

Practical - 7

Plotting the characteristics for the first order PDE

Find the Characteristic Equation of the Curve $(u-y)u_x + y u_y = x+y$

$$dx/(u-y) = dy/y = du/(x+y)$$

On taking I + III and II ,

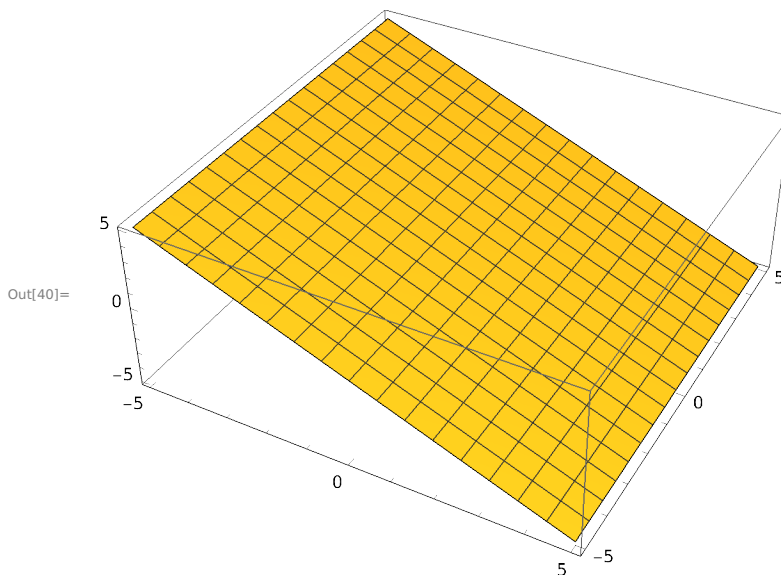
$$\text{we get } (u+x) / y = C_1$$

On taking I + II = III,

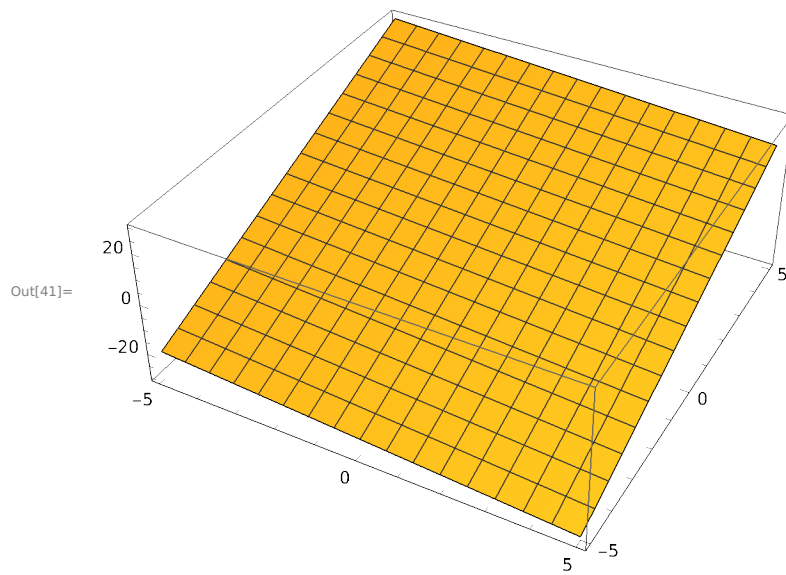
$$\text{we get } (x+y)^2 - u^2 = C_2$$

Now we Integrate to plot these for some particular values

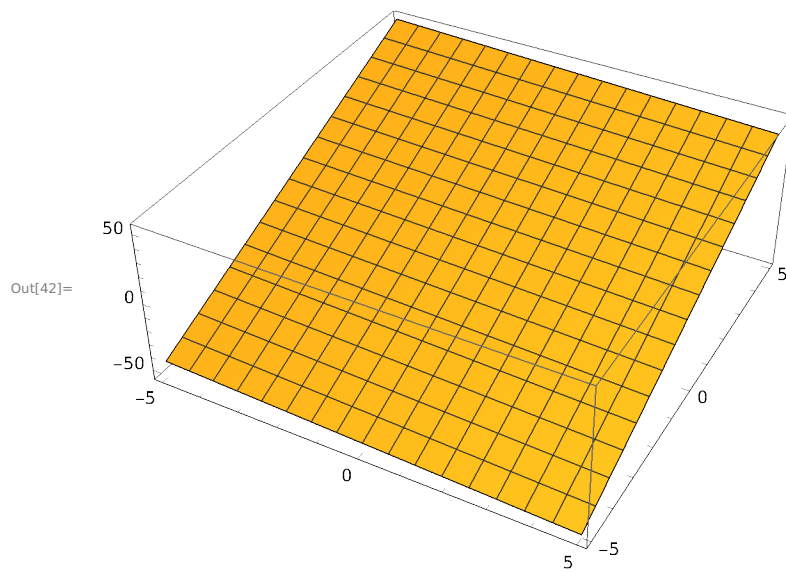
In[40]:= `F0 = Plot3D[-x, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]`



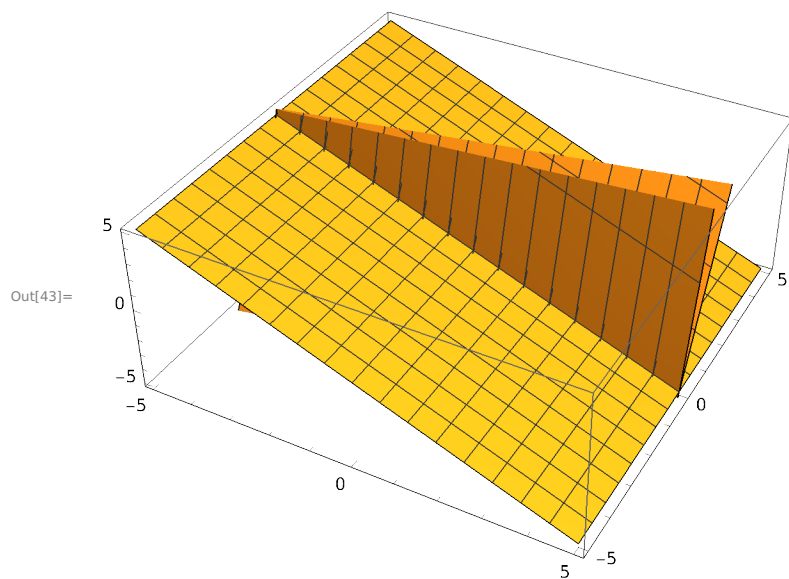
In[41]:= **F1 = Plot3D[5 * y - x, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]**



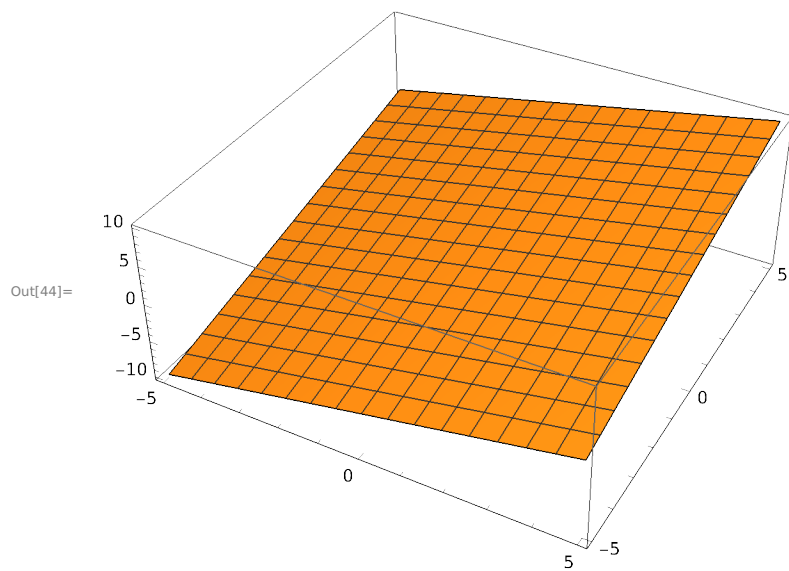
In[42]:= **F2 = Plot3D[10 * y - x, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]**



In[43]:= **G1 = Show[F0, F1, F2]**

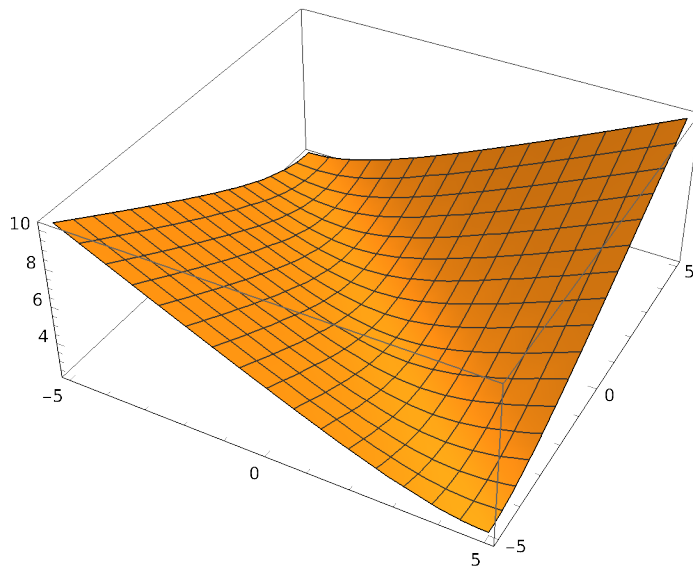


In[44]:= **H0 = Plot3D[x + y, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]**



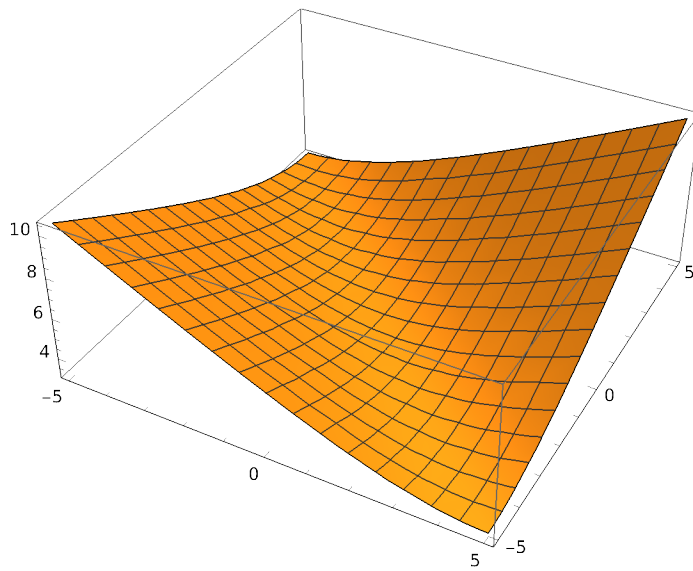
```
In[45]:= H1 = Plot3D[Sqrt[(x + y)^2 + 5], {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```

Out[45]=

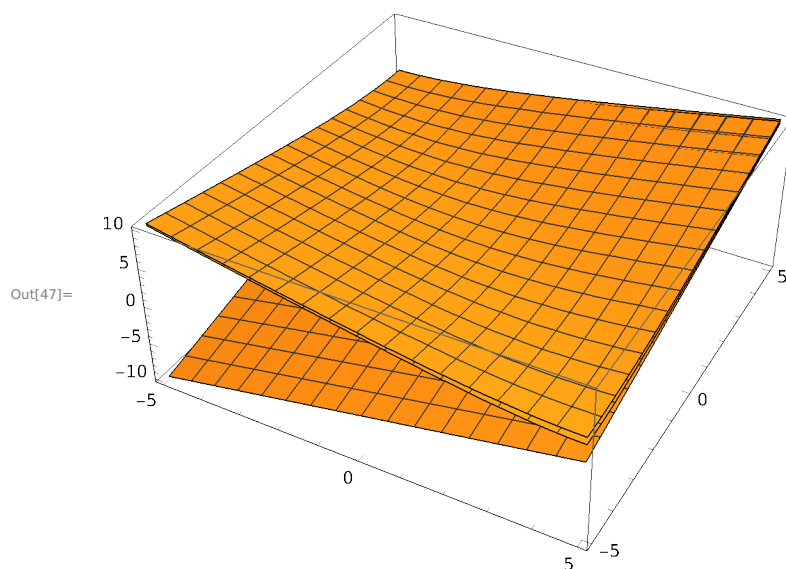


```
In[46]:= H2 = Plot3D[Sqrt[(x + y)^2 + 10], {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```

Out[46]=

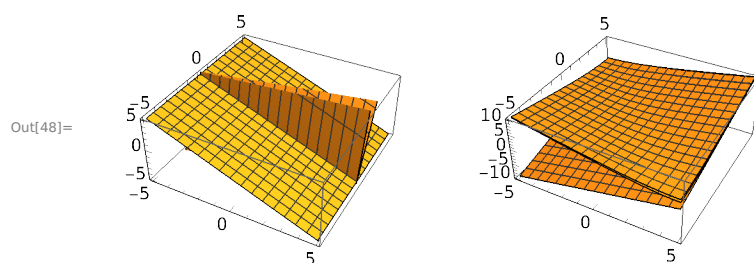


In[47]:= **G2 = Show[H0, H1, H2]**



In[48]:= **Show[GraphicsArray [{G1, G2}]]**

GraphicsArray : GraphicsArray is obsolete . Switching to GraphicsGrid .



Find the Characteristic Equation of the Curve $(u-y)*u_x + y* u_y = x+y$

$dx/(x) = dy/y = du/(u)$

On taking I and III ,

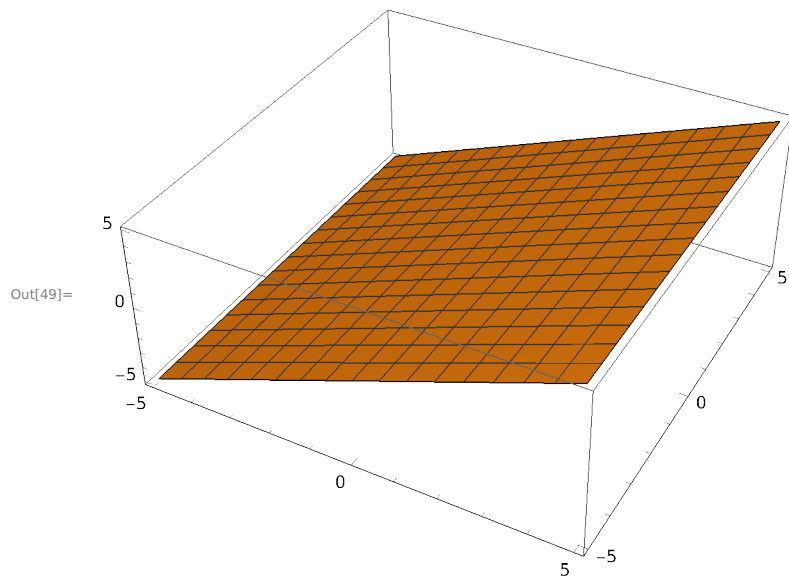
we get $x / u = C1$

On taking II = III,

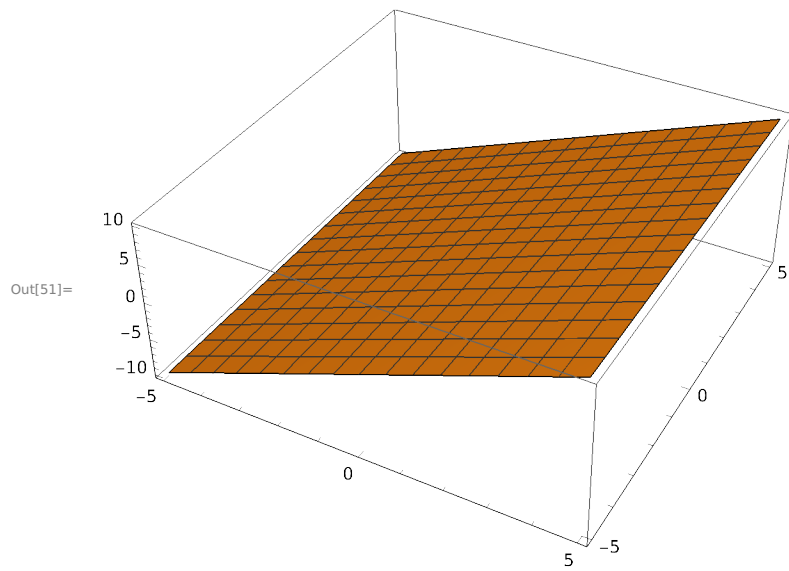
we get $y / u = C2$

Now we Integrate to plot these for some particular values

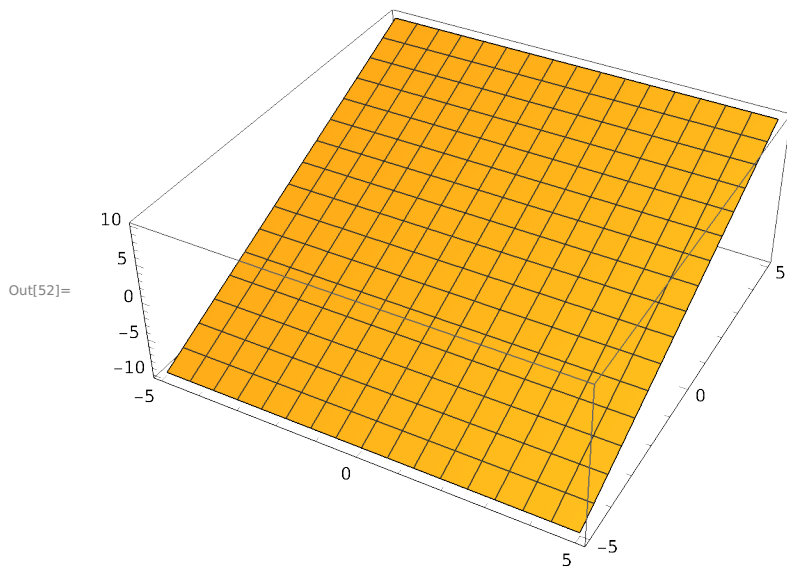
```
In[49]:= F0 = Plot3D[x, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```



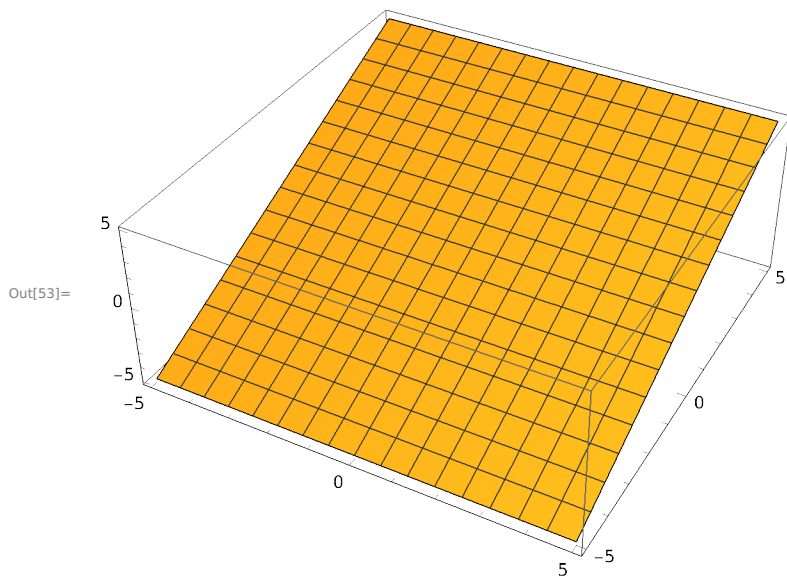
```
In[51]:= F1 = Plot3D[2 x, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```



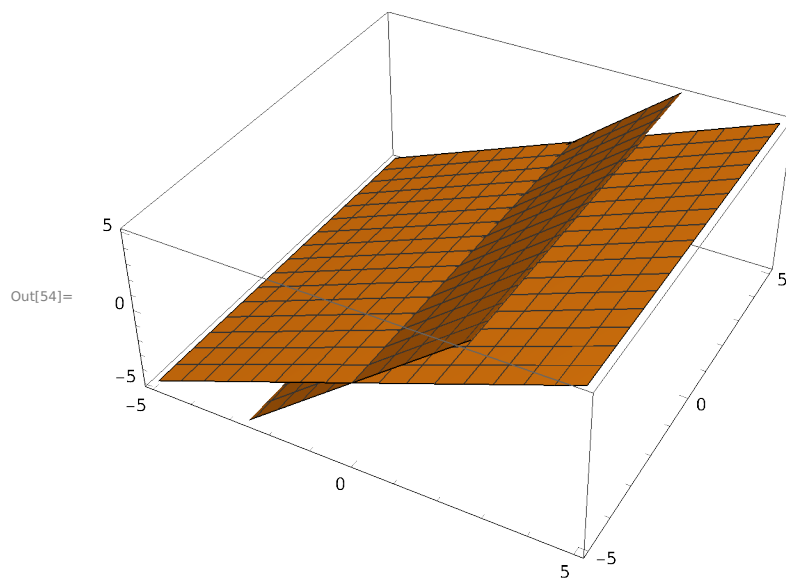
```
In[52]:= H0 = Plot3D[2 y, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```



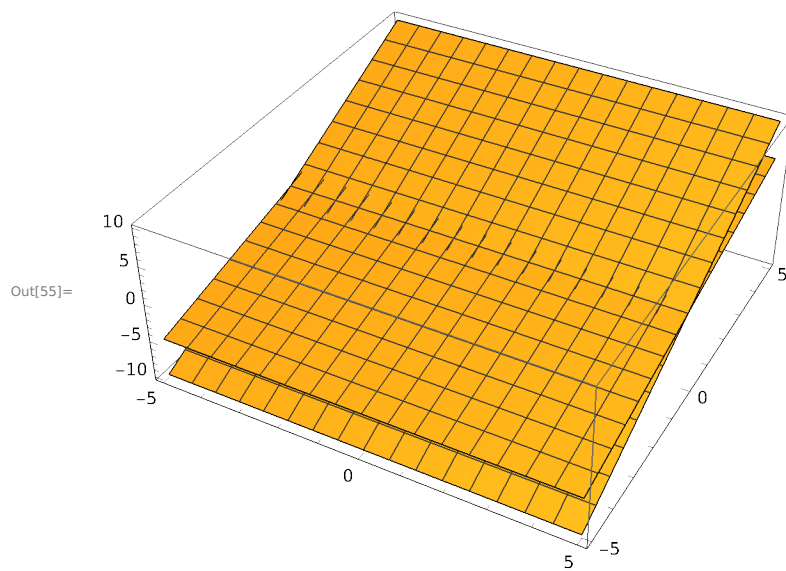
```
In[53]:= H1 = Plot3D[y, {x, -5, 5}, {y, -5, 5}, PlotPoints -> 10]
```



In[54]:= **G1 = Show[F0, F1]**



In[55]:= **G2 = Show[H0, H1]**



In[56]:= **Show[GraphicsArray[{G1, G2}]]**

GraphicsArray : GraphicsArray is obsolete . Switching to GraphicsGrid .

