

Quiz #10

Name: key

You must show your work to get full credit.

1 pt

(1) Let $f(x) = \frac{x^2 - 1}{2x - 3}$.

(a) What is the derivative $f'(2)$?

$f'(2) = \underline{-2.00001}$ Or just -2.0

$$\text{N Deriv } ((x^2 - 1)/(2x - 3), x, 2) = -2.00001$$

1 pt

(b) What is tangent line to $y = f(x)$ at $x = 2$?

$$y_0 = f(2) = \frac{2^2 - 1}{2(2) - 3} = \frac{3}{1} = 3$$

$$x_0 = 2$$

$$\text{so } y - y_0 = m(x - x_0)$$

$$\text{Recall } y - 3 = -2(x - 2)$$

$$\begin{aligned} y &= 3 - 2(x - 2) \\ y - 3 &= -2(x - 2) \\ y &= -2x + 7 \end{aligned}$$

any
of
these
ok.(2) Assume that weight, W , in grams of a cricket is a function of its length, L , in millimeters. That is $W = f(L)$.

1 pt

(a) What are the units for the derivative $\frac{dW}{dL} = f'(L)$?gram/mm.

2 pts

(b) If $f(15) = .8$ and $f'(15) = .05$ give an estimate for $f(15.4)$.

$$\Delta L = 15.4 - 15$$

$$= .4$$

$$f'(15.4) \approx \underline{.82}$$

$$\Delta W \approx f'(15) \Delta L$$

$$= (.05)(.4)$$

$$= .02$$

1 pt for writing
some form of
this.

$$\text{so } f(15.4) \approx f(15) + \Delta W$$

$$= .8 + .02 = .82$$