

*You must show your work to get full credit.*

1. Let  $f(x) = x^3 - 12x + 1$ .

(a) Find the critical points.

solve

$$f'(x) = 3x^2 - 12$$

$$= 3(x^2 - 4)$$

$$= 3(x-2)(x+2) = 0$$

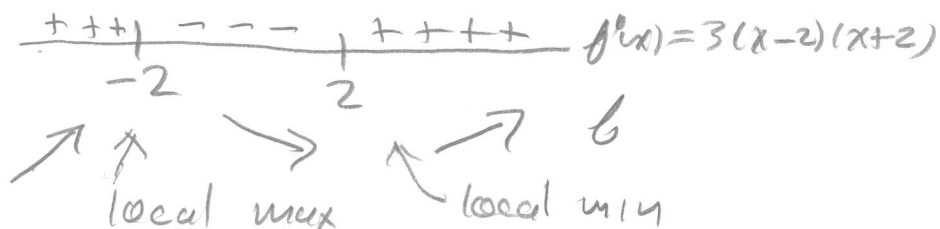
$$x = 2, -2$$

Critical points are: 2, -2

(b) Classify the critical points as to being local maximizers or local minimizers.

The local maximizers are: -2

Method 1



The local minimizers are: 2

Method 2

$$f''(x) = 6x$$

$$f''(-2) = -12 < 0 \text{ concave down } \wedge \text{ so local max}$$

$$f''(2) = 12 > 0 \text{ concave up } \vee \text{ so local min}$$