HOMEWORK #1

Software Project (0368-2161)

Due Date: 24/04/2022

1 Introduction

The K-means algorithm is a popular clustering method for finding a partition of N unlabeled observations into K distinct clusters, where K is a parameter of the method. In this assignment you will implement this algorithm in both Python and C. The goals of the assignment are:

- Practice the material taught in class both for C and Python.
- Transform a known algorithm into working executable code.
- Read input and process it.
- Work with files.
- Create an interface for programs.
- Experience the difference in the programming effort and the running time of both languages.

K-means 1.1

Given a set of N datapoints $x_1, x_2, \ldots, x_N \in \mathbb{R}^d$, the goal is to group the data into $K \in \mathbb{N}$ clusters, each datapoint is assigned to exactly one cluster and the number of clusters K is such that 1 < K < N. We will denote the group of clusters by S_1, S_2, \ldots, S_K , each cluster S_j is represented by it's centroid which is the mean $\mu_i \in \mathbb{R}^d$ of the cluster's members.

Algorithm 1 k-means clustering algorithm

- 1: Initialize centroids $\mu_1, \mu_2, \dots, \mu_K$ as first k datapoints x_1, x_2, \dots, x_K
- 2: repeat
- for $x_i, 0 < i < N$: 3:
- Assign x_i to the closest cluster S_j : argmin $(x_i \mu_j)^2$, $\forall j \ 1 \leq j \leq K$ 4:
- for μ_k , 0 < k < K: 5:

$$\sum_{x \in S} x$$

- Update the centroids: $\mu_k = \frac{\displaystyle\sum_{x_l \in S_k} x_l}{|S_k|}$ 6:
- 8: **until** convergence: ${}^{1}(\|\Delta\mu\|_{2} < \epsilon) \ OR \ (iteration_number = max_iter)$

¹ $\|\Delta\mu\|_2$: Euclidean Norm for each one of the centroids doesn't change more than ϵ . More Info: Euclidean Norm

2 Assignment Description

Implement the k-means algorithm as detailed in 1.1 both in C and Python. The behavior of the program is as follows:

- 1. The program receives the input: K, filename and optional(max_iter):
 - (a) K the number of clusters required.
 - (b) input_filename *.txt file that contains datapoints separated by commas.
 - (c) output_filename *.txt file that contains the centroids separated by commas.
 - (d) max_iter the maximum number of iterations of the K-means algorithm, if not provided the default value is 200.
- 2. Apply K-means on the input, and return the final centroids within the output file.
- 3. use $\epsilon = 0.001$

2.1 Compile and Running

2.1.1 C

The program must compile cleanly (no errors, no warnings) when running the following command:

```
$gcc -ansi -Wall -Wextra -Werror -pedantic-errors kmeans.c -lm -o hw1
```

After successfully running the above command, an executable file called hw1 will be created. Now you can run your program by executing the following line on Nova(assuming K=3, max_iter = 100, filename = "input.txt"):

```
$./hw1 3 100 input.txt output.txt
```

See example below:

```
$#providing max_iter=100
$./hw1 3 100 input.txt output.txt

$#not providing max_iter
$./hw1 3 input.txt output.txt
```

2.1.2 Python

Your program must be executed by (no errors, no warnings) the following line on Nova, with: K = 3, max_iter = 100:

```
$python3 kmeans.py 3 100 input.txt output.txt
```

See examples below:

```
$#providing max_iter=100
$python3 kmeans.py 3 100 input.txt output.txt

$#not providing max_iter
$python3 kmeans.py 3 input.txt output.txt
```

2.2 Assumptions and requirements:

Note that the following list applies to both programs in this assignment:

- 1. You may assume that the input file is in the correct format and that it is provided.
- 2. Validate that the command line arguments are in correct format.
- 3. Outputs must be formatted to 4 decimal places (use: '%.4f') in both languages, for example:
 - $8.88885 \Rightarrow 8.8888$
 - $5.92237098749999997906 \Rightarrow 5.9224$
 - $2.231 \Rightarrow 2.2310$
- 4. Learn about and consider using the following: input(), split() in your Python implementation.
- 5. Learn about and consider using the following: fopen(), fclose(), fscanf(), fprintf(), fgetc(), feof() in your C implementation.
- 6. 3 input files and their corresponding output files examples are provided within the assignment in Moodle. (YES, the files have an extra empty row and this is the expected behaviour)
- 7. Handle errors as following:
 - (a) In case of invalid input, print "Invalid Input!" and terminate the program.
 - (b) Else, print "An Error Has Occurred" and terminate.
- 8. Do not forget to free any memory you allocated.
- 9. For successful running, the C program must return 0 otherwise 1.
- 10. You can assume that all given data points are different.
- 11. You may not import external includes (in C) or modules (in Python) that are not mentioned in this document.
- 12. Use double in C and float in Python for all vector's elements.

2.3 Submission

- 1. Please submit a file named id1_id2_assignment1.zip via Moodle, where id1 and id2 are the ids of the partners.
 - (a) In case of individual submission, id2 must be 1111111111
 - (b) Put the following files **ONLY** in a folder called id1_id2_assignment1:
 - i. kmeans.c
 - ii. kmeans.py
 - (c) Zip the folder using the following Linux cmd:

```
$zip -r id1_id2_assignment1.zip id1_id2_assignment1
```

Do not use other ways to create the zip!

2.4 Remarks

For any question regarding the assignment, please post at the HW_1 discussion forum.