ARRAYS

- > Linear arrays: Memory representation
- Traversal
- Insertion
- Deletion
- Linear Search
- Binary Search
- Merging
- 2D Array : Memory representation

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2.1 Introduction

- Data Structure can be classified as:
 - ✓ linear
 - ✓ non-linear
- Linear (elements arranged in sequential in memory location) i.e. array & linear link-list
- Non-linear such as a tree and graph.
- Operations:
 - ✓ Traversing, Searching, Inserting, Deleting, Sorting, Merging
- Array is used to store a fix size for data and a link-list the data can be varies in size.

2.1 Introduction

- Advantages of an Array:
 - Very simple
 - Economy if full use of memory
 - Random accessed at the same time
- Disadvantage of an Array:
 - wasting memory if not fully used
 - Stores same data types' elements

2.2 Linear Array

- Homogeneous data:
 - a) Elements are represented through indexes.
 - b) Elements are saved in sequential in memory locations.
- Number of elements, N -> length or size of an array.

If:

UB: upper bound (the largest index)

LB: lower bound (the smallest index)

Then: N = UB - LB + 1Length = N = UB when LB = 1

2.2 Linear Array

 All elements in A are written symbolically as, 1 .. n is the subscript.

A1, A2, A3,, An

- In FORTRAN and BASIC \rightarrow A(1), A(2), ..., A(N)
- In Pascal, C/C++ and Java \rightarrow A[0], A[1], ..., A[N-1]
- subscript starts from 0

$$LB = 0, UB = N-1$$

2.2.1 Representation of Array in a Memory

• The process to determine the address in a memory:

X[1]

a) First address – base address.

X[0]

b) Relative address to base address through index function.

```
Example: char X[100];
Let char uses 1 location storage.

If the base address is 1200 then the next element is in 1201.

Index Function is written as:

Loc (X[i]) = Loc(X[0]) + i

, i is subscript and LB = 0
```

X[2]

2.2.1 Representation of Array in a Memory

In general, index function:

$$Loc (X[i]) = Loc(X[LB]) + w*(i-LB);$$

where w is length of memory location required. For real number: 4 byte, integer: 2 byte and character: 1 byte.

Example:

If LB = 5, Loc(X[LB]) = 1200, and w = 4, find Loc(X[8]) ?
Loc(X[8])= Loc(X[5]) +
$$4*(8-5)$$

= 1212

2.2.2 Traversing Algorithm (While loop)

Traversing operation means visit every element once, whether processed or not.

Traversal(LA,N): This is an algorithm to traverse N elements of an array LA..

- 1. [Assign counter]Set K:=0.
- 2. Repeat step 2.1 and 2.2 while $K \leq UB$
 - 2.1 [visit element] do PROCESS on LA[K].
 - 2.2 [add counter]

Set K:=K+1

[end of while loop]

4. exit.

2.2.2 Traversing Algorithm (for loop)

Traversal(LA,N): This is an algorithm to traverse N elements of an array LA.

- 1.Repeat step 2 for K = 0 to N-1
- 2. [visit element]do PROCESS on LA[K].[end of for loop]
- 3. exit.

2.2.3 Insertion Algorithm

Insert item at the back is easy if there is a space. Insert item in the middle requires the movement of all elements to the right as in Figure 1.

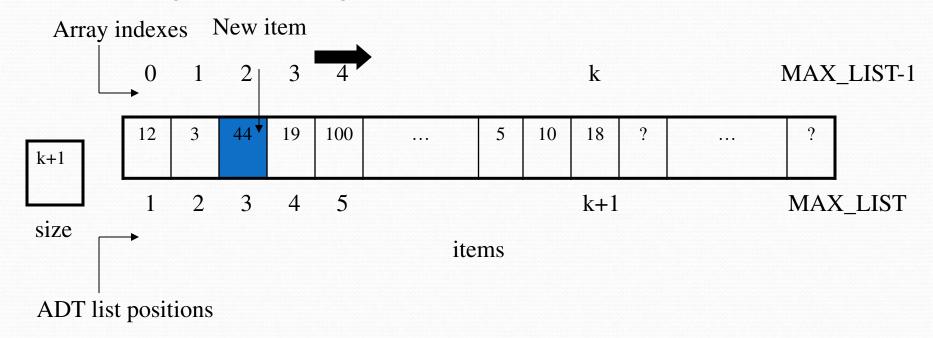


Figure 1: Shifting items for insertion at position 3

2.2.3 Insertion Algorithm(while loop)

Insertion is to insert some element in the array at user defined location

```
INSERT(LA, N, K, ITEM):LA is a linear array with N element, K is integer positive where K < N and LB = 0,Insert an element, ITEM in index K.
```

- 1. [Assign counter], Set J := N-1; [LB = 0]
- 2. Repeat step 2.1 and 2.2 while $J \ge K$
 - 2.1 [shift to the right all elements from J] Set LA[J+1] := LA[J]
- 2.2 [decrement counter] Set J := J 1 [End of while loop]
- 4. [Insert element] Set LA[K] := ITEM
- 5. [Reset N] Set N := N + 1
- 6. Exit

2.2.3 Insertion Algorithm(for loop)

- INSERT(LA, N, K, ITEM):LA is a linear array with N element, K is integer positive where K < N and LB = 0,Insert an element, ITEM in index K.
- 1. Read: K and ITEM [index to perform insertion and value to be inserted] (optional step as mentioned in the declaration)
- 2. Repeat step for j=N-1 to K
- 3. [shift to the right all elements from J]
- Set LA[J+1] := LA[J]

[end of for loop]

- 4. [Insert element] Set LA[K] := ITEM
- 5. [Reset N] Set N := N + 1
- 6. Exit

2.2.4 Deletion Algorithm

Delete item.

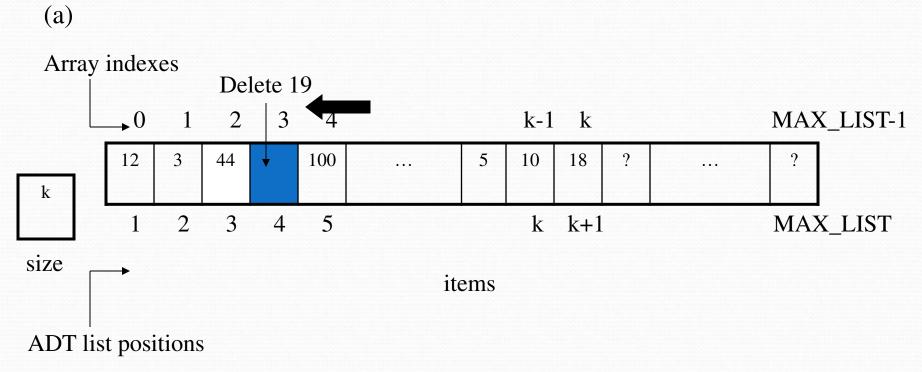


Figure 2: Deletion causes a gap

2.2.4 Deletion Algorithm

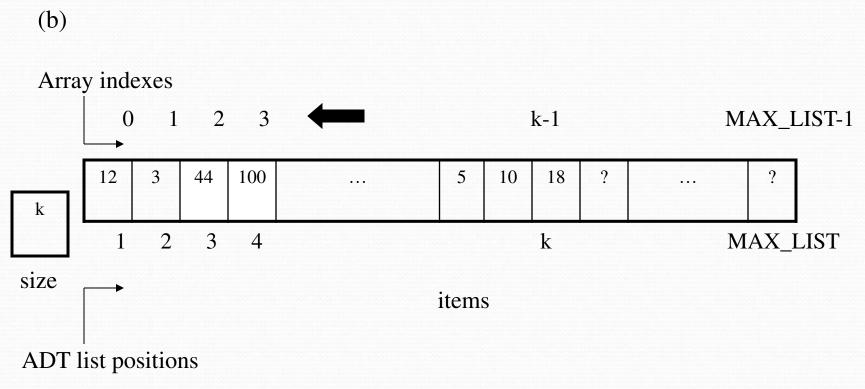


Figure 3: Fill gap by shifting

2.2.4 Deletion Algorithm(for loop)

- DELETE(LA, N, K, ITEM):In an array LA this
- Algo will delete the element ITEM at location
- K.Where LA has N elements.
- 1. Read: K. [index element you want to delete]
- 2. Set ITEM:=LA[K]. [storing value before deleting]
- 3. Repeat step 3.1 for I = K to N-2 [If LB = 0]
- 3.1 [Shift element, forward]
- Set LA[I] := LA[I+1]
- [end of for loop]
- 4. [Reset N in LA]
- Set N := N 1
- 5. Exit

2.2.4 Deletion Algorithm(while loop)

- DELETE(LA, N, K, ITEM):In an array LA this Algorithm will delete the element ITEM at location K. Where LA has N elements.
- 1. Read: K. [index element you want to delete]
- 2. Set ITEM:=LA[K] and Set I:=K. [storing value before deleting]
- 3. Repeat step 3.1 while I < N-1 [If LB = 0]
- 3.1 [Shift element, forward]
- Set LA[I] := LA[I+1] Set I:=I+1
- [end of while loop]
- 4. [Reset N in LA]
- Set N := N 1
- 5. Exit

2.2.5 Sequential Search (while

loop)

Compare successive elements of a given list with a search ITEM until

- 1. either a match is encountered
- 2. or the list is exhausted without a match.



SequentialSearch(**LA**, **N**, **ITEM**, **LOC**): Algorithm to search element ITEM in an array LA having N elements and storing its location in LOC

- 1. Set I := 0
- 2. Repeat step 2.1 while i<N && LA[I] != ITEM 2.1 Set I:=I+1
- 3. If LA[I]=ITEM, then:

write: found at LOC=I

else:

write: not found.

4. Exit

search/sequential search (for loop)

other argument to do inicar

SequentialSearch(**LA**, **N**, **ITEM**, **LOC**, **TEMP**): Algorithm to search element ITEM in an array LA having N elements and storing its location in LOC. Where TEMP ia a flag variable.

```
1. Set TEMP :=0
```

```
2. Repeat step 2.1 for I=0 to N-1
2.1 if LB[I]=ITEM,then:
set TEMP:=1 and LOC:=I
and EXIT for loop
```

```
3. If Temp=1,then:
write:found at LOC
else:
write:not found.
```

4. Exit

- Binary search algorithm is efficient if the array is sorted.
- A binary search is used whenever the list starts to become large.
- Consider to use binary searches whenever the list contains more than 16 elements.
- The binary search starts by testing the data in the element at the middle of the array to determine if the target is in the first or second half of the list.
- If it is in the first half, we do not need to check the second half. If it is in the second half, we do not need to test the first half. In other words we eliminate half the list from further consideration. We repeat this process until we find the target or determine that it is not in the list.

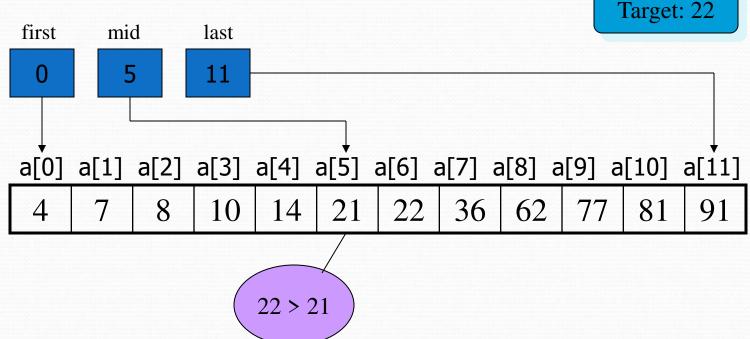
- To find the middle of the list, we need three variables, one to identify the beginning of the list, one to identify the middle of the list, and one to identify the end of the list.
- We analyze two cases here: the target is in the list (target found) and the target is not in the list (target not found).

• **Target found case**: Assume we want to find 22 in a sorted list as follows:

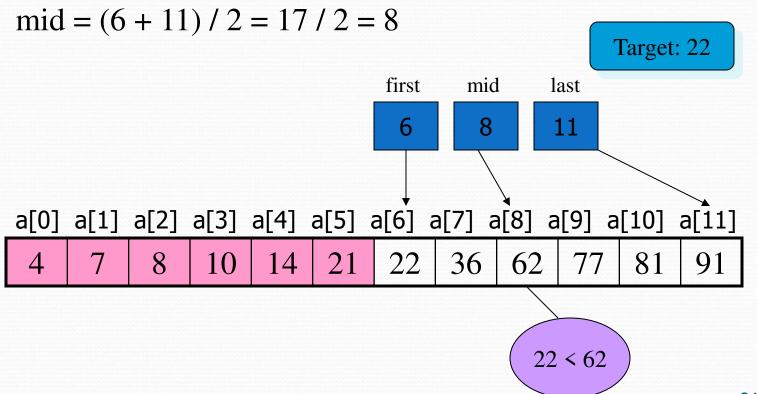
• The three indexes are first, mid and last. Given first as 0 and last as 11, mid is calculated as follows:

mid = (first + last) / 2
mid =
$$(0 + 11) / 2 = 11 / 2 = 5$$

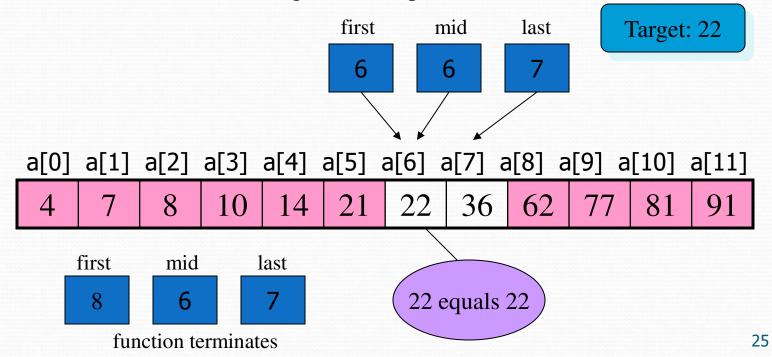
• At index location 5, the target is greater than the list value (22 > 21). Therefore, eliminate the array locations 0 through 5 (mid is automatically eliminated). To narrow our search, we assign mid + 1 to first and repeat the search.



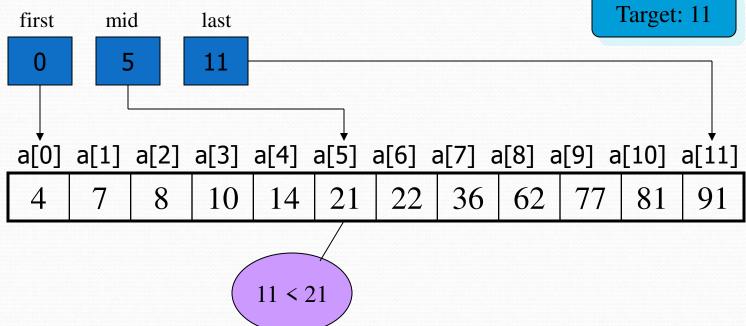
• The next loop calculates mid with the new value for first and determines that the midpoint is now 8 as follows:



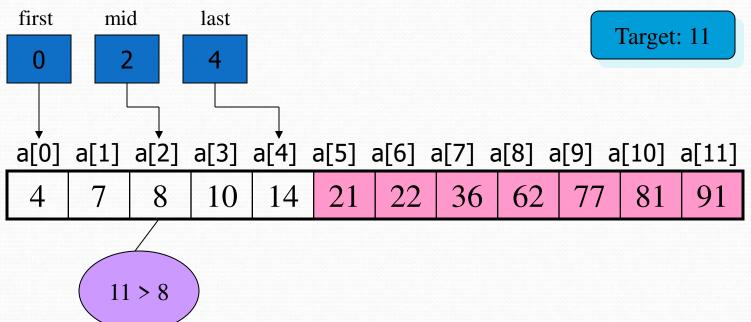
• When we test the target to the value at mid a second time, we discover that the target is less than the list value (22 < 62). This time we adjust the end of the list by setting last to mid − 1 and recalculate mid. This step effectively eliminates elements 8 through 11 from consideration. We have now arrived at index location 6, whose value matches our target. This stops the search.



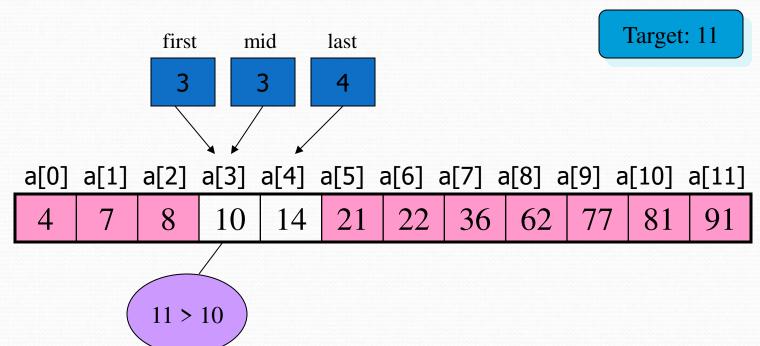
• Target not found case: This is done by testing for first and last crossing: that is, we are done when first becomes greater than last. Two conditions terminate the binary search algorithm when (a) the target is found or (b) first becomes larger than last. Assume we want to find 11 in our binary search array.



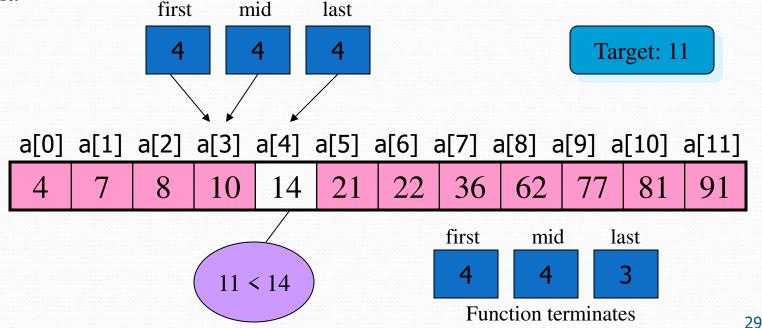
• The loop continues to narrow the range as we saw in the successful search until we are examining the data at index locations 3 and 4.



These settings of first and last set the mid index to 3 as follows: mid = (3 + 4) / 2 = 7 / 2 = 3



- The test at index 3indicates that the target is greater than the list value, so we set first to mid + 1, or 4. We now test the data at location 4 and discover that 11 < 14. The mid is as calculated as follows:
- At this point, we have discovered that the target should be between two adjacent values; in other words, it is not in the list. We see this algorithmically because last is set to mid 1, which makes first greater than last, the signal that the value we are looking for is not in the list.



Example algorithm:

DATA – sorted array

ITEM – Info

LB – lower bound

UB – upper bound

BEG-start Location

MID – middle Location

END – last Location

BINARY SEARCH(DATA,END,ITEM,MID,BEG,N,LOC):binary search is applied on array DATA having N elements. Where BEG represents lower bound LB ,END represents upper bound UB and MID represents middle index of the array.

1. [Define variables]

```
Set BEG := LB, END:= UB
Set MID: = (BEG+END)/2
```

- 2. Repeat steps 3 and 4 While BEG <= END && DATA[MID] != ITEM
- 3. If ITEM < DATA[MID], then:

$$END = MID-1$$

else:

BEG:=MID+1

- 4. Set MID := (BEG+ END)/2 [end of while loop]
- 5. If DATA[MID] = ITEM, then:

Set LOC:=MID.

write :element found at MID

else:

write:not found.

6. Exit

Another way to do binary search algorithm

- BINARYSEARCH(DATA,END,ITEM,MID,BEG,N, LOC):binary search is applied on array DATA having N elements. Where BEG represents lower bound LB, End represents upper bound UB and MID represents middle index of the array.
- 1. [Define variables]
- Set BEG := LB, LAST:= UB
- Set MID: = (BEG+END)/2
- 2. Repeat steps 3 and 4 While BEG <= END

- 3. If ITEM < DATA[MID], then:
- END = MID-1
- else if ITEM=DATA[MID],then:
- write: Element found at MID and EXIT from while loop
- else:
- BEG:=MID+1.
- 4. Set MID := (BEG+ END)/2
- [end of while loop]
- 5. Exit

• Suppose A is a sorted list with r elements and B is a sorted list with s elements. The operation that combines the element of A and B into a single sorted list C with n=r + s elements is called merging.

Algorithm: Merging (A, R,B,S,C,N)

Here A and B be sorted arrays with R and S elements respectively. This algorithm merges A and B into an array C with N=R+ S elements
Step 1: Set NA:=0, NB:=0 and NC:=0
Step 2: Repeat while NA < R and NB < S:

if A[NA] ≤ B[NB], then:

Set C[NC] := A[NA]

Set NA := NA + 1

else

Set C[NC] := B[NB]

Set NB := NB + 1

[End of if-else structure]

Set NC:= NC +1

[End of while Loop]

```
• Step 3: If NA >R, then:
                Repeat while NB < S:
                 Set C[NC]: = B[NB]
                 Set NB := NB+1
                 Set NC := NC +1
                 [End ofwhile Loop]
         else
                Repeat while NA < R:
                Set C[NC] := A[NA]
                Set NC := NC + 1
                Set NA := NA + 1
                [End of while loop]
          [End of if-else structure]
Step 4: Exit
```

• Complexity of merging: The input consists of the total number n=r+s elements in A and B. Each comparison assigns an element to the array C, which eventually has n elements. Accordingly, the number f(n) of comparisons cannot exceed n:

$$f(n) \le n = O(n)$$

Exercises

- Find where the indicated elements of an array a are stored, if the base address of a is 200* and LB = 0
 - a) double a[10]; a[3]?
 - b) int a[26]; a[2]?

^{*(}assume that int(s) are stored in 4 bytes and double(s) in 8 bytes).

2.3 MULTIDIMENSIONAL ARRAY

Two or more subscripts.

2-D ARRAY

- A 2-D array, A with *m X n* elements.
- In math application it is called *matrix*.
- In business application table.
- Example:

Assume 25 students had taken 4 tests.

The marks are stored in 25 X 4 array locations:

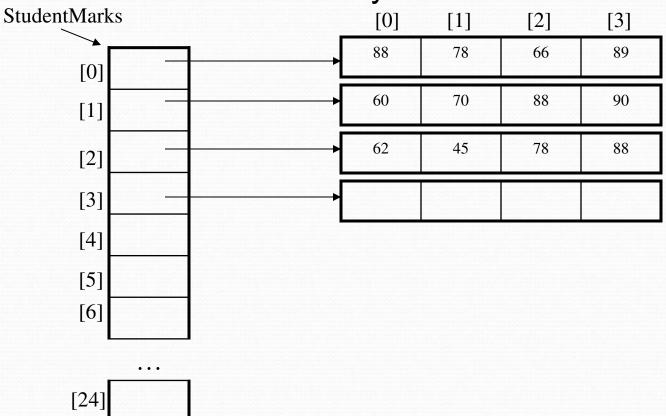
	U0	U1	U2	U3	
Stud 0	88	78	66	89	
Stud 1	60	70	88	90	
Stud 2	62	45	78	88	
					— m
Stud 24	78	88	98	67	

2-D ARRAY

Multidimensional array declaration in C++:int StudentMarks [25][4];
StudentMarks[0][0] = 88;
StudentMarks[0][1] = 78;....
OR
int StudentMarks [25][4] = {{88, 78, 66, 89},
{60, 70, 88, 90},...}

2.3.1 2-D ARRAY

In C++ the 2-D array is visualized as follows:



2.3.2 Representation of2D arrays in Memory

Column Major Order:

$$LOC(A[j, k]) = Base(A) + w[m*k + j]$$

Row Major order:

$$LOC(A[j, k]) = Base(A) + w[n*j + k]$$

Given: A 2-D array, A with m X n elements.

Thank You