

Coding task

1. Preliminaries and rules

The scope of this task is rather large and it is almost impossible to implement a complete solution within the given time frame. It is up to you to define and to control the scope! Please focus on the most important aspects of the task first. Please proceed in an incremental way using small steps! Ensure that at any point in time, your solution can be executed and add small features one by one. In this way, the time limit will not hinder you to deliver at least a partial solution – which is very acceptable!

A note regarding large language models (e.g. ChatGPT): It is allowed to employ them to support solving the task. However, if you decide to do so, please describe your approach in detail.

2. Definition of done

The definition of done for any feature is:

- Unit tests are given that demonstrate the correctness of your code
- The code adheres to high quality standards, best practices and a clear structure. The code is easy to read, easy to maintain and to extend. You can, but do not have to use object oriented features such as inheritance and design patterns to achieve this.
- The resulting software is executable and can be tested by us

3. Problem description

You are going to implement a popular one player game, which is available on many smart phones. The player is given an $n \times n$ board of tiles where each tile is given one of m colors. Each tile is connected to up to four adjacent tiles in the North, South, East, and West directions. A tile is connected to the origin (the tile in the upper left corner) if it has the same color as the origin and there is a connected path to the origin consisting only of tiles of this color. A player does a move by choosing one of the m colors. After the choice is made, all tiles that are connected to the origin are changed to the chosen color. The game proceeds until all tiles of the board have the same color.

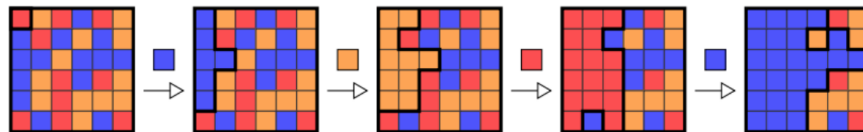


Figure 1: A possible sequence of moves together with the chosen color on a 6 x 6 board initially filled up with 3 distinct colors.

The goal of the game is to change all the tiles to the same color, preferably with the fewest number of moves possible. It has been proven that finding the optimal moves is a very hard computational problem. It has also been shown that finding the minimum number of flooding operations is NP-hard for $m > 3$. This even holds true when the player can perform flooding operations from any position on the board. However, this variant can be solved in polynomial time for the special case of $m = 2$. For an unbounded number of colors, even this variant remains NP-hard for boards of a dimension of at least $n = 3$ and is solvable in polynomial time for boards of dimension $n = 2$.

4. The task

For your solution, you will implement a very simple greedy strategy to solve it:

- for each move, choose the color that will result in the largest number of tiles connected to the origin;
- if there is a tie, break ties by choosing the color that has the lowest rank among the colors.

Please implement the game and an automated player that determines the color choice for each move. We want to determine the amount of moves and the sequence of the colors chosen by the player over the course of a game. Please use unit tests to proof that your code is working properly! There is no need to implement any kind of user interface, simply use your tests as a driver of your software. Please use the Python standard library and a unit test library of your choice, but no other third-party libraries.

If you can implement the simple greedy algorithm quickly, try to implement a better algorithm which provides a more optimal solution.