

Mathematics 122

Quiz #34

Name:

100%

You must show your work to get full credit.

- 2 pts (1) Let b be a constant. Show $F(x) = 2bx^3$ is an antiderivative of $f(x) = 6bx^2$.

This means we want to show

$$F'(x) = f(x). \text{ But}$$

$$F'(x) = (2bx^3)' = 3 \cdot 2bx^2 = 6bx^2 = f(x)$$

as required

3 pts

- (2) Compute $\int_0^2 6bx^2 dx$.

16b

From the fundamental theorem of calculus

$$\int_a^b f(x) dx = F(b) - F(a)$$

In our case this becomes

$$\begin{aligned} \int_0^2 6bx^2 dx &= 2bx^3 \Big|_0^2 = 2b(2)^3 - 2b(0)^3 \\ &= 16b \end{aligned}$$