

### How to Evaluate Prefix and Postfix expressions

- Prefix expression is evaluated by working from right to left. When an operator is encountered, we perform the corresponding operation with the two operands immediately to the right of this operand.

Q18. What is the value of these prefix expressions?

(i)

$$\begin{aligned} & \uparrow - * 3 3 * 4 2 5 \\ & \uparrow - * 3 3 8 5 \\ & \uparrow - 9 8 5 = \uparrow 15 = 1 \end{aligned}$$

(ii)

$$\begin{aligned} & + - \uparrow 3 2 \uparrow 2 3 / 6 - 4 2 \\ & + - \uparrow 3 2 \uparrow 2 3 / 6 2 \\ & + - \uparrow 3 2 \uparrow 2 3 3 \\ & + - \uparrow 3 2 8 3 = + - 9 8 3 \\ & = + 13 = 4 \end{aligned}$$

- Postfix expression is evaluated by working from left to right. When an operator is encountered, we perform the corresponding operation with the two operands immediately to the left of this operand.

Q18. What is the value of these postfix expressions?

(i)

$$5 2 1 - - 3 1 4 + + *$$

$$\begin{aligned}
 & \rightarrow 51 - 314 + + x = 4314 + + x \\
 & = 435 + x \\
 & = 48x = 32
 \end{aligned}$$

(ii)

$$32 * 2 \uparrow 53 - 84 / * -$$

$$62 \uparrow 53 - 84 / * -$$

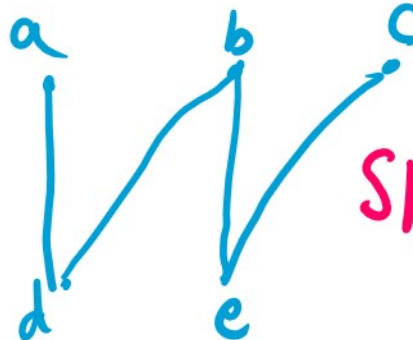
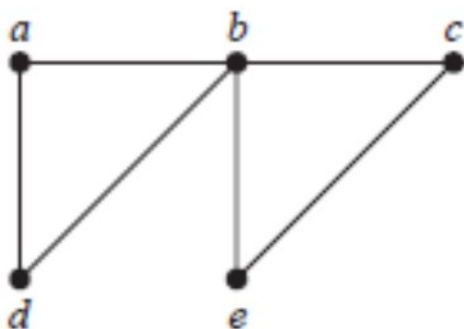
$$36 \uparrow 53 - 84 / * -$$

$$\begin{aligned}
 36 \uparrow 84 / * - &= 36 \uparrow 22 * - \\
 &= 36 \uparrow 4 - \\
 &= 32
 \end{aligned}$$

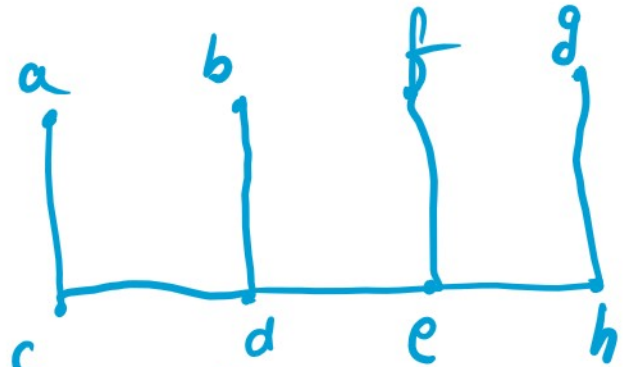
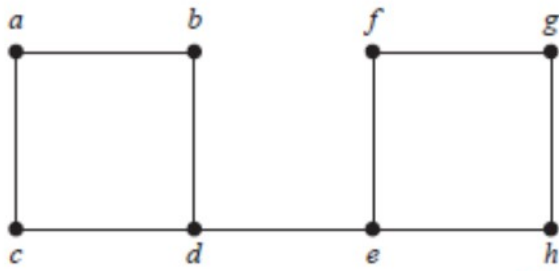
## Spanning Tree

Let  $G$  be a simple graph. A *spanning tree* of  $G$  is a subgraph of  $G$  that is a tree containing every vertex of  $G$ .

Connected, Simple,  
No circuit.



Spanning  
Tree of  $T$ .



Theorem 6:

A simple graph is connected if and only if it has a spanning tree.

Spanning Tree  $\rightarrow$  Connected

Connected

Tree  
 $\downarrow$   
S.T.

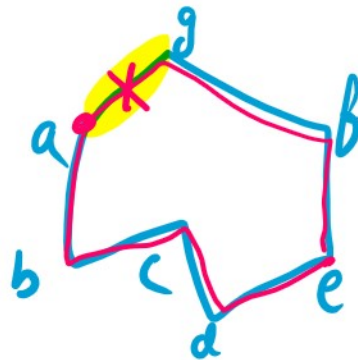
Not Tree

Some circuits

Remove edge

Spanning Tree

Spanning Tree



- Spanning tree of Graph with  $n$  vertices contains  $n-1$  edges.

- No. of edges to be removed from connected graph with  $n$  vertices and  $e$  edges to produce a spanning tree is  $e - (n-1) = e - n + 1$

Q19. How many edges needs to be removed to form a spanning tree.

(i)

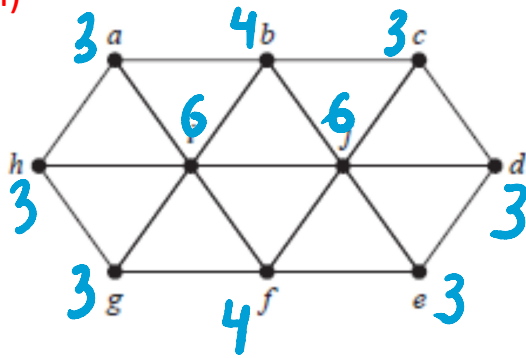
3 a

4 b

3 c

$$\text{vertices} = 10, e = \frac{18+8+12}{2}$$

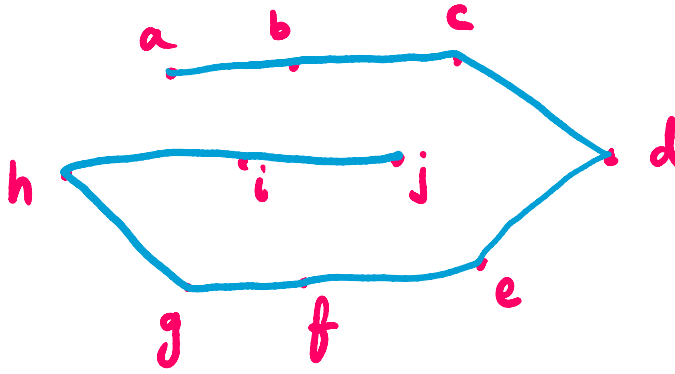
(i)



$$\text{vertices} = 10, e = \frac{18+8+12}{2}$$

$$\text{Tree has edges} = 9$$

$$\begin{aligned} \text{Removed} &= e - 9 \\ &= 19 - 9 \\ &= 10 \end{aligned}$$



(ii)  $K_{4,4}$

$$v = 8, e = 16$$

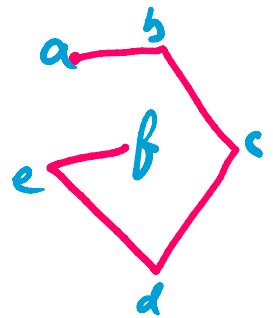
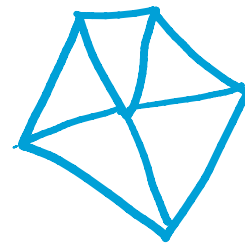
$$\text{To be removed} = 16 - (7) = 9$$

(iii)  $W_5$

(A) 6 (B) 5 (C) 7 (D) 4

$$v = 6, e = 10$$

$$- 10 - (6 - 1) = 5$$



Exercise: Write general formula for  $K_n, C_n, W_n, K_{m,n}$

Q20. Find spanning tree of the following graph by removing edges in simple circuits.

(i)

$$\text{Edmin Tree} = 11$$

(i)

(i)

$$V = 12$$

Edg in Tree = 11

