

Bitwise Not Operator

◆ STEP 1: Convert the number to binary

Take the number:

5

Binary of 5 is:

101

👉 Computers don't work with just 3 bits, they use **fixed size bits** (8 bits, 32 bits, etc.).

So we write 5 in **8-bit binary**:

5 = 00000101

(Leading zeros are normal and important.)

◆ STEP 2: Apply bitwise NOT (~) → 1's complement

~ means **flip every bit**:

- 0 → 1
- 1 → 0

So flip **each bit** of 00000101:

Original (5): 00000101

After ~ (flip): 11111010

👉 This result is called **1's complement**.

⚠ Important:

- This is **NOT the final answer yet**
 - This binary represents a **negative number**, but computers use **2's complement**, not 1's.
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◆ STEP 3: Why 2's complement is needed

Computers store **negative numbers** using **2's complement**, not 1's complement.

So when Python sees:

11111010

it treats it as a **2's complement negative number**.

To understand its value, we must interpret it using **2's complement rules**.

◆ **STEP 4: Convert to 2's complement (to find the value)**

To find the decimal value of a **negative 2's complement number**, do this:

Rule:

1. Take **1's complement**
 2. Add **1**
 3. Convert to decimal
 4. Add a **minus sign**
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Apply to our number:

Binary we got:

11111010

1 Take 1's complement (flip again):

00000101

2 Add 1:

00000101

+ 1

00000110

3 Convert to decimal:

00000110 = 6

4 Add minus sign:

-6

✓ FINAL ANSWER

~5 = -6

◆ **VERY IMPORTANT SHORTCUT (Python rule)**

Instead of doing all these steps every time, Python follows this **always-true formula**:

$$\sim x = -(x + 1)$$

So:

$$\sim 5 = -(5 + 1) = -6$$

$$\sim 3 = -(3 + 1) = -4$$

$$\sim 0 = -(0 + 1) = -1$$

◆ **Why this works (intuitive explanation)**

- \sim flips bits (1's complement)
- Python stores negatives using 2's complement
- 2's complement mathematically equals $-(x + 1)$

That's why the formula works **every time**.

🔑 **FINAL MEMORY POINTS (please remember these)**

1. Convert number to binary
2. \sim flips all bits \rightarrow 1's complement
3. Python uses **2's complement** for negatives
4. Therefore:

$$\sim x = -(x + 1)$$

🔑 **KEY IDEA (this decides everything)**

In **2's complement representation** (which Python uses):

The leftmost bit (MSB – Most Significant Bit) decides the sign

- 0 \rightarrow **Positive number**
- 1 \rightarrow **Negative number**

This leftmost bit is called the **sign bit**.

◆ **Step 1: Look at the binary after \sim**

From your example:

After \sim (flip): 11111010

Now look at the **leftmost bit**:

1 1111010

↑

sign bit

👉 The sign bit is **1**

✅ That means this number is **NEGATIVE**

That's how we determine it.

♦ **Step 2: Why does 1 mean negative?**

Because computers use **2's complement** to store signed integers.

In 2's complement:

Sign bit Meaning

0 Positive or zero

1 Negative

This rule is **fixed** in computer systems.

♦ **Now let's map this to your question**

❓ **"If in 1's complement when it is 0 or 1 what to do?"**

✅ **Correct interpretation:**

- If **leftmost bit = 0**
 - number is **positive**
 - **STOP**
 - convert directly to decimal
- If **leftmost bit = 1**
 - number is **negative**
 - **MUST take 2's complement**
 - then convert to decimal
 - add minus sign

🔑 **FINAL ANSWER** (memorize this)

If sign bit is 1 → take 2's complement

If sign bit is 0 → do NOT take 2's complement

♦ **First: What is "zero" in decimal?**

In normal math, **zero is only one value**:

0

There is **no +0 and -0** in real life math.

◆ **Now see what happens in 1's complement**

Assume **8-bit numbers** (just for understanding).

Positive zero

00000000 → 0

Rule of 1's complement

Negative = flip all bits

So flip 00000000:

11111111

This is treated as **negative zero** in 1's complement.

✗ **Result in 1's complement**

Binary	Meaning
00000000	+0
11111111	-0

👉 **Two different binaries for zero**

👉 This is what “two zeros” means ✗

◆ **Why is this BAD?**

Because now the computer has to handle:

- +0
- -0

Questions like:

- Is +0 equal to -0?
- Which zero should I store?

- Which zero should I print?

This **confuses hardware and logic**.

◆ Now see 2's complement (this fixes it)

Rule of 2's complement

Negative = (flip bits) + 1

Let's try to make **-0**.

Start with zero:

00000000

Flip bits (1's complement):

11111111

Add 1:

11111111

+ 1

00000000

✅ **Result in 2's complement**

Binary	Meaning
00000000	0

👉 There is **NO separate -0**

👉 Both +0 and -0 collapse into **ONE zero**

🔑 **THIS is what “only one zero” means**

- **1's complement** → two ways to write zero ❌
 - **2's complement** → only one way to write zero ✅
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 **One-line understanding (memorize this)**

**In 2's complement, there is no -0.
Only 00000000 represents zero.**

? Does computer always use 2's complement?

✓ Yes. All modern computers and Python use 2's complement, exactly because:

- one zero only
 - simpler arithmetic
 - simpler hardware
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Summary:

1's complement means:

Flip every bit

- $0 \rightarrow 1$
- $1 \rightarrow 0$

2's complement means:

1's complement + 1