Supplementary Information for Inconsistencies of metalens performance and comparison with conventional diffractive optics.

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Table S1: Summary of reported metalens efficiencies (only one example from each reference is shown for brevity). All values in this table are for monochromatic lenses. Those values marked in red exceed bounds dictated by Ref. [12].

Reference	λ	NA	Unit-cell period (Λ/λ)	Radius of focal spot (/FWHM)	Reported eff.	Eff from Fig. S4 (Radius of 3 x FWHM)
[4]	405nm	0.8	0.49	Not disclosed	88%	83%
[6]	660nm	0.85	0.53	2 sim, 4 expt.	84% sim, 60% expt.	79%
[7]	532nm	0.9	0.45	Not disclosed	42%	74%
[8]	532nm	0.98	0.41	3	67%	49%
[9]	405nm	0.8	0.49	Not disclosed	86%	83%
[10]	915nm	0.78	Grating averaging	10	77%	84%
[11]	1,550nm	0.89	0.52	3	72%	75%

References:

- [4] M. Khorasaninejad, W. T. Chen, R. C. Devlin, J. Oh, A. Y. Zhu, and F. Capasso, "Metalenses at visible wavelengths: Diffraction-limited focusing and subwavelength resolution imaging," Science 352, 1190–1194 (2016). [5] J. Engelberg, C. Zhou, N. Mazurski, J. Bar-David, A. Kristensen, and U. Levy, "Near-ir wide-field-of-view huygens metalens for outdoor imag- ing applications," Nanophotonics 9, 361–370 (2020).
- [6] M. Khorasaninejad, A. Y. Zhu, C. Roques-Carmes, W. T. Chen, J. Oh, I. Mishra, R. C. Devlin, and F. Capasso, "Polarization-insensitive metalenses at visible wavelengths," Nano Lett. 16, 7229–7234 (2016). PMID: 27791380. [7] Wei Ting Chen, Alexander Y. Zhu, Mohammadreza Khorasaninejad, Zhujun Shi, Vyshakh Sanjeev, and Federico Capasso, "Immersion Meta-Lenses at Visible Wavelengths for Nanoscale Imaging," *Nano Letters* 2017 17 (5), 3188-3194.
- [8] Haowen Liang, Qiaoling Lin, Xiangsheng Xie, Qian Sun, Yin Wang, Lidan Zhou, Lin Liu, Xiangyang Yu, Jianying Zhou, Thomas F Krauss, and Juntao Li, "Ultrahigh Numerical Aperture Metalens at Visible Wavelengths" *Nano Letters* **2018** *18* (7), 4460-4466.
- [9] M. Khorasaninejad *et al.*, "Visible Wavelength Planar Metalenses Based on Titanium Dioxide," in *IEEE Journal of Selected Topics in Quantum Electronics*, vol. 23, no. 3, pp. 43-58, May-June 2017, Art no. 4700216, doi: 10.1109/JSTQE.2016.2616447.
- [10] Arbabi, A., Arbabi, E., Mansouree, M. et al. Increasing efficiency of high numerical aperture metasurfaces using the grating averaging technique. Sci Rep 10, 7124 (2020).
- [11] Arbabi, A., Horie, Y., Ball, A. et al. Subwavelength-thick lenses with high numerical apertures and large efficiency based on high-contrast transmitarrays. *Nat Commun* 6, 7069 (2015).
- [12] Sang, Di, et al. "Toward high-efficiency ultrahigh numerical aperture freeform metalens: from vector diffraction theory to topology optimization." Laser & Photonics Reviews 16.10 (2022): 2200265..

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