

Convert the following sentences into predicate and clausal normal form.

1. Every child loves Santa
2. Everyone who loves Santa loves any reindeer.
3. Rudolph is a reindeer, and Rudolph has a red nose.
4. Anything which has a red nose is weird or is a clown.
5. No reindeer is a clown.
6. Scrooge does not love anything which is weird.

1. Every child loves Santa.
 $\forall x (CHILD(x) \rightarrow LOVES(x, Santa))$
2. Everyone who loves Santa loves any reindeer.
 $\forall x, \forall y (LOVES(x, Santa) \wedge REINDEER(y) \rightarrow LOVES(x, y))$
3. Rudolph is a reindeer, and Rudolph has a red nose.
 $REINDEER(Rudolph) \wedge REDNOSE(Rudolph)$
4. Anything which has a red nose is weird or is a clown.
 $\forall x (REDNOSE(x) \rightarrow WEIRD(x) \vee CLOWN(x))$
5. No reindeer is a clown.
 $\neg \exists x (REINDEER(x) \wedge CLOWN(x))$
6. Scrooge does not love anything which is weird.
 $\forall x (WEIRD(x) \rightarrow \neg LOVES(Scrooge, x))$
7. (Conclusion) Scrooge is not a child.
 $\neg CHILD(Scrooge)$

1. Anyone whom Mary loves is a football star.
2. Any student who does not pass does not play.
3. John is a student.
4. Any student who does not study does not pass.
5. Anyone who does not play is not a football star.
6. (Conclusion) If John does not study, then Mary does not love John

1. Anyone whom Mary loves is a football star.
 $\forall x (LOVES(Mary, x) \rightarrow STAR(x))$
2. Any student who does not pass does not play.
 $\forall x (STUDENT(x) \wedge \neg PASS(x) \rightarrow \neg PLAY(x))$
3. John is a student.
 $STUDENT(John)$
4. Any student who does not study does not pass.
 $\forall x (STUDENT(x) \wedge \neg STUDY(x) \rightarrow \neg PASS(x))$
5. Anyone who does not play is not a football star.
 $\forall x (\neg PLAY(x) \rightarrow \neg STAR(x))$
6. (Conclusion) If John does not study, then Mary does not love John.
 $\neg STUDY(John) \rightarrow \neg LOVES(Mary, John)$

1. Anyone who rides a Harley is a rough character.
 2. Every biker rides either Harley or bmw.
 3. Anyone who rides a bmw is a yuppie.
 4. Every yuppie is a lawyer.
 5. Any nice girl does not date anyone who is a rough character.
 6. Mary is a nice girl and John is a biker.
 7. (Conclusion) If john is not a lawyer then mary doesnot date john.
- Prove the sentence using resolution.

1. $\forall x: \text{rides}(x, \text{Harley}) \rightarrow \text{roughcharacter}(x)$
2. $\forall x: \text{biker}(x) \rightarrow \text{rides}(x, \text{Harley}) \vee \text{rides}(x, \text{bmw})$
3. $\forall x: \text{rides}(x, \text{bmw}) \rightarrow \text{yuppie}(x)$
4. $\forall x: \text{yuppie}(x) \rightarrow \text{lawyer}(x)$
5. $\forall x: \forall y: \text{nicegirl}(x) \wedge \text{roughcharacter}(y) \rightarrow \sim \text{date}(x, y)$
6. $\text{Nicegirl}(\text{mary}) \wedge \text{biker}(\text{john})$