

## Assignment-based Subjective Questions

**1. From your analysis of the categorical variables from the dataset, what could you infer about their effect on the dependent variable?**

Ans:

- a. Fall and Summer has high median so these seasons have high bike rents . Hence company can more concentrate on Fall and Summer season
- b. Year 2019 has high bike rents compared to 2018
- c. Friday has high median and distribution followed by Saturday so, Business has take necessary action to improve the rents on the other days
- d. Month Aug and Sep has high median value so, these months has high bike rents compared to other months.
- e. Weather is Clear then the count of bike rents are high!!

**2. Why is it important to use drop\_first=True during dummy variable creation?**

Ans:

It helps to reduce the extra column. For N categories N-1 variables are sufficient.

**3. Looking at the pair-plot among the numerical variables, which one has the highest correlation with the target variable?**

Ans:

Tem and Cnt has highest correlation

**4. How did you validate the assumptions of Linear Regression after building the model on the training set?**

Ans:

- a. The  $y_{\text{test}}$  value and  $y$  Predicted value should be Linear
- b. no Multicollinearity between the features
- c. Homoscedasticity :the variance should be constant among all the independent variables
- d. Error should be normally distributed

**5. Based on the final model, which are the top 3 features contributing significantly towards explaining the demand of the shared bikes?**

Ans:

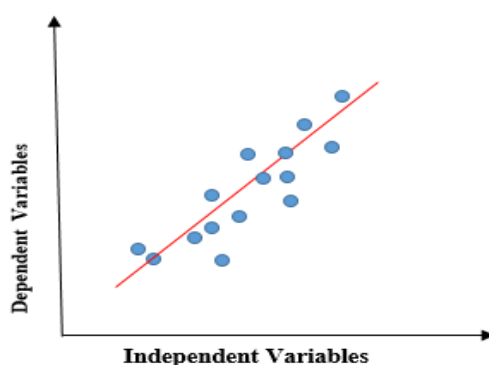
Temperature, Summer and Winter

## General Subjective Questions

**1. Explain the linear regression algorithm in detail.**

Ans:

Linear regression is a quiet and simple statistical regression method used for predictive analysis and shows the relationship between the continuous variables. Linear regression shows the linear relationship between the independent variable (X-axis) and the dependent variable (Y-axis), consequently called linear regression. If there is a single input variable (x), such linear regression is called simple linear regression. And if there is more than one input variable, such linear regression is called multiple linear regression. The linear regression model gives a sloped straight line describing the relationship within the variables.



he above graph presents the linear relationship between the dependent variable and independent variables. When the value of x (independent variable) increases, the value of y (dependent variable) is likewise increasing. The red line is referred to as the best fit straight line. Based on the given data points, we try to plot a line that models the points the best.

To calculate best-fit line linear regression uses a traditional slope-intercept form.

$$Y=mx+c \Rightarrow Y=B_0+B_1X$$

y= Dependent Variable.

x= Independent Variable.

$B_0$ = intercept of the line.

$B_1$  = Linear regression coefficient.

Need of a Linear regression

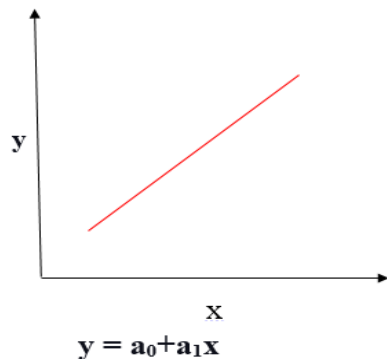
As mentioned above, Linear regression estimates the relationship between a dependent variable and an independent variable. Let's understand this with an easy example:

Let's say we want to estimate the salary of an employee based on year of experience. You have the recent company data, which indicates that the relationship between experience and salary. Here year of experience is an independent variable, and the salary of an employee is a dependent variable, as the salary of an employee is dependent on the experience of an employee. Using this insight, we can predict the future salary of the employee based on current & past information.

A regression line can be a Positive Linear Relationship or a Negative Linear Relationship.

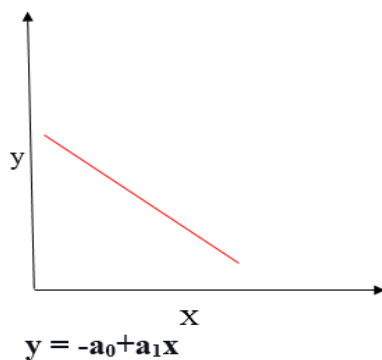
### Positive Linear Relationship

If the dependent variable expands on the Y-axis and the independent variable progress on X-axis, then such a relationship is termed a Positive linear relationship.



### Negative Linear Relationship

If the dependent variable decreases on the Y-axis and the independent variable increases on the X-axis, such a relationship is called a negative linear relationship.



The goal of the linear regression algorithm is to get the best values for  $a_0$  and  $a_1$  to find the best fit line. The best fit line should have the

least error means the error between predicted values and actual values should be minimized.

## **R-squared, R<sup>2</sup> in Linear Regression**

R-squared or R<sup>2</sup> or coefficients of determination is defined as the proportion of variation of data points explained by the regression line or model. It can be determined as a ratio of total variation of data points explained by the regression line (Sum of squared regression) and total variation of data points from the mean (also termed as **sum of squares total or total sum of squares**).

$$R^2 = 1 - \frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

### **2. Explain the Anscombe's quartet in detail.**

Ans:

Anscombe's quartet comprises four datasets that have nearly identical simple statistical properties, yet appear very different when graphed. Each dataset consists of eleven (x,y) points. They were constructed in 1973 by the statistician Francis Anscombe to demonstrate both the importance of graphing data before analyzing it and the effect of outliers on statistical properties.

### **Simple understanding:**

Once Francis John "Frank" Anscombe who was a statistician of great repute found 4 sets of 11 data-points in his dream and requested the council as his last wish to plot those points. Those 4 sets of 11 data-points are given below.

I		II		III		IV	
x	y	x	y	x	y	x	y
10.0	8.04	10.0	9.14	10.0	7.46	8.0	6.58
8.0	6.95	8.0	8.14	8.0	6.77	8.0	5.76
13.0	7.58	13.0	8.74	13.0	12.74	8.0	7.71
9.0	8.81	9.0	8.77	9.0	7.11	8.0	8.84
11.0	8.33	11.0	9.26	11.0	7.81	8.0	8.47
14.0	9.96	14.0	8.10	14.0	8.84	8.0	7.04
6.0	7.24	6.0	6.13	6.0	6.08	8.0	5.25
4.0	4.26	4.0	3.10	4.0	5.39	19.0	12.50
12.0	10.84	12.0	9.13	12.0	8.15	8.0	5.56
7.0	4.82	7.0	7.26	7.0	6.42	8.0	7.91
5.0	5.68	5.0	4.74	5.0	5.73	8.0	6.89

After that, the council analyzed them using only descriptive statistics and found the mean, standard deviation, and correlation between x and y.

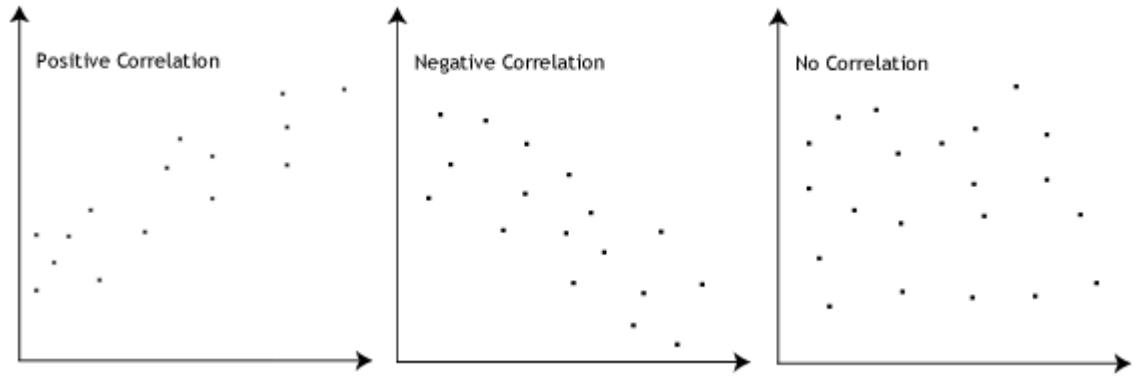
### 3. What is Pearson's R?

Ans:

In statistics, the Pearson correlation coefficient (PCC), also referred to as Pearson's r, the Pearson product-moment correlation coefficient (PPMCC), or the bivariate correlation, is a measure of linear correlation between two sets of data. It is the covariance of two variables, divided by the product of their standard deviations; thus it is essentially a normalised measurement of the covariance, such that the result always has a value between  $-1$  and  $1$ .

The Pearson's correlation coefficient varies between  $-1$  and  $+1$  where:

- $r = 1$  means the data is perfectly linear with a positive slope ( i.e., both variables tend to change in the same direction)
- $r = -1$  means the data is perfectly linear with a negative slope ( i.e., both variables tend to change in different directions)
- $r = 0$  means there is no linear association
- $r > 0 < 5$  means there is a weak association
- $r > 5 < 8$  means there is a moderate association
- $r > 8$  means there is a strong association



## Pearson r Formula

$$r = \frac{\sum (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 \sum (y_i - \bar{y})^2}}$$

Here,

- =correlation coefficient
- =values of the x-variable in a sample
- =mean of the values of the x-variable
- =values of the y-variable in a sample
- =mean of the values of the y-variable

## 4. What is scaling? Why is scaling performed? What is the difference between normalized scaling and standardized scaling?

Ans:

Scaling:

It is a step of data Pre-Processing which is applied to independent variables to normalize the data within a particular range. It also helps in speeding up the calculations in an algorithm.

Why is scaling:

Most of the times, collected data set contains features highly varying in magnitudes, units and range. If scaling is not done then algorithm only takes magnitude in account and not units hence incorrect modelling. To solve this issue, we have to do scaling to bring all the variables to the same level of magnitude.

It is important to note that **scaling just affects the coefficients** and none of the other parameters like **t-statistic**, **F-statistic**, **p-values**, **R-squared**, etc.

### Normalization/Min-Max Scaling:

- It brings all of the data in the range of 0 and 1.
  1. **sklearn.preprocessing.MinMaxScaler** helps to implement normalization in python.

$$\text{MinMax Scaling: } x = \frac{x - \min(x)}{\max(x) - \min(x)}$$

### Standardization Scaling:

- Standardization replaces the values by their Z scores. It brings all of the data into a standard normal distribution which has mean ( $\mu$ ) zero and standard deviation one ( $\sigma$ ).

$$\text{Standardisation: } x = \frac{x - \text{mean}(x)}{\text{sd}(x)}$$

- **sklearn.preprocessing.scale** helps to implement standardization in python.



- One disadvantage of normalization over standardization is that it **loses** some information in the data, especially about **outliers**.

**5. You might have observed that sometimes the value of VIF is infinite. Why does this happen?**

Ans:

If there is perfect correlation, then  $VIF = \infty$ . This shows a perfect correlation between two independent variables. In the case of perfect correlation, we get  $R^2 = 1$ , which leads to  $1/(1-R^2)$  infinity. To solve this problem we need to drop one of the variables from the dataset which is causing this perfect multicollinearity.

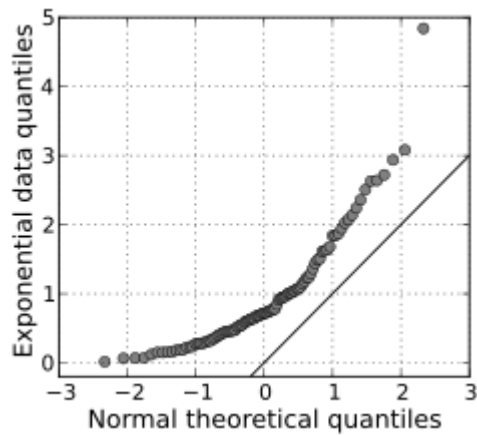
An infinite VIF value indicates that the corresponding variable may be expressed exactly by a linear combination of other variables (which show an infinite VIF as well).

**6. What is a Q-Q plot? Explain the use and importance of a Q-Q plot in linear regression.**

Ans:

Q-Q Plots (Quantile-Quantile plots) are plots of two quantiles against each other. A quantile is a fraction where certain values fall below that quantile. For example, the median is a quantile where 50% of the data fall below that point and 50% lie above it. The purpose of Q-Q plots is to find out if two sets of data come from the same distribution. A 45 degree line is plotted on the Q-Q plot; if the two data sets come from a common distribution, the points will fall on that reference line.

A Q-Q plot showing the 45 degree reference line:



If the two distributions being compared are similar, the points in the Q–Q plot will approximately lie on the line  $y = x$ . If the distributions are linearly related, the points in the Q–Q plot will approximately lie on a line, but not necessarily on the line  $y = x$ . Q–Q plots can also be used as a graphical means of estimating parameters in a location-scale family of distributions.

A Q–Q plot is used to compare the shapes of distributions, providing a graphical view of how properties such as location, scale, and skewness are similar or different in the two distributions.

