

# Mathematics 172

Quiz #2

Name: Key

*You must show your work to get full credit.*

A cell has volume  $V = 5.2 \times 10^{-6} \text{mm}^3$  and surface area  $A = 7.5 \times 10^{-3} \text{mm}^2$ . Assume that oxygen,  $O_2$ , passes through the cell membrane at a rate of  $.38(\text{mg}/\text{mm}^2)/\text{hr}$ .

1. What is the total amount of  $O_2$  that is coming into the cell per hour?

$$\begin{aligned} \text{Amount of } O_2/\text{hour is } & \underline{.00285 \text{ mg/hr}} \\ = (\text{rate}) \times (\text{Area}) & = (.38)(7.5 \times 10^{-3}) = .00285 \text{ mg/hr} \end{aligned}$$

2. What is the amount of  $O_2$  per volume coming into the cell per hour?

$$\begin{aligned} \text{Amount of } O_2 \text{ per volume per hour is } & \underline{548.1 (\text{mg/hr})/\text{mm}^3} \\ \text{Divide answer to 1 by volume} & \\ = \frac{.00285}{5.2 \times 10^{-6}} & = 548.1 (\text{mg/hr})/\text{mm}^3 \end{aligned}$$

3. If the cell needs  $58(\text{mg}/\text{mm}^3)/\text{hr}$  of  $O_2$  to survive, then how much can it be magnified before it dies from lack of oxygen?

Let  $a = \text{magnification factor}$ . Computing by a factor of 9.45  
as above

$$V_{\text{mag}} = 5.2 \times 10^{-6} a^3 \text{mm}^3$$

$$A_{\text{mag}} = 7.5 \times 10^{-3} a^2 \text{mm}^2$$

$$(\text{Amount } O_2)_{\text{mag}} = .00285 a^2 \text{ mg/hr.}$$

$$(\text{Amount of } O_2/\text{vol})_{\text{mag}} = \frac{.00285 a^2}{5.2 \times 10^{-6} a^3} = \frac{548.1}{a} (\text{mg}/\text{mm}^3)/\text{hr}$$

The cut off is

$$\frac{548.1}{a} = 58 \quad \text{so} \quad a = \frac{548.1}{58} = 9.45$$