

You must show your work to get full credit.

A group 13 annual cicadas get blown by a storm onto an island that has no cicadas. Ten years later there are 73 cicadas on the island.

1. What is per capita growth rate of the cicadas population?

$$P_t = P_0 \lambda^t = 13 \lambda^t$$

$$r = \underline{.1883}$$

We know

$$P_{10} = 13 \lambda^{10} = 73$$

$$\lambda^{10} = 73/13$$

$$\lambda = (73/13)^{(1/10)} = 1.1883$$

$$\text{So } r = \lambda - 1 = .1883$$

2. How long until the cicadas population reaches 1,000?

Solve

Time to a thousand cicadas: 25.172 or round up to 26.

$$P_t = 13(1.1883)^t = 1,000$$

$$(1.1883)^t = 1000/13$$

$$t \ln(1.1883) = \ln(1000/13)$$

$$t = \ln(1000/13) / \ln(1.1883) \\ = 25.172$$