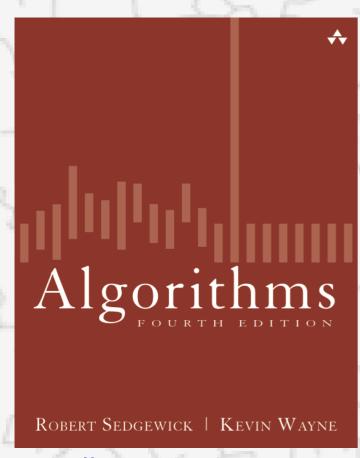
Algorithms



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3.1 SYMBOL TABLES

- · API
- elementary implementations
- ordered operations

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ROBERT SEDGEWICK | KEVIN WAYNE

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Symbol tables

Key-value pair abstraction.

- Insert a value with specified key.
- Given a key, search for the corresponding value.

Ex. DNS lookup.

Insert domain name with specified IP address.

key

Given domain name, find corresponding IP address.

domain name	IP address
www.cs.princeton.edu	128.112.136.11
www.princeton.edu	128.112.128.15
www.yale.edu	130.132.143.21
www.harvard.edu	128.103.060.55
www.simpsons.com	209.052.165.60



Symbol table applications

application	purpose of search	key	value		
dictionary	find definition	word	definition		
book index	find relevant pages	term	list of page numbers		
file share	find song to download	name of song	computer ID		
financial account	process transactions	account number	transaction details		
web search	find relevant web pages	keyword	list of page names		
compiler	find properties of variables	variable name	type and value		
routing table	route Internet packets	destination	best route		
DNS	find IP address	domain name	IP address		
reverse DNS	find domain name	IP address	domain name		
genomics	find markers	DNA string	known positions		
file system	find file on disk	filename	location on disk		

Associative memory (eg. CAM content adressable memory)

We can not only index but we can efficiently search for content (keys) stored in the array and get and index, or value/data asociated with the content/key



Symbol tables: context

Also known as: maps, dictionaries, associative arrays.

Generalizes arrays. Keys need not be between 0 and N-1.

Language support.

- External libraries: C, VisualBasic, Standard ML, bash, ...
- Built-in libraries: Java, C#, C++, Scala, ...
- Built-in to language: Awk, Perl, PHP, Tcl, JavaScript, Python, Ruby, Lua.

every array is an every object is an associative array associative array

table is the only primitive data structure

hasNiceSyntaxForAssociativeArrays["Python"] = true

hasNiceSyntaxForAssociativeArrays["Java"] = false

legal Python code



Basic symbol table API

Associative array abstraction. Associate one value with each key.

public class ST <k< th=""><th>ey, Value></th><th></th><th></th></k<>	ey, Value>		
	ST()	create an empty symbol table	
void	put(Key key, Value val)	put key-value pair into the table	_ a[key] = val;
Value	get(Key key)	value paired with key ←	a[key]
boolean	contains(Key key)	is there a value paired with key?	
void	delete(Key key)	remove key (and its value) from table	
boolean	isEmpty()	is the table empty?	
int	size()	number of key-value pairs in the table	
Iterable <key></key>	keys()	all the keys in the table	



Conventions

- Values are not null.
 Java allows null value
- Method get() returns null if key not present.
- Method put() overwrites old value with new value.

Intended consequences.

Easy to implement contains().

```
public boolean contains(Key key)
{ return get(key) != null; }
```

Can implement lazy version of delete().

```
public void delete(Key key)
{ put(key, null); }
```

—

Keys and values

Value type. Any generic type.

Key type: several natural assumptions.

- Assume keys are Comparable, use compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality; use hashCode() to scramble key.

built-in to Java (stay tuned)

Best practices. Use immutable types for symbol table keys.

- Immutable in Java: Integer, Double, String, java.io.File, ...
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

specify Comparable in API.



Equality test

All Java classes inherit a method equals().

Java requirements. For any references x, y and z:

- Reflexive: x.equals(x) is true.
- Symmetric: x.equals(y) iff y.equals(x).
- Transitive: if x.equals(y) and y.equals(z), then x.equals(z).
- Non-null: x.equals(null) is false.

relation

do x and y refer to the same object?

Default implementation. (x == y)

Customized implementations. Integer, Double, String, java.io.File, ...

User-defined implementations. Some care needed.



Implementing equals for user-defined types

Seems easy.

```
class Date implements Comparable<Date>
public
  private final int month;
  private final int day;
  private final int year;
  public boolean equals(Date that)
   if (this.day != that.day ) return false;
   if (this.month != that.month) return false;
   if (this.year != that.year ) return false;
    return true;
```

check that all significant fields are the same



Implementing equals for user-defined types

Seems easy, but requires some care. typically unsafe to use equals() with inheritance (would violate symmetry) public final class Date implements Comparable<Date> private final int month; must be Object. Why? Experts still debate. private final int day; private final int year; public boolean equals(Object y) optimize for true object equality if (y == this) return true; check for null if (y == null) return false; if (y.getClass() != this.getClass()) objects must be in the same class return false; (religion: getClass() vs. instanceof) Date that = (Date) y; if (this.day != that.day) return false; cast is guaranteed to succeed if (this.month != that.month) return false; check that all significant if (this.year != that.year) return false; fields are the same return true;

Equals design

"Standard" recipe for user-defined types.

- Optimization for reference equality.
- Check against null.
- Check that two objects are of the same type and cast.
- Compare each significant field:
 - if field is a primitive type, use == but use Double.compare() with double (or otherwise deal with -0.0 and NaN)
 - if field is an object, use equals()
 - if field is an array, apply to each entry -

apply rule recursively

can use Arrays.deepEquals(a, b)

but not a.equals(b)

Best practices.

- e.g., cached Manhattan distance
- No need to use calculated fields that depend on other fields.
- Compare fields mostly likely to differ first.
- Make compareTo() consistent with equals().

x.equals(y) if and only if (x.compareTo(y) == 0)



ST test client for traces

Build ST by associating value i with i^{th} string from standard input.

```
public static void main(String[] args)
{
   ST<String, Integer> st = new ST<String, Integer>();
   for (int i = 0; !StdIn.isEmpty(); i++)
   {
      String key = StdIn.readString();
      st.put(key, i);
   }
   for (String s : st.keys())
      StdOut.println(s + " " + st.get(s));
}
```

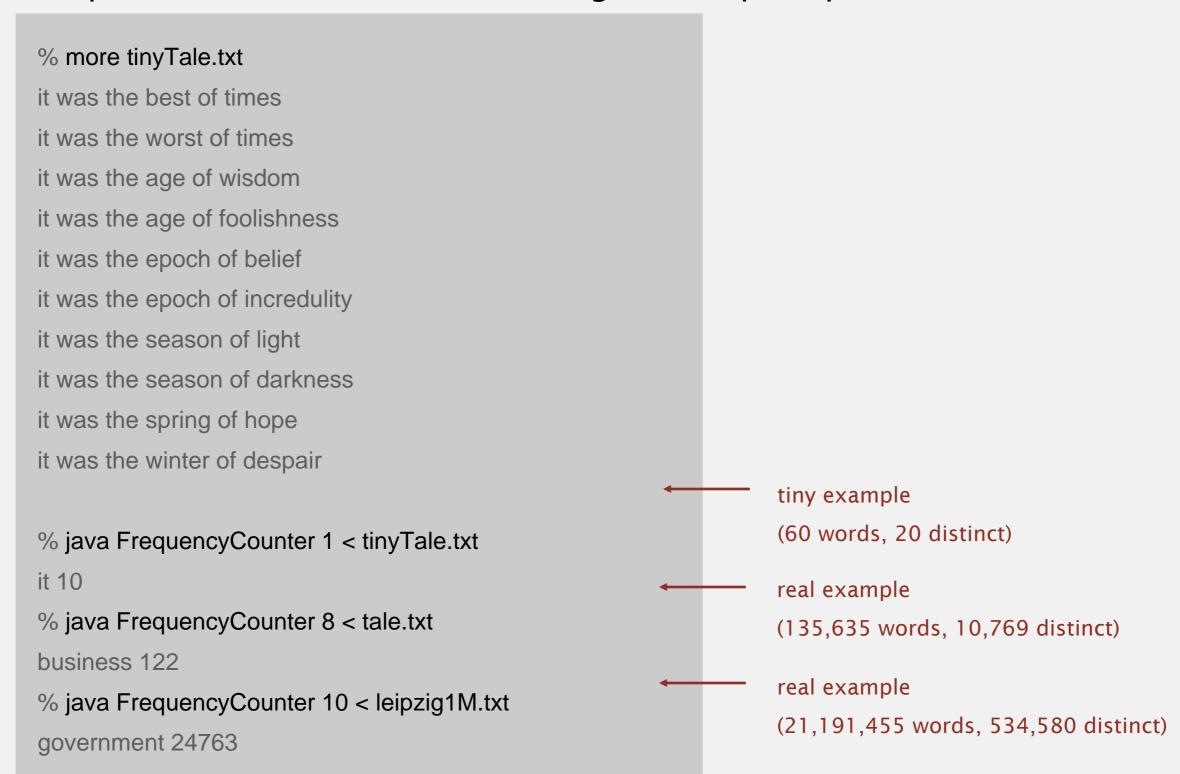
```
keys S E A R C H E X A M P L E values 0 1 2 3 4 5 6 7 8 9 10 11 12
```

output

```
A 8
C 4
E 12
H 5
L 11
M 9
P 10
R 3
S 0
X 7
```

ST test client for analysis

Frequency counter. Read a sequence of strings from standard input and print out one that occurs with highest frequency.





Frequency counter implementation

```
public class FrequencyCounter
 public static void main(String[] args)
   int minlen = Integer.parseInt(args[0]);
    ST<String, Integer> st = new ST<String, Integer>();
                                                                                                         create ST
   while (!StdIn.isEmpty())
     String word = StdIn.readString();
                                                                        ignore short strings
                                                                                                         read string and
     if (word.length() < minlen) continue;</pre>
                                                                                                         update frequency
     if (!st.contains(word)) st.put(word, 1);
                       st.put(word, st.get(word) + 1);
     else
    String max = "";
                                                                                                         print a string
   st.put(max, 0);
                                                                                                         with max freq
   for (String word : st.keys())
     if (st.get(word) > st.get(max))
        max = word;
    StdOut.println(max + " " + st.get(max));
```

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API

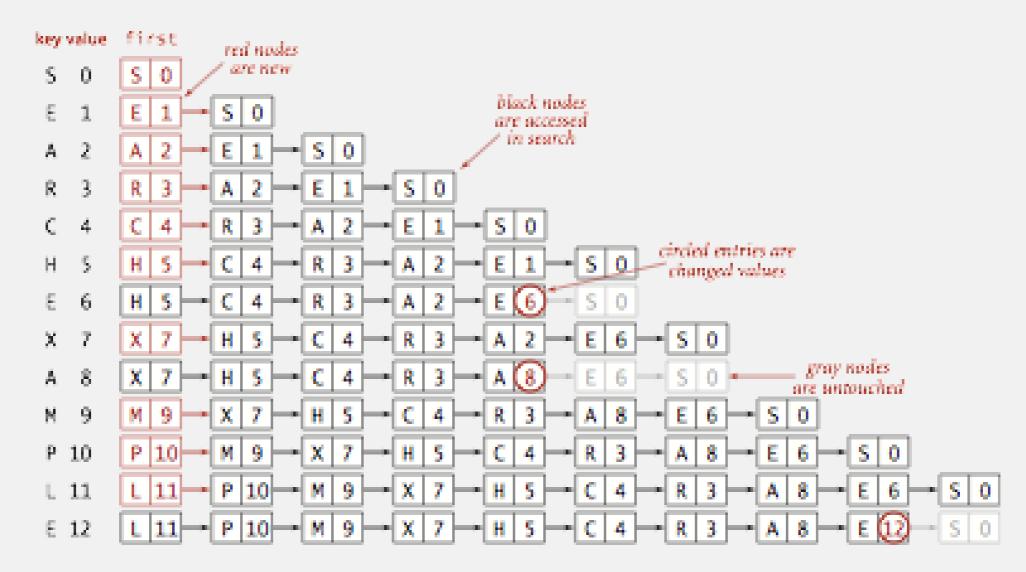
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Sequential search in a linked list

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.



Trace of linked-list ST implementation for standard indexing client



Elementary ST implementations: summary

CT impolence antation	guara	ıntee	avera	key	
ST implementation	search	insert	search hit	insert	interface
sequential search (unordered list)	N	N	N / 2	N	equals()

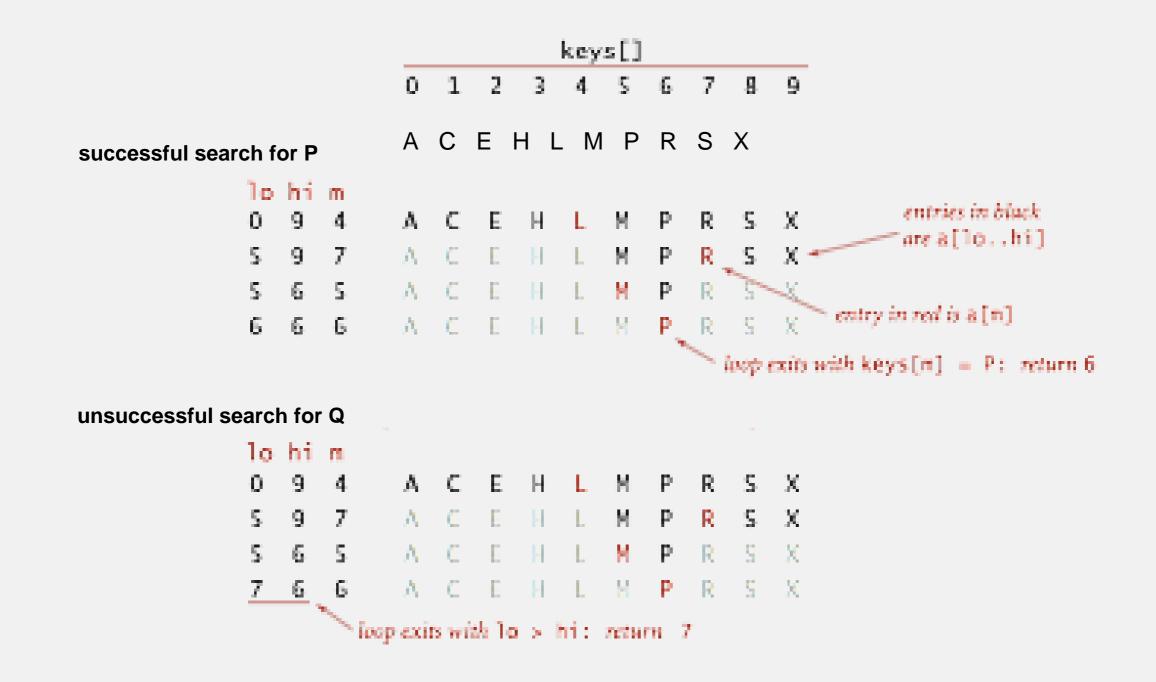
Challenge. Efficient implementations of both search and insert.



Binary search in an ordered array

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?



Binary search: Java implementation

```
public Value get(Key key)
 if (isEmpty()) return null;
 int i = rank(key);
 if (i < N && keys[i].compareTo(key) == 0) return vals[i];
 else return null;
private int rank(Key key)
                                                               number of keys < key
 int lo = 0, hi = N-1;
 while (lo <= hi)
    int mid = lo + (hi - lo) / 2;
    int cmp = key.compareTo(keys[mid]);
         (cmp < 0) hi = mid - 1;
    else if (cmp > 0) lo = mid + 1;
    else
                       return mid;
 return lo;
```

Binary search: trace of standard indexing client

Problem. To insert, need to shift all greater keys over.

						key	s []										va"	ls[]	1			
key	value	0	1	2	3	4	5	6	7	8	9	N	0	1	2	3	4	5	6	7	8	9
S	0	S										1	0									
E	1	E	S				nerie	s im r	red.			2	1	0					tries ved to			
A	2	A	Ε	S				nseri				3	2	1	0		/				r oggene	•
R	3	Λ	E	R	S							4	2	1	3	0						
C	4	Λ	C	E	R	S			en	tries	in gra	_{0′} 5	2	4	1	3	0					
Н	5	Λ	C	Ε	Н	R	5				a mar		2	4	1	5	3	0			ntria d voi	s are lives
E	6	Α	C	Γ	Н	R	5					6	2	4	(6)	5	3	0				
Х	7	Λ	C	Ε	Н	R	5	Х				7	2	4	6	5	3	0	7			
A	8	Α	C	Ε	Н	R	5	X				7	(B)	4	6	5	3	0	7			
M	9	Λ	C	Γ	Н	М	R	S	Х			8	8	4	6	5	9	3	0	7		
P	10	Λ	C	Ī.	Н	Н	Р	R	5	Х		9	R	4	6	5	9	10	3	0	7	
L	11	Λ	C	Ε	Н	L	М	Р	R	S	Х	10	R	4	6	5	11	9	10	3	0	7
E	12	Α	C	Ε	Н	L	M	P	R	5	X	10	8	4 (12)	5	11	9	10	3	0	7
		A	\mathbf{C}	E	Н	L.	М	Р	R	S	Х		8	4	12	5	11	9	10	3	0	7



Elementary ST implementations: summary

CT impolence antation	guara	ıntee	avera	key	
ST implementation	search	insert	search hit	insert	interface
sequential search (unordered list)	N	N	N/2	N	equals()
binary search (ordered array)	log N	N	log N	(N/2)	compareTo()

Challenge. Efficient implementations of both search and insert.

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AP

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Examples of ordered symbol table API

```
values
                                keys
                   min() -- 09:00:00
                                        Chicago
                                       Phoenix
                            09:00:03
                            09:00:13 - Houston
           get(09:00:13) 09:00:59
                                        Chicago
                            09:01:10
                                        Houston
                                        Chicago
         floor(09:05:00) \longrightarrow 09:03:13
                            09:10:11
                                        Seattle
               select(7) -- 09:10:25
                                       Seattle
                            09:14:25
                                       Phoenix
                            09:19:32
                                        Chicago
                            09:19:46
                                        Chicago
keys(09:15:00, 09:25:00) \longrightarrow |09:21:05|
                                        Chicago
                            09:22:43
                                        Seattle
                            09:22:54
                                       Seattle
                            09:25:52
                                       Chicago
       ceiling(09:30:00) \longrightarrow 09:35:21
                                        Chicago
                            09:36:14
                                        Seattle
                   max() \longrightarrow 09:37:44
                                        Phoenix
size(09:15:00, 09:25:00) is 5
     rank(09:10:25) is 7
```



Ordered symbol table API

public class ST<Key extends Comparable<Key>, Value> Key min() smallest key Key max() largest key Key floor(Key key) largest key less than or equal to key Key ceiling(Key key) smallest key greater than or equal to key int rank(Key key) number of keys less than key Key select(int k) key of rank k void deleteMin() delete smallest key void deleteMax() delete largest key int size(Key Io, Key hi) number of keys between lo and hi lterable<Key> keys() all keys, in sorted order Iterable<Key> keys(Key lo, Key hi) keys between lo and hi, in sorted order



Binary search: ordered symbol table operations summary

	sequential search	binary search
search	N	$\log N$
insert / delete	N	N
min / max	N	1
floor / ceiling	N	$\log N$
rank	N	$\log N$
select	N	1
ordered iteration	$N \log N$	N

order of growth of the running time for ordered symbol table operations