

Sorting Techniques

- Bubble sort
- Insertion sort
- Selection sort

Sorting Algorithm

- Sorting takes an unordered collection and makes it an ordered one.

1	2	3	4	5	6
77	42	35	12	101	5



1	2	3	4	5	6
5	12	35	42	77	101

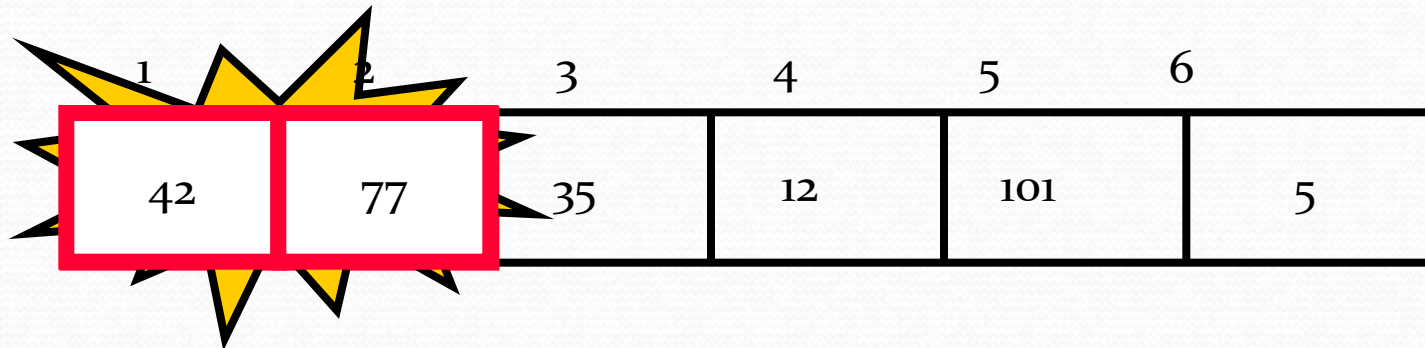
"Bubbling Up" the Largest Element

- Traverse a collection of elements
 - Move from the front to the end
 - “Bubble” the **largest value** to the end using **pair-wise comparisons and swapping**

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77	42	35	12	101	5

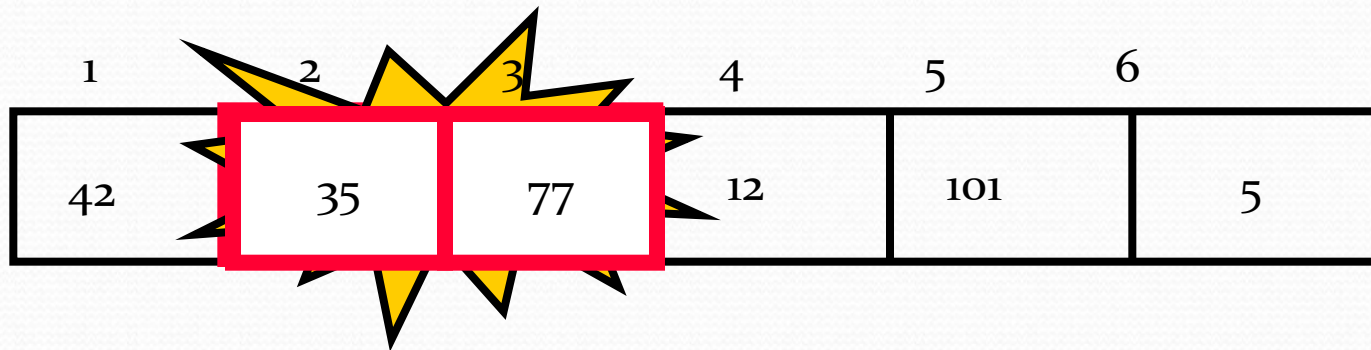
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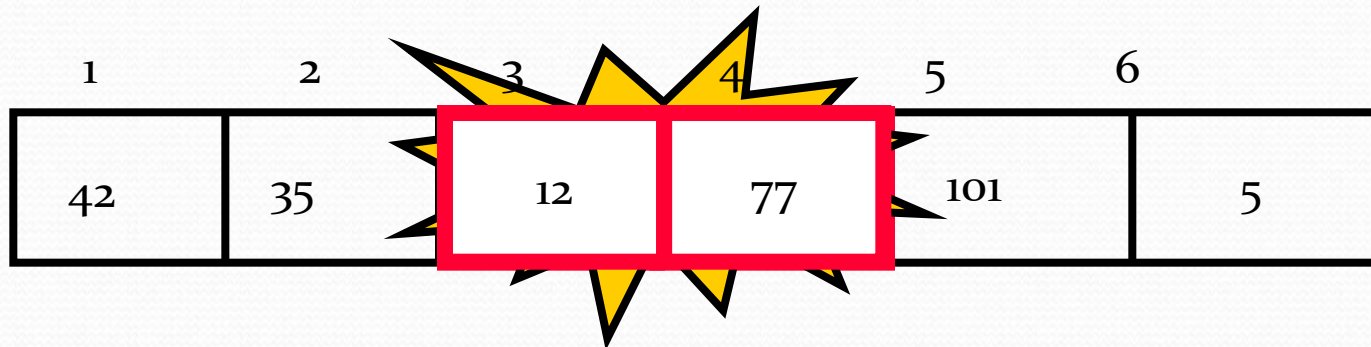
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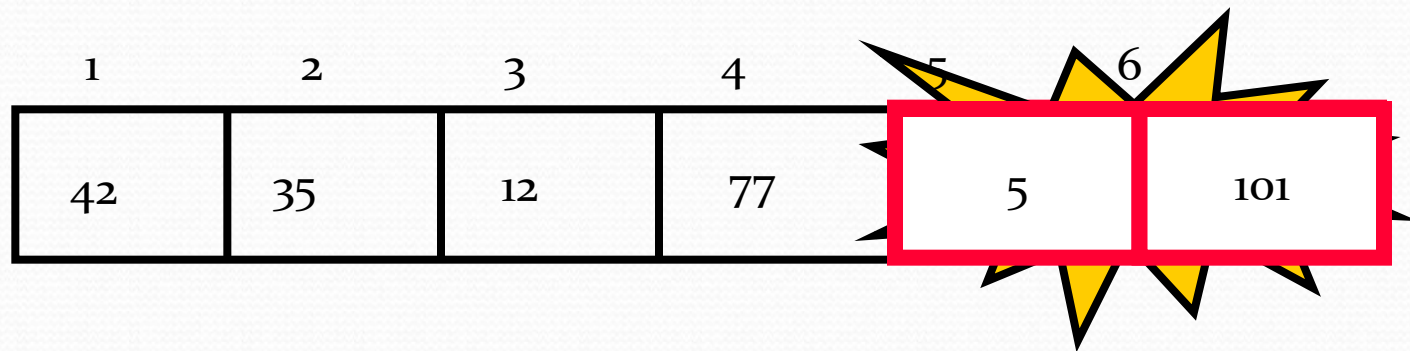
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No need to swap

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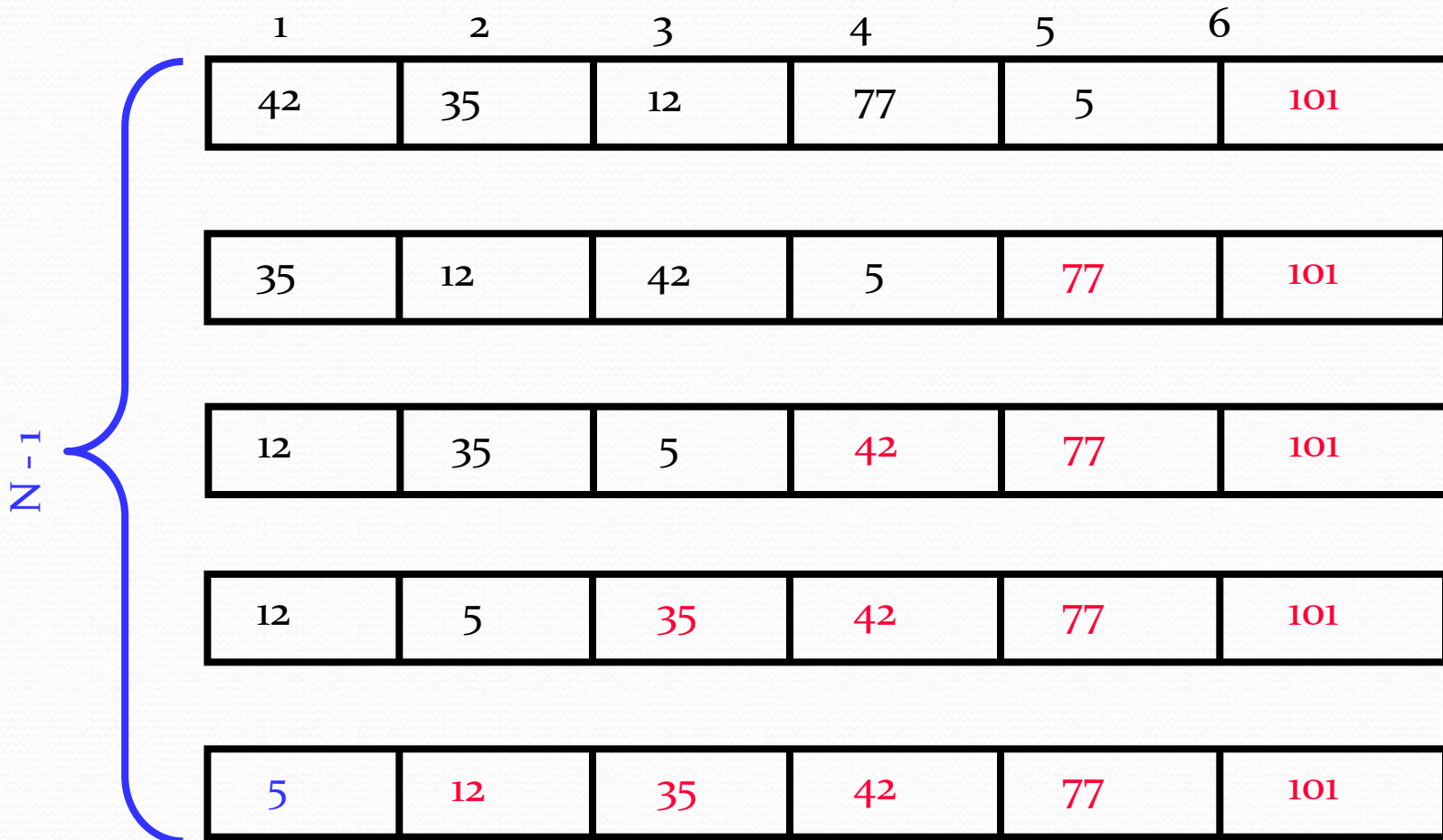
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Largest value correctly placed

Repeat “Bubble Up” How Many Times?

- If we have N elements...
- And if each time we bubble an element, we place it in its correct location...
- Then we repeat the “bubble up” process $N - 1$ times.
- This guarantees we’ll correctly place all N elements.

“Bubbling” All the Elements



Bubble Sort

BubbleSORT(A,N): it will sort the elements of an array A with N elements in ascending order.

1. Repeat step 2 to 3 for $I = 1$ to $n-1$ do
2. Repeat step 3 for $J = 1$ to $n-i$ do
3. if ($A[j+1] < A[j]$), then:
 swap $A[j]$ and $A[j+1]$.
 [End of if structure]
 [End of inner for loop]
 [End of outer for loop]
4. EXIT

Analysis:

In general, if the list has n elements, we will have to do
 $(n-1) + (n-2) + \dots + 2 + 1 = \frac{(n-1)n}{2}$ comparisons.
 $=O(n^2)$

Insertion Sort

INSERTION_SORT (A, N): it will sort the elements of an array A with N elements in ascending order.

1. Set $A[0] = -\infty$.
2. Repeat Step 3 to 5 for $K = 2$ to N :
3. Set $TEMP := A[K]$ and $PTR := K - 1$.
4. Repeat step a and b while $TEMP < A[PTR]$:
 - (a) Set $A[PTR+1] := A[PTR]$
 - (b) Set $PTR := PTR - 1$.[End of while Loop.]
5. Set $A[PTR+1] := TEMP$.
[End of for Loop]
6. Exit

Insertion Sort Example

- Sort: 34 8 64 51 32 21
- 34 8 64 51 32 21
 - The algorithm sees that 8 is **smaller** than 34 so it swaps.
- 8 34 64 51 32 21
 - 51 is **smaller** than 64, so they swap.
- 8 34 51 64 32 21
- 8 34 51 64 32 21 (from previous slide)
 - The algorithm sees 32 as another **smaller** number and moves it to its appropriate location between 8 and 34.
- 8 32 34 51 64 21
 - The algorithm sees 21 as another **smaller** number and moves into between 8 and 32.
- Final sorted numbers:
- 8 21 32 34 51 64

Insertion Sort Complexity

- This Sorting algorithm is frequently used when n is very small.
- Worst case occurs when array is in reverse order. The inner loop must use $K - 1$ comparisons.

$$\begin{aligned}f(n) &= 1 + 2 + 3 + \dots + (n - 1) \\&= n(n - 1)/2 \\&= O(n^2)\end{aligned}$$

- In average case, there will be approximately $(K - 1)/2$ comparisons in the inner loop.

$$\begin{aligned}f(n) &= (1 + 2 + 3 + \dots + (n - 1))/2 \\&= n(n - 1)/4 \\&= O(n^2)\end{aligned}$$

Selection Sort

This algorithm sorts an array A with N elements.

SELECTION(A, N) it will sort the elements of an array A with N elements in ascending order.

1. Repeat steps 2 and 3 for $k=1$ to $N-1$:
2. Call MIN(A, K, N, LOC).
3. [Interchange $A[k]$ and $A[LOC]$]
 Set $Temp := A[k]$.
 $A[k] := A[LOC]$
 $A[LOC] := Temp$.
 [End of step for Loop.]
4. Exit.

MIN(A, K, N, LOC).

1. Set $MIN := A[K]$ and $LOC := K$.
2. Repeat for $j=k+1$ to N :
 If $Min > A[j]$, then: Set $Min := A[j]$ and $LOC := J$.
 [End of if structure]
3. Return.

Method 2: Selection sort (1 algo)

SELECTION(A, N) it will sort the elements of an array A with N elements in ascending order.

1. Repeat steps 2 and 3 for $k=1$ to $N-1$:
2. Set $MIN:=a[K]$ and Set $LOC:=k$
3. Repeat step 4 for $j=k+1$ to N :
4. If $Min > A[j]$, then:
 Set $Min:= A[j]$ and $LOC:=j$.
 [End of if structure]
 [end of inner for loop]
5. [Interchange $A[k]$ and $A[LOC]$]
 Set $Temp:= A[k]$.
 $A[k]:= A[LOC]$
 $A[LOC]:=Temp$.
 [End of outer for Loop.]
6. EXIT.

Selection Sort Example

8	4	6	9	2	3	1
---	---	---	---	---	---	---

1	4	6	9	2	3	8
---	---	---	---	---	---	---

1	2	6	9	4	3	8
---	---	---	---	---	---	---

1	2	3	9	4	6	8
---	---	---	---	---	---	---

1	2	3	4	9	6	8
---	---	---	---	---	---	---

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Selection Sort Complexity

The number $f(n)$ of comparisons in selection sort algorithm is independent of original order of elements. There are $n-1$ comparisons during pass 1 to find the smallest element, $n-2$ comparisons during pass 2 to find the second smallest element, and so on.

Accordingly,

$$\begin{aligned} f(n) &= (n-1) + (n-2) + \dots + 2 + 1 \\ &= n(n-1)/2 \\ &= O(n^2) \end{aligned}$$

The $f(n)$ holds the same value $O(n^2)$ both for worst case and average case.

Comparing the Algorithms

	Best Case	Average Case	Worst Case
• Bubble Sort	$O(n)$	$O(n^2)$	$O(n^2)$
• Insertion Sort	$O(n)$	$O(n^2)$	$O(n^2)$
• Selection Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$



Thank You