Quiz 23

Name: Key

You must show your work to get full credit.

For the predator-prey system

$$\frac{dx}{dt} = rx\left(1 - \frac{x}{K}\right) - sxy$$
$$\frac{dy}{dt} = -uy + vxy$$

where

x =size of prey population,

y = size of predator population,

r = per capita growth rate of x-species,

K = carrying capacity of x -species with no predators,

u = per capacity death rate of y-species without any prey,

s, v = constants that tell the rate of interaction between the two species.

For the system

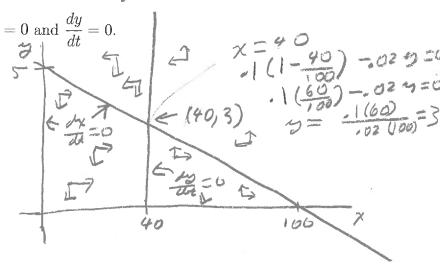
$$\frac{dx}{dt} = .1x\left(1 - \frac{x}{100}\right) - .02xy = \chi\left(.1\left(\frac{\chi}{100}\right) - .02y\right) = 0$$

$$\frac{dy}{dt} = -.4y + .01xy = \chi\left(-.4 + .01\chi\right) = 0$$

1. Draw the phase plane showing where $\frac{dx}{dt} = 0$ and $\frac{dy}{dt} = 0$. $\chi = 0 \Rightarrow \frac{1}{\sqrt{3}} = 0$ (0, 5) is $\frac{1}{\sqrt{3}} = 0$

 $\frac{(100,0)}{-.4 + .01} = 40$ $x = \frac{-.4}{.01} = 40$

2. What are the rest points?



Rest points are (0,0), (40,0), (40,3)

3. Draw in arrows in each region that show what directions the points are moving.