) 1 (b) 2  
(c) 3 (d) 4

15. The order of the differential equation whose solution is  $y = a \cos x + b \sin x + ce^{-x}$  is

- (a) 3 (b) 2  
(c) 1 (d) None of these

16. The order of the differential equation of all circles of radius  $r$ , having centre on  $y$ -axis and passing through the origin is

- (a) 1 (b) 2  
(c) 3 (d) 4

17. The differential equation of the family of curves represented by the equation  $x^2 + y^2 = a^2$  is

- (a)  $x + y \frac{dy}{dx} = 0$  (b)  $y \frac{dy}{dx} = x$   
(c)  $y \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$  (d) None of these

18. The differential equation for the line  $y = mx + c$  is (where  $c$  is arbitrary constant)

- (a)  $\frac{dy}{dx} = m$  (b)  $\frac{dy}{dx} + m = 0$   
(c)  $\frac{dy}{dx} = 0$  (d) None of these

19. The differential equation for all the straight lines which are at a unit distance from the origin is

- (a)  $\left(y - x \frac{dy}{dx}\right)^2 = 1 - \left(\frac{dy}{dx}\right)^2$  (b)  $\left(y + x \frac{dy}{dx}\right)^2 = 1 + \left(\frac{dy}{dx}\right)^2$   
(c)  $\left(y - x \frac{dy}{dx}\right)^2 = 1 + \left(\frac{dy}{dx}\right)^2$  (d)  $\left(y + x \frac{dy}{dx}\right)^2 = 1 - \left(\frac{dy}{dx}\right)^2$

20. The differential equation of all circles which passes through the origin and whose centre lies on  $y$ -axis, is

- (a)  $(x^2 - y^2) \frac{dy}{dx} - 2xy = 0$  (b)  $(x^2 - y^2) \frac{dy}{dx} + 2xy = 0$  (c)  $(x^2 - y^2) \frac{dy}{dx} - xy = 0$  (d)  $(x^2 - y^2) \frac{dy}{dx} + xy = 0$

**21. The differential equation corresponding to primitive  $y = e^{cx}$  is**

or

The elimination of the arbitrary constant  $m$  from the equation  $y = e^{mx}$  gives the differential equation is

- (a)  $\frac{dy}{dx} = \left(\frac{y}{x}\right) \log x$       (b)  $\frac{dy}{dx} = \left(\frac{x}{y}\right) \log y$   
 (c)  $\frac{dy}{dx} = \left(\frac{y}{x}\right) \log y$       (d)  $\frac{dy}{dx} = \left(\frac{x}{y}\right) \log x$

**22. The differential equation whose solution is  $y = A \sin x + B \cos x$ , is**

- (a)  $\frac{d^2y}{dx^2} + y = 0$       (b)  $\frac{d^2y}{dx^2} - y = 0$   
 (c)  $\frac{dy}{dx} + y = 0$       (d) None of these

**23. If  $y = ce^{\sin^{-1} x}$ , then corresponding to this the differential equation is**

- (a)  $\frac{dy}{dx} = \frac{y}{\sqrt{1-x^2}}$       (b)  $\frac{dy}{dx} = \frac{1}{\sqrt{1-x^2}}$   
 (c)  $\frac{dy}{dx} = \frac{x}{\sqrt{1-x^2}}$       (d) None of these

**24.  $y = ae^{mx} + be^{-mx}$  satisfies which of the following differential equations**

- (a)  $\frac{dy}{dx} - my = 0$       (b)  $\frac{dy}{dx} + my = 0$   
 (c)  $\frac{d^2y}{dx^2} + m^2y = 0$       (d)  $\frac{d^2y}{dx^2} - m^2y = 0$

**25. The differential equation of all straight lines passing through the point  $(1, -1)$  is**

- (a)  $y = (x+1) \frac{dy}{dx} + 1$       (b)  $y = (x+1) \frac{dy}{dx} - 1$   
 (c)  $y = (x-1) \frac{dy}{dx} + 1$       (d)  $y = (x-1) \frac{dy}{dx} - 1$

**26. The differential equation of all parabolas whose axes are parallel to y-axis is**

- (a)  $\frac{d^3y}{dx^3} = 0$       (b)  $\frac{d^2x}{dy^2} = c$   
 (c)  $\frac{d^3y}{dx^3} + \frac{d^2x}{dy^2} = 0$       (d)  $\frac{d^2y}{dx^2} + 2 \frac{dy}{dx} = c$

27. The differential equation of the family of curves represented by the equation  $x^2y = a$ , is

- (a)  $\frac{dy}{dx} + \frac{2y}{x} = 0$       (b)  $\frac{dy}{dx} + \frac{2x}{y} = 0$   
 (c)  $\frac{dy}{dx} - \frac{2y}{x} = 0$       (d)  $\frac{dy}{dx} - \frac{2x}{y} = 0$

28. Differential equation whose solution is  $y = cx + c - c^3$ , is

- (a)  $\frac{dy}{dx} = c$       (b)  $y = x \frac{dy}{dx} + \frac{dy}{dx} - \left(\frac{dy}{dx}\right)^3$   
 (c)  $\frac{dy}{dx} = c - 3c^2$       (d) None of these

29. The differential equation whose solution is  $y = c_1 \cos ax + c_2 \sin ax$  is

(Where  $c_1, c_2$  are arbitrary constants)

- (a)  $\frac{d^2y}{dx^2} + y^2 = 0$       (b)  $\frac{d^2y}{dx^2} + a^2y = 0$   
 (c)  $\frac{d^2y}{dx^2} + ay^2 = 0$       (d)  $\frac{d^2y}{dx^2} - a^2y = 0$

30. Family of curves  $y = e^x(A \cos x + B \sin x)$ , represents the differential equation

- (a)  $\frac{d^2y}{dx^2} = 2 \frac{dy}{dx} - y$       (b)  $\frac{d^2y}{dx^2} = 2 \frac{dy}{dx} - 2y$   
 (c)  $\frac{d^2y}{dx^2} = \frac{dy}{dx} - 2y$       (d)  $\frac{d^2y}{dx^2} = 2 \frac{dy}{dx} + y$

31. If  $y = ax^{n+1} + bx^{-n}$ , then  $x^2 \frac{d^2y}{dx^2}$  equals to

- (a)  $n(n-1)y$       (b)  $n(n+1)y$   
 (c)  $ny$       (d)  $n^2y$

32. Differential equation of  $y = \sec(\tan^{-1} x)$  is

- (a)  $(1+x^2) \frac{dy}{dx} = y + x$       (b)  $(1+x^2) \frac{dy}{dx} = y - x$   
 (c)  $(1+x^2) \frac{dy}{dx} = xy$       (d)  $(1+x^2) \frac{dy}{dx} = \frac{x}{y}$

33. If  $x = \sin t$ ,  $y = \cos pt$ , then

- (a)  $(1 - x^2)y_2 + xy_1 + p^2y = 0$
- (b)  $(1 - x^2)y_2 + xy_1 - p^2y = 0$
- (c)  $(1 + x^2)y_2 - xy_1 + p^2y = 0$
- (d)  $(1 - x^2)y_2 - xy_1 + p^2y = 0$

34. The differential equation for which  $\sin^{-1} x + \sin^{-1} y = c$  is given by

- (a)  $\sqrt{1 - x^2} dx + \sqrt{1 - y^2} dy = 0$
- (b)  $\sqrt{1 - x^2} dy + \sqrt{1 - y^2} dx = 0$
- (c)  $\sqrt{1 - x^2} dy - \sqrt{1 - y^2} dx = 0$
- (d)  $\sqrt{1 - x^2} dx - \sqrt{1 - y^2} dy = 0$

35. The solution of the differential equation  $\frac{dy}{dx} + \frac{1 + x^2}{x} = 0$  is

- (a)  $y = -\frac{1}{2} \tan^{-1} x + c$
- (b)  $y + \log x + \frac{x^2}{2} + c = 0$
- (c)  $y = \frac{1}{2} \tan^{-1} x + c$
- (d)  $y - \log x - \frac{x^2}{2} = c$

36. The solution of the differential equation  $\frac{dy}{dx} = e^x + \cos x + x + \tan x$  is

- (a)  $y = e^x + \sin x + \frac{x^2}{2} + \log \cos x + c$
- (b)  $y = e^x + \sin x + \frac{x^2}{2} + \log \sec x + c$
- (c)  $y = e^x - \sin x + \frac{x^2}{2} + \log \cos x + c$
- (d)  $y = e^x - \sin x + \frac{x^2}{2} + \log \sec x + c$

37. The solution of the equation  $\sin^{-1}\left(\frac{dy}{dx}\right) = x + y$  is

- (a)  $\tan(x + y) + \sec(x + y) = x + c$
- (b)  $\tan(x + y) - \sec(x + y) = x + c$
- (c)  $\tan(x + y) + \sec(x + y) + x + c = 0$
- (d) None of these

**38. The solution of the differential equation  $\frac{dy}{dx} = (1+x)(1+y^2)$  is**

- (a)  $y = \tan(x^2 + x + c)$  (b)  $y = \tan(2x^2 + x + c)$   
 (c)  $y = \tan(x^2 - x + c)$  (d)  $y = \tan\left(\frac{x^2}{2} + x + c\right)$

**39. The solution of the equation  $\frac{dy}{dx} + \sqrt{\frac{1-y^2}{1-x^2}} = 0$  is**

- (a)  $x\sqrt{1-y^2} - y\sqrt{1-x^2} = c$   
 (b)  $x\sqrt{1-y^2} + y\sqrt{1-x^2} = c$   
 (c)  $x\sqrt{1+y^2} + y\sqrt{1+x^2} = c$   
 (d) None of these

**40. Solution of the equation  $\cos x \cos y \frac{dy}{dx} = -\sin x \sin y$  is**

- (a)  $\sin y + \cos x = c$  (b)  $\sin y - \cos x = c$   
 (c)  $\sin y \cdot \cos x = c$  (d)  $\sin y = c \cos x$

**41. The solution of the differential equation  $(x^2 - yx^2) \frac{dy}{dx} + y^2 + xy^2 = 0$  is**

- (a)  $\log\left(\frac{x}{y}\right) = \frac{1}{x} + \frac{1}{y} + c$  (b)  $\log\left(\frac{y}{x}\right) = \frac{1}{x} + \frac{1}{y} + c$   
 (c)  $\log(xy) = \frac{1}{x} + \frac{1}{y} + c$  (d)  $\log(xy) + \frac{1}{x} + \frac{1}{y} = c$

**42. The solution of the differential equation  $\frac{dy}{dx} = \sec x (\sec x + \tan x)$  is**

- (a)  $y = \sec x + \tan x + c$  (b)  $y = \sec x + \cot x + c$   
 (c)  $y = \sec x - \tan x + c$  (d) None of these

**43. The solution of the differential equation  $\frac{dy}{dx} = \frac{(1+x)y}{(y-1)x}$  is**

- (a)  $\log xy + x + y = c$  (b)  $\log\left(\frac{x}{y}\right) + x - y = c$   
 (c)  $\log xy + x - y = c$  (d) None of these

**44. The solution of  $\frac{dy}{dx} = \sin(x+y) + \cos(x+y)$  is**

- (a)  $\log\left[1 + \tan\left(\frac{x+y}{2}\right)\right] + c = 0$
- (b)  $\log\left[1 + \tan\left(\frac{x+y}{2}\right)\right] = x + c$
- (c)  $\log\left[1 - \tan\left(\frac{x+y}{2}\right)\right] = x + c$
- (d) None of these

**45. The solution of the differential equation  $\frac{dy}{dx} = \frac{x-y+3}{2(x-y)+5}$  is**

- (a)  $2(x-y) + \log(x-y) = x + c$
- (b)  $2(x-y) - \log(x-y+2) = x + c$
- (c)  $2(x-y) + \log(x-y+2) = x + c$
- (d) None of these

**46. Solution of the equation  $(e^x + 1)ydy = (y+1)e^x dx$  is**

- (a)  $c(y+1)(e^x + 1) + e^y = 0$  (b)  $c(y+1)(e^x - 1) + e^y = 0$
- (c)  $c(y+1)(e^x - 1) - e^y = 0$  (d)  $c(y+1)(e^x + 1) = e^y$

**47. The solution of the differential equation  $(x+y)^2 \frac{dy}{dx} = a^2$  is**

- (a)  $(x+y)^2 = \frac{a^2}{2}x + c$  (b)  $(x+y)^2 = a^2x + c$
- (c)  $(x+y)^2 = 2a^2x + c$  (d) None of these

**48. The solution of  $(x\sqrt{1+y^2})dx + (y\sqrt{1+x^2})dy = 0$  is**

- (a)  $\sqrt{1+x^2} + \sqrt{1+y^2} = c$
- (b)  $\sqrt{1+x^2} - \sqrt{1+y^2} = c$
- (c)  $(1+x^2)^{3/2} + (1+y^2)^{3/2} = c$
- (d) None of these

**49. The general solution of the differential equation  $ydx + (1+x^2)\tan^{-1}x dy = 0$ , is**

- (a)  $y \tan^{-1}x = c$  (b)  $x \tan^{-1}y = c$
- (c)  $y + \tan^{-1}x = c$  (d)  $x + \tan^{-1}y = c$



**50. The solution of the differential equation  $(1+x^2)(1+y)dy + (1+x)(1+y^2)dx = 0$  is**

- (a)  $\tan^{-1} x + \log(1+x^2) + \tan^{-1} y + \log(1+y^2) = c$   
 (b)  $\tan^{-1} x - \frac{1}{2} \log(1+x^2) + \tan^{-1} y - \frac{1}{2} \log(1+y^2) = c$   
 (c)  $\tan^{-1} x + \frac{1}{2} \log(1+x^2) + \tan^{-1} y + \frac{1}{2} \log(1+y^2) = c$   
 (d) None of these

**51. For solving  $\frac{dy}{dx} = (4x + y + 1)$ , suitable substitution is**

- (a)  $y = vx$  (b)  $y = 4x + v$   
 (c)  $y = 4x$  (d)  $y + 4x + 1 = v$

**52. The solution of  $\log\left(\frac{dy}{dx}\right) = ax + by$  is**

- (a)  $\frac{e^{by}}{b} = \frac{e^{ax}}{a} + c$  (b)  $\frac{e^{-by}}{-b} = \frac{e^{ax}}{a} + c$   
 (c)  $\frac{e^{-by}}{a} = \frac{e^{ax}}{b} + c$  (d) None of these

**53. The solution of the differential equation  $(x - y^2x)dx = (y - x^2y)dy$  is**

- (a)  $(1 - y^2) = c^2(1 - x^2)$  (b)  $(1 + y^2) = c^2(1 - x^2)$   
 (c)  $(1 + y^2) = c^2(1 + x^2)$  (d) None of these

**54. The general solution of the differential equation  $\log\left(\frac{dy}{dx}\right) = x + y$  is**

- (a)  $e^x + e^y = c$  (b)  $e^x + e^{-y} = c$   
 (c)  $e^{-x} + e^y = c$  (d)  $e^{-x} + e^{-y} = c$

**55. The solution of  $\frac{dy}{dx} + \sqrt{\frac{1-y^2}{1-x^2}} = 0$  is**

- (a)  $\tan^{-1} x + \cot^{-1} x = c$  (b)  $\sin^{-1} x + \sin^{-1} y = c$   
 (c)  $\sec^{-1} x + \operatorname{cosec}^{-1} x = c$  (d) None of these

**56. The number of solutions of  $y' = \frac{y+1}{x-1}, y(1) = 2$  is**

- (a) None (b) One  
 (c) Two (d) Infinite

**57. The solution of the differential equation  $\cos y \log(\sec x + \tan x)dx = \cos x \log(\sec y + \tan y)dy$  is**

- (a)  $\sec^2 x + \sec^2 y = c$  (b)  $\sec x + \sec y = c$   
 (c)  $\sec x - \sec y = c$  (d) None of these

**58. The solution of  $e^{2x-3y} dx + e^{2y-3x} dy = 0$  is**

- (a)  $e^{5x} + e^{5y} = c$  (b)  $e^{5x} - e^{5y} = c$   
 (c)  $e^{5x+5y} = c$  (d) None of these

**59. The solution of  $(\operatorname{cosec} x \log y) dy + (x^2 y) dx = 0$  is**

- (a)  $\frac{\log y}{2} + (2 - x^2) \cos x + 2 \sin x = c$   
 (b)  $\left(\frac{\log y}{2}\right)^2 + (2 - x^2) \cos x + 2x \sin x = c$   
 (c)  $\frac{(\log y)^2}{2} + (2 - x^2) \cos x + 2x \sin x = c$   
 (d) None of these

**60. The solution of the equation  $\frac{dy}{dx} = \frac{y^2 - y - 2}{x^2 + 2x - 3}$  is**

- (a)  $\frac{1}{3} \log \left| \frac{y-2}{y+1} \right| = \frac{1}{4} \log \left| \frac{x+3}{x-1} \right| + c$  (b)  $\frac{1}{3} \log \left| \frac{y+1}{y-2} \right| = \frac{1}{4} \log \left| \frac{x-1}{x+3} \right| + c$   
 (c)  $4 \log \left| \frac{y-2}{y+1} \right| = 3 \log \left| \frac{x-1}{x+3} \right| + c$  (d) None of these

**61. Solution of the differential equation  $\frac{dy}{dx} \tan y = \sin(x+y) + \sin(x-y)$  is**

- (a)  $\sec y + 2 \cos x = c$  (b)  $\sec y - 2 \cos x = c$   
 (c)  $\cos y - 2 \sin x = c$  (d)  $\tan y - 2 \sec y = c$   
 (e)  $\sec y + 2 \sin x = c$

**62. Solution of  $\frac{dy}{dx} = \frac{x \log x^2 + x}{\sin y + y \cos y}$  is**

- (a)  $y \sin y = x^2 \log x + c$  (b)  $y \sin y = x^2 + c$   
 (c)  $y \sin y = x^2 + \log x + c$  (d)  $y \sin y = x \log x + c$

**63. The solution of  $e^{dy/dx} = (x+1)$ ,  $y(0) = 3$  is**

- (a)  $y = x \log x - x + 2$   
 (b)  $y = (x+1) \log |x+1| - x + 3$   
 (c)  $y = (x+1) \log |x+1| + x + 3$   
 (d)  $y = x \log x + x + 3$   
 (e)  $y = -(x+1) \log |x+1| + x + 3$

**64. The solution of the differential equation  $(x^2 + y^2)dx = 2xydy$  is**

- (a)  $x = c(x^2 + y^2)$  (b)  $x = c(x^2 - y^2)$   
 (c)  $x + c(x^2 - y^2) = 0$  (d) None of these

**65.  $(x^2 + y^2)dy = xydx$  . If  $y(x_0) = e$  ,  $y(1) = 1$  , then value of  $x_0 =$**

- (a)  $\sqrt{3}e$  (b)  $\sqrt{e^2 - \frac{1}{2}}$   
 (c)  $\sqrt{\frac{e^2 - 1}{2}}$  (d)  $\sqrt{\frac{e^2 + 1}{2}}$

**66. The solution of  $ye^{-x/y}dx - (xe^{-x/y} + y^3)dy = 0$  is**

- (a)  $\frac{y^2}{2} + e^{-x/y} = k$  (b)  $\frac{x^2}{2} + e^{-x/y} = k$   
 (c)  $\frac{x^2}{2} + e^{x/y} = k$  (d)  $\frac{y^2}{2} + e^{x/y} = k$

**67. The solution of the differential equation,  $y dx + (x + x^2y)dy = 0$  is**

- (a)  $\log y = cx$  (b)  $-\frac{1}{xy} + \log y = c$   
 (c)  $-\frac{1}{xy} + \log y = c$  (d)  $-\frac{1}{xy} + \log y = c$

**68. Solution of the differential equation,  $y dx - x dy + xy^2 dx = 0$  can be**

- (a)  $2x + x^2y = \lambda y$  (b)  $2y + y^2x = \lambda y$   
 (c)  $2y - y^2x = \lambda y$  (d) None of these

**69. If  $xdy = y(dx + ydy)$ ,  $y > 0$  and  $y(1) = 1$ , then  $y(-3)$  is equal to**

- (a) 1 (b) 3  
 (c) 5 (d) -1

**70. The solution of  $(x - y^3)dx + 3xy^2dy = 0$  is**

- (a)  $\log x + \frac{x}{y^3} = k$  (b)  $\log x + \frac{y^3}{x} = k$   
 (c)  $\log x - \frac{x}{y^3} = k$  (d)  $\log xy - y^3 = k$

**71. The solution of the differential equation  $(3xy + y^2)dx + (x^2 + xy)dy = 0$  is**

- (a)  $x^2(2xy + y^2) = c^2$  (b)  $x^2(2xy - y^2) = c^2$   
 (c)  $x^2(y^2 - 2xy) = c^2$  (d) None of these

**72. The solution of the differential equation  $x^2 \frac{dy}{dx} = x^2 + xy + y^2$  is**

- (a)  $\tan^{-1}\left(\frac{y}{x}\right) = \log x + c$       (b)  $\tan^{-1}\left(\frac{y}{x}\right) = -\log x + c$   
 (c)  $\sin^{-1}\left(\frac{y}{x}\right) = \log x + c$       (d)  $\tan^{-1}\left(\frac{x}{y}\right) = \log x + c$

**73. The solution of the differential equation  $x dy - y dx = (\sqrt{x^2 + y^2})dx$  is**

- (a)  $y - \sqrt{x^2 + y^2} = cx^2$       (b)  $y + \sqrt{x^2 + y^2} = cx^2$   
 (c)  $y + \sqrt{x^2 + y^2} + cx^2 = 0$       (d) None of these

**74. The solution of the equation  $\frac{dy}{dx} = \frac{x+y}{x-y}$  is**

- (a)  $c(x^2 + y^2)^{1/2} + e^{\tan^{-1}(y/x)} = 0$   
 (b)  $c(x^2 + y^2)^{1/2} = e^{\tan^{-1}(y/x)}$   
 (c)  $c(x^2 - y^2) = e^{\tan^{-1}(y/x)}$   
 (d) None of these

**75. The solution of the equation  $\frac{dy}{dx} = \frac{y}{x} \left( \log \frac{y}{x} + 1 \right)$  is**

- (a)  $\log\left(\frac{y}{x}\right) = cx$       (b)  $\frac{y}{x} = \log y + c$   
 (c)  $y = \log y + 1$       (d)  $y = xy + c$

**76. The solution of the differential equation  $\frac{dy}{dx} = \frac{xy}{x^2 + y^2}$  is**

- (a)  $ay^2 = e^{x^2/y^2}$       (b)  $ay = e^{x/y}$   
 (c)  $y = e^{x^2} + e^{y^2} + c$       (d)  $y = e^{x^2 + y^2} + c$

**77. Integrating factor of equation  $(x^2 + 1) \frac{dy}{dx} + 2xy = x^2 - 1$  is**

- (a)  $x^2 + 1$       (b)  $\frac{2x}{x^2 + 1}$   
 (c)  $\frac{x^2 - 1}{x^2 + 1}$       (d) None of these

**78. The solution of the equation  $x \frac{dy}{dx} + 3y = x$  is**

- (a)  $x^3 y + \frac{x^4}{4} + c = 0$       (b)  $x^3 y = \frac{x^4}{4} + c$   
 (c)  $x^3 y + \frac{x^4}{4} = 0$       (d) None of these

**79 .The solution of the differential equation  $x \log x \frac{dy}{dx} + y = 2 \log x$  is**

- (a)  $y = \log x + c$  (b)  $y = \log x^2 + c$   
 (c)  $y \log x = (\log x)^2 + c$  (d)  $y = x \log x + c$

**80 .Solution of the differential equation  $\frac{dy}{dx} + y \sec^2 x = \tan x \sec^2 x$  is**

- (a)  $y = \tan x - 1 + ce^{-\tan x}$   
 (b)  $y^2 = \tan x - 1 + ce^{\tan x}$   
 (c)  $ye^{\tan x} = \tan x - 1 + c$   
 (d)  $ye^{-\tan x} = \tan x - 1 + c$

**81. Integrating factor of the differential equation  $\frac{dy}{dx} + P(x)y = Q(x)$  is**

- (a)  $\int P dx$  (b)  $\int Q dx$   
 (c)  $e^{\int P dx}$  (d)  $e^{\int Q dx}$

**82. The solution of the equation  $(x + 2y^3) \frac{dy}{dx} - y = 0$  is**

- (a)  $y(1 - xy) = Ax$  (b)  $y^3 - x = Ay$   
 (c)  $x(1 - xy) = Ay$  (d)  $x(1 + xy) = Ay$

Where A is any arbitrary constant

**83. The solution of  $\frac{dy}{dx} + 2y \tan x = \sin x$ , is**

- (a)  $y \sec^3 x = \sec^2 x + c$  (b)  $y \sec^2 x = \sec x + c$   
 (c)  $y \sin x = \tan x + c$  (d) None of these

**84. The solution of  $dy = \cos x(2 - y \operatorname{cosec} x)dx$  where  $y = 2$  when  $x = \frac{\pi}{2}$  is**

- (a)  $y = \sin x + \operatorname{cosec} x$   
 (b)  $y = \tan \frac{x}{2} + \cot \frac{x}{2}$   
 (c)  $y = \frac{1}{\sqrt{2}} \sec \frac{x}{2} + \sqrt{2} \cos \frac{x}{2}$   
 (d) None of these

85. The solution of the differential equation  $\frac{dy}{dx} + \frac{3x^2}{1+x^3}y = \frac{\sin^2 x}{1+x^3}$  is

(a)  $y(1+x^3) = x + \frac{1}{2} \sin 2x + c$

(b)  $y(1+x^3) = cx + \frac{1}{2} \sin 2x$

(c)  $y(1+x^3) = cx - \frac{1}{2} \sin 2x$

(d)  $y(1+x^3) = \frac{x}{2} - \frac{1}{4} \sin 2x + c$

86. The solution of the differential equation  $\frac{dy}{dx} + \frac{y}{x} = x^2$  is

(a)  $4xy = x^4 + c$

(b)  $xy = x^4 + c$

(c)  $\frac{1}{4}xy = x^4 + c$

(d)  $xy = 4x^4 + c$

87. The equation of the curve passing through the origin and satisfying the equation

$(1+x^2)\frac{dy}{dx} + 2xy = 4x^2$  is

(a)  $3(1+x^2)y = 4x^3$

(b)  $3(1-x^2)y = 4x^3$

(c)  $3(1+x^2) = x^3$

(d) None of these

88. The integrating factor of the differential equation  $(x \log x)\frac{dy}{dx} + y = 2 \log x$  is

(a)  $\log x$

(b)  $\log(\log x)$

(c)  $e^x$

(d)  $x$

89. Solution of the equation  $(x + \log y)dy + y dx = 0$  is

(a)  $xy + y \log y = c$

(b)  $xy + y \log y - y = c$

(c)  $xy + \log y - x = c$

(d) None of these

90. An integrating factor of the differential equation  $x \frac{dy}{dx} + y \log x = xe^x x^{\frac{1}{2} \log x}$ , ( $x > 0$ ) is

(a)  $x^{\log x}$

(b)  $(\sqrt{x})^{\log x}$

(c)  $(\sqrt{e})^{\log x}$

(d)  $e^{x^2}$

91. The solution of the equation  $\frac{d^2y}{dx^2} = e^{-2x}$  is

(a)  $\frac{1}{4}e^{-2x}$

(b)  $\frac{1}{4}e^{-2x} + cx + d$

(c)  $\frac{1}{4}e^{-2x} + cx^2 + d$

(d)  $\frac{1}{4}e^{-2x} + c + d$

**92. A particle starts at the origin and moves along the  $x$ -axis in such a way that its velocity at the point  $(x, 0)$  is given by the formula  $\frac{dx}{dt} = \cos^2 \pi x$ . Then the particle never reaches the point on**

- (a)  $x = \frac{1}{4}$  (b)  $x = \frac{3}{4}$   
(c)  $x = \frac{1}{2}$  (d)  $x = 1$

**93. The differential equation  $y \frac{dy}{dx} + x = a$  ( $a$  is any constant) represents**

- (a) A set of circles having centre on the  $y$ -axis  
(b) A set of circles centre on the  $x$ -axis  
(c) A set of ellipses  
(d) None of these

**94. The equation of the curve which passes through the point  $(1, 1)$  and whose slope is given by  $\frac{2y}{x}$ , is**

- (a)  $y = x^2$  (b)  $x^2 - y^2 = 0$   
(c)  $2x^2 + y^2 = 3$  (d) None of these

**95. A function  $y = f(x)$  has a second order derivatives  $f''(x) = 6(x - 1)$ . If its graph passes through the point  $(2, 1)$  and at that point the tangent to the graph is  $y = 3x - 5$ , then the function is**

- (a)  $(x + 1)^3$  (b)  $(x - 1)^3$   
(c)  $(x + 1)^2$  (d)  $(x - 1)^2$

**96. The equation of the curve through the point  $(1, 0)$  and whose slope is  $\frac{y - 1}{x^2 + x}$  is**

- (a)  $(y - 1)(x + 1) + 2x = 0$  (b)  $2x(y - 1) + x + 1 = 0$   
(c)  $x(y - 1)(x + 1) + 2 = 0$  (d) None of these

**97. The slope of the tangent at  $(x, y)$  to a curve passing through a point  $(2, 1)$  is  $\frac{x^2 + y^2}{2xy}$ , then**

**the equation of the curve is**

- (a)  $2(x^2 - y^2) = 3x$  (b)  $2(x^2 - y^2) = 6y$   
(c)  $x(x^2 - y^2) = 6$  (d)  $x(x^2 + y^2) = 10$

98. The solution of  $\frac{d^2 y}{dx^2} = \sec^2 x + xe^x$  is

- (a)  $y = \log(\sec x) + (x - 2)e^x + c_1 x + c_2$   
 (b)  $y = \log(\sec x) + (x + 2)e^x + c_1 x + c_2$   
 (c)  $y = \log(\sec x) - (x + 2)e^x + c_1 x + c_2$   
 (d) None of these

99. The solution of the differential equation  $x \frac{dy}{dx} = y(\log y - \log x + 1)$  is

- (a)  $y = xe^{cx}$  (b)  $y + xe^{cx} = 0$   
 (c)  $y + e^x = 0$  (d) None of these

100. The general solution of  $y^2 dx + (x^2 - xy + y^2) dy = 0$  is

- (a)  $\tan^{-1}\left(\frac{x}{y}\right) + \log y + c = 0$   
 (b)  $2 \tan^{-1}\left(\frac{x}{y}\right) + \log x + c = 0$   
 (c)  $\log(y + \sqrt{x^2 + y^2}) + \log y + c = 0$   
 (d)  $\sinh^{-1}\left(\frac{x}{y}\right) + \log y + c = 0$

101. The differential equation of the family of curves  $y = Ae^{3x} + Be^{5x}$ , where  $A$  and  $B$  are arbitrary constants, is

- (a)  $\frac{d^2 y}{dx^2} + 8 \frac{dy}{dx} + 15y = 0$  (b)  $\frac{d^2 y}{dx^2} - 8 \frac{dy}{dx} + 15y = 0$   
 (c)  $\frac{d^2 y}{dx^2} - \frac{dy}{dx} + y = 0$  (d) None of these

102. The order of the differential equation whose general solution is given by  $y = C_1 e^{2x+C_2} +$

$C_3 e^x + C_4 \sin(x + C_5)$  is

- (a) 5 (b) 4  
 (c) 3 (d) 2



**103. The differential equation of the family of parabolas with focus at the origin and the  $x$ -axis as axis is**

(a)  $y \left( \frac{dy}{dx} \right)^2 + 4x \frac{dy}{dx} = 4y$     (b)  $-y \left( \frac{dy}{dx} \right)^2 = 2x \frac{dy}{dx} - y$

(c)  $y \left( \frac{dy}{dx} \right)^2 + y = 2xy \frac{dy}{dx}$     (d)  $y \left( \frac{dy}{dx} \right)^2 + 2xy \frac{dy}{dx} + y = 0$

# DIFFERENTIAL EQUATIONS

## HINTS AND SOLUTIONS

1. (b)  $\frac{d^2y}{dx^2} = -\sqrt{1 + \left(\frac{dy}{dx}\right)^3} \Rightarrow \left(\frac{d^2y}{dx^2}\right)^2 = 1 + \left(\frac{dy}{dx}\right)^3$

degree is 2.

2. (c) Here power on the differential coefficient is fractional, therefore change it into positive integer, so

$$\left[4 + \left(\frac{dy}{dx}\right)^2\right]^{2/3} = \frac{d^2y}{dx^2} \Rightarrow \left[4 + \left(\frac{dy}{dx}\right)^2\right]^2 = \left[\frac{d^2y}{dx^2}\right]^3$$

3. (a) order is 1.

4. (a) order = 2, degree = 2.

5. (d) Clearly, order = 2, degree = 3.

6. (b) degree is 4.

7. (c)  $y = 1 + t + \frac{t^2}{2!} + \frac{t^3}{3!} + \dots + \infty$  where  $t = \frac{dy}{dx}$

$$\Rightarrow y = e^t, \therefore t = \log y \Rightarrow \frac{dy}{dx} = \log y. \text{ Hence degree is 1.}$$

8. (c)

9. (b)

10. (d)  $\left(\frac{d^2y}{dx^2}\right)^4 = y + \left(\frac{dy}{dx}\right)^2$

Obviously, order is 2 and degree is 4.

11. (a)  $(x-h)^2 + (y-k)^2 = r^2$ . Here  $r$  is arbitrary constant

$\therefore$  order of differential equation = 1.

12. (a) Differentiating the given equation, we get  $\frac{dy}{dx} = A$

$$\therefore y = x \left(\frac{dy}{dx}\right) + \left(\frac{dy}{dx}\right)^3 \text{ which is of degree 3.}$$

13. (b)  $y^2 = \pm 4a(x-h)$

$$\Rightarrow 2y y_1 = \pm 4a \Rightarrow y y_1 = \pm 2a \Rightarrow y_1^2 + y y_2 = 0$$

Hence degree = 1, order = 2.

14. (c) order of the differential equation is 3.

15. (a)

16. (a) The equation of a family of circles of radius  $r$  passing through the origin and having centre on y-axis is  $(x-0)^2 + (y-r)^2 = r^2$  or  $x^2 + y^2 - 2ry = 0$ . (a) Given equation  $x^2 + y^2 = a^2$ . Differentiate it w.r.t.  $x$ ,

$$\text{we get } 2x + 2y \frac{dy}{dx} = 0 \Rightarrow x + y \frac{dy}{dx} = 0.$$

17. (a) Differentiate it w.r.t.  $x$ , we get  $\frac{dy}{dx} = m$ .

18. (c)

19. (a) The system of circles pass through origin and centre lies on y-axis is  $x^2 + y^2 - 2ay = 0$

$$\Rightarrow 2x + 2y \frac{dy}{dx} - 2a \frac{dy}{dx} = 0 \Rightarrow 2a = 2y + 2x \frac{dx}{dy}$$

Therefore, the required differential equation is

20. (a)  $x^2 + y^2 - 2y^2 - 2xy \frac{dx}{dy} = 0 \Rightarrow (x^2 - y^2) \frac{dy}{dx} - 2xy = 0$ .

21. (c)  $y = e^{mx} \Rightarrow \log y = mx \Rightarrow m = \frac{\log y}{x}$

$$\text{Now } y = e^{mx} \Rightarrow \frac{dy}{dx} = me^{mx} = \frac{\log y}{x} \cdot y = \left(\frac{y}{x}\right) \log y.$$

22. (a) standard problem

23. (a)  $y = ce^{\sin^{-1} x}$ . Differentiate it w.r.t.  $x$ , we get

$$\frac{dy}{dx} = ce^{\sin^{-1} x} \cdot \frac{1}{\sqrt{1-x^2}} = \frac{y}{\sqrt{1-x^2}} \text{ or } \frac{dy}{dx} = \frac{y}{\sqrt{1-x^2}}.$$

24. (d) standard problem.

25. (d) Since the equation of line passing through  $(1, -1)$  is  $y + 1 = m(x - 1)$

$$\Rightarrow y + 1 = \frac{dy}{dx}(x - 1) \Rightarrow y = (x - 1) \frac{dy}{dx} - 1.$$

26. (a) standard problem

27. (a)  $x^2 y = a$

$$x^2 \frac{dy}{dx} + y \frac{d}{dx}(x^2) = 0 \Rightarrow x^2 \frac{dy}{dx} + 2xy = 0$$

$$\Rightarrow \frac{dy}{dx} + \frac{2y}{x} = 0.$$

28. (b) Differentiating, we have  $\frac{dy}{dx} = c$

$$\text{Hence differential equation is, } y = x \frac{dy}{dx} + \frac{dy}{dx} - \left(\frac{dy}{dx}\right)^3.$$

29. (b) Differentiate 2 times w.r.t.  $x$

30. (b) standard problem

31. (b) standard problem

32. (c)  $y = \sec(\tan^{-1} x)$

$$\frac{dy}{dx} = \sec(\tan^{-1} x) \tan(\tan^{-1} x) \cdot \frac{1}{1+x^2} = \frac{xy}{1+x^2}$$

$$\Rightarrow (1+x^2) \frac{dy}{dx} = xy$$

33. (d)  $x = \sin t$ ,  $y = \cos pt$

$$\frac{dx}{dt} = \cos t; \quad \frac{dy}{dt} = -p \sin pt; \quad \frac{dy}{dx} = \frac{-p \sin pt}{\cos t}$$

$$\frac{d^2y}{dx^2} = \frac{-\cos t p^2 \cos pt (dt/dx) - p \sin pt \sin t (dt/dx)}{\cos^2 t}$$

$$\Rightarrow (1-x^2) \frac{d^2y}{dx^2} - x \frac{dy}{dx} + p^2 y = 0$$

$$\text{or } (1-x^2)y_2 - xy_1 + p^2 y = 0$$

34. (b)  $\sin^{-1} x + \sin^{-1} y = c$

On differentiating w.r.t. to  $x$ , we get d.eq

35. (b)  $\frac{dy}{dx} + \frac{1+x^2}{x} = 0 \Rightarrow dy + \left(\frac{1}{x} + x\right) dx = 0$

36. (b)  $\frac{dy}{dx} = e^x + \cos x + x + \tan x$

37. (b) Here  $\frac{dy}{dx} = \sin(x+y)$

38. Now put  $x+y = v$  (d)  $\frac{dy}{dx} = (1+x)(1+y^2) \Rightarrow \frac{dy}{1+y^2} = (1+x)dx$

39. (b)  $\frac{dy}{dx} + \sqrt{\frac{1-y^2}{1-x^2}} = 0 \Rightarrow \int \frac{dy}{\sqrt{1-y^2}} = -\int \frac{dx}{\sqrt{1-x^2}}$

40. (d)  $\cos x \cos y \frac{dy}{dx} = -\sin x \sin y$   
 $\Rightarrow \frac{\cos y}{\sin y} dy = -\frac{\sin x}{\cos x} dx \Rightarrow \cot y dy = -\tan x dx$

41. (a)  $(x^2 - yx^2) \frac{dy}{dx} + y^2 + xy^2 = 0 \Rightarrow \frac{1-y}{y^2} dy + \frac{1+x}{x^2} dx = 0$

$$\Rightarrow \left(\frac{1}{y^2} - \frac{1}{y}\right) dy + \left(\frac{1}{x^2} + \frac{1}{x}\right) dx = 0$$

42. (a)  $\frac{dy}{dx} = \sec x (\sec x + \tan x) \Rightarrow \frac{dy}{dx} = \sec^2 x + \sec x \tan x$

43. (c)  $\frac{dy}{dx} = \frac{(1+x)y}{(y-1)x}$

$$\frac{y-1}{y} dy = \frac{(1+x)}{x} dx \Rightarrow \left(1 - \frac{1}{y}\right) dy = \left(1 + \frac{1}{x}\right) dx$$

44. (b) Put  $x+y=v$

45. (c) Let  $x-y=v$

46. (d)  $(e^x + 1)ydy = (y+1)e^x dx$

$$\Rightarrow \left(\frac{y}{y+1}\right) dy = \left(\frac{e^x}{e^x+1}\right) dx$$

47. (d) Put  $x+y=v$

48. (a)  $x\sqrt{1+y^2} dx = -y\sqrt{1+x^2} dy$

$$\Rightarrow \int \frac{x}{\sqrt{1+x^2}} dx + \int \frac{y}{\sqrt{1+y^2}} dy = c$$

49. (a)  $ydx + (1+x^2)\tan^{-1} x dy = 0$

$$\Rightarrow \int \frac{dx}{(1+x^2)\tan^{-1} x} = -\int \frac{dy}{y}$$

50. (c)  $(1+x^2)(1+y)dy + (1+x)(1+y^2)dx = 0$

$$\Rightarrow \frac{(1+y)}{(1+y^2)} dy = -\frac{(1+x)}{(1+x^2)} dx$$

51. (d) Put  $y+4x+1=v$ .

52. (b)  $\log\left(\frac{dy}{dx}\right) = ax+by \Rightarrow \frac{dy}{dx} = e^{ax+by} = e^{ax} \cdot e^{by}$

$$\Rightarrow e^{-by} dy = e^{ax} dx \Rightarrow \frac{e^{-by}}{-b} = \frac{e^{ax}}{a} + c.$$

53. (a)  $\frac{x}{1-x^2} dx = \frac{y}{1-y^2} dy$

54. (b)  $\log\left(\frac{dy}{dx}\right) = x+y \Rightarrow e^{x+y} = \frac{dy}{dx} \Rightarrow e^x e^y = \frac{dy}{dx}$

55. (b)  $\int \frac{dy}{\sqrt{1-y^2}} + \int \frac{dx}{\sqrt{1-x^2}} = 0$

56. (a)  $\frac{dy}{dx} = \frac{y+1}{x-1} \Rightarrow \frac{dy}{y+1} = \frac{dx}{x-1}$

57. (d)  $\cos y \log(\sec x + \tan x) dx = \cos x \log(\sec y + \tan y) dy$

58. (a)  $e^{2x-3y} dx + e^{2y-3x} dy = 0$

$$e^{3x+3y} \Rightarrow e^{5x} dx + e^{5y} dy = 0$$

59. (c)  $(\operatorname{cosec} x \log y) dy + (x^2 y) dx = 0 \Rightarrow \frac{1}{y} \log y dy = -x^2 \sin x dx$

$$60. (c) \frac{dy}{dx} = \frac{y^2 - y - 2}{x^2 + 2x - 3} \Rightarrow \frac{dy}{(y-2)(y+1)} = \frac{dx}{(x+3)(x-1)}$$

$$61. (a) \frac{dy}{dx} \tan y = \sin(x+y) + \sin(x-y)$$

$$\frac{dy}{dx} (\tan y) = 2 \sin x \cos y \Rightarrow \frac{\sin y}{\cos^2 y} dy = 2 \sin x dx$$

$$62. (a) \frac{dy}{dx} = \frac{x \log x^2 + x}{\sin y + y \cos y}.$$

$$63. (b) \frac{dy}{dx} = \log(x+1) \Rightarrow dy = \log(x+1) dx$$

$$64. (b) \frac{dy}{dx} = \frac{x^2 + y^2}{2xy}$$

$$\text{put } y = vx$$

$$65. (a) x^2 dy + y^2 dy = xy dx \Rightarrow x(xdy - ydx) = -y^2 dy$$

$$\Rightarrow x \frac{(ydx - xdy)}{y^2} = dy \Rightarrow \frac{x}{y} d\left(\frac{x}{y}\right) = \frac{dy}{y}$$

$$66. (a) y e^{-x/y} dx - (x e^{-x/y} + y^3) dy = 0 \quad e^{-x/y} (ydx - xdy) = y^3 dy \Rightarrow e^{-x/y} \frac{(ydx - xdy)}{y^2} = y dy$$

$$e^{-x/y} d\left(\frac{x}{y}\right) = y dy.$$

$$67. (b) ydx + xdy = -x^2 y dy \Rightarrow \frac{1}{(xy)^2} dxy = -\frac{dy}{y}$$

$$68. (a) \frac{ydx - xdy}{y^2} = -x dx \Rightarrow d\left(\frac{x}{y}\right) = -x dx$$

$$69. (b) xdy = y(dx + ydy) \Rightarrow \frac{xdy - ydx}{y^2} = dy \Rightarrow -d\left(\frac{x}{y}\right) = dy$$

$$70. (b) xdx - y^3 dx + 3xy^2 dy = 0$$

$$\text{Put } y^3 = t \Rightarrow dt = 3y^2 dy$$

$$x dx - t dx + x dt = 0 \Rightarrow x dx + x dt - t dx = 0$$

$$\Rightarrow \frac{dx}{x} + d\left(\frac{t}{x}\right) = 0$$

$$71. (a) \frac{dy}{dx} = -\frac{3xy + y^2}{x^2 + xy} \text{ put } y = vx$$

$$72. (a) \frac{dy}{dx} = \frac{x^2 + xy + y^2}{x^2} \text{ put } y = vx$$

$$73. (b) \text{put } y = vx$$

74. (b)  $\frac{dy}{dx} = \frac{x+y}{x-y}$  put  $y = vx$

75. (a)  $y = vx \Rightarrow \frac{dy}{dx} = v + x \cdot \frac{dv}{dx}$

76. (a)  $\frac{dy}{dx} = \frac{xy}{x^2 + y^2}$ . Put  $y = vx$  ;

77. (a)  $\frac{dy}{dx} + \frac{2x}{1+x^2} y = \frac{x^2 - 1}{x^2 + 1}$

I.F. =  $e^{\int \frac{2x}{1+x^2} dx} = e^{\log(1+x^2)} = 1 + x^2$ .

78. b)  $x \frac{dy}{dx} + 3y = x \Rightarrow \frac{dy}{dx} + \frac{3y}{x} = 1$

79. (c)  $x \log x \frac{dy}{dx} + y = 2 \log x \Rightarrow \frac{dy}{dx} + \frac{1}{x \log x} y = \frac{2}{x}$

80. (a) I.F. =  $e^{\int \sec^2 x dx} = e^{\tan x}$

81. (c)

82. (b)  $(x + 2y^3) \frac{dy}{dx} = y \Rightarrow \frac{dy}{dx} = \frac{y}{x + 2y^3}$

$\Rightarrow \frac{dx}{dy} = \frac{x + 2y^3}{y}$

83. (b)  $\frac{dy}{dx} + 2y \tan x = \sin x$

84. (a)  $\frac{dy}{dx} = 2 \cos x - y \cot x \Rightarrow \frac{dy}{dx} + y \cot x = 2 \cos x$

85. (d)  $\frac{dy}{dx} + \frac{3x^2}{1+x^3} y = \frac{\sin^2 x}{1+x^3}$

86. (a) The given equation  $\frac{dy}{dx} + \frac{y}{x} = x^2$

87. (a)  $\frac{dy}{dx} + \frac{2x}{1+x^2} y = \frac{4x^2}{1+x^2}$

88. (a) I.F. =  $e^{\int \frac{1}{x \log x} dx} = e^{\log(\log x)} = \log x$ .

89. (b)  $xdy + ydx + \log y dy = 0 \Rightarrow xdy + ydx = -\log y dy$

$y \frac{dx}{dy} + x = -\log y \Rightarrow \frac{dx}{dy} + \frac{x}{y} = -\frac{\log y}{y}$

90. (b)  $\frac{dy}{dx} + \left( \frac{\log x}{x} \right) y = e^x x^{\frac{1}{2} \log x}$

91. (b)  $\frac{d^2 y}{dx^2} = e^{-2x}$

Integrate both sides 2times

92. (c) Given  $\frac{dx}{dt} = \cos^2 \pi x$ . Differentiate w.r.t.  $t$ ,

$$\frac{d^2 x}{dt^2} = -2\pi \sin 2\pi x = -ve$$

$$\therefore \frac{d^2 x}{dt^2} = 0 \Rightarrow -2\pi \sin 2\pi x = 0 \Rightarrow \sin 2\pi x = \sin \pi$$

$$\Rightarrow 2\pi x = \pi \Rightarrow x = 1/2.$$

93. (b) We have  $y \frac{dy}{dx} + x = a$  or  $y dy + x dx = a dx$

$$\text{Integrating, we get } \frac{y^2}{2} + \frac{x^2}{2} = ax + c$$

94. (a) Slope  $\frac{dy}{dx} = \frac{2y}{x}$

$$\Rightarrow 2 \int \frac{dx}{x} = \int \frac{dy}{y} \Rightarrow 2 \log x = \log y + \log c \Rightarrow x^2 = yc$$

95. (b) verification

96. (a) Slope  $= \frac{dy}{dx}$

$$\Rightarrow \frac{dy}{dx} = \frac{y-1}{x^2+x} \Rightarrow \frac{dy}{y-1} = \frac{dx}{x^2+x}$$

97. (a)  $\frac{dy}{dx} = \frac{x^2+y^2}{2xy}$ . Put  $y = vx$

98. (a)  $\frac{d^2 y}{dx^2} = \sec^2 x + xe^x$  Integrate both sides 2 times

99. (a)  $\frac{dy}{dx} = \frac{y}{x} \left( \log \frac{y}{x} + 1 \right)$  put  $y = vx$

100. (a)  $\frac{dx}{dy} + \frac{x^2 - xy + y^2}{y^2} = 0$

$$\frac{dx}{dy} + \left( \frac{x}{y} \right)^2 - \left( \frac{x}{y} \right) + 1 = 0$$

Put  $v = x/y$

101. (b)  $y = Ae^{3x} + Be^{5x}$

$$\Rightarrow \frac{dy}{dx} = 3Ae^{3x} + 5Be^{5x} \Rightarrow \frac{d^2 y}{dx^2} = 9Ae^{3x} + 25Be^{5x}$$

$$\Rightarrow \frac{d^2 y}{dx^2} - 8 \frac{dy}{dx} + 15y = 0$$

102. (c) order = no. of arbitrary constants = 3

103. (b) Given family of parabolas is  $y^2 = 4a(x+a)$ . Eliminate  $a$  from this equation.