

Assignment 1

AI1110:Probability And Random Variables

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12.13.6.19: If A and B are any two events such that $\Pr(A) + \Pr(B) - \Pr(AB) = \Pr(A)$, then choose the correct option

- (a) $\Pr(B|A) = 1$
- (b) $\Pr(A|B) = 1$
- (c) $\Pr(B|A) = 0$
- (d) $\Pr(A|B) = 0$

Solution: Given

$$\Pr(A) + \Pr(B) - \Pr(AB) = \Pr(A) \quad (1)$$

$$\Pr(B) - \Pr(AB) = 0 \quad (2)$$

$$\Pr(B) = \Pr(AB) \quad (3)$$

1) $\Pr(B|A)$

$$\Pr(B|A) = \frac{\Pr(AB)}{\Pr(A)} \quad (4)$$

$$\Rightarrow = \frac{\Pr(B)}{\Pr(A)} \quad (5)$$

2) $\Pr(A|B)$

$$\Pr(A|B) = \frac{\Pr(AB)}{\Pr(B)} \quad (6)$$

$$\Rightarrow = \frac{\Pr(B)}{\Pr(B)} \quad (7)$$

$$\Rightarrow = 1 \quad (8)$$

\therefore Option b is Correct