

Q1. Given fuzzy two sets A and B compute following:

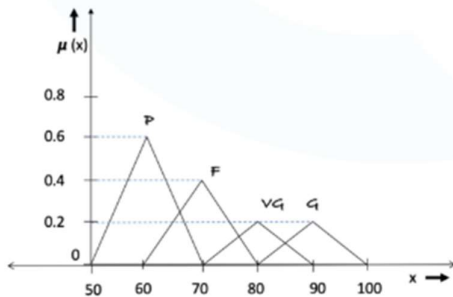
$$A = \{(x_1, 0.6), (x_2, 0.2), (x_3, 0.3)\}$$

$$B = \{(x_1, 0.7), (x_2, 0.3), (x_3, 0.4)\}$$

- (i)  $(A \cup B)$
- (ii)  $(A \cap B)$
- (iii)  $\text{Sum}(A+B)$
- (iv)  $\text{Difference}(A-B)$
- (v)  $\text{Disjunctive Sum}(A \oplus B)$

Q2:

Let A be a fuzzy set that tells about a student as shown in figure below. Here, the linguistic variable P represents a Pass student, F stands for a Fair student, G represents a Good student and VG represents a Very Good student. Calculate the defuzzified value for the fuzzy set A with weighted average method and center of sums.



Q 3:

Consider the fuzzy relation

$$R = \begin{bmatrix} 1 & 0.8 & 0 & 0.1 & 0.2 \\ 0.8 & 1 & 0.4 & 0 & 0.9 \\ 0 & 0.4 & 1 & 0 & 0 \\ 0.1 & 0 & 0 & 1 & 0.5 \\ 0.2 & 0.9 & 0 & 0.5 & 1 \end{bmatrix}$$

Perform  $\lambda$ -cut operations for the values of  $\lambda = 0.9, 0^+$

Q4: List the five functional blocks FIS is constructed on with a block diagram.

Q5: Explain the methods used for decomposition of compound linguistic rules into simple canonical rules.

Q6: Explain the Roulette wheel technique for traditional GA selection.

Q7: Describe the various stopping conditions for genetic algorithm flow.

Q8: Differentiate between Mamdani FIS and Sugeno FIS.

Q9: What is Fuzzy Inference System (FIS)? Illustrate Mamdani FIS and Sugeno FIS with examples?

Q10: What are Genetic Algorithms (GA)? Explain the operators in GA?

Q11. a) Explain four mutation methods?

b) List the stopping condition for Genetic Algorithm Flow?

**Q 12:** Define the initial population for the following problem:

$$\text{Minimize } f(x) = \frac{x^2}{2} + \frac{x^2}{2}$$

Where  $0 < x < 15$

- Population Size 5 and Initial Population 13, 5, 8, 14, 11
- Encoding technique: Binary encoding
- Selection operator: roulette wheel selection
- Single point crossover at 2

Compute for 1 iteration

Q13: Proof the following properties of fuzzy set:

- Commutativity
- Associativity
- Distributivity
- Absorption
- Idempotency / Tautology

Q2. Given fuzzy four sets A, B, C, D compute following:

$$A = \{(x_1, 0.6), (x_2, 0.2), (x_3, 0.3)\}$$

$$B = \{(y_1, 0.7), (y_2, 0.3), (y_3, 0.4)\}$$

$$C = \{(x_1, 0.6), (x_2, 0.2), (x_3, 0.3)\}$$

$$D = \{(y_1, 0.7), (y_2, 0.3), (y_3, 0.4)\}$$

Compute R1 and R2

$$i) R1 = \min\{\mu_{A(x)}, \mu_{B(y)}\} \quad R2 = \max\{\mu_{C(x)}, \mu_{D(y)}\}$$

ii) Union ( $R1 \cup R2$ ) and Intersection ( $R1 \cap R2$ )

Q3.

The Lambda-cut method for a fuzzy set can also be extended to fuzzy relation also.

**Example:** For a fuzzy relation  $R$

$$R = \begin{bmatrix} 1 & 0.2 & 0.3 \\ 0.5 & 0.9 & 0.6 \\ 0.4 & 0.8 & 0.7 \end{bmatrix}$$

We are to find  $\lambda$ -cut relations for the following values of  $\lambda = 0, 0.2, 0.9, 0.5$

$$R_0 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \text{ and } R_{0.2} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \text{ and}$$
$$R_{0.9} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \text{ and } R_{0.5} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

### Lambda-cut sets : Example

Two fuzzy sets  $P$  and  $Q$  are defined on  $x$  as follows.

$\mu(X)$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$
P	0.1	0.2	0.7	0.5	0.4
Q	0.9	0.6	0.3	0.2	0.8

Find the following :

(a)  $P_{0.2}, Q_{0.3}$

(b)  $(P \cup Q)_{0.6}$

(c)  $(P \cup \bar{P})_{0.8}$

(d)  $(P \cap Q)_{0.4}$

Q Explain PSO algorithm with suitable example?

Q Explain ACO algorithm with suitable example?

Q Explain BAT algorithm with suitable example?

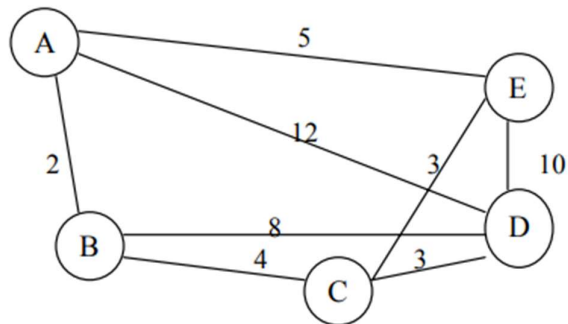
Q Explain Crow algorithm with suitable example?

Q Explain Bee algorithm with suitable example?

Q Explain whale algorithm with suitable example?

Q Explain cuckoo algorithm with suitable example?

Q Compute Pheromone update using without vaporization technique for given Cost graph  
pheromone initial value is 1 for the tour  $A \rightarrow E \rightarrow C \rightarrow D \rightarrow B \rightarrow A$ ?



Q Compute Pheromone update using with vaporization technique for given Cost graph  
pheromone initial value is 1 for the tour  $A \rightarrow D \rightarrow E \rightarrow C \rightarrow B \rightarrow A$ ?

