

1. **Otsu's Thresholding:**

Write your own MATLAB function to perform Otsu's thresholding of the input grayscale image.

**Input Images:** coins.jpg, building.jpg, an image of your own hand-written notes! The input to the program is a grayscale image and the outputs of your program should be

- (i) Plot the histogram of the input image with Otsu-based threshold value marked on it.
- (ii) Display the resulting segmentation image. Write your observations from these results and also compare your results with the results of the "graythresh" command in MATLAB.

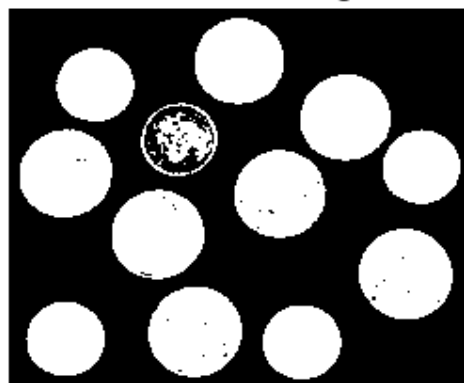
**Aim:** To perform Otsu's thresholding of the input grayscale image for given images and plot the histogram for resultant image and mark the threshold values in the histogram.

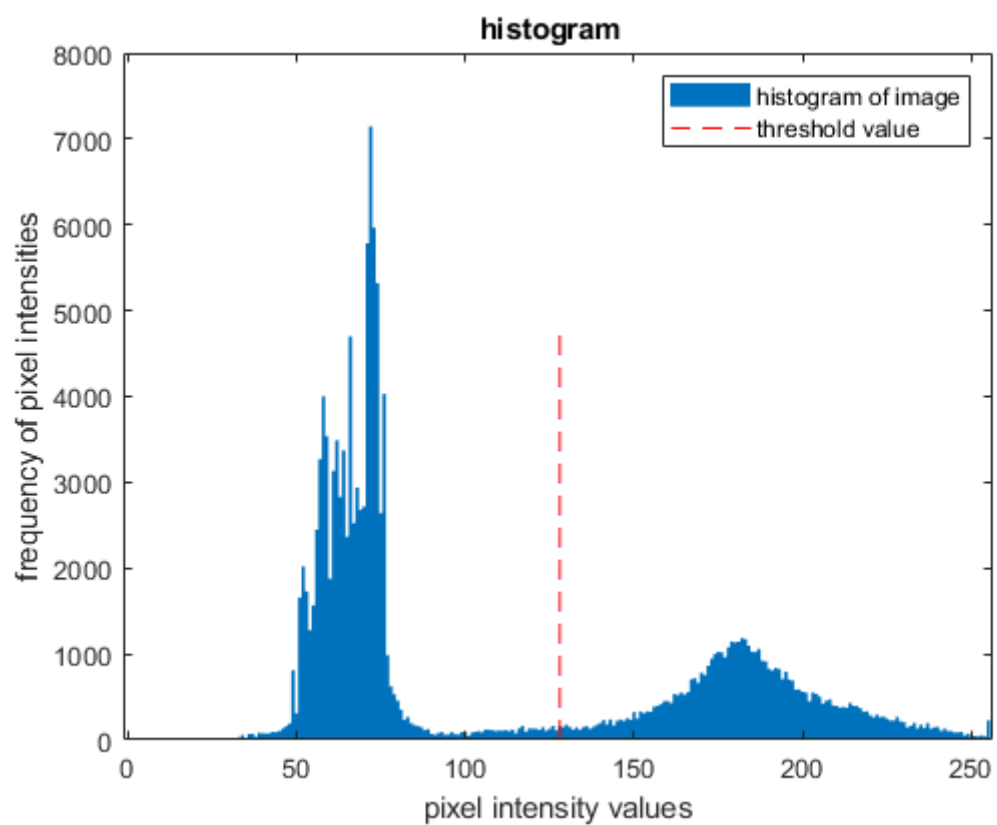
**Output:**

given image



after thresholding

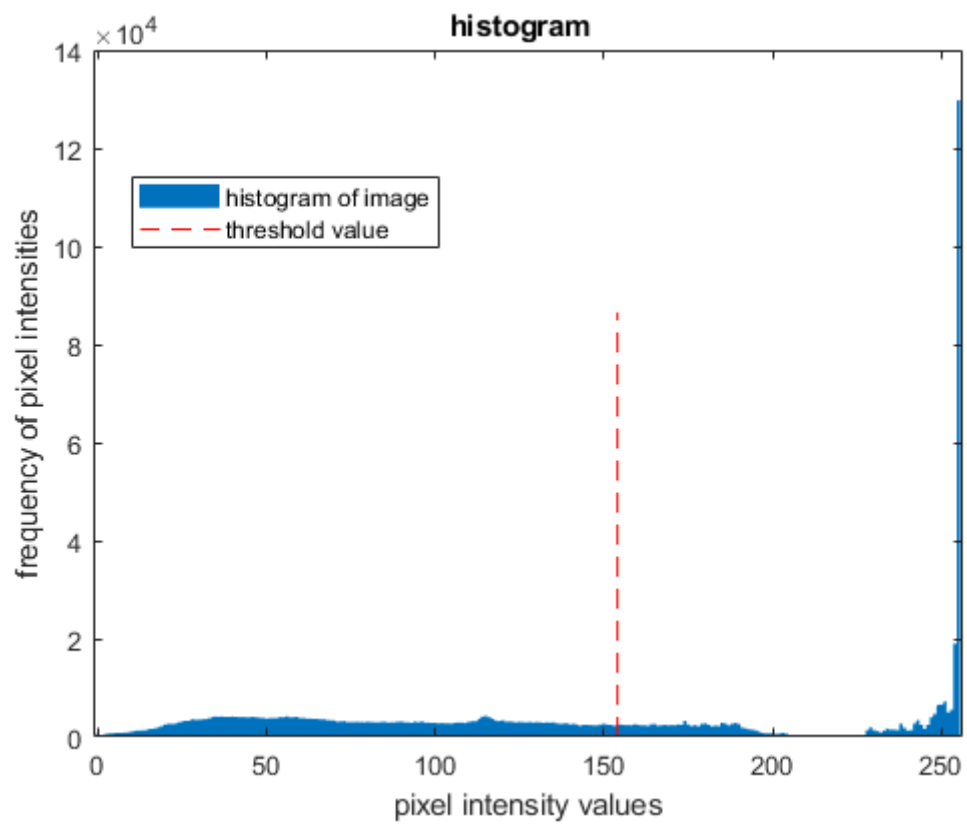




given image



after thresholding



given image

minimum mean square error estimator (MMSE)

Criteria:  $E[(y - \hat{y})^2]$  , ,  $\hat{y} = c$  ,  $y = y_1, y_2, y_3, \dots$

so, estimation good (or) not

Checking min  $J = \int_{-\infty}^{\infty} (y - \hat{y})^2 \cdot f_y(y) dy$

$$= \min \int (y - c)^2 f_y(y) dy$$

$$\frac{dJ}{dc} = \int 2(y - c) f_y(y) dy = 0$$

$$\Rightarrow \int y f_y(y) dy = c \underbrace{\int f_y(y) dy}_{1}$$

$$\Rightarrow c = E[y]$$

after thresholding

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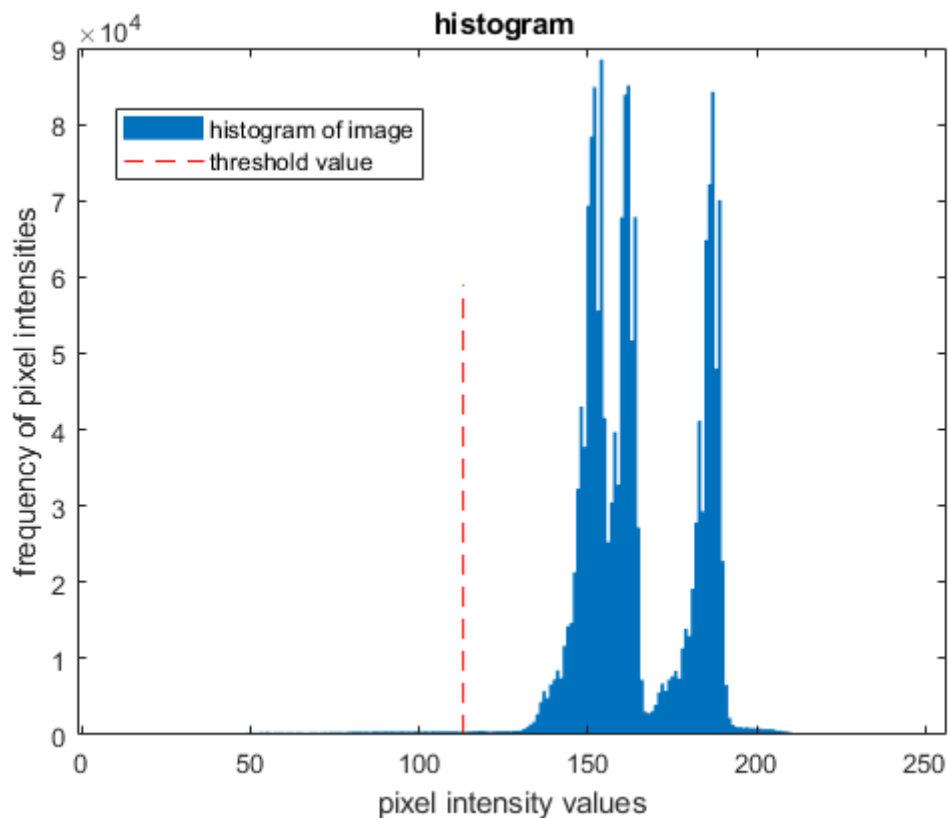
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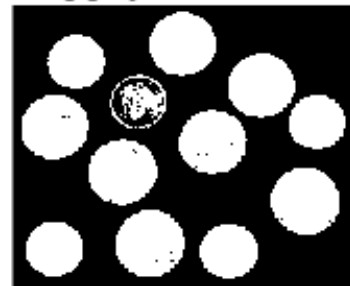
#### Inferences:

1. I used the red dotted line (line command) to mark the threshold value found using Otsu thresholding in the histogram.
2. I used the **between class variance** method to find the threshold value using Otsu method, because some of the given images size is too high, so computation is more for **with-in class variance** method.
3. We select the threshold value as, the threshold value which gives the maximum between class variance.
4. When we compare the results with inbuilt command "**graythresh**" both are almost similar. Comparison results are listed below.

after thresholding



using graythresh command



after thresholding



using graythresh command



after thresholding

$$\begin{aligned} \frac{d}{dt} \left( \frac{1}{2} m \dot{x}^2 \right) &= m \dot{x} \ddot{x} = m \dot{x} \left( -\frac{1}{2} \frac{v^2}{r} \right) = -\frac{1}{2} m \dot{x} \frac{v^2}{r} \\ &= -\frac{1}{2} m \dot{x} \frac{(\dot{x}^2 + \dot{y}^2)}{r} = -\frac{1}{2} m \dot{x} \frac{v^2}{r} \end{aligned}$$

using graythresh command

[illegible]