

Quiz 14

Name: Key.*You must show your work to get full credit.*

Let $A(t)$ be the number of grams of algae after t days in a bucket left out in the sun. Assume that

$$\frac{dA}{dt} = .12A \left(1 - \frac{A}{135} \right).$$

1. If $A(7) = 150$ then what is $A'(7)$?

$$A'(7) = \underline{-2}$$

$$\begin{aligned} A'(7) &= .12 A(7) \left(1 - \frac{A(7)}{135} \right) \\ &= .12 (150) \left(1 - \frac{150}{135} \right) \\ &= -2 \end{aligned}$$

2. If $A(7) = 150$ then estimate the following:

$$A(7.5) \approx \underline{149.}$$

In these problems we use the approximation

$$\begin{aligned} A(x) &\approx A(7) + A'(7)(x-7) \\ &= 150 - 2(x-7) \end{aligned}$$

$$A(7.1) \approx \underline{149.8}$$

$$\begin{aligned} \text{So } A(7.5) &\approx 150 - 2(7.5-7) \\ &= 149 \end{aligned}$$

$$A(6.8) \approx \underline{150.4}$$

$$\begin{aligned} A(7.1) &\approx A(7) + A'(7)(7.1-7) \\ &= 150 - 2(7.1-7) \\ &= 149.8 \end{aligned}$$

$$\begin{aligned} A(6.8) &\approx A(7) + A'(7)(6.8-7) \\ &= 150 - 2(6.8-7) \\ &= 150.4 \end{aligned}$$