

Wal-timise Challenge

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0.0.2 Members:

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0.0.3 Method Used: Mixed-Integer Programming

1. We first formulate the problem as a mixed-integer optimization problem.
2. The objective function being to minimize the total hit value:

$$\min \sum_{i=1}^{300} H_i^T X_i$$

where X is the required assignment / solution, and H is the hit value corresponding to each assignment, both in suitable encoding.

3. Subject to the constraints being on revenue percentage, and quantity percentage.

$$\frac{\sum_{i=0}^{300} R_i^T X_i - \text{Base_Revenue}}{\text{Base_Revenue}} \geq x$$

$$\frac{\sum_{i=0}^{300} Q_i^T X_i - \text{Base_Quantity}}{\text{Base_Quantity}} \geq y$$

where R and Q capture the revenue, and quantity associated with each item, again everything in suitable encoding.

4. Our choice of was multi-staged. First we converted to one-hot encoding. Then we flatten the resulting 2-D vector into 1-D by laying it out linearly. Resulting in additional 300 constraints to make sure each item is assigned to only 1 price (out of the 5 possible options).
5. Thus, the formulated optimization problem is on 1500 (= 300 x 5) binary-variables (vector X), subject to 302 constraints.

6. We implement and solve this mixed-integer program using the Coin-or-branch and Cut (CBC), which is an open-source mixed integer programming solver in C++.
7. The OR-Tools is a library by Google, providing an interface to several third-party mixed-integer programming (MIP) solvers. The Coin-or branch and cut (CBC) solver is included in OR-Tools.
8. Our solution takes only **13-14 seconds** to solve this problem (tested on Core i7 8th Gen laptop, with 16 GB RAM). Thus, it is very efficient and can be scaled to much larger problem sizes.

0.0.4 Code:

```
[ ]: from __future__ import print_function
from ortools.linear_solver import pywraplp

import numpy as np
import pandas as pd

'''
    Scenario 1. X = 10%, Y = 25%
    For other scenarios change the below x,y,scen variables
'''

x = 0.10
y = 0.25
scen = 'scenario1'

print('X={0}%, Y={1}%, Scenario = {2} \n'.format(np.round(x*100),np.
↪round(y*100),scen))

# Reading and processing the data
data = pd.read_csv('dataset.csv')
data = data.drop(columns=['Item_id'])
data = data.to_numpy()
data = data.T

R = []
Q = []
H = []

for i in range(5):
    R.append(data[2*i]*data[2*i+1])
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    Q.append(data[2*i+1])
    H.append(np.abs(data[2*i]-data[0])*data[2*i+1])

R = np.array(R)
Q = np.array(Q)
H = np.array(H)

base_revenue = np.sum(R[0])
base_quantity = np.sum(Q[0])

R = R.T
Q = Q.T
H = H.T

for i in range(len(R)):
    R[i] = R[i]-R[i][0]
    Q[i] = Q[i]-Q[i][0]

reven = R.flatten()
quan = Q.flatten()
hit = H.flatten()

more_cons = np.zeros((300,1500))

for i in range(300):
    for j in range(5):
        more_cons[i][5*i+j] = 1

more_bnds = np.ones(300)

bounds = []
cons = []

cons.append(reven)
bounds.append(x*base_revenue)
cons.append(quan)
bounds.append(y*base_quantity)

for i in range(300):
    cons.append(more_cons[i])
    bounds.append(more_bnds[i])

tmp = []

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def mip_formulation():
    """Preparing the MIP formulation"""
    data = {}
    data['constraint_coeffs'] = cons
    data['bounds'] = bounds
    data['obj_coeffs'] = hit
    data['num_vars'] = 1500
    data['num_constraints'] = 302
    return data

def main():
    data = mip_formulation()
    # Create the mip solver with the CBC backend.
    solver = pywraplp.Solver.CreateSolver('simple_mip_program', 'CBC')
    infinity = solver.infinity()

    # Setting the variables
    x = {}
    for j in range(data['num_vars']):
        x[j] = solver.IntVar(0, 1, 'x[%i]' % j)
    print('Number of variables =', solver.NumVariables())

    # Adding the constraints
    for i in range(data['num_constraints']):
        constraint_expr = [data['constraint_coeffs'][i][j] * x[j] for j in
→range(data['num_vars'])]
        if i<2:
            solver.Add(sum(constraint_expr) >= data['bounds'][i])
        else:
            solver.Add(sum(constraint_expr) == data['bounds'][i])
    print('Number of constraints =', solver.NumConstraints())

    # Defining the objective
    obj_expr = [data['obj_coeffs'][j] * x[j] for j in range(data['num_vars'])]
    solver.Minimize(solver.Sum(obj_expr))

    # Calling the solver
    status = solver.Solve()

    if status == pywraplp.Solver.OPTIMAL:
        print('Final Hit value obtained=', solver.Objective().Value())
        for j in range(data['num_vars']):
            # print(x[j].name(), ' = ', x[j].solution_value())
            tmp.append(x[j].solution_value())
        print()
        print('Problem solved in %f milliseconds' % solver.wall_time())

```

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else:
    print('The problem does not have an optimal solution.')

if __name__ == '__main__':
    main()

    # Processing the output
    tmp = np.array(tmp)
    sols = []
    for i in range(300):
        for j in range(5):
            if tmp[5*i+j] > 0.5:
                sols.append(j)
                break

    lst = range(1,301)

    # Saving the solution
    df = pd.DataFrame(list(zip(lst,sols)),columns = ['Item_id','Price'])
    df['Price'] = df['Price'].map({0:'Base_Price',1:'Price1',2:'Price2',3:
↪ 'Price3',4:'Price4'})
    df.to_csv(scen + '.csv',index=False)

```