

Quiz 4

Name: Key

You must show your work to get full credit.

Consider the rate equation

$$\frac{dN}{dt} = -.05N(N-5)(N-15)$$

1. If $N(3) = 12$, what is $N'(3)$?

$N'(3) = \underline{12.6}$

$$\begin{aligned} N'(3) &= -.05N(3)(N(3)-5)(N(3)-15) \\ &= -.05(12)(12-5)(12-15) \\ &= 12.6 \end{aligned}$$

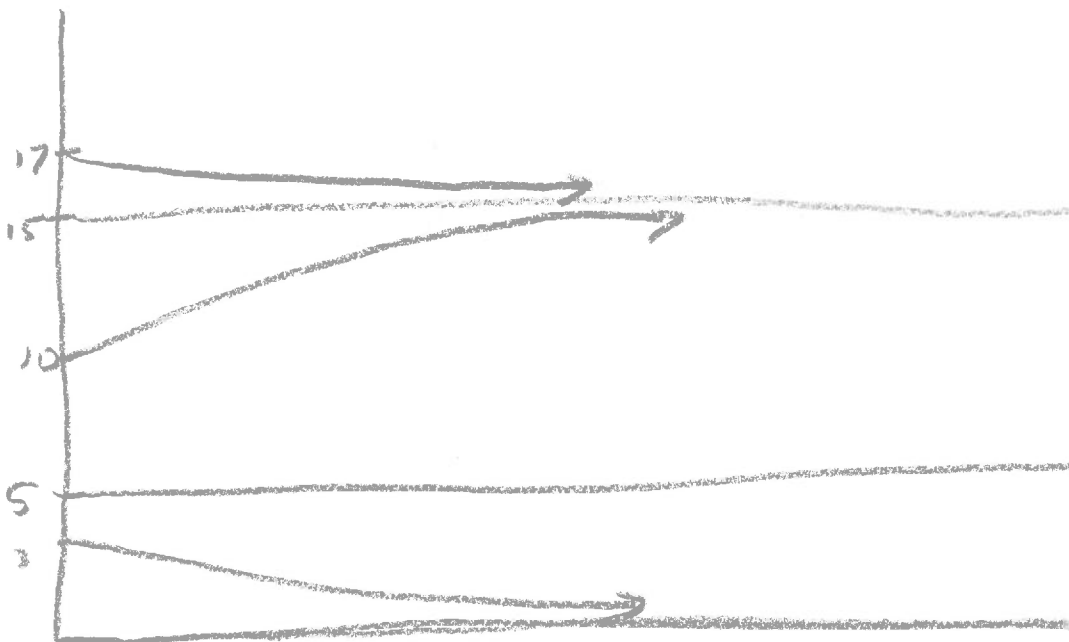
2. What are the rest points of the equation?

Rest points are: 0, 5, 15

solve $-.05N(N-5)(N-15)$

to get $N = 0, 5, 15$

3. Make a picture showing the rest solutions, the solution with $N(0) = 3$, the solution with $N(0) = 10$ and the solution with $N(0) = 17$.



$$\begin{aligned} N' &< 0 \\ 10 \\ N &\searrow \end{aligned}$$

$$\begin{aligned} N' &> 0 \\ 10 \\ N &\nearrow \end{aligned}$$

$$\begin{aligned} N' &< 0 \\ 10 \\ N &\searrow \end{aligned}$$

4. If $N(0) = 3$ estimate $N(100)$.

$N(100) \approx \underline{0}$

This solution decreases to 0

5. If $N(0) = 10$ estimate $N(143)$.

$N(143) \approx \underline{15}$

This solution increases to 15