

COMPUTATIONAL GEOMETRY PROJECT REPORT

on

"Sweep-line Algorithm"

at

"Department of Mathematics, SPPU"

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This is a great pleasure and immense satisfaction to express our deepest sense of gratitude and thanks to everyone who has directly or indirectly helped us in completing our Computational Geometry Project successfully.

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Abstract

Our Computational Geometry project, conducted by the department, explores the application of the sweep-line algorithm to detect and report intersections among line segments within a two-dimensional plane. Utilizing event-driven processing, the algorithm efficiently identifies intersecting segment pairs, which are essential in computational geometry fields such as computer graphics, geographic information systems, and collision detection.

Key challenges addressed include managing overlapping segments, handling shared endpoints, and optimizing data structures for performance improvements.

The report outlines the algorithm's design and implementation, details weekly progress across various development phases, and analyzes testing results on complex datasets. These insights demonstrate the algorithm's robustness, scalability, and potential applications in dynamic computational geometry environments.

Keywords:

slope, orientation, point, segment, event, vector, intersection, sweep line

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Chapter 1

Computational Geometry

Course

Computational Geometry is the study of algorithms to solve geometric problems, like finding the shortest paths, detecting intersections, and analyzing shapes. It has applications in fields like computer graphics, mapping, robotics, and data analysis.

This course conducted by Savitribai Phule Pune University introduces key techniques, such as the sweep-line algorithm for finding intersecting line segments and Voronoi diagrams for identifying nearest points. By learning these methods, students will gain skills in designing efficient solutions for real-world problems involving spatial data. This foundation in computational geometry will prepare students for roles in academia and industries that use mathematical and computational tools for spatial problem-solving.

This course requires a minimum of one semester. Each student registers for this course will be given **4 credits**.

Chapter 2

Prerequisites

2.1 Orientation of three ordered pairs

2.1.1 Problem Statement

Given three points a , b and c , the task is to determine the orientation of these three points.

2.1.2 Definition: Orientation

Orientation of an ordered triplet of points in the plane can be

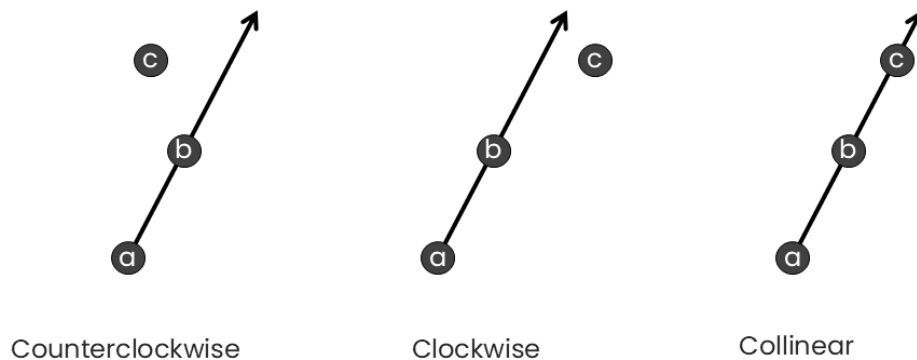


Figure 2.1: Orientation of three points a , b , c

Note:

- If orientation of (a, b, c) is collinear, then orientation of (c, b, a) is also collinear.
- If orientation of (a, b, c) is clockwise, then orientation of (c, b, a) is counterclockwise and vice versa is also true.

2.1.3 How to compute orientation?

The idea is to use the slope.

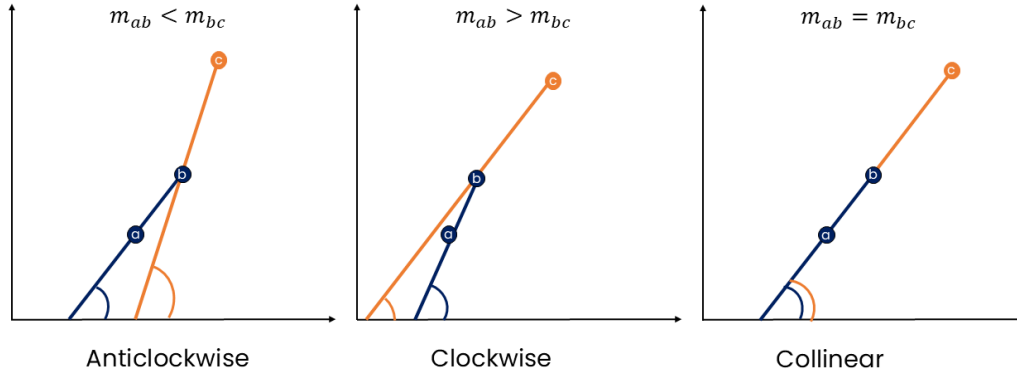


Figure 2.2: Orientation using slope

Here, slopes of ab and bc are given by:

$$m_{ab} = \frac{y_2 - y_1}{x_2 - x_1} \quad \& \quad m_{bc} = \frac{y_3 - y_2}{x_3 - x_2}$$

- **Anticlockwise:**

$$\begin{aligned} m_{ab} &< m_{bc} \\ \frac{y_2 - y_1}{x_2 - x_1} &< \frac{y_3 - y_2}{x_3 - x_2} \\ (y_2 - y_1) * (x_3 - x_2) &< (y_3 - y_2) * (x_2 - x_1) \\ (y_2 - y_1) * (x_3 - x_2) - (y_3 - y_2) * (x_2 - x_1) &< 0 \end{aligned}$$

- **Clockwise:**

$$\begin{aligned} m_{ab} &> m_{bc} \\ \frac{y_2 - y_1}{x_2 - x_1} &> \frac{y_3 - y_2}{x_3 - x_2} \\ (y_2 - y_1) * (x_3 - x_2) &> (y_3 - y_2) * (x_2 - x_1) \\ (y_2 - y_1) * (x_3 - x_2) - (y_3 - y_2) * (x_2 - x_1) &> 0 \end{aligned}$$

- **Collinear:**

$$m_{ab} = m_{bc}$$

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{y_3 - y_2}{x_3 - x_2}$$

$$(y_2 - y_1) * (x_3 - x_2) = (y_3 - y_2) * (x_2 - x_1)$$

$$(y_2 - y_1) * (x_3 - x_2) - (y_3 - y_2) * (x_2 - x_1) = 0$$

2.1.4 Algorithm

- Calculate slopes of line formed by points (a, b) and (b, c).
- If slopes are equal, then points are collinear
- If slope of (a,b) < slope of (b,c), then points are in counter clockwise orientation
- If slope of (a,b) > slope of (b,c), then points are in clockwise orientation

2.1.5 Code snippet:

```

1  #include<iostream>
2  using namespace std;
3
4  //Function to check orientation
5  string Orientation(int p1[], int p2[], int p3[])
6  {
7      int slope1 = (p2[1] - p1[1]) * (p3[0] - p2[0]);
8      int slope2 = (p3[1] - p2[1]) * (p2[0] - p1[0]);
9
10     if(slope1 - slope2 < 0)
11         return "Anticlockwise";
12     else if(slope1 - slope2 > 0)
13         return "Clockwise";
14     else
15         return "Collinear";
16 }
17 int main(){
18     int p1[] = { 0, 0 };
19     int p2[] = { 4, 4 };
20     int p3[] = { 1, 1 };
21     cout << Orientation(p1, p2, p3) << endl;
22
23     return 0;
24 }
```

2.2 Finding if two line segment intersects

2.2.1 Problem Statement

Given two line segments $(p1, q1)$ and $(p2, q2)$, find if the given line segments intersect with each other.

2.2.2 How orientation is useful here?

2.2.2.1 General Cases

The figure below shows general cases for segments' intersections:

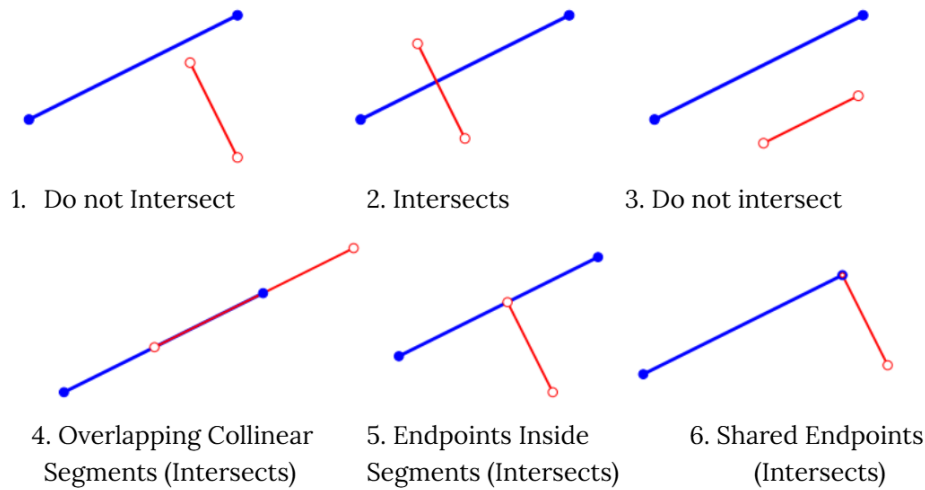


Figure 2.3: General cases

Here, we observe that two segments $(p1, q1)$ and $(p2, q2)$ intersect each other if following two conditions satisfies:

- Points $(p1, q1, p2)$ and $(p1, q1, q2)$ have different orientations.
- Points $(p2, q2, p1)$ and $(p2, q2, q1)$ have different orientations.

2.2.2.2 Special Cases

The figure below shows special cases for segments' intersections:

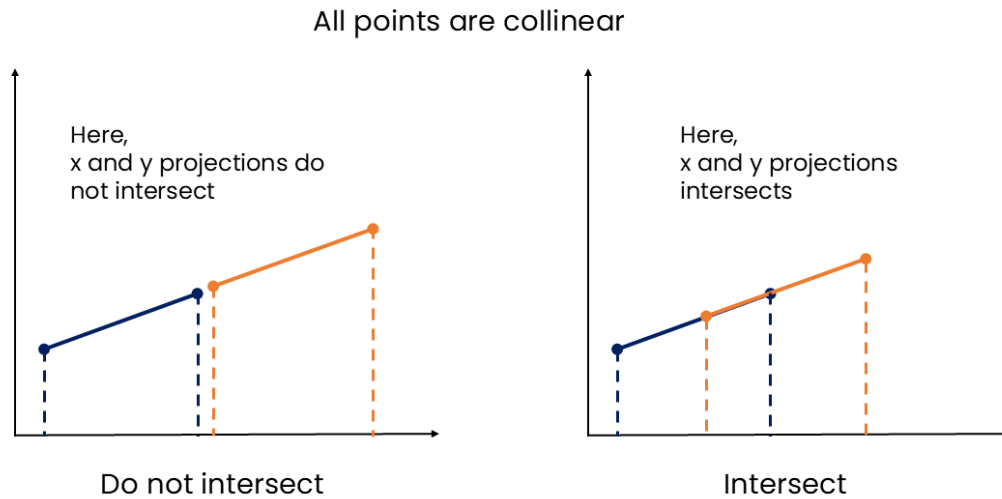


Figure 2.4: Special Cases

Here, we observe that two segments $(p1, q1)$ and $(p2, q2)$ intersect each other:

- Special Case:
 - If all points $(p1, q1, p2)$, $(p1, q1, q2)$, $(p2, q2, p1)$, $(p2, q2, q1)$ have same orientations i.e. they are parallel, then check if the x and y projections of $(p1, q1)$ and $(p2, q2)$ intersect

2.2.3 Code Snippet

```
1 #include<iostream>
2 using namespace std;
3
4 //Struct Point
5 struct Point
6 {
7     int x, y;
8 };
9
10 int orientation(Point p1, Point p2, Point p3)
11 {
12     int slope = (p2.y - p1.y) * (p3.x - p2.x)
13               - (p3.y - p2.y) * (p2.x - p1.x);
14
15     if(slope == 0) //Collinear
16         return 0;
17     else if(slope > 0) //Clockwise
18         return 1;
19     else //Counter Clockwise
20         return 2;
21 }
22
23 //Checks if Point B lies on line segment 'AC'
24 bool onSegment(Point A, Point B, Point C)
25 {
26     if( (B.x <= max(A.x, C.x) && B.x >= min(A.x, C.x)) &&
27         (B.y <= max(A.y, C.y) && B.y >= min(A.y, C.y)))
28         return true;
29
30     return false;
31 }
32
33 bool doIntersect(Point p1, Point q1, Point p2, Point q2)
34 {
35     int o1 = orientation(p1, q1, p2);
36     int o2 = orientation(p1, q1, q2);
37     int o3 = orientation(p2, q2, p1);
38     int o4 = orientation(p2, q2, q1);
39
40     if(o1 != o2 && o3 != o4)
41         return true;
42
43     //Check if (p1, q1, p2) are collinear and p2 lies between
44     //line segment (p1, q1)
45     if(o1 == 0 && onSegment(p1, p2, q1))
46         return true;
```

```

47 //Check if (p1, q1, q2) are collinear and q2 lies between
   line segment (p1, q1)
48 if(o2 == 0 && onSegment(p1, q2, q1))
49     return true;
50
51 //Check if (p2, q2, p1) are collinear and q1 lies between
   line segment (p2, q2)
52 if(o3 == 0 && onSegment(p2, q2, p1))
53     return true;
54
55 //Check if (p2, q2, q1) are collinear and q1 lies between
   line segment (p2, q2)
56 if(o4 == 0 && onSegment(p2, q2, q1))
57     return true;
58
59 return false; //Doesn't fall in any above condition
60 }
61
62 int main(){
63     struct Point p1 = {1, 1}, q1 = {10, 1};
64     struct Point p2 = {1, 2}, q2 = {10, 2};
65
66     doIntersect(p1, q1, p2, q2)? cout << "Yes\n": cout << "No
   \n";
67
68     p1 = {10, 0}, q1 = {0, 10};
69     p2 = {0, 0}, q2 = {10, 10};
70     doIntersect(p1, q1, p2, q2)? cout << "Yes\n": cout << "No
   \n";
71
72     p1 = {-5, -5}, q1 = {0, 0};
73     p2 = {1, 1}, q2 = {10, 10};
74     doIntersect(p1, q1, p2, q2)? cout << "Yes\n": cout << "No
   \n";
75 return 0;
76 }

```

Chapter 3

Intersection of n line segments

Naive Approach

3.1 Problem Statement

Given n line segments $(p_1, q_1), (p_2, q_2), \dots, (p_n, q_n)$, find if the given line segments intersect with each other or not.

3.2 Input

- First Line: Enter the number of line segments, **n**.
- Next n Lines: Each line contains the coordinates of the endpoints of a line segment, formatted as **x1 y1 x2 y2**, where (x_1, y_1) and (x_2, y_2) are the coordinates of the two endpoints of the line segment.

3.3 Output

List all intersecting pairs of line segments. Each intersection should be reported as a pair of segment indices, with the index starting from 1.

3.4 Example

For input:

```
4
1 1 4 4
2 1 2 5
3 0 3 3
```


4 2 6 2

The output might be:

1 2

1 3

3.5 Algorithm: findIntersections

Input: A vector `segments` of `Segment` objects, where each segment represents a line segment.

Output: Prints pairs of intersecting segments if any intersections are found; otherwise, prints a message indicating no intersections.

Working:

1. Initialize Variables:

- Let `n` be the number of segments in the `segments` vector.
- Set a boolean variable `hasIntersections` to `false`. This will be used to track if any intersections are found.

2. Check for Intersections:

- For each segment `segments[i]` (loop variable `i` ranges from 0 to `n-1`)
- For each subsequent segment `segments[j]` (loop variable `j` ranges from `i+1` to `n-1`):
 - Call the `doIntersect()` with `segments[i]` and `segments[j]` as arguments to check if they intersect.
 - If `doIntersect()` returns `true`:
 - * Print a message indicating that `Segment i+1` intersects with `Segment j+1`.
 - * Set `hasIntersections` to `true`.

3. Final Output:

If `hasIntersections` remains `false` after all pairs are checked, print "No Intersections found."

Complexity: This algorithm has a time complexity of $O(n^2)$ due to the nested loops that check all pairs of segments.

3.6 Code Snippet

```
1 #include<iostream>
2 #include <vector>
3 using namespace std;
4
5 //Point class having data members x and y
6 class Point
7 {
8 public:
9     int x, y; //data members
10    Point() //Default constructor
11    {
12        x = 0; y = 0;
13    }
14
15    Point(int x, int y) //Parametrised constructor
16    {
17        this->x = x; this->y = y;
18    }
19 };
20
21 //Class for segment in 2D Plane
22 class Segment
23 {
24 public:
25     //data members
26     Point left, right; int id;
27
28     Segment() //default constructor
29     {
30         left = { 0, 0 };
31         right = { 0, 0 };
32         id = 0;
33     }
34
35     Segment(Point left, Point right, int id) //parametrized
36         constructor
37     {
38         this->left = left;
39         this->right = right;
40         this->id = id;
41     }
42 };
43
44 // Function to find the orientation of ordered triplet (p, q,
45 // r)
46 int orientation(Point p, Point q, Point r)
```

```
45 {
46     int slope = (q.y - p.y) * (r.x - q.x) - (q.x - p.x) * (r.y
47         - q.y);
48     if (slope == 0) //collinear
49         return 0;
50     return (slope > 0)
51         ? 1 //clockwise
52         : 2; //anticlockwise
53 }
54 // Function to check if a point q lies on segment pr
55 bool onSegment(Point p, Point q, Point r)
56 {
57     return q.x <= max(p.x, r.x) && q.x >= min(p.x, r.x) &&
58         q.y <= max(p.y, r.y) && q.y >= min(p.y, r.y);
59 }
60
61 // Function that returns true if two segments 's1' and 's2'
62 // intersect
63 bool doIntersect(Segment s1, Segment s2)
64 {
65     Point p1 = s1.left, q1 = s1.right; //segment s1 = segment
66     p1q1
67     Point p2 = s2.left, q2 = s2.right; //segment s2 = segment
68     p2q2
69
70     int o1 = orientation(p1, q1, p2);
71     int o2 = orientation(p1, q1, q2);
72     int o3 = orientation(p2, q2, p1);
73     int o4 = orientation(p2, q2, q1);
74
75     //General case
76     if (o1 != o2 && o3 != o4)
77         return true;
78
79     //Special cases
80     if (o1 == 0 && onSegment(p1, p2, q1))
81         return true;
82     if (o2 == 0 && onSegment(p1, q2, q1))
83         return true;
84     if (o3 == 0 && onSegment(p2, p1, q2))
85         return true;
86     if (o4 == 0 && onSegment(p2, q1, q2))
87         return true;
88     return false;
89 }
90 //Function that checks for any intersection between segments
```

```
90 void findIntersections(vector<Segment>& segments)
91 {
92     int n = segments.size(); //returns the size of Segments
93     vector
94     bool hasIntersections = false;
95
96     //Now to check all pairs of intersection
97     for (int i = 0; i < n; i++){
98         for (int j = i + 1; j < n; j++)
99         {
100             if (doIntersect(segments[i], segments[j]))
101             {
102                 cout << "Segment " << i + 1 << " intersects with
103                 Segment " << j + 1 << "\n";
104                 hasIntersections = true;
105             }
106         }
107     }
108
109     if (!hasIntersections)
110         cout << "No Intersections found." << endl;
111 }
112
113 int main()
114 {
115     int n;
116     cout << "Enter the number of segments: ";
117     cin >> n;
118     vector<Segment> segments;
119
120     //Input the segments
121     for (int i = 0; i < n; i++)
122     {
123         int x1, y1, x2, y2;
124
125         cout << "Enter segment " << i + 1 << " coordinates (x1
126         y1 x2 y2): ";
127         cin >> x1 >> y1 >> x2 >> y2;
128
129         segments.push_back(Segment(Point(x1, y1), Point(x2, y2)
130         , (i+1)));
131     }
132
133     //Find and print intersecting segments
134     findIntersections(segments);
135
136     return 0;
137 }
```

Chapter 4

Sweep Line Algorithm

4.1 Introduction

The Sweep Line Algorithm is a fundamental computational geometry technique used to detect intersections between line segments in a 2D plane. By "sweeping" a vertical line from left to right across the plane, the algorithm identifies and processes events where intersections may occur, efficiently finding overlapping or intersecting line segments. This method is widely used in computer graphics, GIS, and robotic path-finding due to its ability to handle a large number of segments with reduced computational complexity.

4.2 Problem Definition

4.2.1 Objective

Implement the sweep line algorithm to detect intersections between a set of line segments in a 2D plane. The algorithm should efficiently identify all intersecting pairs of line segments.

4.2.2 Input

1. **First Line:** Enter number of line segments, n
2. **Next n Lines:** Each line contains the coordinates of the endpoints of a line segment, formatted as $x1\ y1\ x2\ y2$, where $(x1,y1)$ and $(x2,y2)$ are the coordinates of the two endpoints of the line segment.

4.2.3 Output

List all intersecting pairs of line segments. Each intersection should be reported as a pair of segment indices, with the index starting from 1.

4.2.4 Example

For input:

```
4
1 1 4 4
2 1 2 5
3 0 3 3
4 2 6 2
```

The output must be:

```
1 2
1 3
```

4.3 Weekly Tasks Assigned for Project

- **Week 1:** Implement the basic sweep line algorithm to detect intersections between line segments. Focus on correctly handling the event points where the sweep line intersects with segment endpoints.
- **Week 2:** Extend your implementation to handle complex cases such as overlapping line segments and segments that share endpoints. Ensure that all intersections are detected and reported accurately.
- **Week 3:** Optimize your algorithm to improve performance. Investigate and apply techniques to efficiently manage the status structure and handle a large number of line segments.
- **Week 4:** Test your implementation with a variety of complex input cases, including line segments that create multiple intersecting regions, to ensure robustness and accuracy.
- **Week 5:** Research and incorporate advanced features, such as handling special cases or optimizing the data structures used in the algorithm. Ensure that your implementation is both efficient and accurate.
- **Week 6:** Review and finalize your project. Make any necessary adjustments based on testing results, document your code and findings, and prepare for submission.

4.4 Sweep Line Algorithm to findIntersections

Input: A vector `segments` of `Segment` objects, where each segment represents a line segment.

Output: Prints pairs of intersecting segments if any intersections are found.

Working:

1. Initialize Variables:
 - Let `n` be the number of `segments` in the segments vector.
 - Create an empty vector `events` to store endpoint events of each segment.
2. Prepare Events for Sorting:
 - For each segment `segments[i]` (with index `i` from 0 to `n-1`):
 - Add an event for the left endpoint of `segments[i]`, marking it as a "left" event with `SegID = i`.
 - Add an event for the right endpoint of `segments[i]`, marking it as a "right" event with `SegID = i`.
 - Sort the `events` vector in ascending order based on the x-coordinates (and y-coordinates if x-coordinates are the same).
3. Sweep Line Algorithm to Find Intersections:
 - (a) Create an empty vector `activeSegments` to maintain segments that are currently active in the sweep line.
 - (b) For each event in `events` (loop index `i` from 0 to `2*n-1`):
 - Let `curr_index` be the segment index associated with the current event (`events[i].SegID`).
 - If the current event is a "left" endpoint:
 - Add this segment to `activeSegments`.
 - If `activeSegments` contains more than one segment:
 - * For each segment in `activeSegments` before this newly added segment:
 - Check if the new segment and the segment being iterated over intersect using the `doIntersect()`.

- If they intersect, print that Segment `it -> SegID + 1` intersects with Segment `curr_index + 1`.
- If the current event is a "right" endpoint:
 - Remove the segment with index `curr_index` from `activeSegments`.

Time Complexity: Sorting the events takes $O(n \log n)$, and processing each event within `activeSegments` involves iterating through active segments, making this approach efficient for finding intersections among multiple segments.

Note: The `doIntersect()` checks if two segments intersect based on their coordinates. This approach uses a sweep line technique with an active set to improve efficiency by only checking intersections among nearby segments.

4.5 Code implementation

```
1 #include <iostream>
2 #include <fstream> // For file handling
3 #include <vector>
4 #include <algorithm>
5 using namespace std;
6
7 //Point class having x and y coordinates
8 class Point
9 {
10 public:
11     int x, y;
12     Point()
13     {
14         x = 0;
15         y = 0;
16     }
17     Point(int x, int y)
18     {
19         this->x = x;
20         this->y = y;
21     }
22 };
23
24 //Segment class with start and end point and Segment ID
25 class Segment
26 {
27 public:
28     Point left, right;
```



```
29     int id;
30     Segment() {
31         left = { 0, 0 };
32         right = { 0, 0 };
33         id = 0;
34     }
35     Segment(Point left, Point right, int id)
36     {
37         this->left = left;
38         this->right = right;
39         this->id = id;
40     }
41 };
42
43 \\Event class
44 class Event
45 {
46 public:
47     int x, y;
48     bool isLeft;
49     int SegID;
50
51     Event() {
52         x = 0;
53         y = 0;
54         isLeft = true;
55         SegID = 0;
56     }
57
58     Event(int x, int y, bool isLeft, int segID)
59     {
60         this->x = x;
61         this->y = y;
62         this->isLeft = isLeft;
63         this->SegID = segID;
64     }
65
66     bool operator<(const Event& other) const {
67         if (x == other.x) return y < other.y;
68         return x < other.x;
69     }
70
71 };
72
73 // Function to find the orientation of ordered triplet (p, q,
74 // r)
75 int orientation(Point p, Point q, Point r)
76 {
77     int slope = (q.y - p.y) * (r.x - q.x) - (q.x - p.x) * (r.
```

```
    y - q.y);
77     if (slope == 0)
78         return 0;
79     return (slope > 0) ? 1 : 2;
80 }
81
82 // Function to check if a point q lies on segment pr
83 bool onSegment(Point p, Point q, Point r)
84 {
85     return q.x <= max(p.x, r.x) && q.x >= min(p.x, r.x) &&
86         q.y <= max(p.y, r.y) && q.y >= min(p.y, r.y);
87 }
88
89 // Function that returns true if two segments 's1' and 's2'
    intersect
90 bool doIntersect(Segment s1, Segment s2)
91 {
92     Point p1 = s1.left, q1 = s1.right;
93     Point p2 = s2.left, q2 = s2.right;
94
95     int o1 = orientation(p1, q1, p2);
96     int o2 = orientation(p1, q1, q2);
97     int o3 = orientation(p2, q2, p1);
98     int o4 = orientation(p2, q2, q1);
99
100     if (o1 != o2 && o3 != o4)
101         return true;
102
103     if (o1 == 0 && onSegment(p1, p2, q1)) return true;
104     if (o2 == 0 && onSegment(p1, q2, q1)) return true;
105     if (o3 == 0 && onSegment(p2, p1, q2)) return true;
106     if (o4 == 0 && onSegment(p2, q1, q2)) return true;
107
108     return false;
109 }
110
111 // Function that checks for any intersection between segments
112 void findIntersections(vector<Segment>& segments)
113 {
114     int n = segments.size();
115     vector<Event> events;
116
117     for (int i = 0; i < n; i++)
118     {
119         events.push_back(Event(segments[i].left.x, segments[i]
120 ].left.y, true, i));
121         events.push_back(Event(segments[i].right.x, segments[
122 i].right.y, false, i));
123     }
```

```
122     sort(events.begin(), events.end());
123
124
125     vector<Event> activeSegments;
126
127     for (int i = 0; i < 2 * n; i++)
128     {
129         int curr_index = events[i].SegID;
130         if (events[i].isLeft) {
131             activeSegments.push_back(events[i]);
132             if (activeSegments.size() > 1) {
133                 for (auto it = activeSegments.rbegin() + 1;
134 it != activeSegments.rend(); ++it)
135                 {
136                     if (doIntersect(segments[curr_index],
137 segments[it->SegID]))
138                     {
139                         cout << "Line " << (it->SegID) + 1 <<
140 " " << curr_index + 1 << " intersects" << endl;
141                     }
142                 }
143             }
144         }
145         else
146         {
147             vector<Event> ::iterator iter; //make an iterator
148             iter to search in activeSegments vector
149             for (iter = activeSegments.begin(); iter !=
150 activeSegments.end(); iter++)
151             {
152                 if (iter->SegID == curr_index) //if iter's
153 segID == curr_index
154                 {
155                     activeSegments.erase(iter); //then erase
156 that element from activeSegments by passing iter to it
157                     break; //and break it once found
158                 }
159             }
160         }
161     }
162 }
163
164
165 int main()
166 {
167     ifstream inFile("input.txt"); // Open the input file
168     if (!inFile) {
169         cerr << "Error opening file!" << endl;
170         return 1;
171     }
172 }
```

```
164
165     int n;
166     inFile >> n; // Read the number of segments from the file
167     vector<Segment> segments;
168
169     for (int i = 0; i < n; i++)
170     {
171         int x1, y1, x2, y2;
172         inFile >> x1 >> y1 >> x2 >> y2; // Read each segment's
173         // coordinates from the file
174         segments.push_back(Segment(Point(x1, y1), Point(x2,
175         y2), i + 1));
176     }
177
178     inFile.close(); // Close the file
179
180     // Find and print intersecting segments
181     findIntersections(segments);
182
183     return 0;
184 }
```

4.6 Applications of Sweep Line Algorithm

Here are some of the key areas where it is used:

1. Geographic Information Systems (GIS):

- **Line segment intersection:** Detecting intersections between roads, rivers, or other linear features.
- **Polygon operations:** Performing operations like union, intersection, and difference on polygons representing land parcels, water bodies, or administrative boundaries.
- **Map overlay:** Combining multiple layers of geographic data (e.g., terrain, land use, population density) to create comprehensive maps.

2. Computer-Aided Design (CAD):

- **Collision detection:** Identifying overlapping objects or parts in a 3D model to prevent design errors.
- **Boolean operations:** Performing operations like union, intersection, and difference on 3D shapes.

- **Layout generation:** Optimizing the placement of objects within a design, such as electrical components on a circuit board or furniture in a room.

3. Robotics and Motion Planning:

- **Obstacle avoidance:** Planning collision-free paths for robots in environments with static or dynamic obstacles.
- **Motion planning:** Generating smooth and efficient motion trajectories for robots performing tasks like assembly or manipulation.

4. VLSI Design:

- **Circuit layout:** Optimizing the placement and routing of components on integrated circuits.
- **Design rule checking:** Verifying that the design adheres to specific manufacturing constraints.

5. Bioinformatics:

- **Genome analysis:** Identifying overlapping or intersecting regions in DNA sequences.
- **Protein structure prediction:** Analyzing the spatial arrangement of amino acids in proteins.

6. Image Processing:

- **Image segmentation:** Identifying and separating different objects or regions within an image.
- **Feature extraction:** Extracting relevant features from images, such as edges, corners, or textures.

7. Game Development:

- **Collision detection:** Detecting collisions between game objects, such as characters, projectiles, and obstacles.
- **Physics simulation:** Simulating the physical behavior of objects in a game world.

These are just a few examples of the many real-world applications of the sweep line algorithm. Its versatility and efficiency make it a valuable tool for solving a wide range of geometric problems.

Chapter 5

Conclusion

5.1 Summary of Project Objective

In this project, we successfully developed an algorithm to detect intersections between line segments using a sweep line approach, implemented in C++ with the Standard Template Library (STL). The project focused on creating an efficient solution to a common computational geometry problem and involved the use of custom data structures and event-driven processing to optimize intersection detection.

5.2 Key Achievements

Key accomplishments included designing and implementing the code to handle segment events efficiently, leveraging sorting and active set management for optimized performance.

5.3 Challenges Overcome

In this project managing complex geometric conditions and optimizing it efficiently for large data sets was bit challenging for us. Through the use of Visual Studio's debugging tools, we were able to gain a detailed understanding of each step in the algorithm, allowing us to troubleshoot and refine our approach to ensure accurate results.

5.4 Skills Gained

1. **Algorithmic Thinking:** Learned to break down the intersection problem and apply a sweep line algorithm, optimizing for efficiency.

2. Data Structures:

- Used **vectors** for dynamic storage and manipulation of events and active segments.
- Applied **sorting techniques** to prepare event points in a specific order for efficient processing.
- Utilized **iterators and STL algorithms** like `remove_if` for managing active segments.

3. Coding in C++:

- Practiced advanced C++ programming skills, including working with STL containers and algorithms, lambda functions, and custom structures.
- Improved debugging and code optimization, focusing on both time and space efficiency.

4. Debugging and Development Tools:

Visual Studio: Gained proficiency in using Visual Studio as an IDE, especially utilizing its debugging tools to step through code execution. This helped identify logical errors, understand the control flow, and verify the behavior of complex conditions in real time.

References & Links

1. YouTube Videos -

- (a) (https://youtube.com/playlist?list=PL5DyztRVgtRVHE6fulR_qOW_pNd8JdMlb&si=i3haw80BKlA1gVoI)
- (b) (https://youtube.com/playlist?list=PL5DyztRVgtRVHE6fulR_qOW_pNd8JdMlb&si=i3haw80BKlA1gVoI)
- (c) (https://youtu.be/rEVlLMt-fwk?si=qvqgY127gbT_FGjK)

2. Online articles-

- (a) (<https://www.geeksforgeeks.org/given-a-set-of-line-segments-find-if-any>)
- (b) (https://web.mit.edu/urban_or_book/www/book/chapter7/7.2.4.html)
- (c) (<https://cplusplus.com/reference/vector/vector/>)