Software Engineering

Testing, Part III

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[1]Based on material from Wolfgang Aherndt,..

Overview of this Lecture

This lecture is all about unit testing

Specific topics:

- Recap: JUnit- a framework for rapid unit testing
- **Principles of test set construction**
- **Quality criteria for test sets**

JUnit (Recap.)

- JAVA testing framework to write and run automated tests
- JUnit features include:
  - Assertions for testing expected results
  - Annotations to designate test cases
  - Sharing of common test data
  - Graphical and textual test runners
- JUnit is widely used in industry
- JUnit used from command line or within an IDE (e.g., Eclipse)

Recap: JUnit and Extreme Testing

- Extreme testing
  - Test-cases first: Clear idea of what program should do before coding.
  - Understanding of specification and requirements.
  - Write test-cases first then implementation.

Recap: JUnit and Extreme Testing

- Extreme testing
  - Test-cases first: Clear idea of what program should do before coding.
  - Understanding of specification and requirements.
  - Write test-cases first then implementation.
- Regression testing
  - re-run after changes to code.

Today

Terminology recap

- Specification
- Test case
- Test suite

Today: Principles of test suite construction

How do we pick test cases? When do we know we have enough test cases?

Test Suites

Test Suite

A test suite is a set of test cases.

Most central activity of testing is the creation of test suites

How do we know if we have

- Enough test cases?
- The right test cases?
- Quality of test suites defines quality of overall testing effort

When do we have enough tests

Example

```
public static boolean and(boolean a, boolean b)
```

The output is true if and only if both the inputs are true and false otherwise.

Tests

- and(false,false) == false
- and(false,true) == false
- and(true,false) == false
- and(true,true) == true

When do we have enough tests

Example

```
public static Integer[] sort(Integer[] a) {
        ...
        }
```

- Complete/exhaustive testing is impossible in general.
- When do we have enough tests? (an answer: coverage criteria)
- Coverage criteria: How much of the code is covered by the set of tests?
- Different ways to define covered.

Coverage Criteria

Most metrics used as quality criteria for test suites describe the degree of some kind of coverage.

These metrics are called coverage criteria.

Crucial for testing safety critical software.
Requirements of testing to certain coverage criteria.

Categories of Coverage Criteria

Following the categorisation of [AmmannOffutt] (simplified), we group coverage criteria as follows:

Coverage Criteria Grouping

- Control flow graph coverage
- Logic coverage
- Input space partitioning

Control Flow Graph

Control Flow Graph

Represent implementation under test as graph:

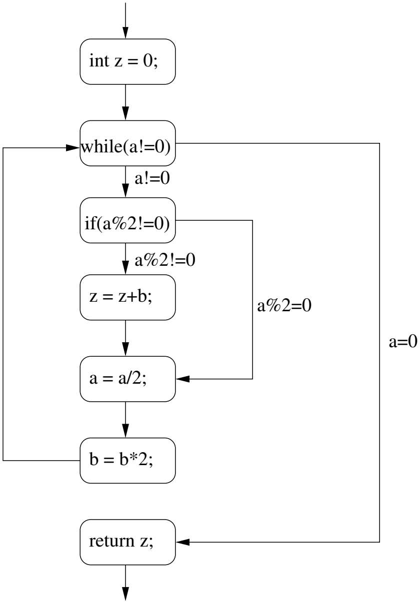
- Every statement represented by a node
- Edges describe control flow between statements
- Edges can be constrained by conditions

Example

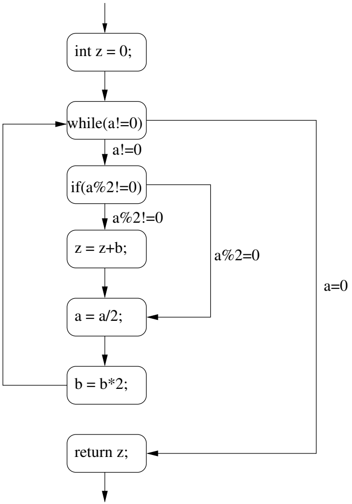
```c
int russianMultiplication(int a, int b){
    int z = 0;
    while(a != 0){
        if(a%2 != 0){
            z = z+b;
        }
        a = a/2;
        b = b*2;
    }
    return z;
}
```

[example and graph by Christian Engel]

Control Flow Graph of `russianMultiplication()`



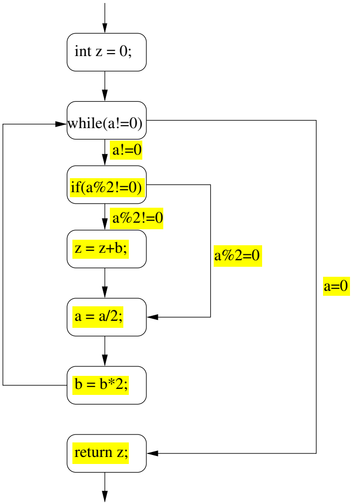
Control Flow Graph Notions



Execution Path

A path through a control flow graph, that starts at the entry point and is either infinite or ends at one of the exit points.

Statement Coverage



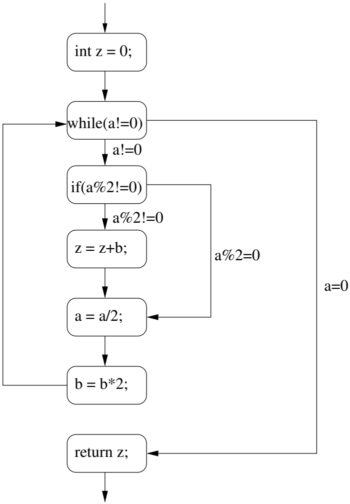
Statement Coverage (SC)

SC is satisfied by a test suite *TS*, iff for every node *n* in the control flow graph there is at least one test in *TS* causing an execution path via *n*.

For `russianMultiplication()`:

- $TS = \{(\mathtt{a} = 1, \mathtt{b} = 0)\}$ satisfies statement coverage

Branch Coverage



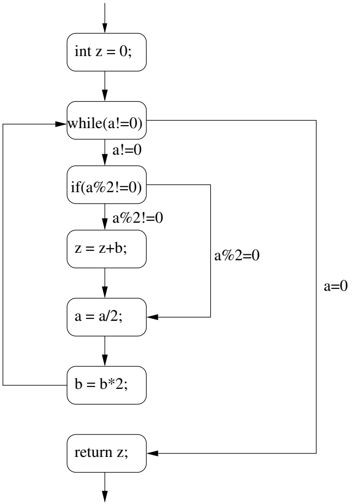
Branch Coverage (BC)

BC is satisfied by a test suite *TS*, iff for every edge *e* in the control flow graph there is at least one test in *TS* causing an execution path via *e*.

For `russianMultiplication()`:

- Does the $TS = \{(\mathtt{a} = 1, \mathtt{b} = 0)\}$ satisfy branch coverage?

Branch Coverage



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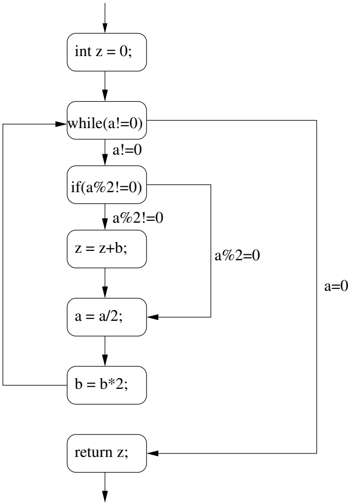
- Does the $TS = \{(\mathtt{a} = 1, \mathtt{b} = 0)\}$ satisfy branch coverage?
- Does the $TS = \{(\mathtt{a} = 2, \mathtt{b} = 0)\}$ satisfy branch coverage?

Branch Coverage



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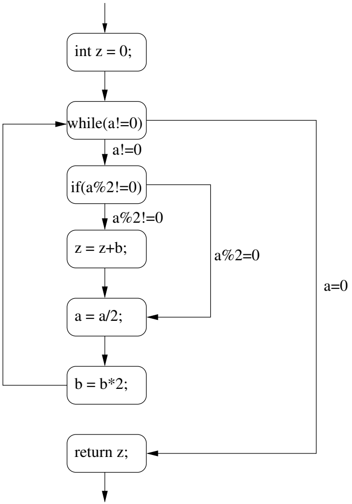
BC subsumes SC

Path Coverage



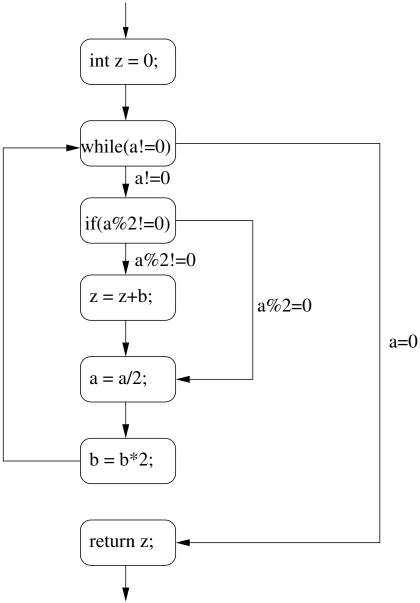
Path Coverage (PC)

PC is satisfied by a test suite *TS*, iff for every execution path *ep* of the control flow graph there is at least one test in *TS* causing *ep*.

- PC cannot be achieved in practice

PC subsumes BC

Mini Quiz: Graph Coverage



Does the following test cases satisfy Statement Coverage, Branch Coverage and/or Path Coverage?

- `[a=3, b=3]`
- `[a=0, b=2]`
- `[a=4, b=1]`

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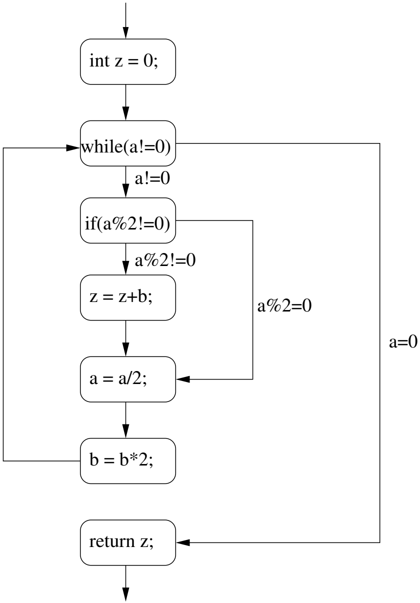

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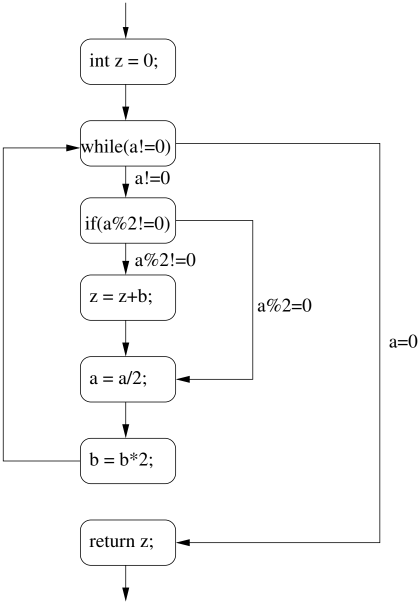

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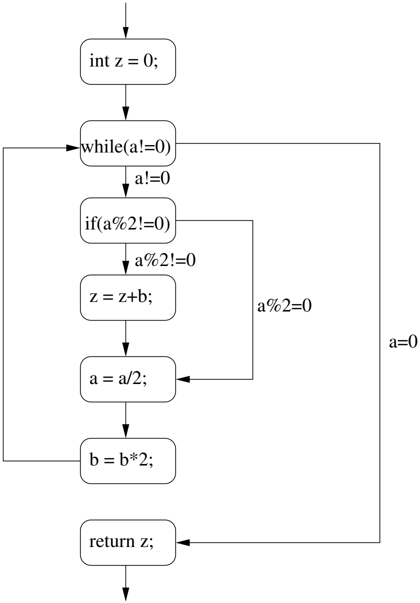

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- `[a=0, b=2]` neither
- `[a=4, b=1]` SC and BC

Logic Coverage

Logical (`boolean`) expressions can come from many sources:

1. Decisions in source code (e.g., `if`, `while`)
2. Decisions in software models (FSMs and statecharts)
3. Case distinctions in requirements

We focus on 1.

Decision Coverage

Let the decisions of a program p, $D(p)$, be the set of all boolean expressions which p branches on.

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Decision Coverage (DC)

For a given decision d, DC is satisfied by a test suite TS if it

- Contains at least two tests
- one where d evaluates to *false*
- one where d evaluates to *true*

For a given program p, DC is satisfied by TS if it satisfies DC for all decisions $d \in D(p)$.

Decision Coverage

Example

For decision $((a < b) \mid\mid D)\ \&\&\ (m \geq n * o))$,
DC is satisfied for instance if TS triggers executions with:

Decision Coverage

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For decision $((a < b) \,||\, D)\ \&\&\ (m \geq n * o))$,
DC is satisfied for instance if TS triggers executions with:

$a = 5, b = 10, D = true, m = 1, n = 1, o = 1$
and
$a = 10, b = 5, D = false, m = 1, n = 1, o = 1$

Decision Coverage

Example

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Inner Value Problem

- the above values are not test case inputs, but values at the time of executing the decision
- finding corresponding input values

Condition Coverage

Let the conditions of a program p, $C(p)$, be the set of all boolean sub-expressions c of decisions in $D(p)$, such that c does not contain other boolean sub-expressions.

Given the decision $((a < b) \mid\mid D)$ && $(m \geq n * o))$,
the conditions are: $(a < b)$, D, and $(m \geq n * o)$.

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- one where c evaluates to *false*
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For a given program p, CC is satisfied by TS if it satisfies CC for all conditions $c \in C(p)$.

Condition Coverage

Example

For *each condition* in $((a < b) \mid\mid D)$ && $(m \geq n * o))$,
CC is satisfied for instance if *TS* triggers executions with:

$a = 5, b = 10, D = true, m = 1, n = 1, o = 1$
and
$a = 10, b = 5, D = false, m = 1, n = 2, o = 2$

Condition Coverage

Example

For *each condition* in $((a < b) \mid\mid D)$ && $(m \geq n * o))$,
CC is satisfied for instance if TS triggers executions with:

$a = 5, b = 10, D = true, m = 1, n = 1, o = 1$
and
$a = 10, b = 5, D = false, m = 1, n = 2, o = 2$

No subsumption

- Consider $p \mid\mid q$, tests $= \{(true, false), (false, true)\}$
- Note that condition coverage does not imply decision coverage or vice versa, above example has no decision coverage.

Modified Condition Decision Coverage, MCDC

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For a given condition c in decision d, MCDC is satisfied by a test suite TS if it

- contains at least two tests,
- one where c evaluates to *false*,
- one where c evaluates to *true*,
- d evaluates differently in both, and
- other conditions in d evaluate identically in both

For a given program p, MCDC is satisfied by TS if it satisfies MCDC for all $c \in C(p)$.

Modified Condition Decision Coverage, MCDC

Example

For condition $a < b$ in decision $((a < b) \,||\, D)$ && $(m \geq n * o))$, MCDC is satisfied for instance if TS triggers executions with:

$a = 5, b = 10,\ D = false, m = 1, n = 1, o = 1$
and
$a = 10, b = 5,\ D = false, m = 8, n = 2, o = 3$

Modified Condition Decision Coverage, MCDC

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Note: To have MCDC for whole decision also need test-cases for conditions D and $(m \geq n * o)$

Modified Condition Decision Coverage, MCDC

MCDC in industrial certification standard

MCDC is required in the avionics certification standard DO-178 as the criterion to test adequately Level A software (failure of which is classified as 'Catastrophic').

Mini Quiz: Logical Coverage

Suppose a program contains the decision `if(x < 1 || y > z)`
Does the following test sets satisfy Decision Coverage, Condition Coverage and/or MCDC?

- `[x=0, y=0, z=1]` and `[x=2, y=2, z=1]` and `[x=2, y=1, z=2]`
- `[x=2, y=2, z=1]` and `[x=2, y=0, z=1]`
- `[x=2, y=2, z=2]`, `[x=0, y=0, z=1]`, `[x=2, y=0, z=0]`, `[x=2, y=2, z=1]`

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  CC, DC, MCDC
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- `[x=2, y=2, z=2]`, `[x=0, y=0, z=1]`, `[x=2, y=0, z=0]`, `[x=2, y=2, z=1]`
  DC, CC, MCDC

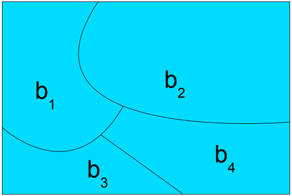
Input Space Partitioning

- Ultimately all testing is about choosing elements from input space
- Input space partitioning takes that view in a more direct way
- Input space partitioned into regions that are assumed to contain 'equally useful values'
- Test cases contain values from each region

Partitioning Domains

A partitioning q of a domain D defines a set of blocks, $B_q = \{b_1, \ldots, b_n\}$, such that:

- the blocks b_i are pairwise disjoint (no overlap)
- together the blocks cover the domain D (complete)



Normally, different partitionings are combined (example later)

Examples

Consider the domain of integer arrays.

Are the following blocks a partitioning?

- $b_1 =$ sorted in ascending order
- $b_2 =$ sorted in descending order
- $b_3 =$ arbitrary order

Examples

Consider the domain of integer arrays.

Are the following blocks a partitioning?

- $b_1 =$ sorted in ascending order
- $b_2 =$ sorted in descending order
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Answer: no!

- The array [1] belongs to all blocks

Combining Partitionings

When creating test cases for `findElement (int[] arr, int elem)`

partitioning q: `arr` is `null` (b_{q1}) or not (b_{q2})

partitioning r: `arr` is empty (b_{r1}) or not (b_{r2})

partitioning s: number of `elem` in `arr` is 0 (b_{s1}), 1 (b_{s2}), or >1 (b_{s3})

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Note:

- r is a sub-partitioning of b_{q2}
- b_{s2} and b_{s3} are sub-blocks of b_{r2}
- b_{s1} overlaps with b_{r1} and b_{q2}
  (fine, as r and s are different partitionings)

Strategies for Identifying Values

After partitioning, one still has to choose values from the blocks.

Strategies

- Include valid, invalid and special values
- Sub-partition some blocks
- Explore boundaries of domains

Example

Example

```java
public static int binarySearch(int[] arr, int
 elem)
```

Specification

requires: arr !=null, arr is sorted ascendingly
ensures: if there exists an element of arr that is equal to elem then arr[result] == elem, otherwise result == -1

- Partition 1: elem in array, elem not in array
  - Sub-partition of not in array: elem < min(array), min(array) <= elem <= max(array), max(array) < elem
  - Sub-partition of in array: left of middle, middle, right of middle

Example (cont.)

- Partition 1: elem in array, elem not in array
  - Sub-partition of not in array: elem $<$ min(array), min(array) $<=$ elem $<=$ max(array), max(array) $<$ elem
  - Sub-partition of in array: left of middle, middle, right of middle

- Not in array:
  - binarySearch($\{1, 3, 5, 8\}, 0$); $<$
  - binarySearch($\{2, 4, 76, 40\}, 3$); in
  - binarySearch($\{34, 64, 75, 100\}, 101$); $>$
- In array:
  - binarySearch($\{0, 2, 4, 6, 44\}, 0$); left border
  - binarySearch($\{4, 5, 34, 55, 66\}, 5$); left/middle
  - binarySearch($\{4, 5, 34, 55, 66\}, 34$); middle
  - binarySearch($\{4, 5, 34, 55, 66\}, 55$); right/middle
  - binarySearch($\{3, 4, 5, 6, 432, 1000\}, 1000$); rightborder

Input Space Partitioning

- Look at specification
- Divide input space into regions with for which the program acts similar
- Take some inputs from regions, especially from borders

Use multiple partitions, subdivide partitions when sensible

This is a guideline, not a formal procedure

Black-box Vs. White-box testing

Black-box testing

Deriving test suites from external descriptions of the software, e.g.

- Specifications
- Requirements / Design
- Input space knowledge

Does not require knowledge of internals (i.e., source code)

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White-box testing

Deriving test suites from the source code internals of the software, e.g.

- Conditions
- Branches in execution
- Statements

Summary

- Control Flow Graph Coverage
  - Statement coverage: every node visited.
  - Branch coverage: every edge traversed.
  - Path coverage: every excecution path (usually too many!)
- Logic Based Coverage
  - Decision coverage: test for each decision true/false.
  - Condition coverage: each sub-expression true/false.
  - MCDC: sub-expression true/false AND affecting decision.
- Input Space Partitioning
  - Input space split into disjoint regions.

Literature related to this Lecture

- Introduction to Software Testing - by Paul Ammann, Jeff Offutt
  - Graph coverage (Chapter 2),
  - Logic coverage (Chapter 3), and
  - Input space partitioning (Chapter 4).