**Utility modules** random, math, fractions.

### **RANDOM NUMBERS**

To make an interesting computer game, it's good to introduce some randomness into it. Python comes with a module, called random, that allows us to use random numbers in our programs. At this point, there is only one function, called **randint**, that we will need from the **random module**. To load this function, we use the following statement:

from random import randint

### **Random Number Functions**

Random numbers are used for games, simulations, testing, security, and privacy applications. Python includes the following functions that are commonly used.

Function	Description
choice(seq):	A random item from a list, tuple, or string.
randrange ([start,] stop	A randomly selected element from range(start,vstop,
[,step]):	step).
random():	A random float r, such that 0 is less than or equal to r
	and r is less than 1.
seed([x]):	Sets the integer starting value used in generating
	random numbers. Call this function before calling
	any other random module function. Returns None.
shuffle(lst):	Randomizes the items of a list in place. Returns
	None.
uniform(x, y):	A random float r, such that x is less than or equal to r
	and r is less than y.

The following example shows the usage of the **choice()** method.

```
import random
print ("returns a random number from range(100): ",random.choice(range(100)))
print ("returns random element from list [1, 2, 3, 5, 9]): ", random.choice([1,2, 3, 5, 9]))
print ("returns random character from string 'Hello World': ",
random.choice('Hello World'))
```

When we run the above program, it produces a result similar to the following

```
returns a random number from range(100): 19 returns random element from list [1, 2, 3, 5, 9]): 9 returns random character from string 'Hello World': r
```

```
The following example shows the usage of the randrange() method. import random
# randomly select an odd number between 1-100
print ("randrange(1,100, 2): ", random.randrange(1, 100, 2))
# randomly select a number between 0-99
print ("randrange(100): ", random.randrange(100))
```

When we run the above program, it produces the following result

randrange(1,100, 2): 83 randrange(100): 93

```
The following example shows the usage of the random() method.
import random
# First random number
print ("random(): ", random.random())
# Second random number
print ("random(): ", random.random())

When we run the above program, it produces the following result
random(): 0.281954791393
random(): 0.309090465205
```

```
The following example shows the usage of the seed() method. import random random.seed() print ("random number with default seed", random.random()) random.seed(10) print ("random number with int seed", random.random()) random.seed("hello",2) print ("random number with string seed", random.random())

When we run above program, it produces following result random number with default seed 0.2524977842762465 random number with int seed 0.5714025946899135
```

random number with string seed 0.3537754404730722

```
The following example shows the usage of the shuffle() method. import random list = [20, 16, 10, 5]; random.shuffle(list) print ("Reshuffled list: ", list) random.shuffle(list) print ("Reshuffled list: ", list)

When we run the above program, it produces the following result-

Reshuffled list: [16, 5, 10, 20] reshuffled list: [20, 5, 10, 16]
```

```
The following example shows the usage of the uniform() method. import random print ("Random Float uniform(5, 10): ", random.uniform(5, 10)) print ("Random Float uniform(7, 14): ", random.uniform(7, 14))

Let us run the above program. This will produce the following result-

Random Float uniform(5, 10): 5.52615217015

Random Float uniform(7, 14): 12.5326369199
```

Using randint is simple: randint(a,b) will return a random integer between a and b including both a and b. (Note that randint includes the right endpoint b unlike the range function). Here is a short example:

```
>>> from random import randint
>>> x = randint(1,10)
>>> print('A random number between 1 and 10: ', x)
A random number between 1 and 10: 7
```

The random number will be different every time we run the program.

### **PYTHON'S MATH LIBRARY**

```
The following example shows the usage of the ceil() method.

import math # This will import math module

print ("math.ceil(-45.17): ", math.ceil(-45.17))

print ("math.ceil(100.12): ", math.ceil(100.12))

print ("math.ceil(100.72): ", math.ceil(100.72))

print ("math.ceil(math.pi): ", math.ceil(math.pi))

When we run the above program, it produces the following result

math.ceil(-45.17): -45

math.ceil(100.12): 101

math.ceil(100.72): 101

math.ceil(math.pi): 4
```

```
The following example shows the usage of exp() method.
import math  # This will import math module
print ("math.exp(-45.17): ", math.exp(-45.17))
print ("math.exp(100.12): ", math.exp(100.12))
print ("math.exp(100.72): ", math.exp(100.72))
print ("math.exp(math.pi): ", math.exp(math.pi))

When we run the above program, it produces the following result

math.exp(-45.17): 2.4150062132629406e-20
math.exp(100.12): 3.0308436140742566e+43
math.exp(100.72): 5.522557130248187e+43
math.exp(math.pi): 23.140692632779267
```

# NUMBERS - B

```
The following example shows the usage of the <code>fabs()</code> method.

import math  # This will import math module

print ("math.fabs(-45.17): ", math.fabs(-45.17))

print ("math.fabs(100.12): ", math.fabs(100.12))

print ("math.fabs(100.72): ", math.fabs(100.72))

print ("math.fabs(math.pi): ", math.fabs(math.pi))

When we run the above program, it produces following result

math.fabs(-45.17): 45.17

math.fabs(100): 100.0

math.fabs(100.72): 100.72

math.fabs(math.pi): 3.141592653589793
```

```
The following example shows the usage of the floor() method. import math # This will import math module print ("math.floor(-45.17): ", math.floor(-45.17)) print ("math.floor(100.12): ", math.floor(100.12)) print ("math.floor(100.72): ", math.floor(100.72)) print ("math.floor(math.pi): ", math.floor(math.pi))

When we run the above program, it produces the following result math.floor(-45.17): -46 math.floor(100.12): 100 math.floor(100.72): 100 math.floor(math.pi): 3
```

```
The following example shows the usage of the log() method.
                          # This will import math module
import math
print ("math.log(100.12): ", math.log(100.12))
print ("math.log(100.72): ", math.log(100.72))
print ("math.log(math.pi) : ", math.log(math.pi))
When we run the above program, it produces the following result
math.log(100.12): 4.6063694665635735
math.log(100.72): 4.612344389736092
math.log(math.pi): 1.1447298858494002
The following example shows the usage of the log10() method.
import math
                          # This will import math module
print ("math.log10(100.12): ", math.log10(100.12))
print ("math.log10(100.72): ", math.log10(100.72))
print ("math.log10(119): ", math.log10(119))
print ("math.log10(math.pi) : ", math.log10(math.pi))
```

When we run the above program, it produces the following result

math.log10(100.12): 2.0005208409361854 math.log10(100.72): 2.003115717099806 math.log10(119): 2.0755469613925306 math.log10(math.pi): 0.49714987269413385

```
The following example shows the usage of the pow() method. import math # This will import math module print ("math.pow(100, 2): ", math.pow(100, 2)) print ("math.pow(100, -2): ", math.pow(100, -2)) print ("math.pow(2, 4): ", math.pow(2, 4)) print ("math.pow(3, 0): ", math.pow(3, 0))

When we run the above program, it produces the following result math.pow(100, 2): 10000.0 math.pow(100, -2): 0.0001 math.pow(2, 4): 16.0 math.pow(3, 0): 1.0
```

The following example shows the usage of **sqrt()** method. import math # This will import math module print ("math.sqrt(100): ", math.sqrt(100)) print ("math.sqrt(7): ", math.sqrt(7)) print ("math.sqrt(math.pi): ", math.sqrt(math.pi))

When we run the above program, it produces the following result

math.sqrt(100): 10.0

math.sqrt(7): 2.6457513110645907

math.sqrt(math.pi): 1.7724538509055159

### **TRIGONOMETRY**

```
The following example shows the usage of the acos() method. import math print ("acos(0.64): ", math.acos(0.64)) print ("acos(0): ", math.acos(0)) print ("acos(-1): ", math.acos(-1)) print ("acos(1): ", math.acos(1))

When we run the above program, it produces the following result acos(0.64): 0.876298061168 acos(0): 1.57079632679 acos(-1): 3.14159265359 acos(1): 0.0
```

```
The following example shows the usage of the asin() method. import math print ("asin(0.64): ", math.asin(0.64)) print ("asin(0): ", math.asin(0)) print ("asin(-1): ", math.asin(-1)) print ("asin(1): ", math.asin(1))

When we run the above program, it produces the following result asin(0.64): 0.694498265627 asin(0): 0.0 asin(-1): -1.57079632679 asin(1): 1.5707963267
```

```
The following example shows the usage of the atan() method.
import math
print ("atan(0.64): ", math.atan(0.64))
print ("atan(0) : ", math.atan(0))
print ("atan(10) : ", math.atan(10))
print ("atan(-1) : ", math.atan(-1))
print ("atan(1) : ", math.atan(1))
When we run the above program, it produces the following result
atan(0.64): 0.569313191101
atan(0): 0.0
atan(10): 1.4711276743
atan(-1): -0.785398163397
atan(1): 0.785398163397
The following example shows the usage of atan2() method.
import math
print ("atan2(-0.50,-0.50): ", math.atan2(-0.50,-0.50))
print ("atan2(0.50,0.50): ", math.atan2(0.50,0.50))
print ("atan2(5,5): ", math.atan2(5,5))
print ("atan2(-10,10): ", math.atan2(-10,10))
print ("atan2(10,20): ", math.atan2(10,20))
```

```
When we run the above program, it produces the following result atan2(-0.50,-0.50): -2.35619449019 atan2(0.50,0.50): 0.785398163397 atan2(5,5): 0.785398163397 atan2(-10,10): -0.785398163397 atan2(10,20): 0.463647609001
```

```
The following example shows the usage of cos() method. import math print ("cos(3): ", math.cos(3)) print ("cos(-3): ", math.cos(-3)) print ("cos(0): ", math.cos(0)) print ("cos(math.pi): ", math.cos(math.pi)) print ("cos(2*math.pi): ", math.cos(2*math.pi))

When we run the above program, it produces the following result cos(3): -0.9899924966
cos(-3): -0.9899924966
cos(0): 1.0
cos(math.pi): -1.0
cos(2*math.pi): 1.0
```

```
The following example shows the usage of hypot() method.
import math
print ("hypot(3, 2): ", math.hypot(3, 2))
print ("hypot(-3, 3): ", math.hypot(-3, 3))
print ("hypot(0, 2): ", math.hypot(0, 2))

When we run the above program, it produces the following result

hypot(3, 2): 3.60555127546
hypot(-3, 3): 4.24264068712
hypot(0, 2): 2.0
```

```
The following example shows the usage of sin() method.

import math

print ("sin(3): ", math.sin(3))

print ("sin(-3): ", math.sin(-3))

print ("sin(0): ", math.sin(0))

print ("sin(math.pi): ", math.sin(math.pi))

print ("sin(math.pi/2): ", math.sin(math.pi/2))

When we run the above program, it produces the following result

sin(3): 0.14112000806

sin(-3): -0.14112000806

sin(0): 0.0

sin(math.pi): 1.22460635382e-16

sin(math.pi/2): 1
```

```
The following example shows the usage of degrees() method. import math print ("degrees(3): ", math.degrees(3)) print ("degrees(-3): ", math.degrees(-3)) print ("degrees(0): ", math.degrees(0)) print ("degrees(math.pi): ", math.degrees(math.pi)) print ("degrees(math.pi/2): ", math.degrees(math.pi/2)) print ("degrees(math.pi/4): ", math.degrees(math.pi/4))

When we run the above program, it produces the following result degrees(3): 171.88733853924697 degrees(-3): -171.88733853924697 degrees(0): 0.0 degrees(math.pi): 180.0 degrees(math.pi/2): 90.0 degrees(math.pi/4): 45.0
```

```
The following example shows the usage of radians() method. import math print ("radians(3): ", math.radians(3)) print ("radians(-3): ", math.radians(-3)) print ("radians(0): ", math.radians(0)) print ("radians(math.pi): ", math.radians(math.pi)) print ("radians(math.pi/2): ", math.radians(math.pi/2)) print ("radians(math.pi/4): ", math.radians(math.pi/4))

When we run the above program, it produces the following result radians(3): 0.0523598775598 radians(-3): -0.0523598775598 radians(0): 0.0 radians(math.pi): 0.0548311355616 radians(math.pi/2): 0.0274155677808 radians(math.pi/4): 0.0137077838904
```

## **MATHEMATICAL CONSTANTS**

The module also defines two mathematical constants-

pi The mathematical constant pi. e The mathematical constant e.

#### **FRACTIONS**

```
>>> import fractions

>>> x = fractions.Fraction(1, 3)

>>> x

Fraction(1, 3)

>>> x * 2

Fraction(2, 3)

>>> fractions.Fraction(6, 4)

Fraction(3, 2)
```

- 1. To start using fractions, import the fractions module.
- 2. To define a fraction, create a Fraction object and pass in the numerator and denominator.
- 3. You can perform all the usual mathematical operations with fractions. Operations return a new Fraction

```
object. 2 * (1/3) = (2/3)
```

- 4. The Fraction object will automatically reduce fractions. (6/4) = (3/2)
- 5. Python has the good sense not to create a fraction with a zero denominator.

```
>>> from fractions import Fraction
>>> print(Fraction(11, 35))
11/35
>>> print(Fraction(10, 18))
5/9
>>> print(Fraction())
>>> print(Fraction(1.13))
1272266894732165/1125899906842624
>>> print(Fraction('1.13'))
113/100
>>> print(Fraction(18, 5) * Fraction(16, 19))
288/95
>>>
>>>import math
>>> print(math.sqrt(Fraction(28,3)))
3.0550504633038935
>>> print(Fraction(math.sin(math.pi/3)))
3900231685776981/4503599627370496
>>>
```