

19/03/2025 Genetic Algorithm :-

↳ 1965, Prof. J. Holland.

↳ Evolutionary - Algorithm.

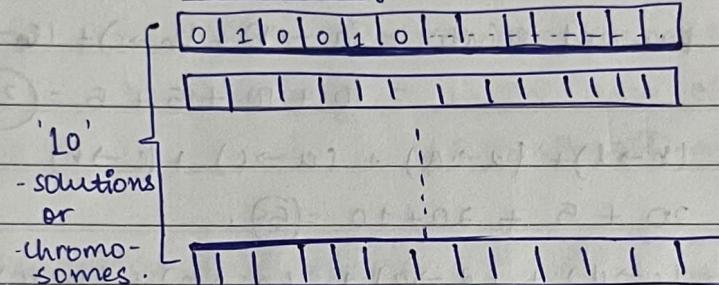
- Discrete - Optimization - Problems.
- Evolution by mimicking natural living organisms - Evolution.
- Guided Random - Search Techniques.
- Implicitly perform parallel - search simultaneously.
- Less - probable to trap into the local - optima.

Main Task of GA :-

① Initialization of Population.

* let $N = 10$ (Population) -

Chromosome (vector with multiple elements) -



∴ we've
'N'-no. of
solutions or
chromosomes

* NOTE :- ① Content of chromosomes = '0' or '1'.

② All elements are diff. attributes/features, which are marked '0' or '1'.

Eg :- Travelling - salesman - Problem :-

		a	b	c	d	e	f	g	h	
		000	a	0						
		001	b	10	0					
		010	c	20	10	0				
		011	d	5	20	5	0			
100	e	10	5	20	15	0				
101	f	20	5	30	40	200				
110	g	10	5	40	15	20	10	0		
111	h	10	30	20	25	15	5	10	0	

we'll take only 4-cities * Reward - Table from
 8-cities will be time consuming
 travelling b/w 2-cities
 * length of each-chromosome :-
 8x3 = 24.

① let no. of Population $\Rightarrow N = 4$.

chromosome-1	a	b	c	d
	0	0	0	1

chromosome-2	b	d	a	c
	0	1	1	1

chromosome-3	c	a	a	b
	1	0	1	1

chromosome-4	a	b	d	c
	0	0	0	1

→ order of cities taken is random
here.

② calculate Objective-function :-

∴ start = end
in TSP =

$$f(\text{ch1}) = \text{Reward-Point} = (a \rightarrow b) + (b \rightarrow c) + (c \rightarrow d) + (d \rightarrow a)$$

$$= 10 + 10 + 5 + 5 = 30.$$

$$f(\text{ch2}) = (b \rightarrow d) + (d \rightarrow a) + (a \rightarrow c) + (c \rightarrow b)$$

$$= 20 + 5 + 20 + 10 = 55.$$

$$f(\text{ch3}) = (c \rightarrow d) + (d \rightarrow a) + (a \rightarrow b) + (b \rightarrow c)$$

$$= 5 + 5 + 10 + 10 = 30.$$

$$f(\text{ch4}) = (a \rightarrow b) + (b \rightarrow d) + (d \rightarrow c) + (c \rightarrow a)$$

$$= 10 + 20 + 5 + 20 = 55.$$

③ selection for mating-pool :-

roulette-wheel

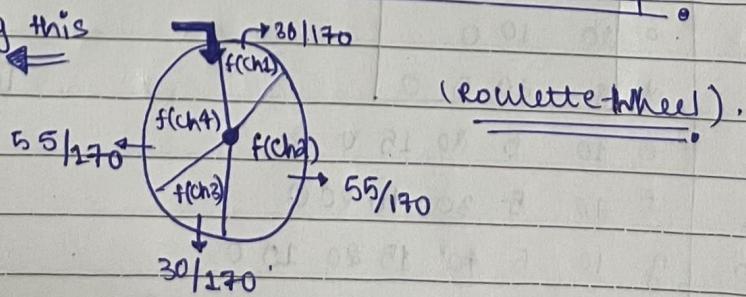
→ proportional-based-selection.

Process based on Darwin's-Principles.

④ Let's say, after rotating this wheel, we get (randomly).

Ch2
Ch4
Ch3
Ch1

Mating Pairs.



21/03/2025 (Previous Problem continued)...

① let's say $\begin{bmatrix} \text{ch2} \\ \text{ch4} \end{bmatrix}$ are selected.

$\begin{bmatrix} \text{ch3} \\ \text{ch4} \end{bmatrix}$

④ crossover-operation :- → chosen randomly.

Bisexual

one-point

crossover

$\begin{bmatrix} \text{ch1} & [0|1|1|1|1|0|1|0] \\ \text{ch4} & [0|0|0|1|1|1|1|0] \end{bmatrix} \Rightarrow \text{Offspring-1} = [0|1|1|1|1|1|1|0]$ (crossovers-chosen)

$\begin{bmatrix} \text{ch3} & [1|0|1|1|0|0|0|1] \\ \text{ch4} & [0|0|0|1|1|1|1|0] \end{bmatrix} \Rightarrow \text{Offspring-2} = [0|0|0|1|0|0|1|0]$

$\begin{bmatrix} \text{ch1} & [0|1|1|1|1|1|1|0] \\ \text{ch4} & [0|0|0|1|1|1|1|0] \end{bmatrix} \Rightarrow \text{Offspring-3} = [1|0|1|1|1|1|1|0]$

$\begin{bmatrix} \text{ch1} & [0|1|1|1|1|1|1|0] \\ \text{ch4} & [0|0|0|1|0|0|0|1] \end{bmatrix} \Rightarrow \text{Offspring-4} = [0|0|0|1|0|0|0|1]$

* NOTE :- How do you choose crossover-point?

↳ choose random-no. between 0 & 1. (for e.g. '0.5')

↳ Multiply it with size of chromosome (i.e.; 8)

$0.5 \times 8 = 4 \rightarrow$ it's the crossover.

⑤ mutation-rate = 0.05.

* For each attribute of chromosome,
we'll generate a random-no. $\stackrel{0 \times 1}{\text{blue}}$ mutation

• if random-no. > 0.05 (MR)

- No change.

• if random
no. $< MR$

= Mutation.

NOTE :- $0.05 \times (4 \times 8) = 1.6 \approx 2 \rightarrow$ ∵ max. '2' mutations can occur.

$$\therefore f(\text{Offspr.1}) = f(b, d, \cancel{a}, \overset{c}{\cancel{a}}, a)$$

*** (Smp.)

↳ No-repetitions-allowed -

$$f(\text{Offspr.2}) = f(a, b, \cancel{d}, \overset{a}{\cancel{c}}, c)$$

* replace with
the left-out

$$f(\text{Offspr.3}) = f(c, b, a, \overset{c}{\cancel{a}}, \overset{c}{\cancel{d}})$$

ones.

$$f(\text{Offspr.4}) = f(a, b, \cancel{a}, \overset{c}{\cancel{d}}, d)$$

- ⑥ Replace all in the actual chromosomes & calculate
Objective-functions of new-offspring :-

Offspr. 1 =

0	1	1	1	1	1	0	0	0
---	---	---	---	---	---	---	---	---

Offspr. 2 =

0	0	0	1	1	1	1	0
---	---	---	---	---	---	---	---

Offspr. 3 =

1	0	0	1	1	1	1	0	0
---	---	---	---	---	---	---	---	---

Offspr. 4 =

0	0	1	0	1	1	0	1	1
---	---	---	---	---	---	---	---	---

$$\therefore f(\text{Offspr. 1}) = f(b, d, c, a) = 20 + 5 + 20 + 10 = 55.$$

$$f(\text{Offspr. 2}) = f(a, b, d, c) = 10 + 20 + 5 + 20 = 55.$$

$$f(\text{Offspr. 3}) = f(c, b, d, a) = 10 + 20 + 5 + 20 = 55.$$

$$f(\text{Offspr. 4}) = f(a, b, c, d) = 10 + 10 + 5 + 5 = \boxed{30}.$$

- ⑦ optional) select chromosomes for next-iteration.

* Elitist-Solution \Rightarrow Offspr. 1 = b d c a



Offspr. 2 = a b d c

* NOTE *

→ These two
are same,
so choose
the second
best solution
from prev.
iteration.

Replace "worst"

-fit~~ness~~ -solution

with best-sol".

from prev.-iteration

Offspr. 3 = c b d a

Ch-4 = a b d c

chosen
from

roulette-wheel-
store from
prev. iteration.

↓
∴ replace
ch-4 by
ch-3.

- ⑧ Stopping-criteria :-

yes \Rightarrow Stop \Rightarrow return best-solution

No \Rightarrow Return to Step-03.

26/03/2025 Genetic - Algorithm

* out of 200 - features of a dataset, you have to select 6 features.

$$D = 200, d = 6$$

I. Initiation :- Binary integer character

chr. [6 | 38 | 49 | 109 | 179 | 16]

; Objective- f? calculated.

For e.g. TSP : 6 city

[a | b | c | d | e]

II. Selection of Mating-Pool :-

i. Random

ii. Proportional-Based (Roulette-Wheel).

↳ Disadvantage :- Dominance - ~~dominance~~ of certain-solution.

Ch1 96

Ch2 2

Ch3 0.5

Ch4 0.5

- of chromosomes

3. Tournament-Based → A small group is selected randomly & choose the best-solution.

↓
Disadvantage :-

4. Rank-based-solution

	obj.f's.	Rank	Weight (whichever like)
Ch1	96	1	10ways you
Ch2	2	2	8
Ch3	0.75	3	6
Ch4	0.25	4	4

* Probability of best-fit & worst-fit ~~80%~~ being in the small group are same.

III. Reproduction / Crossover-Operation :-

No. of Parents

(i) Asexual

(ii) Bisexual : Discussed

(iii) Multisexual

Probabilities : 0.3 0.7 0.4 0.8 0.2 0.8

RP = 0.6

mutat.
Rate

P1 : [1 | 0 | 0 | 1 | 1 | 1]

↓

[1 | 1 | 0 | 1 | 1 | 0]

[1 | 0 | 0 | 1 | 1]

[0 | 1 | 0 | 1 | 0]

[1 | 1 | 1 | 0 | 0]

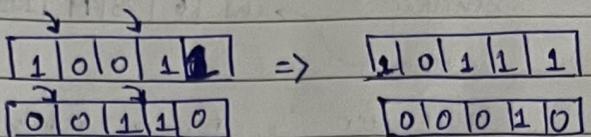
Offspring \Rightarrow 1 [1 | 1 | 0 | 0 | 0]

2 [1 | 0 | 0 | 1 | 0]

3 [0 | 1 | 1 | 1 | 1]

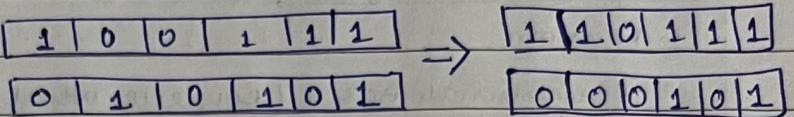
Point crossover

- ① One-Point
- ② Two-Point



- ③ Uniform-Crossover *

$$r_i \quad 0.1 \quad 0.4 \quad 0.8 \quad 0.6 \quad 0.3 \quad 0.2$$



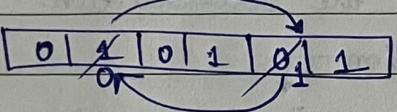
* if $MR < r_i$ = same
else = choose from
other parent.

IV. Mutation :-

1. Uniform

2. Inorder ~~shuffle~~

will take 2-passes. randomness. & interchange the values.



V. Selection of next-generation - chromosomes :-

1. All offsprings.

2. some percentage of best-parent-chromosomes, should be

3. Elitist - Method \rightarrow Best-Parent should be kept.
replace the worst-offspring.

4. Hall of fame.

VI. Stopping-criteria:-

1. After a certain - no. of steps.

2. when set of chromosomes (population-set) isn't going to change.

3. when best obj.fⁿ. stops changing.

28/03/2025

Differential Evolution :-1. Initialization \Rightarrow No. of Population = N.

Here, these are "population-vectors", "chromosomes"-term is used in genetic-algorithm.

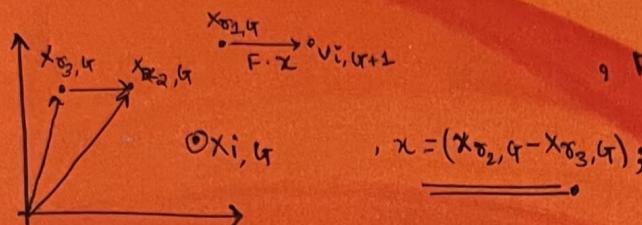
35	40	125	139	140	$x_{i,G}$
29	27	99	148	96	$x_{\tau_1,G}$
17	08	22	33	199	$x_{\tau_2,G}$
292	179	187	181	97	$x_{\tau_3,G}$

$d = 200$

$d = 5$

 $x_{i,G} = i^{\text{th}} \text{- population-vector of generation } G.$ 2. Mutation \Rightarrow For each population-vector $x_{i,G}$, calculate mutation-vector

$v_{i,G+1} = x_{\tau_1,G} + F(x_{\tau_2,G} - x_{\tau_3,G})$

where τ_1, τ_2, τ_3 are random-no. in b/w 1 & N & not equal to i .

$x = (x_{\tau_2,G} - x_{\tau_3,G})$

$0.1 < F < 2$

$$\begin{aligned} v_{i,G+1} &= [29 \ 27 \ 99 \ 148 \ 96] + \frac{1}{2} [175 \ -171 \ -165 \ -148 \ 202] \\ &= [-58 \ -56 \ 17 \ 74 \ 147]. \end{aligned}$$

Rectifying \Rightarrow ① remove & replace all negatives with random-no.s.

② If multiple-same no.s are there, just keep one & change others with some random-no.s.

3. Crossover \Rightarrow

$x_{i,G} = [35 \ 40 \ 125 \ 139 \ 140]$

$v_{i,G+1} = [85 \ 72 \ 17 \ 74 \ 147]$

crossover

$\text{rate} = 0.6$

(CR).

Trial Vector/

crossOver-Vector

$$\Rightarrow v_{ij,G+1} = \begin{cases} v_{ij,G+1}, & \text{if } \tau_i > CR. \\ x_{ij,G+1}, & \text{if } \tau_i \leq CR \end{cases}$$

$\rightarrow \tau_i \ 0.2 \ 0.4 \ 0.7 \ 0.9 \ 0.3$

$\therefore v_{ij,G+1} = [35 \ 40 \ 17 \ 74 \ 140]$

4. Selection \Rightarrow $x_{i,G+1} = \begin{cases} x_{i,G}, & \text{if } f(x_{i,G}) > f(v_{i,G+1}) \\ v_{i,G+1}, & \text{else.} \end{cases}$

Next-gener.
 i^{th} -populat.
vector.

Objective-fn's will be predefined by you or in question.

(contd.) \rightarrow (On next to next-section)

28/03/25

→ S.C.

* changes w.r.t Genetic Algorithms :-

- Mutations performed before crossover.
- Only 1-type of crossover-possible. (Asexual).
- search-space is found by difference in vector.
- selection-for-mating pool not required.
- only 1-type of 'selection'-possible.

variations of DE :-

- DE | rand | 1 → one-diff. operation.

Addition with one random vector.

$$v_{i,t+1} = x_{r_1,t} + F(x_{r_2,t} - x_{r_3,t})$$

- DE | rand | 2.

$$v_{i,t+1} = x_{r_1,t} + F_1(x_{r_2,t} - x_{r_3,t}) + F_2(x_{r_4,t} - x_{r_5,t})$$

- DE | Best | 1.

$$v_{i,t+1} = x_{best,t} + F(x_{r_2,t} - x_{r_3,t})$$

⇒ Amplification - Factor :-

$$0.1 < F < 2$$

reducing effect of Difference Vector maximizing effect of Difference Vector.

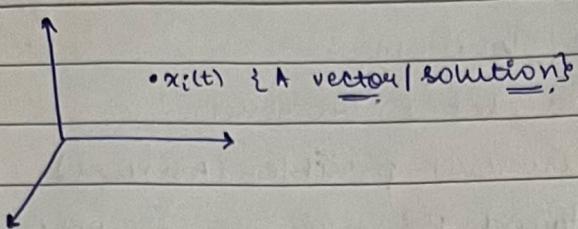
02/04/2025

Particle - swarm - Optimization :-

↪ Population-based Evolutionary Algorithm. mimicing the concept of fown of a swarm of birds.

↪ A particle improves its position by its own-experience and experience of swarm.

Let $x_i(t) \Rightarrow$ denotes position of particle 'i' at time 't'.



$$\therefore x_i(t+1) \Rightarrow x_i(t) + v_i(t+1) \quad (1)$$

$i = 1 \text{ to } N$, where N is the no. of particles in the swarm.

velocity :-

↳ derive the optimization process.

↳ reflects the experiential knowledge of the particle.

↳ socially exchange information from particle - neighbors.

$$x_i \in \mathbb{R}^D$$

① $v_i(t+1)$ = velocity of particle 'i' at time $t+1$.

(self-improvement)
cognitive component

$$\therefore v_{ij}(t+1) = v_{ij}(t) + c_1 \cdot r_{1j}(t) \cdot [y_{ij}(t) - x_{ij}(t)]$$

$$+ c_2 \cdot r_{2j}(t) \cdot [\hat{y}_{ij}(t) - x_{ij}(t)]$$

— (2)

↳ social component.

, $v_{ij}(t+1)$ = velocity of particle 'i' w.r.t dimension 'j' at time $t+1$.

y_i = the personal-best-position of particle 'i' since the first time step.

x_i = current-position of particle 'i'.

Minimization

Problem :- $y_i(t+1) = \begin{cases} y_i(t), & \text{if } f(x_i(t+1)) > f(y_i(t)) \\ x_i(t+1), & \text{if } f(x_i(t+1)) < f(y_i(t)) \end{cases}$

\hat{y} = global-best-position.

- the best-position

discovered by any of the particle so far.



, $f(\cdot) \Rightarrow$ Objective-funct.

(Minimization-f".)

$$\hat{y}(t) \in \{y_1(t), \dots, y_N(t) \mid f(\hat{y}(t)) = \min \{f(y_1(t)), \dots,$$

$\tau_{1j}, \tau_{2j} \Rightarrow$ random No. b/w 0 to 1.

$c_1, c_2 \Rightarrow$ Positive Acceleration-constant used to scale the contribution of the cognitive & social components respectively.

Algorithm :-

- Create & initialize a D-Dimensional swarm of N-particles, & initialize parameters c_1 & c_2 .
- Repeat
 - for each particle $i=1$ to N
 - { if $f(x_i) < f(y_i)$ then
 $y_i = x_i$
 - if $f(y_i) < f(\hat{y})$ then
 $\hat{y} = y_i$
- for each particle $i=1$ to N do
 - {
 - Update velocity using Eq.(2).
 - Update position using Eq.(1).
- until (stopping-criterion).

- ① All particles will move/incline towards global-best (will have one-component that) - position
- ② It's a problem as soln. will get trapped in local-optima so, it's called \downarrow
 - PSO with Gr.Best. :-
 - converge fast
 - lack of diversity
 - susceptible to get trapped into local-optima.

04/04/2025 * To tackle the problem of gbest PSO, we now study :-

① lbest - PSO :-

$$v_j(t+1) = \dots + \dots + c_{\alpha} r_{\alpha j} [\tilde{y}_{ij}(t) - x_{ij}(t)]$$

(Here ' j ' denotes the component
-int.)

$N_i \Rightarrow$ Nbrhd. of particle ' i '.
 \Rightarrow it contains 10-different
- nbs.

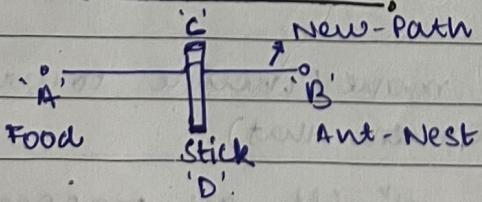
$$\tilde{y}_i \Rightarrow \tilde{y}_i \in \{y_i \mid y_i = \min(x_i \in N_i)\}$$

so, the Advantage of lbest :-

- ① Diversity \uparrow .
- ② less susceptible to be trapped in local-optima.
- ③ convergence lately (i.e., will take more time or more iterations to converge).

* lbest \Rightarrow local-best
gbest \Rightarrow global-best

Ant-colony Optimization :-



stigmergy : (how ants interact with each other).

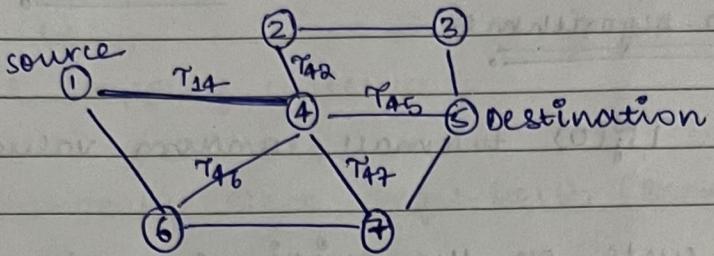
\rightarrow stigma \rightarrow sign
 \rightarrow ergon \rightarrow work

- ① The ants communicate via:- pheromone-trail
(pheromones-deposit ^{#Learnthesmarterway} on the path
from ants' body).

* Stigmergy = it's the mechanism that mediate animal-to-animal interaction.

→ ACO, :- proposed by Marco Dorigo.

suppose there's graph : $G(V, E)$ (we're finding the shortest path here).



$T_{ij}(t)$ = pheromone-concentration is associated with edge (i, j) .

* From the possible set of paths take whose ' T ' is large. $T_{ij}(0)$ = a very small random-no. (close-to-'0').

(i) Pheromone-Deposition } phe. conc.

(ii) Pheromone-Evaporation } depends on these '2'.



$$T_{ij}(t+1) = T_{ij}(t) \cdot (1 - \rho) ; \rho = \text{Evaporation-Rate.}$$

— (2)

* $\Delta T_{ij}^k(t)$ = Pheromone deposition by an ant 'k' at edge 'ij' at time 't'.

$\alpha \frac{1}{L^k(t)}$, L^k = length of path constructed by ant 'k'. {path-src to dest}.

Modification of ph. conc.

of an edge.

$$T_{ij}(t+1) = T_{ij}(t) + \sum_{k=1}^{n_k} \Delta T_{ij}^k(t)$$

* consider - short path. 1]

long path. 2]

consider both

ant have same
pheromone extract &
cover path in same
time. #learnthesmarterway

① longer path will have = pheromone extract & lesser depos.

$$* \quad \beta_{ij}^k(t) = \begin{cases} \gamma_{ij}^{\alpha}(t), & \text{if } j \in N_i^k \\ 0, & \text{if } j \notin N_i^k \end{cases}; \quad \alpha = \text{Amplific. factor.}$$

↑
transition
probability
(for taking decn.)

Nbrs. — (1).
(possible paths).

Determines which path an ant chooses to move to the nxt. node.

thus, ACO-Algorithm :-

[Initialize $\gamma_{ij}^k(0)$ to small random-value ($t=0$)

[Place n_k ants on the original node.

Repeat

for each ant $k=1$ to n_k do
 $x^k(t)=0$; # soln. for ant 'k'.

repeat

→ Select next-node based on probability calculated by eqn. (1).

→ Add edge (i,j) to $x^k(t)$.

→ until destination-node has been reached

* some soln's. may contain loops :

so :

Remove all loops from $x^k(t)$.

calculate path length $f(x^k(t))$;

End;

for each edge (i,j) of the graph do.

reduce the pheromone $\gamma_{ij}(t)$ using eqn (2)

End;

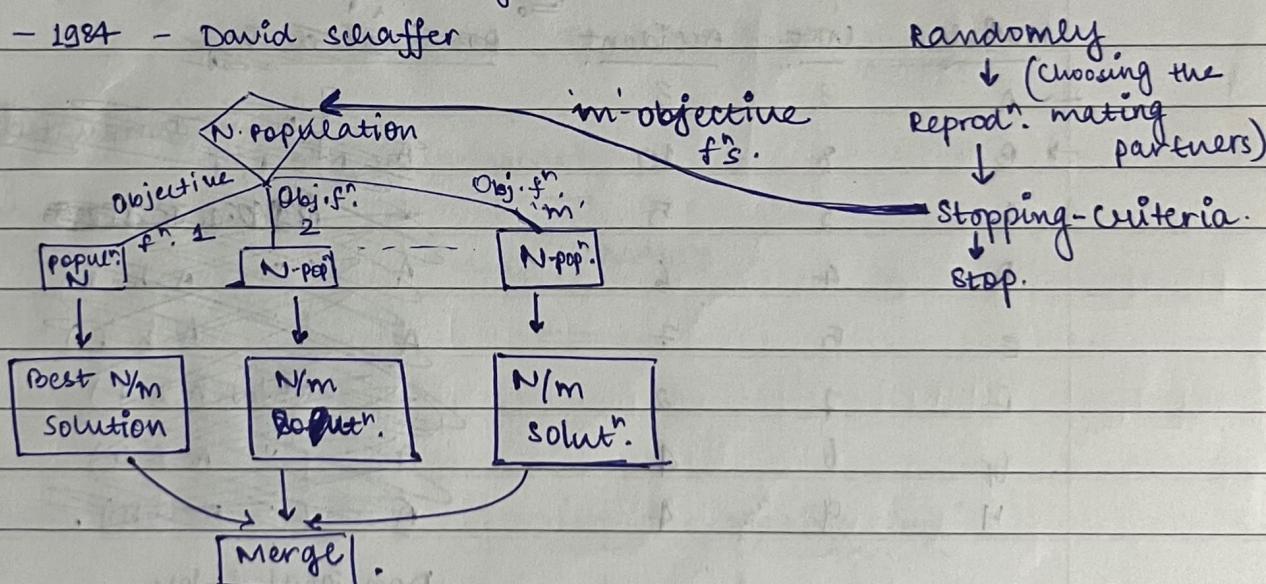
for each ant $k=1, \dots, n_k$ do.
 for each edge (i, j) of $x^k(t)$ do.
 $\Delta T_{ij}^k = \frac{1}{f(x^k(t))}$.
 update T_{ij} using eq. ①.
End;
 $t = t + 1$;
until stopping criteria;

NOTE :- * Evolutionary - Algos. Engel-Berth (BOOK). {for all Algos.}.

07/04/2025 Multi-Objective-Function :-

* Vector-Evaluated-Genetic-Algorithm (VEGA)

- 1984 - David Schaffer



- 1896 - Vilfredo Pareto \Rightarrow for multi-objective-fns., there is a set

⊗ of solutions, not a single-solution.

The Pareto-optimal front is the set of all non-dominated solutions — the "best trade-offs" among the objectives.

A solution is non-dominated (or Pareto-optimal) if no other solution is better in all objectives.

✓ \Rightarrow for multi-obj. fn., the optimal set contains a set of solutions, where each element is not dominated by any other sol. on the search space w.r.t. any of the obj. func.

* Dominated and Non-Dominated - Solution :-

Let there be m - obj. fⁿ, \rightarrow (minimization)

$$f_i(\cdot), i=1 \text{ to } m.$$

NOTE: In minimization problem, this'll be vice-versa.

Let there be two-solutions u^1 & u^2 . u^1 will dominate u^2 if following conditions satisfy.

$$\textcircled{1} \quad f_i(u^1) \nleq f_i(u^2), \text{ i.e., } f_i(u^1) \geq f_i(u^2), i=1 \text{ to } m.$$

$$\textcircled{2} \quad \text{Atleast one-objective-} f^n.$$

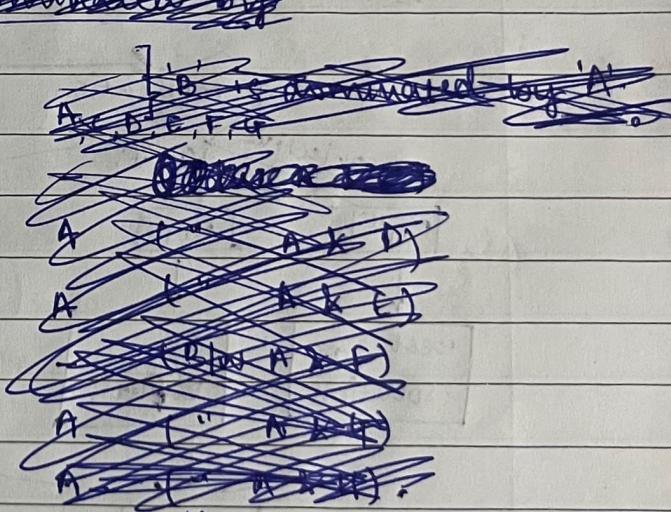
$$f(u^1) > f(u^2).$$

For e.g. car-data-set :-

pareto-

(Q.) Find optimal set for this problem?

Model	Cost	Accident
A	3	3
B	8	10
C	2	5
D	4	6
E	5	7
F	7	8
G	6	4
H	9	4



Dominated-by

A, C, D, E, F, G

(A)

(B)

(C)

(D)

(E)

(F)

(G)

A, C

A, C, D

A

A, F, G

Pareto
Optimal
set
 $\Rightarrow \{A, C, F\}$

because

these are

not

dominated by anyone.

- Weighted-sum-Approach := (Achibonghi & Murata, 1996).

$$m - \text{Obj. f}^n. \quad f_i(\underline{x}) \quad i=1 \text{ to } m$$

Population = N.

Pareto-optimal set contains 'n-solutions'.

Keep - n - solution seperately and (N-n) - chromosomes.

\underline{x} \Rightarrow chromosome.

$$\begin{aligned} f(\underline{x}) &= w_1 f_1(\underline{x}) + w_2 f_2(\underline{x}) + \dots + w_m f_m(\underline{x}) \\ &= \sum_{i=1}^m w_i \cdot f_i(\underline{x}). \end{aligned}$$

$$w_i = \frac{r_i}{\sum_{i=1}^m r_i} ; \quad r_1, r_2, \dots, r_m \Rightarrow \text{random-Number.}$$

$$\begin{array}{l} \text{-tive} \\ \text{relative} \\ \text{fitness} \\ \text{value} \\ \text{of the} \\ \text{chromosome.} \end{array} \quad \begin{array}{l} p(\underline{x}) = f(\underline{x}) - f_{\min}(\text{current}) \\ \hline \sum_{x \in \text{current}} \{f(x) - f_{\min}(\text{current})\} \end{array}$$

After this, we go for "Selection for mating-Pool".

Crossover



Mutation



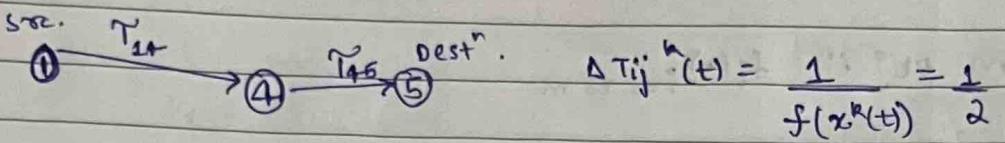
$\rightarrow (N-n)$ offsprings

+ n pareto-optimal-sol:



N-solution.

In ACO (studied prev.):



* Here, it's a unit-edge.

$$f(x^k(t)) = \text{Path-length} = 1+1=2$$

$$\tilde{T}_{14}(t+1) = \tilde{T}_{14}(t) + \Delta \tilde{T}_{14}^k(t)$$

for k^{th} -ant,
pheromone
density on
this path.

* In weighted-edge-graph; $f(x^k(t)) = 5+10=15$.

$$\boxed{\Delta \tilde{T}_{ij}^k(t) = \frac{w_{ij}}{f(x^k(t))}}$$

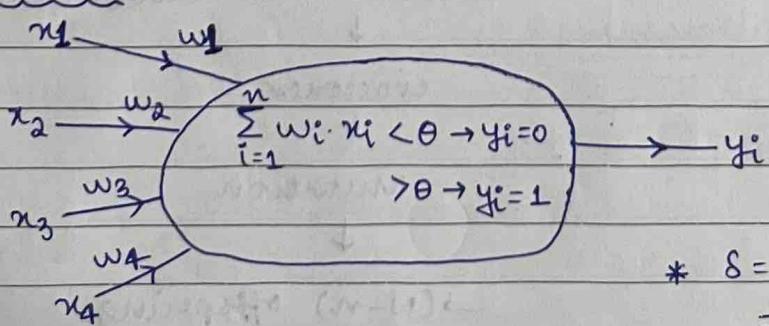
$$\tilde{T}_{14}(t+1) = \tilde{T}_{14}(t) + \frac{5}{15}$$

$$\tilde{T}_{45}(t+1) = \tilde{T}_{45}(t) + \frac{10}{15}$$

11/04/25. ① Taught through slides... (Neural-Networks)

16/04/25. ANN (Artificial-Neural-Network):

Perception:



$$\begin{aligned} * \quad \delta &= \text{Actual - Predicted} \\ &= y_i - \hat{y}_i \end{aligned}$$

$$① \quad w_i^o(t+1) = w_i^o(t) + \Delta w_i^o$$

$$\{ \Delta w_i^o = \eta \delta x_i \}$$

η = Learning-Rate (constant parameter)
 δ = error = $y_i - \hat{y}_i$

Eg:- AND

x_1	x_2	y
0	0	0
0	1	0
1	0	0
1	1	1

Assume: $\theta = 1.5$, $\eta = 0.5$.Iteration-01. :- ① $w_1 = 0, w_2 = 1 \mid x_1 = 0 = x_2$

$$\sum w_i \cdot x_i = 0 + 0 = 0 < 1.5 \Rightarrow y = 0.$$

$$\delta = 0 - 0 = 0$$

\therefore no changes in the output.

② $x_1 = 0, x_2 = 1 \mid w_1 = 0, w_2 = 1$

$$\sum w_i \cdot x_i = 1 < 1.5 \Rightarrow y = 0.$$

$\therefore \delta = 0 - 0$, no change.

③ $x_2 = 0, x_1 = 1; w_1 = 0, w_2 = 1$

$$\sum w_i \cdot x_i = 0 \xrightarrow[1.5]{\wedge} y = 0 \quad \therefore \delta = 0 - 0 = 0$$

\therefore NO change

④ $x_1 = 1, x_2 = 1 \mid w_1 = 0, w_2 = 1$

$$\sum w_i \cdot x_i = 1 < 1.5 \Rightarrow y = 0.$$

$$\therefore \delta = 1 - 0 = 1,$$

$$\therefore w_1 = 0 + 0.5(1)(1) = \underline{0.5}$$

$$w_2 = 1 + 0.5(1)(1) = \underline{1.5}.$$

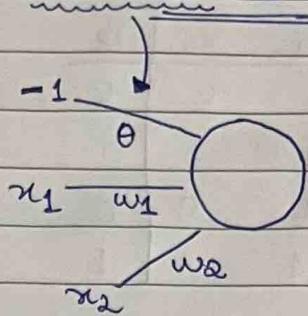
Iteration-02 :- $w_1 = 0.5, w_2 = 1.5$.

- If η is very high, ' w_i '-value will fluctuate b/w values.

- If η is very small, it'll take very long time to converge to actual-value.

⇒ Except the i/p-node, there's a bias node as well &

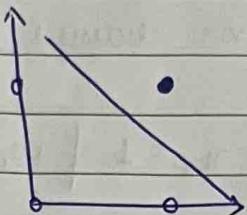
$$\begin{aligned} \text{i/p-value} &= -1 \\ \text{weight} &= \theta \end{aligned}$$



$$\sum_{i=1}^n w_i \cdot x_i < \theta$$

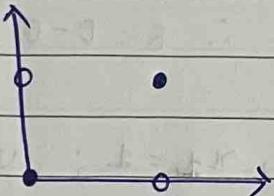
$$\sum_{i=1}^n w_i \cdot x_i - \theta < 0$$

→ AND-Gate

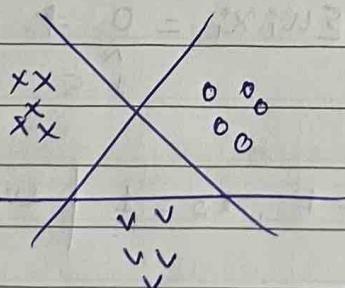


→ can be separated using single-perceptron.

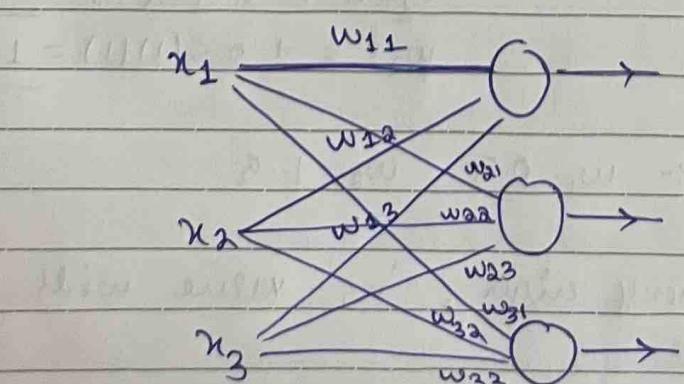
→ XOR



→ can't be separated using a single-perceptron.



⇒ Multiple-Neurons



- Multi-layer gives convex-regⁿ. as o/p.
- 2-convex-regⁿ. give concave-regⁿ. as o/p.

O/p.