§ 5.2. Практическая работа (решение задач)

Найти интегралы:

8.5.2.
$$\int \frac{dx}{\sin x}$$

8.5.3.
$$\int \frac{dx}{5\cos x + 3}.$$

8.5.5.
$$\int \frac{dx}{3\sin^2 x + 5\cos^2 x}.$$

8.5.6.
$$\int \frac{dx}{\sin^5 x \cdot \cos x}.$$

8.5.8.
$$\int \sin^3 x \, dx.$$

8.5.9.
$$\int \frac{\cos^3 x \, dx}{\sin^4 x}.$$

8.5.11.
$$\int \cos^4 x \, dx$$
.

8.5.12.
$$\int \sin^2 x \cdot \cos^2 x \, dx.$$

8.5.14.
$$\int \cos 2x \cdot \sin 4x \, dx.$$

8.5.15.
$$\int \sin \frac{x}{2} \sin \frac{3x}{2} dx$$
.

8.5.17.
$$\int \operatorname{ctg}^3 x \, dx$$
.

8.5.18.
$$\int tg^2 x dx$$
.

Ответы

8.5.2.
$$\ln \left| \operatorname{tg} \frac{x}{2} \right| + C$$
. **8.5.3.** $\frac{1}{4} \ln \left| \frac{\operatorname{tg} \frac{x}{2} + 2}{\operatorname{tg} \frac{x}{2} - 2} \right| + C$. **8.5.5.** $\frac{1}{\sqrt{15}} \cdot \operatorname{arctg} \left(\sqrt{\frac{3}{5}} \operatorname{tg} x \right) + C$.

8.5.6.
$$C - \frac{1}{4} \operatorname{ctg}^4 x - \operatorname{ctg}^2 x + \ln |\operatorname{tg} x|$$
. **8.5.8.** $\frac{1}{3} \cos^3 x - \cos x + C$.

8.5.9.
$$\frac{1}{\sin x} - \frac{1}{3\sin^3 x} + C$$
. **8.5.11.** $\frac{3}{8}x + \frac{1}{4}\sin 2x + \frac{1}{32}\sin 4x + C$.

8.5.12.
$$\frac{1}{8}x - \frac{1}{32}\sin 4x + C$$
. **8.5.14.** $C - \frac{1}{12}\cos 6x - \frac{1}{4}\cos 2x$.

8.5.15.
$$\frac{1}{2}\sin x - \frac{1}{4}\sin 2x + C$$
. **8.5.17.** $C - \frac{\cot^2 x}{2} - \ln|\sin x|$. **8.5.18.** $\tan x - x + C$.