

# Mathematics 122

Quiz #20

Name: Key

*You must show your work to get full credit.*

Let  $a$ ,  $b$  and  $c$  be constants. Compute the following derivatives.

(1)  $y = 3(x^2 + 7)^5$   $y' = \underline{6x(x^2 + 7)^4}$   
 $y' = \underline{3(x^2 + 7)^4 (2x)}$  both are ok →

(2)  $f(t) = 4e^{2t^3 + 3t^2}$   $f'(t) = \underline{24(t^2 + t)e^{2t^3 + 3t^2}}$   
 $f'(t) = 4e^{2t^3 + 3t^2} (6t^2 + 6t)$  ↖ both are ok.

(3)  $w = 6 \ln(e^z + 1)$   $\frac{dw}{dz} = \underline{\frac{6e^z}{e^z + 1}}$   
 $\frac{dw}{dz}$

(4)  $A(r) = a\sqrt{1-r^2} = a(1-r^2)^{\frac{1}{2}}$   $A'(r) = \underline{-r(1-r^2)^{-\frac{1}{2}}}$   
 $A'(r) = \underline{\frac{a}{2}(1-r^2)^{-\frac{1}{2}}(-2r)}$  ↖ both are ok.

(5)  $y = be^{\frac{1}{x}} + c \ln(3x+2)$   $\frac{dy}{dx} = \underline{-bx^{-2}e^{x^{-1}} + \frac{3c}{3x+2}}$   
 $= be^{x^{-1}} + c \ln(3x+2)$  ↖  
 $\frac{dy}{dx} = be^{x^{-1}}(-1)x^{-2} + \frac{c \cdot 3}{3x+2}$  both are ok.