

Q1) Obtain the convolution of the given finite sequences

$$x1 = [4 \ 2 \uparrow \ 6 \ 3 \ 8 \ 1 \ 5]$$

$$x2 = [3 \ 8 \ 6 \uparrow \ 9 \ 6 \ 7]$$

Note: arrow points to zero location in above sequences. Since MATLAB command does not give time index of the convolved result, derive it from the signals to be convolved.

AIM: To find the convolution of 2 sequences.

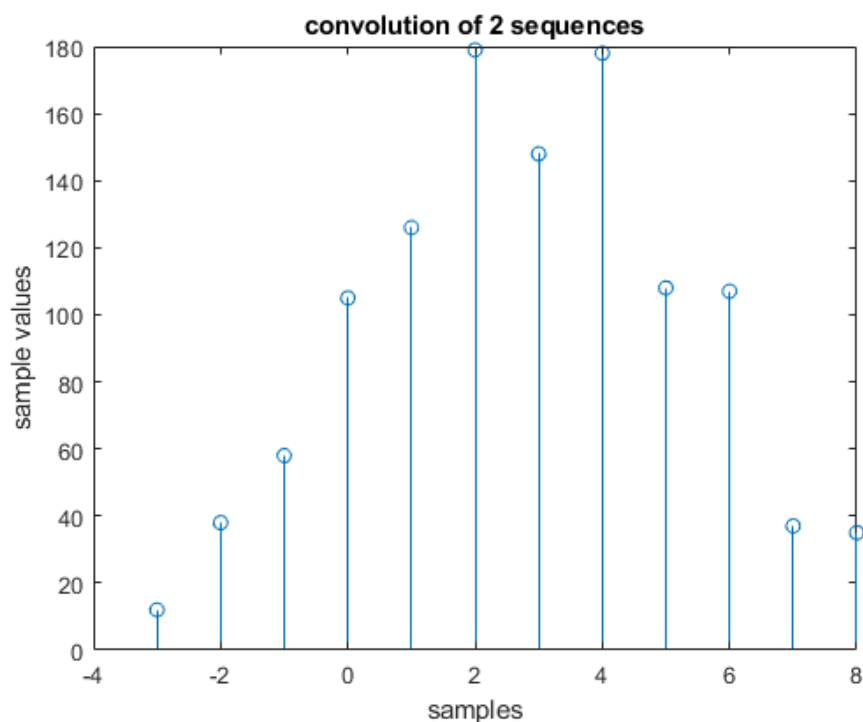
Short Theory: Convolution is a mathematical operation used to express the relation between input and output of an LTI system. It relates input, output and impulse response of an LTI system as

$$y(n) = x(n) * h(n) \\ = \sum_{-\infty}^{\infty} x(k)h(n-k)$$

Key Commands:

Conv %it convolves the 2 sequences

Plots:



Inferences/comments:

Inbuilt command in MATLAB for convolution doesn't give the exact zero index of resultant sequence for the given input but still we can write the program in such a way that the resultant convolved sequence can plot the output sequence along with the exact index .

Q2. Find the auto correlation and cross correlation of x1 and x2, with the help of convolution.

x1=[4 2↑ 6 3 8 1 5]

x2=[3 8 6↑ 9 6 7]

AIM: To find the auto correlation and cross correlation 2 sequences.

Short Theory: Correlation is a measure of similarity between two signals.

Auto correlation function is a measure of similarity between a signal & its time delayed version.

$$R_x(n) = x(k) * x(-k) = \sum_{-\infty}^{\infty} x(k)x(n+k)$$

Cross correlation is the measure of similarity between two different signals.

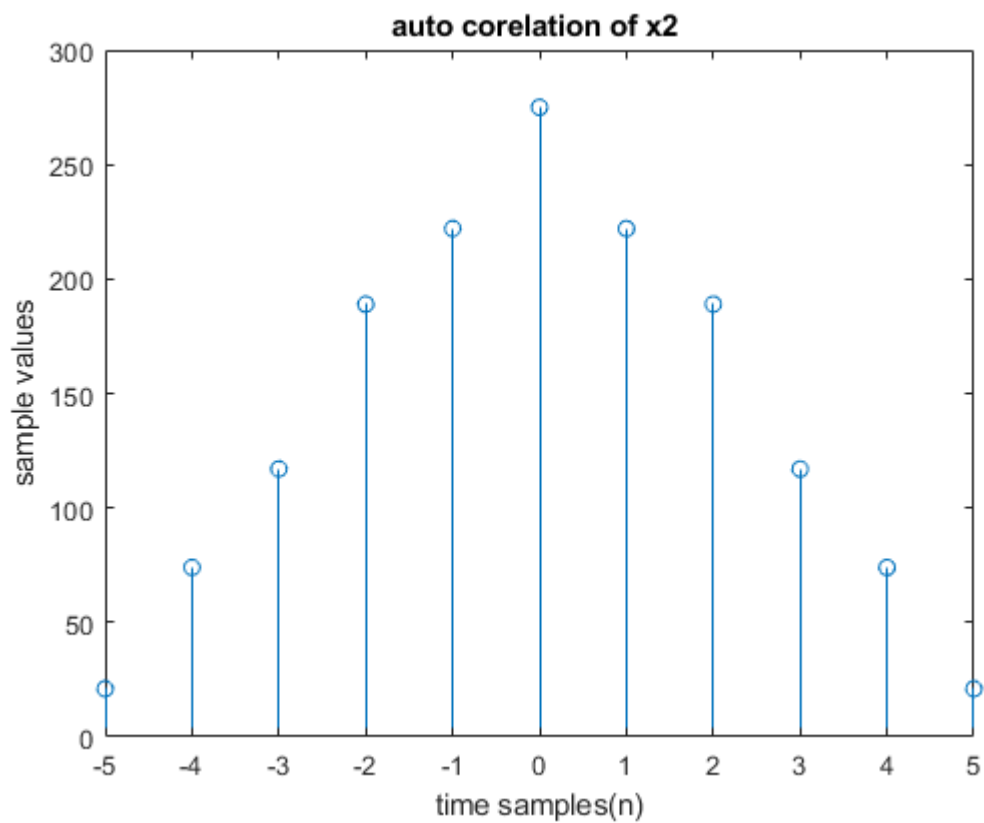
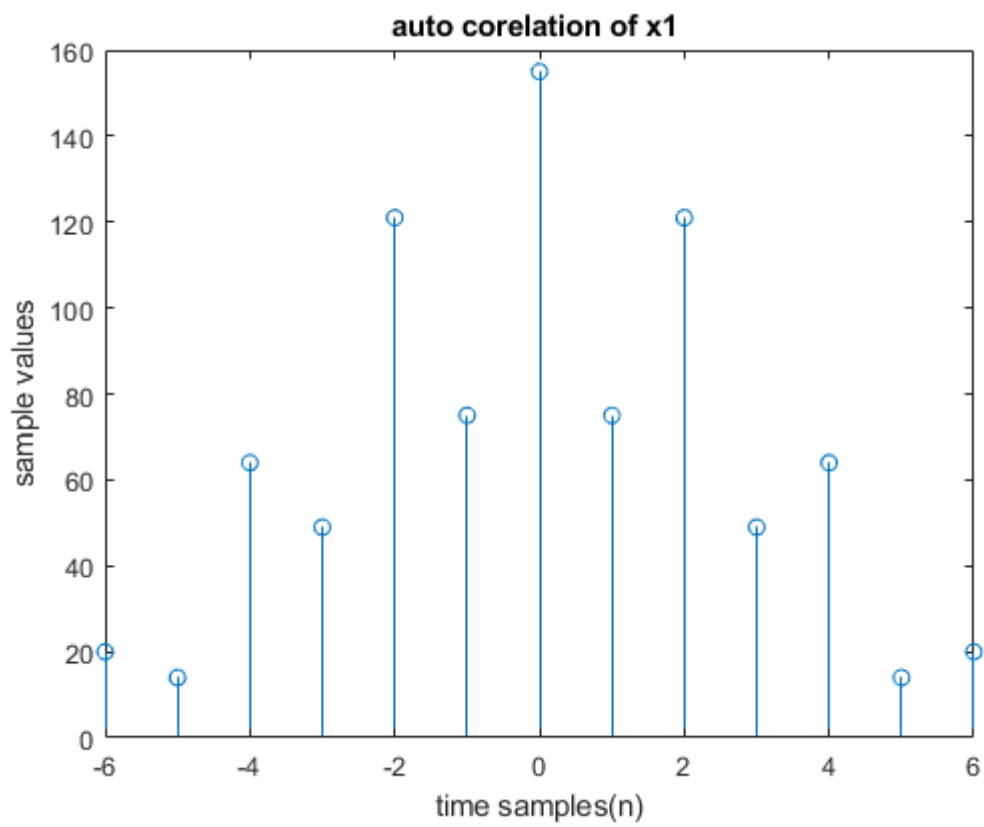
$$R_{xy}(n) = x(k) * y(-k) = \sum_{-\infty}^{\infty} x(k)y(n+k)$$

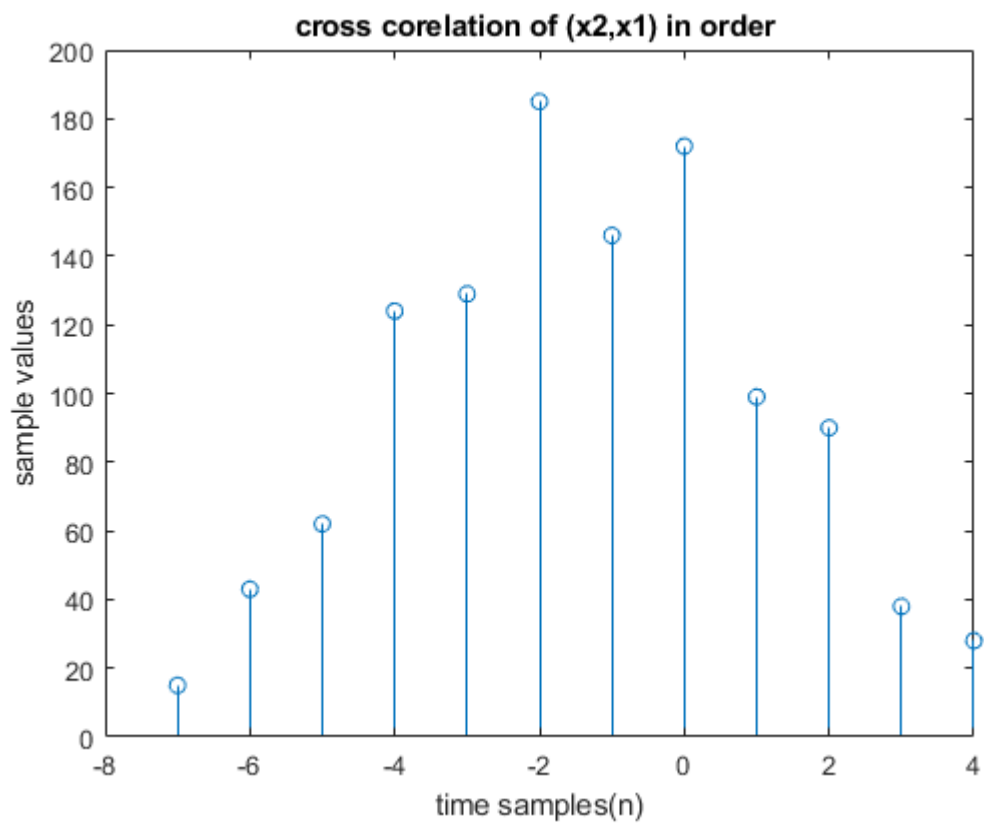
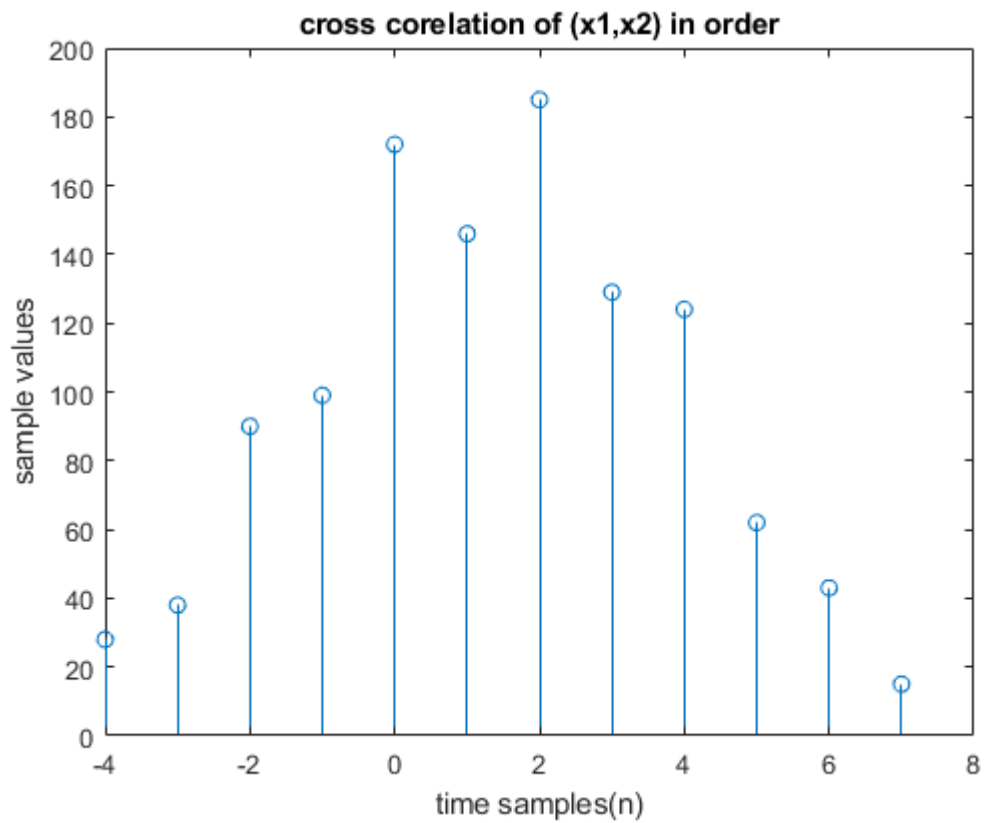
Key Commands:

Conv % it convolve the 2 sequences

xcorr % it correlate the 2 signals

Plots:





Inferences/comments:

- 1) From the auto correlation plot we can clearly observe that the max value is occurs at $n=0$.

3. $\exp(x)$ is the exponential of the elements of x (i.e., e^x). For complex number $z=x+iy$, $\exp(z) = \exp(x) * (\cos(y) + i * \sin(y))$. Taking appropriate values for z ,
- (a) generate and plot a complex-valued exponentially decaying sinusoidal sequence.
 - (b) generate and plot a complex-valued exponentially growing sinusoidal sequence using MATLAB.

AIM: To find the exponential sequence of a complex number. And plot the decay/growing sinusoidal sequence by taking suitable example.

Short Theory:

$\exp(x)$ is the exponential of the elements of x (i.e., e^x).

For complex number $z=x+iy$, $e^z = e^{\cos(y) + i * \sin(y)}$

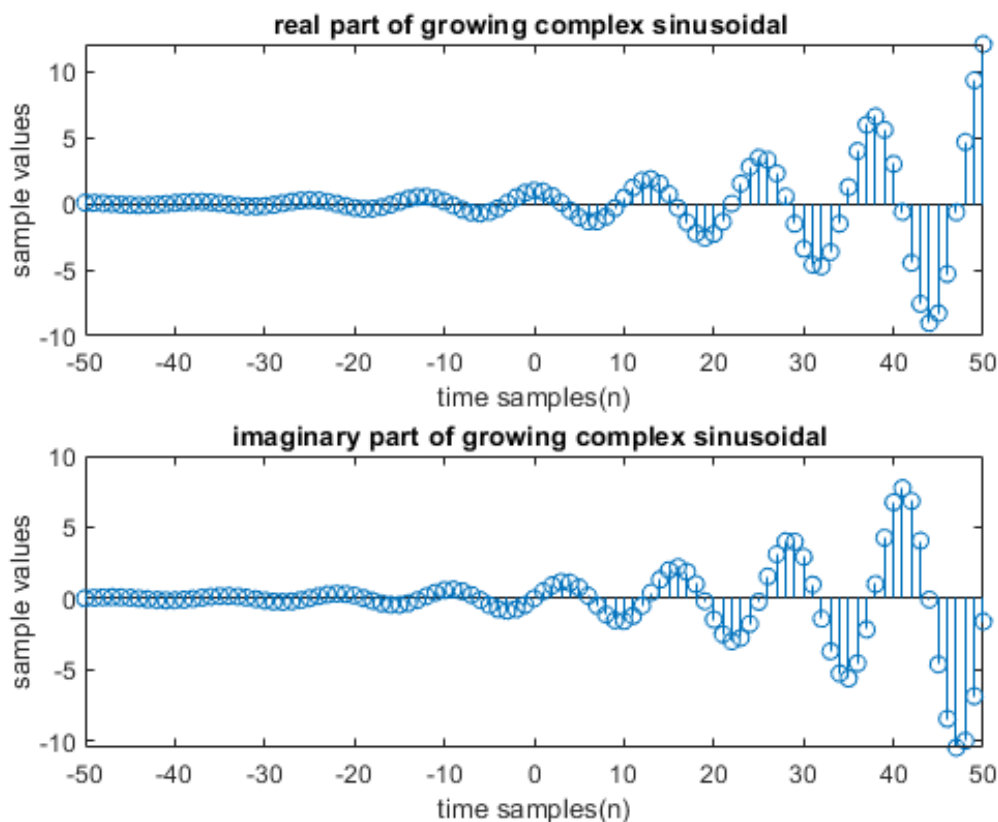
Key Commands:

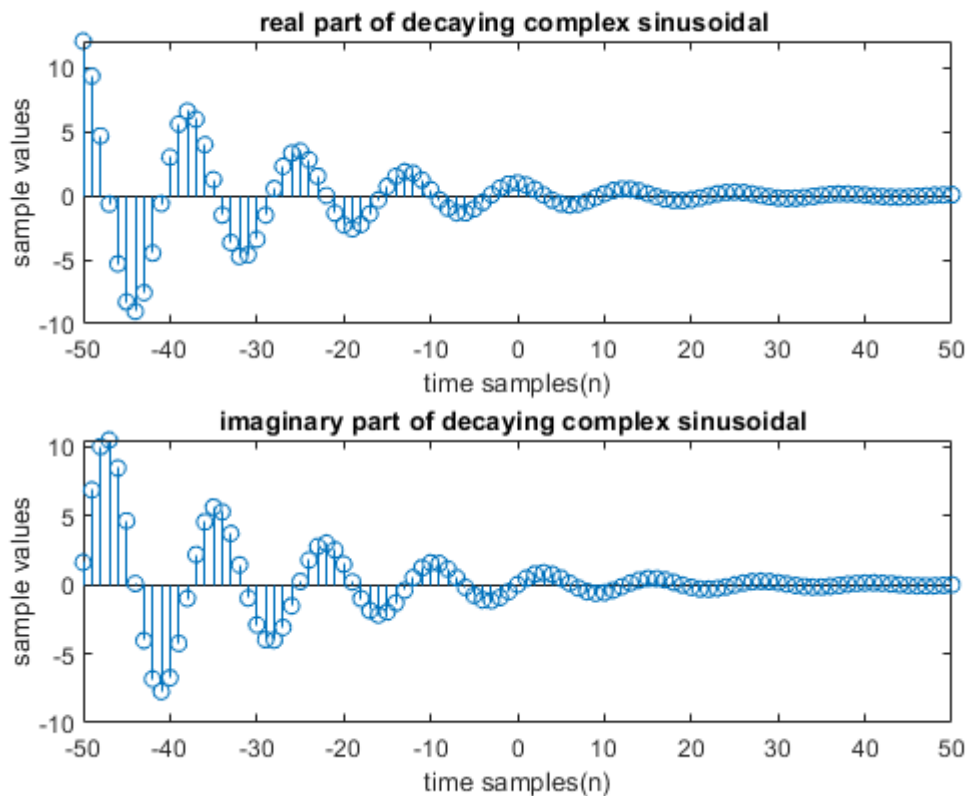
`exp(x)` % This command gives the exponential of x .

`sin` % it gives the values of $\sin(x)$

`cos` % it gives the value of $\cos(x)$

Plots:





Inferences/comments:

Let complex number $Z=a+jb$, then if $a<0$ then it will give the decaying sinusoid, if $a>0$ then it gives growing sinusoid.

Q4. Find solution for $y[n]$ from difference equation $y[n] = ay[n-1]+x[n]$, with $x[n] = \delta[n]$ and simulate it using “filter” command. Can you relate it to any of the standard signals? assume the initial conditions are zeros.

AIM: To solve the difference equation $y[n] = ay[n-1]+x[n]$, by taking different values of ‘a’.

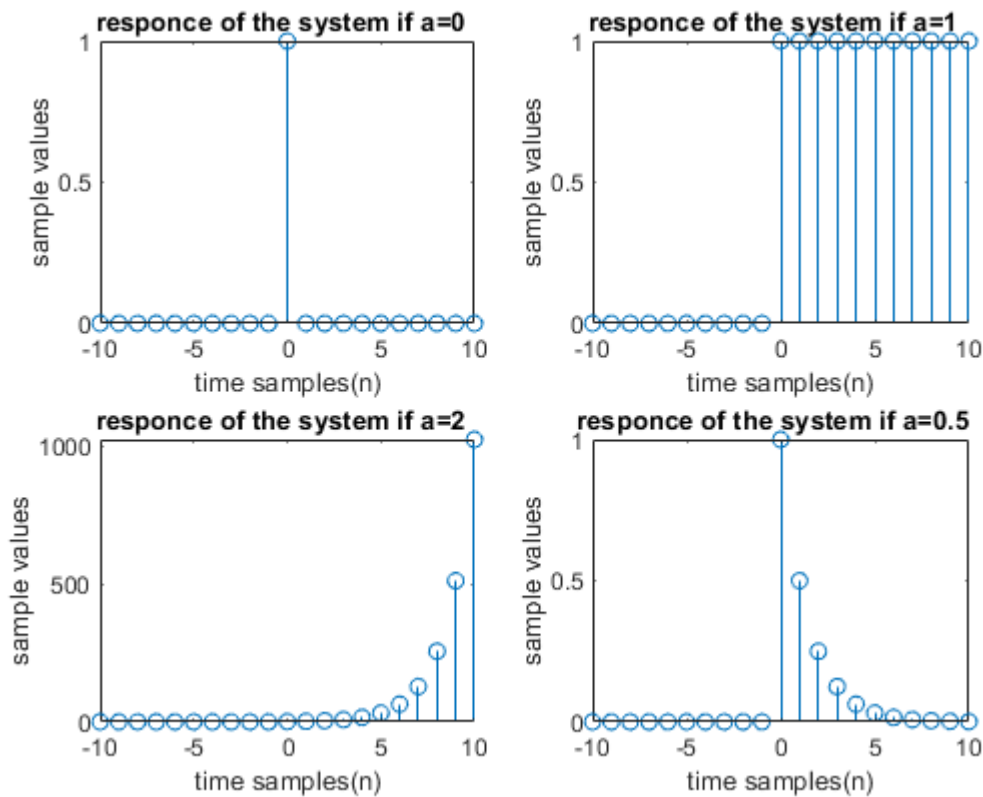
Short Theory:

The solution of a difference equation $y[n]$ can be obtained by converting given difference equation into transfer function ($H[n]=Y[n]/X[n]$). Then multiplying the $H[n]$ with the given input signal $x[n]$.

Key Commands:

Filter % `filter(b,a,x)` filters the input data x using a rational transfer function defined by the numerator and denominator coefficients b and a

Plots:



Inferences/comments:

- 1)if we take $a=0$, the output plot as unit impulse signal,
- 2)if we take $a=1$, the output plot as unit step signal.
- 3)if we take $a=2$ the output plot as growing exponential signal.
- 4)if we take $a=0.5$, the output plot as decaying exponential signal

Q5. Generate complex exponential signal as impulse response to the following difference equation: with initial conditions are zero.

$$y[n] = z_0 y[n-1] + x[n], \text{ where, } z_0 = 0.8e^{j\pi/3}.$$

AIM: To generate and plot the complex exponential sequence from the differential equation.

Short Theory: The solution of a differential equation $y[n]$ can be obtained by converting given differential equation into transfer function ($h[n]=y[n]/x[n]$). Then multiplying the $h[n]$ with the given input signal $x[n]$.

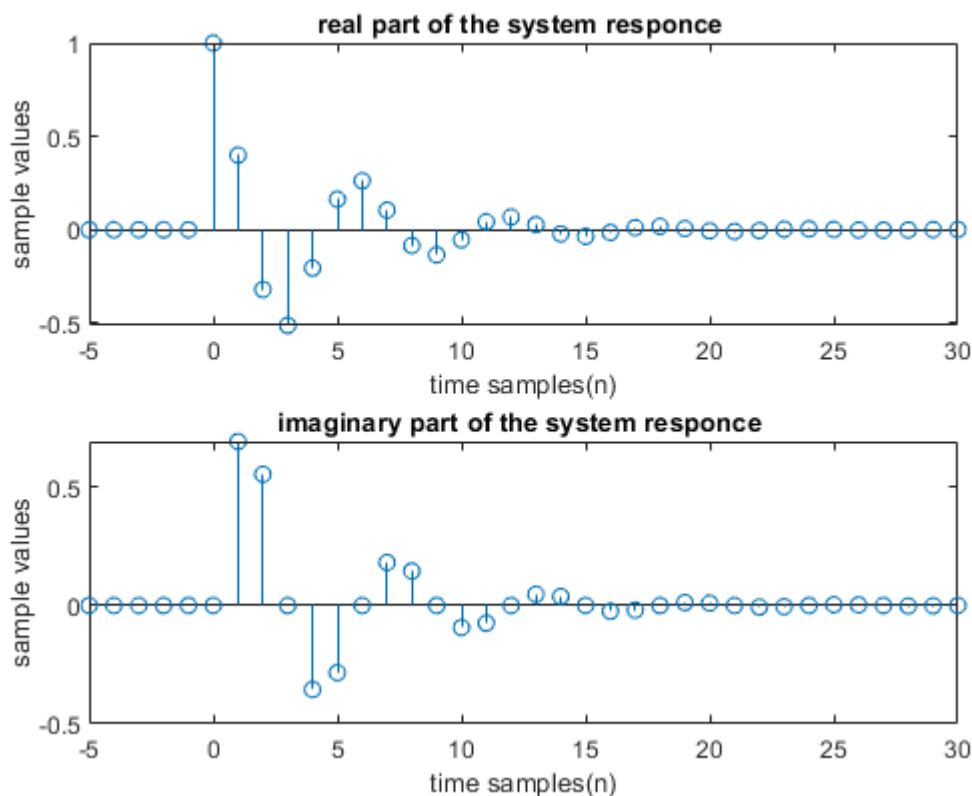
Key Commands:

Real % it gives the real part of the signal

Imag % it gives the imaginary part of the signal

Filter % `filter(b,a,x)` filters the input data x using a rational transfer function defined by the numerator and denominator coefficients b and a

Plots:



Inferences/comments:

We can observe that for a complex coefficients the output response is a sinusoidal response, where as if the coefficient is real, it will give different signal for different coefficients.

Q6. Use “filter” function to generate and plot the impulse response $h[n]$ of the following difference equation. Plot $h[n]$ in the range $-10 \leq n \leq 100$. assume the initial conditions are zeros
$$y[n] - 1.8\cos(\pi/16)y[n - 1] + 0.81y[n - 2] = x[n] + 0.5x[n - 1]$$

AIM: To generate and plot the impulse response $h[n]$ of the following difference equation in the range -10 to 100 .

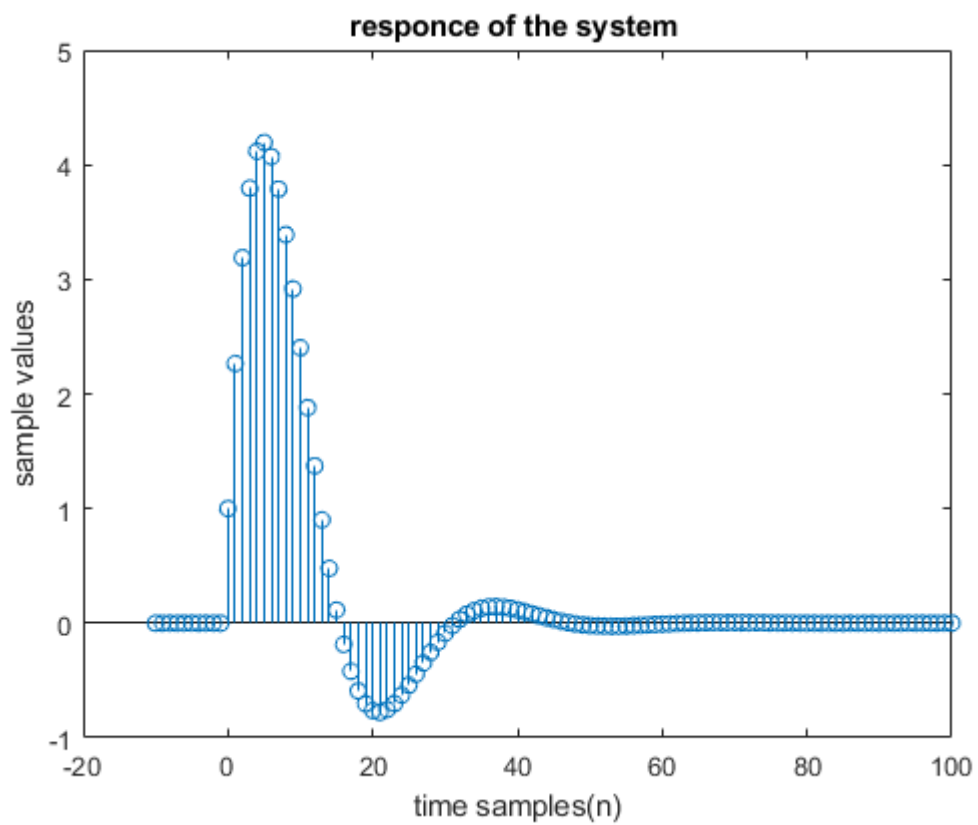
Short Theory:

The solution of a differential equation $y[n]$ can be obtained by converting given differential equation into transfer function ($h[n]=y[n]/x[n]$). Then multiplying the $h[n]$ with the given input signal $x[n]$.

Key Commands:

Filter % `filter(b,a,x)` filters the input data x using a rational transfer function defined by the numerator and denominator coefficients b and a

Plots:



Inferences/comments:

The output response of the given signal is a decaying sinusoidal signal.