

MATRICES

What should be the condition of Identity Matrix

$$A \cdot A^{-1} = I$$

If any Matrix is having inverse of same

So there will be three conditions:-

1. Determinant of $A \neq 0$
2. It should be square matrix i.e 2×2 or 3×3 ant etc.
3. $AB = BA = I$

If B is inverse of A and A is inverse of B then it will give you Identity Matrix.

$$4 \cdot \frac{1}{4} = 1.$$

So by using this concept

Lets solve this equation by using Matrix method

$$4x + 2y = 8$$

$$5x + 3y = 11$$

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$$\begin{bmatrix} 4 & 2 \\ 5 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 8 \\ 11 \end{bmatrix}$$

$$A \quad X \quad B$$

:- A is Coefficient of Unknown variable and B is scalar or constant values.

1. $AX=B$ ---Eq.(1)

2. Can we multiply A^{-1} at both sides, So we will get

$$AA^{-1}B=A^{-1}B$$

We can club it by using Associativity Rule.

$$IX=A^{-1}B$$

$$X=A^{-1}B$$

Lets find A^{-1} by considering as $a=4, b=2, c=5, d=3$

$$A^{-1} = \frac{1}{(ad-bc)} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

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$$1. \begin{bmatrix} 1 \\ 2 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

Or $X=1$ and $Y=2$

Lets put values of x and y in equations

$$4*1+2*2=8$$

This is solution for particular equation

$$Q1. X_1+X_2+X_3=3$$

$$X_1-X_2 = 0$$

$$X_1-X_2+X_3 = 1 \quad \text{Solve this } 3*3 \text{ Matrix}$$

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Solve this by using the A-1 formula as

$$A^{-1} = \text{Adj}(A) / |A|^{-1}$$

Linear Transformation

Let take U and V are two vector spaces

A mapping $F: U \rightarrow V$ is called Linear Transformation of u into v if

1. $f(x+y) = f(x) + f(y)$

2. $f(ax) = a \cdot f(x)$

x, y belongs to U

$f(x)$ and $f(y)$ are the elements of V

The mapping who will satisfy these two conditions will be called as linear transformations

LINEAR TRANSFORMATION

How we can solve this:

$T: V_3(R) \rightarrow V_2(R)$ by

$$T(x_1, x_2, x_3) = (x_1 - x_2, x_1 + x_3)$$

Let

$(x_1, x_2, x_3) = x$ belongs to V_3

Whereas x_1 and x_2 are points

$$\begin{aligned} T(x+y) &= T[(x_1, x_2, x_3) + (y_1, y_2, y_3)] \\ &= T[(x_1+y_1, x_2+y_2, x_3+y_3)] \\ &\quad \begin{matrix} x_1 & x_2 & x_3 \end{matrix} \end{aligned}$$

As per formula

$$= T[(x_1+y_1-x_2-y_2, x_1+x_3+y_1+y_3)]$$

Rearrange the points

$$= T[(x_1-x_2+y_1-y_2, x_1+x_3+y_1+y_3)]$$

So we can add X coordinates in X and Y coordinates in Y as per dimensions

LINEAR TRANSFORMATION

$$(x_1 - x_2, x_1 + x_3) + (y_1 - y_2, y_1 + y_3)$$

$$T(x_1, x_2, x_3) + T(y_1, y_2, y_3)$$

$$T(x) + T(y)$$

2) Let we take 2nd condition

$$T(ax) = T[a(x_1, x_2, x_3)]$$

$$T(ax_1, ax_2, ax_3)$$

If it will multiplied that a with x_1, x_2, x_3

ax_1 will become x coordination and other y and z

$$= T[(ax_1 - ax_2), (ax_1 + ax_3)]$$

$$= a(x_1 - x_2, x_1 + x_3)$$

$$aT(x)$$

Hence T is Linear Transformation