

#### Program 4

Consider S and T as variables and the following relation representing the relationships:

a:  $\neg(S \vee T)$

b:  $(S \wedge T)$

c:  $T \vee \neg T$

d:  $\neg(S \wedge S)$

e:  $\neg S \vee \neg T$

Analyse the following for PL-TT entailment and show whether

(i). 'a' entails 'b',

(ii). 'a' entails 'c',

(iii). 'a' entails 'd' and

(iv). 'a' entails 'e'

```
1  N = 4
2  def main():
3
4      s = [1,0,1,0]
5      t = [1,1,0,0]
6      a=[]
7      b=[]
8      c=[]
9      d=[]
10     e=[]
11
12
13     for i in range(N):
14         a.append(not(s[i] or t[i]))
15         b.append(bool(s[i] and t[i]))
16         c.append(bool(t[i] or (not(t[i]))))
17         d.append(not(bidir(s[i],s[i])))
18         e.append(imp((not(s[i])),(not(t[i])))))
19     print("Truth table of a: ",a)
20     print("Truth table of b: ", b)
21     print("Truth table of c: ", c)
22     print("Truth table of d: ", d)
23     print("Truth table of e: ", e)
24
25     p=entails(a, b)
26     q=entails(a,c)
27     r=entails(a, d)
28     s=entails(a, e)
29     print("a entails b: ",p)
```

```

30     print("a entails c: ", q)
31     print("a entails d: ", r)
32     print("a entails e: ", s)
33
34
35
36
37 ▾ def imp(j,k):
38     return (not(j)) or k
39
40 ▾ def bidir(j,k):
41     return (imp(j,k) and imp(j,k))
42
43
44 ▾ def entails(m,n):
45 ▾     #for i in j:
46 ▾     for i in range(N):
47 ▾         for j in range(N):
48 ▾             if (m[i] and n[j]== 1):
49 ▾                 if(i==j):
50 ▾                     return "yes"
51 ▾                 break
52
53     return "NO"
54
55
56
57
58 ▾ if __name__ == '__main__':

```

```

59     main()

```

Output

```

Truth table of a:  [False, False, False, True]
Truth table of b:  [True, False, False, False]
Truth table of c:  [True, True, True, True]
Truth table of d:  [False, False, False, False]
Truth table of e:  [True, False, True, True]
a entails b:  NO
a entails c:  yes
a entails d:  NO
a entails e:  yes

```