

Min-Max Algorithm

max-player(s)

for a in A_s

$s' \leftarrow \text{Result}(s, a)$

$v(a) \leftarrow \text{min-eval}(s', 2)$

return value = max $v(a)$, action = argmax $v(a)$

min-eval(s,d):

if $d > \text{depth}$; return eval(s)

if s is terminal; return eval(s)

$v \leftarrow +\text{infinity}$

for a in A_s

$s' \leftarrow \text{Result}(s, a)$

$v \leftarrow \min \{ v, \text{max-eval}(s', d+1) \}$

return v

max-eval(s,d):

if $d > \text{depth}$; return eval(s)

if s is terminal; return eval(s)

$v \leftarrow -\text{infinity}$

for a in A_s

$s' \leftarrow \text{Result}(s, a)$

$v \leftarrow \max \{ v, \text{min-eval}(s', d+1) \}$

return v

Alpha Beta Pruning

max-player(s)

alpha = -infinity, **beta** = +infinity

for a in A_s

$s' = \text{Result}(s, a)$

$v(a) \leftarrow \text{min-eval}(s', 2, \mathbf{alpha}, \mathbf{beta})$

alpha $\leftarrow \max \{ \mathbf{alpha}, v(a) \}$

return value = max $v(a)$, action = argmax $v(a)$

min-eval(s,d,alpha,beta):

beta_{local} \leftarrow **beta**

if $d > \text{depth}$; return eval(s)

if s is terminal; return eval(s)

$v \leftarrow +\text{infinity}$

for a in A_s

$s' = \text{Result}(s, a)$

$v \leftarrow \min \{ v, \text{max-eval}(s', d+1, \mathbf{alpha}, \mathbf{beta}_{\text{local}}) \}$

if $v \leq \mathbf{alpha}$; **then return** v

beta_{local} $\leftarrow \min \{ \mathbf{beta}_{\text{local}}, v \}$

return v

max-eval(s,d,alpha,beta):

alpha_{local} \leftarrow **alpha**

if $d > \text{depth}$; return eval(s)

if s is terminal; return eval(s)

$v \leftarrow -\text{infinity}$

for a in A_s

$s' = \text{Result}(s, a)$

$v \leftarrow \max \{ v, \text{min-eval}(s', d+1, \mathbf{alpha}_{\text{local}}, \mathbf{beta}) \}$

if $v \geq \mathbf{beta}$; **then return** v

alpha_{local} $\leftarrow \max \{ \mathbf{alpha}_{\text{local}}, v \}$

return v