

Q		Answer
1a	$\lim_{(x,y) \rightarrow (x_0, y_0)} f(x, y)$ will exist if (a) Limit is path dependent (c) Limit is both finite and unique along all possible paths reaching $(x_0, y_0)$ (b) Limit is not finite (d) None of these	c
2a	The value of $\lim_{(x,y) \rightarrow (0,0)} \frac{x}{\sqrt{x^2+y^2}}$ (a) 0 (b) 1 (c) Does not exist (d) 1/2	c
3a	A function $z = f(x, y)$ is said to be continuous at a point $(x_0, y_0)$ , if (a) $f(x, y)$ is defined at the point $(x_0, y_0)$ (b) $\lim_{(x,y) \rightarrow (x_0, y_0)} f(x, y)$ exist (c) $\lim_{(x,y) \rightarrow (x_0, y_0)} f(x, y) = f(x_0, y_0)$ (d) All of above	d
4a	Partial derivatives are used when (a) Function depends on one variable (b) Function depends on more than one variable (c) Function is constant (d) None of these	b
5a	If $f(x, y, z) = (xy)^{\sin z}$ then value of $\frac{\partial f}{\partial x}$ at $(3, 5, \frac{\pi}{2})$ is (a) 3 (b) 5 (c) 0 (d) 15	b
6a	Composite function is defined as (a) $y = f(x)$ (b) $z = f(x, y)$ (c) $f(x, y) = \text{constant}$ (d) $z = f(x, y), x = g(t), y = h(t)$	d
7a	If $x^y + y^x = c$ , where $c$ is a constant then value of $\frac{dy}{dx}$ at $(1, 1)$ is (a) 0 (b) 1 (c) -1 (d) -2	c
8a	If $f(x, y) = x^y, (x, y) \neq (0, 0)$ then the value of $f_{xy}$ is (a) $x^{y-1}(1 + y \log x)$ (b) $x^y(1 + y \log x)$ (c) $y^{x-1}(1 + y \log x)$ (d) $x^{y-1}(1 + \log x)$	a
9a	$\lim_{h \rightarrow 0} \frac{f(x+h, y) - f(x, y)}{h}$ if exist, called partial derivative of $f(x, y)$ with respect to (a) $x$ at $(a, b)$ (b) $y$ at $(a, b)$ (c) $x$ at $(x, y)$ (d) $y$ at $(x, y)$	c
10a	If $u = f(y - z, z - x, x - y)$ , then the value of $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z}$ is (a) 0 (b) 3 (c) 1 (d) None of these	a
11a	If $f(x, y) = c$ , then the value of $\frac{dx}{dy}$ is (a) $\frac{\partial f}{\partial x}$ (b) $\frac{\partial f}{\partial y}$ (c) $-\frac{\partial f / \partial x}{\partial f / \partial y}$ (d) $-\frac{\partial f / \partial y}{\partial f / \partial x}$	d
12a	If $f(x, y) = e^{xy}$ then the value of $\frac{\partial f}{\partial y}$ at $(0, 0)$ is (a) 0 (b) 1 (c) $e$ (d) None of these	a
13a	If $z = f(x, y), x = g(t), y = h(t)$ , then the value of $\frac{dz}{dt}$ is	c

	(a) $\frac{dz}{dx} \frac{dx}{dt} + \frac{dz}{dy} \frac{dy}{dt}$ (b) $-\frac{\frac{\partial z}{\partial x}}{\frac{\partial z}{\partial y}}$ (c) $\frac{\partial z}{\partial x} \frac{dx}{dt} + \frac{\partial z}{\partial y} \frac{dy}{dt}$ (d) $\frac{\partial z}{\partial x} \frac{\partial x}{\partial t} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial t}$	
14a	If $u = \sqrt{y^2 - x^2} \sin^{-1}\left(\frac{x}{y}\right)$ , then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ a) 0 b) $u$ c) $2u$ d) $3u$	b
15a	$f(x, y) = \frac{\sqrt{x}-\sqrt{y}}{\sqrt{x}+\sqrt{y}}$ is a homogeneous function of degree a) 0 b) 1 c) 2 d) 3	a
16a	Function $z = f(x, y)$ is homogeneous of degree $n$ if it can be written as (a) $z = x^n f(y)$ (b) $z = y^n f(x)$ (c) $z = y^n f(y/x)$ (d) $z = y^n f(x/y)$	d
17a	Which of the given options represent a homogeneous function ? (a) $\frac{x^2+y^3}{2xy}$ (b) $\sin^{-1}\left(\frac{x^4+y^4}{x^3}\right)$ (c) $\tan^{-1}\left(\frac{x^2y^2}{2x^4+y^4}\right)$ (d) None of these	c
18a	If a homogeneous function $u(x, y)$ satisfies $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = 30u$ , then the degree of $u(x, y)$ is (a) 12 (b) 6 (c) 4 (d) 3	b
19a	If $u = \frac{y^3-x^3}{y^2+x^2}$ then $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$ is a) $3u$ b) $2u$ c) $u$ d) 0	d
20a	If $z = f(x, y)$ then which of the following conditions will give us point of minima at a stationary point (a) $rt - s^2 > 0$ and $r > 0$ (b) $rt - s^2 > 0$ and $r < 0$ (c) $rt - s^2 = 0$ (d) $rt - s^2 < 0$	a
21a	If $f(x, y) = x^3 - y^3 - 2xy + 6$ stationary points of $f(x, y)$ is (a) $(0,0)$ & $\left(-\frac{2}{3}, \frac{2}{3}\right)$ (b) $(0,0)$ & $\left(\frac{2}{3}, \frac{2}{3}\right)$ (c) $(0,0)$ & $\left(\frac{2}{3}, -\frac{2}{3}\right)$ (d) None of these	b
22a	For the function $f(x, y) = 2xy - 5x^2 - 2y^2 + 4x + 4y - 4$ the critical point $\left(\frac{2}{3}, \frac{4}{3}\right)$ is a point of a) Maxima b) Minima c) Saddle point d) None of these	c
23a	For the function $f(x, y) = x^2 - 4xy + y^2 + 6y + 2$ the critical point $(2, 1)$ is a point of a) Maxima b) Minima c) Saddle point d) None of these	c
24a	For the function $f(x, y) = x^4 + y^4 + z^4 - 4xyz$ the critical point $(1, 1, 1)$ is a point of a) Maxima b) Minima c) Saddle point d) None of these	