

Quiz #21

Name: Key

You must show your work to get full credit.

These first problems are just to see if you have learned the derivatives of the basic functions.

Let a, b, c, k be constants. Compute the following derivatives.

1. $y = \ln(x)$.

$y' = \frac{1}{x}$

2. $w = e^z$.

$\frac{dw}{dz} = e^z$

3. $y = 5^x$

$y' = 5^x \ln(5)$

4. $f(x) = \frac{1}{x^2} + 5\sqrt{x}$.

$= x^{-2} + 5x^{\frac{1}{2}}$

$f'(x) = -2x^{-3} + \frac{5}{2}x^{-\frac{1}{2}}$

5. $s(t) = 8 \ln(2t + 1)$.

$s'(t) = 8 \frac{1}{2t+1} (2) = \frac{16}{2t+1}$

6. $h(w) = (w^4 - 2w)^5$

$h'(w) = 5(w^4 - 2w)^4 (4w^3 - 2)$

7. $f(t) = 2te^t$

$f'(t) = 2e^t + 2te^t$

$f'(t) = 2e^t + 2te^t = (2+2t)e^t$

8. $w(r) = \frac{ar^2}{b+r^3}$

$w'(r) = \frac{2abr - 4ar^4}{(b+r^3)^2}$

$w' = \frac{(ar^2)'(b+r^3) - ar^2(b+r^3)'}{(b+r^3)^2}$

$= \frac{2ar(b+r^3) - ar^2(3r^2)}{(b+r^3)^2} = \frac{2abr + 2ar^4 - 6ar^4}{(b+r^3)^2}$

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