

# Problem L. Array Elimination

**Time limit** 2000 ms

**Mem limit** 524288 kB

You are given array  $a_1, a_2, \dots, a_n$ , consisting of non-negative integers.

Let's define operation of "elimination" with integer parameter  $k$  ( $1 \leq k \leq n$ ) as follows:

- Choose  $k$  distinct array indices  $1 \leq i_1 < i_2 < \dots < i_k \leq n$ .
- Calculate  $x = a_{i_1} \& a_{i_2} \& \dots \& a_{i_k}$ , where  $\&$  denotes the [bitwise AND operation](#) (notes section contains formal definition).
- Subtract  $x$  from each of  $a_{i_1}, a_{i_2}, \dots, a_{i_k}$ ; all other elements remain untouched.

Find all possible values of  $k$ , such that it's possible to make all elements of array  $a$  equal to 0 using a finite number of elimination operations with parameter  $k$ . It can be proven that exists at least one possible  $k$  for any array  $a$ .

Note that you **firstly choose  $k$**  and **only after that perform elimination operations with value  $k$**  you've chosen initially.

## Input

Each test contains multiple test cases. The first line contains the number of test cases  $t$  ( $1 \leq t \leq 10^4$ ). Description of the test cases follows.

The first line of each test case contains one integer  $n$  ( $1 \leq n \leq 200\,000$ ) — the length of array  $a$ .

The second line of each test case contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i < 2^{30}$ ) — array  $a$  itself.

It's guaranteed that the sum of  $n$  over all test cases doesn't exceed 200 000.

## Output

For each test case, print all values  $k$ , such that it's possible to make all elements of  $a$  equal to 0 in a finite number of elimination operations with the given parameter  $k$ .

**Print them in increasing order.**

## Sample 1

| Input       | Output    |
|-------------|-----------|
| 5           | 1 2 4     |
| 4           | 1 2       |
| 4 4 4 4     | 1         |
| 4           | 1         |
| 13 7 25 19  | 1 2 3 4 5 |
| 6           |           |
| 3 5 3 1 7 1 |           |
| 1           |           |
| 1           |           |
| 5           |           |
| 0 0 0 0 0   |           |

**Note**

In the first test case:

- If  $k = 1$ , we can make four elimination operations with sets of indices  $\{1\}$ ,  $\{2\}$ ,  $\{3\}$ ,  $\{4\}$ . Since  $\&$  of one element is equal to the element itself, then for each operation  $x = a_i$ , so  $a_i - x = a_i - a_i = 0$ .
- If  $k = 2$ , we can make two elimination operations with, for example, sets of indices  $\{1, 3\}$  and  $\{2, 4\}$ :  $x = a_1 \& a_3 = a_2 \& a_4 = 4 \& 4 = 4$ . For both operations  $x = 4$ , so after the first operation  $a_1 - x = 0$  and  $a_3 - x = 0$ , and after the second operation —  $a_2 - x = 0$  and  $a_4 - x = 0$ .
- If  $k = 3$ , it's impossible to make all  $a_i$  equal to 0. After performing the first operation, we'll get three elements equal to 0 and one equal to 4. After that, all elimination operations won't change anything, since at least one chosen element will always be equal to 0.
- If  $k = 4$ , we can make one operation with set  $\{1, 2, 3, 4\}$ , because  $x = a_1 \& a_2 \& a_3 \& a_4 = 4$ .

In the second test case, if  $k = 2$  then we can make the following elimination operations:

- Operation with indices  $\{1, 3\}$ :  $x = a_1 \& a_3 = 13 \& 25 = 9$ .  $a_1 - x = 13 - 9 = 4$  and  $a_3 - x = 25 - 9 = 16$ . Array  $a$  will become equal to  $[4, 7, 16, 19]$ .
- Operation with indices  $\{3, 4\}$ :  $x = a_3 \& a_4 = 16 \& 19 = 16$ .  $a_3 - x = 16 - 16 = 0$  and  $a_4 - x = 19 - 16 = 3$ . Array  $a$  will become equal to  $[4, 7, 0, 3]$ .
- Operation with indices  $\{2, 4\}$ :  $x = a_2 \& a_4 = 7 \& 3 = 3$ .  $a_2 - x = 7 - 3 = 4$  and  $a_4 - x = 3 - 3 = 0$ . Array  $a$  will become equal to  $[4, 4, 0, 0]$ .
- Operation with indices  $\{1, 2\}$ :  $x = a_1 \& a_2 = 4 \& 4 = 4$ .  $a_1 - x = 4 - 4 = 0$  and  $a_2 - x = 4 - 4 = 0$ . Array  $a$  will become equal to  $[0, 0, 0, 0]$ .

**Formal definition of bitwise AND:**

Let's define bitwise AND ( $\&$ ) as follows. Suppose we have two non-negative integers  $x$  and  $y$ , let's look at their binary representations (possibly, with leading zeroes):  $x_k \dots x_2 x_1 x_0$  and

$y_k \dots y_2 y_1 y_0$ . Here,  $x_i$  is the  $i$ -th bit of number  $x$ , and  $y_i$  is the  $i$ -th bit of number  $y$ . Let  $r = x \& y$  is a result of operation  $\&$  on number  $x$  and  $y$ . Then binary representation of  $r$  will be  $r_k \dots r_2 r_1 r_0$ , where:

$$r_i = \begin{cases} 1, & \text{if } x_i = 1 \text{ and } y_i = 1 \\ 0, & \text{if } x_i = 0 \text{ or } y_i = 0 \end{cases}$$