# **Analysing Given Original Grammar**

(February 20, 2023)

## **COLORS** in this document

Black: for original rules in the grammar in ERPLAG specification document

Blue: causes for the trouble but do not need modifications in the rule directly

**Red**: specifies needs for modifications Green: rules do not require modification

```
→ <moduleDeclarations> <otherModules> <driverModule> <otherModules>
1. program>
               FIRST(<program>) = (FIRST(<module Declarations>) - \{\epsilon\}) U (FIRST(<otherModules> - \{\epsilon\}) U <driverModule>
                                  = {DECLARE} U {DEF} U{ DRIVERDEF}
                                  = { DECLARE, DEF, DRIVERDEF}
2. <moduleDeclarations> \rightarrow <moduleDeclaration> <moduleDeclaration> | \epsilon
          FIRST(<moduleDeclarations>) = FIRST(<moduleDeclaration> <moduleDeclarations>) U { \epsilon } = {DECLARE} U { \epsilon }
          FOLLOW(<moduleDeclarations>)
                 =FIRST(<otherModules><driverModule><otherModules>)
                 =(FIRST(<otherModules>)-{\epsilon}) U FIRST(<driverModule>)
                 ={DEF}U {DRIVERDEF}
                 = {DEF, DRIVERDEF}
          Since <moduleDeclarations> \rightarrow \epsilon, we can see that
          FIRST(<moduleDeclaration><moduleDeclaration>>) ∩ FOLLOW(<moduleDeclarations>)
          = \{ DECLARE \} \cap \{ DEF, DRIVERDEF \}
          =\Phi
          That is, LL(1) property that no element in FIRST(<moduleDeclaration><moduleDeclarations>) should be in
          FOLLOW(<moduleDeclarations>) holds good.
```

[Note: I am not specifying explicitly at each rule that LL(1) properties like no ambiguity, no left recursion, no left factoring needed, etc., unless it is to be reported because of presence of these in the grammar rules.]

3. <moduleDeclaration> → DECLARE MODULE ID SEMICOL

As there is only one rule for the non terminal <moduleDeclaration>, and is not left recursive, LL(1) property hold good. FIRST(<moduleDeclaration>) = {DECLARE}

4.  $\langle \text{otherModules} \rangle$   $\rightarrow$   $\langle \text{module} \rangle \langle \text{otherModules} \rangle | \epsilon$ 

 $= \phi$ .

```
Using rule 6 to compute FIRST(<module><otherModules>) we get FIRST(<module><otherModules>) = FIRST(<module>) = {DEF} And FIRST(<otherModules>) = {DEF} U {\epsilon} = {DEF, \epsilon}
```

Since <otherModules> $\rightarrow$   $\epsilon$  also, then LL(1) property is violated if any element in FIRST(<modules>) is also in FOLLOW(<otherModules>). Using rule 1,

```
FOLLOW(<otherModules>) = FIRST(<driverModule><otherModules>) U FOLLOW(<program>) = {DRIVERDEF} U {$} = {DRIVERDEF, $}
```

The FIRST(<module><otherModules>)  $\cap$  FOLLOW(<otherModules>) = {DEF}  $\cap$ {DRIVERDEF, \$}

5. <driverModule> → DRIVERDEF DRIVER PROGRAM DRIVERENDDEF <moduleDef>

Only one rule for the non terminal <driverModule>
FIRST(<driverModule>) = {DRIVERDEF}

6. <module> DEF MODULE ID ENDDEF TAKES INPUT SQBO <input plist> SQBC semicol <ret><moduleDef>

Only one rule for the non terminal <module> FIRST(<module>) = {DEF}

```
7. <ret>
                          \rightarrow RETURNS SQBO < output plist> SQBC SEMICOL | \varepsilon
           FIRST(\langle ret \rangle) = \{RETURNS, \epsilon\}
           Let \alpha represent the RHS of the first rule and \beta represent the RHS of the second rule for the non terminal <ret>
           FIRST(\alpha) = \{RETURNS\}
           From rule 12, we get
           FIRST(<moduleDef>) = {START}
           From rule 6, we get
           FOLLOW(<ret>)
                                 = FIRST(<moduleDef>) ={START}
           As rule 7 derives epsilon, we need to verify the following LL(1) property.
           FIRST(RETURNS SQBO <output plist> SQBC SEMICOL) ∩ FOLLOW(<ret>)
           = \{RETURNS\} \cap \{START\} = \Phi
           Observe that an element in the set FIRST(\alpha) is not in FOLLOW(\langle \text{ret} \rangle) as {RETURNS} and {START} are disjoint.
           Hence epsilon production does not violate the LL(1) property.
8. <input plist>
                          → <input plist> COMMA ID COLON <dataType> | ID COLON <dataType>
           This rule involves left recursion, which violates the LL(1) property.
           Hence needs left recursion elimination.
           let.
                   α represent COMMA ID COLON <dataType>
                   β represent ID COLON <dataType>
                   Then the rule
                   <input_plist> \rightarrow <input_plist> \alpha \mid \beta
                   is modified as follows
                   <input plist>
                                                 \beta <N1>
```

[Note: I will introduce the non terminal symbols as N1, N2, N3, and so on wherever we will require for the modification of rules.]

Replacing  $\alpha$  and  $\beta$  with the actual strings, we get the modified rules as

 $\alpha < N1 > |\epsilon$ 

<N1>

```
<input plist>
                                        \rightarrow
                                               ID COLON <dataType><N1>
                                                                                                .....8a
                                               COMMA ID COLON <a href="color: blue;">dataType> <N1> | E
                  <N1>
                                                                                                 .....8b
                  Now let us analyze these new rules and whether they conform to the LL(1) property or not.
                  Rule 8a:
                         Only one non recursive rule for the non terminal <input plist>
                         FIRST(<input plist>) = {ID}
                  Rule 8b:
                         FIRST(COMMA ID COLON < dataType> < N1>) = {COMMA}
                         As <N1>\rightarrow \epsilon
                         we must look at the FOLLOW(<N1>).
                         Using rule 6, we find FOLLOW(<input plist>) as {SQBC} and get
                         FOLLOW(<N1>) = FOLLOW(<input plist>) = {SQBC}
                         i.e.
                         FOLLOW(<N1>) ∩ FIRST(COMMA ID COLON <dataType> <N1>)
                         = \{SQBC\} \cap \{COMMA\}
                         = \phi
                         Therefore, both rules for the non terminal <N1> (as specified in 8b) conform to LL(1).
                         → <output plist> COMMA ID COLON <type> | ID COLON <type>
9. <output plist>
           This rule involves left recursion, which violates the LL(1) property.
           Hence needs left recursion elimination.
                  α represent COMMA ID COLON <type>
                  β represent ID COLON <type>
                  Then the rule
                  \langle \text{output plist} \rangle \rightarrow \langle \text{output_plist} \rangle \alpha \mid \beta
                  is modified as follows
```

let.

$$\begin{array}{ccc} & & & & & \beta < N2 > \\ & < N2 > & & & \alpha < N2 > & | \epsilon \end{array}$$

Which becomes

The new rules 9a and 9b conform to LL(1) (refer 8 for similar description)

Here one rule is modified as follows

where <range\_arrays> accommodates variable identifiers in defining range of array type. The <range> was only deriving ranges using only the integer values (static constants, e.g. array[2..10] of integer) while the <range\_arrays> can derive array types as array[a..b] of integers (e.g.) where a and b are variable identifiers. Also, negative integers and identifiers can also be accommodated using this new rule.

The non-terminal <index\_arr> is described in rule number 23.

The <range> non-terminal continues to be used in defining the iterative statement for the FOR loop with the newly formed rules.

Let the strings of grammar symbols on the right hand side of the production rules for  $\langle$ dataType $\rangle$  are represented by the greek letters  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$  such that

- α represents INTEGER
- β represents REAL
- γ represents BOOLEAN
- δ represents ARRAY SQBO <a href="range\_arrays">range\_arrays</a> SQBC OF <a href="type">SQBC OF <a href="type">square</a>

```
FIRST(\alpha) = {INTEGER}
FIRST(\beta) ={ REAL}
FIRST(\gamma)={BOOLEAN}
FIRST(\delta)= {ARRAY}
```

We observe that

14. <statement>

FIRST sets of the right hand sides of the 4 rules are disjoint.

The rule is not left recursive and does not need left factoring.

Both of these are disjoint, hence LL(1) compatible.

There is no nullable production, hence there no need to check the disjointness of the FOLLOW(<dataType>) and the first sets of RHS of non null productions.

```
11. <type>
                                       | REAL | BOOLEAN
                        → INTEGER
          Let
          α represents INTEGER
          β represents REAL
          γ represents BOOLEAN
          Then, first sets of the RHS are disjoint.
                 FIRST(\alpha) = \{INTEGER\}
                 FIRST(\beta) = \{REAL\}
                 FIRST(\gamma) = \{BOOLEAN\}
          The production rules for the non terminal <type> conform to the LL(1) property.
12. <moduleDef>
                        → START <statements> END
          Only one rule for the non terminal <moduleDef>
          FIRST(<moduleDef>) = {START}
                        \rightarrow<statement> <statements> | \epsilon
13. <statements>
          FOLLOW(<statements>) = {END, BREAK}
                                                                               ......From RHS of rules 12, 42, 44 and 45
          FIRST(<statement><statement>) = FIRST(<statement>)
                               = { GET VALUE, PRINT, ID, SQBO, USE, DECLARE, SWITCH, FOR, WHILE}
```

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→<ioStmt>|<simpleStmt>|<declareStmt>|<condionalStmt>|<iterativeStmt>

Let us compute the set intersection of FIRST sets of the RHSs of the rule for <statement>. We get,

```
FIRST(\langle ioStmt \rangle) \qquad ......get from 15
\cap \qquad FIRST(\langle simpleStmt \rangle) \qquad ......from 18
\cap \qquad FIRST(\langle declareStmt \rangle)
\cap \qquad FIRST(\langle condionalStmt \rangle)
\cap \qquad FIRST(\langle iterativeStmt \rangle)
= \{GET\_VALUE, PRINT\} \ \cap \ \{ID, SQBO, USE\} \ \cap \{DECLARE\} \ \cap \ \{SWITCH\} \ \cap \ \{FOR, WHILE\}
= \emptyset
```

Therefore, the RHSs of all five rules for <statement> above have disjoint FIRST sets . therefore the LL(1) compatibility is ensured.

Also, we compute FIRST(<statement>) for use in 13 above.

```
FIRST(<ioStmt>) = FIRST(<ioStmt>) .....get from 15

U FIRST(<simpleStmt>) .....from 18

U FIRST(<declareStmt>)

U FIRST(<condionalStmt>

U FIRST(<iterativeStmt>)

={GET_VALUE, PRINT} U {ID, SQBO, USE} U{DECLARE} U {SWITCH} U {FOR, WHILE}

= { GET VALUE, PRINT, ID, SQBO, USE, DECLARE, SWITCH, FOR, WHILE}
```

#### 15. <ioStmt>→GET\_VALUE BO ID BC SEMICOL | PRINT BO <var print> BC SEMICOL

Let

α represents GET VALUE BO ID BC SEMICOL

β represents PRINT BO <var print> BC SEMICOL

Then, first sets of the RHS are disjoint.

```
FIRST(\alpha) = \{ GET_VALUE \}
```

 $FIRST(\beta) = \{ PRINT \}$ 

There is no nullable production for <ioStmt>, therefore no need to look at the FOLLOW(ioStmt).

[Recall that the rule  $A \rightarrow \varepsilon$  is used to populate the parsing table entry T(A,a) for all symbols 'a' in FOLLOW(A)]

Hence, FIRST( $\langle ioStmt \rangle$ ) = union of sets FIRST( $\alpha$ ) and FIRST( $\beta$ ) ={ GET\_VALUE, PRINT }

This contributes to the first set of <statement> (rule 14), which in turn will be used to verify (rule 13's LL(1) compatibility) whether the FIRST(<statement>) and FOLLOW(<statements>) are disjoint.

Rule 16 is modified to accommodate printing of variable identifiers, integer, and real numbers, boolean constants true and false, and array elements [refer to rules 16 e and f]. Note that the array element in print cannot use an expression.

#### 16. <var> → ID <whichId> | NUM | RNUM

To facilitate printing of true and false values, let us introduce a new rule for deriving boolean constants true and false.

```
<boolConstt> →TRUE | FALSE
                                                                                              ..... 16 a
FIRST(TRUE) \cap FIRST(FALSE) = \{TRUE\} \cap \{FALSE\} = \Phi
Therefore, rules of <boolConst> are LL(1) compatible.
Also, we will introduce a new nonterminal < id num rnum> as follows
< id num rnum> \rightarrow ID | NUM | RNUM
                                                                                              .....16 b
FIRST(ID) \cap FIRST(NUM) \cap FIRST(RNUM) = \{ID\} \cap \{NUM\} \cap \{RNUM\} = \Phi
Therefore, rules of \leq id num rnum \geq are LL(1) compatible.
Array element formation for print as in print(A[4]), print(A[k]) etc. is constructed as follows,
<array element for print> → ID SQBO <new index> SQBC
                                                                                              .....16 c
[refer < new index > from 23 b]
Then, we modify the rules for <var> [renamed <var print>] as follows
.....16 d
Since FIRST(\langle id \text{ num rnum} \rangle) \cap FIRST(\langle boolConstt \rangle) = \Phi, and
      FIRST(\langle id \text{ num rnum} \rangle) \cap FIRST (\langle array \text{ element for print} \rangle) = {ID}, left factoring is applied here.
Then rules are redefined as
<var print>→ ID <P1> | NUM | RNUM | <boolConstt>
                                                                                               .....16 e
```

```
.....16 f
          <P1> \rightarrow SQBO < new_index> SQBC | \epsilon
          FIRST(ID < P1 >) \cap FIRST(NUM) \cap FIRST(RNUM) \cap FIRST(<br/>soolConstt>)
                                      = \{ID\} \cap \{NUM\} \cap \{RNUM\} \cap \{TRUE, FALSE\} = \Phi
          And.
          FIRST(SOBO <new index> SOBC ) ∩ FOLLOW(<P1>)
                                             = {SQBO} ∩ FOLLOW(<var print>)
                                             = \{SOBO\} \cap \{BC\}
                                             =\Phi
          Therefore, rules of < var print > and <P1> are LL(1) compatible.
          Since array elements for print statement are taken care of, the rule 17 is discarded.
17. <whichId> > SOBO ID SOBC | c
18. <simpleStmt>
                        → <assignmentStmt> | <moduleReuseStmt>
          FIRST(<assignmentStmt>) and FIRST( <moduleReuseStmt>) should be disjoint
                 \{ID\} \cap \{SOBO, USE\} = \varphi
                                                       .....refer 19 and 24
          Hence rules for the nonterminal <simpleStmt> conform to LL(1)
          Also FIRST(<simpleStmt>) = {ID, SQBO, USE}
19. <assignmentStmt>
                        → ID <whichStmt>
                 FIRST(<assignmentStmt>) = FIRST(ID <whichStmt>) = {ID}
                        →<|valueIDStmt>| <|valueARRStmt>
20. <whichStmt>
          FIRST(<|valueIDStmt>) and FIRST(<|valueARRStmt>) should be disjoint.
          Refer 21 and 22 to see that the above rule conforms to LL(1) specifications
                        → ASSIGNOP <expression> SEMICOL
21. <lvalueIDStmt>
          FIRST(<lvalueIDStmt>) = {ASSIGNOP}
                        → SQBO <index> SQBC ASSIGNOP <expression> SEMICOL
22. <lvalueARRStmt>
          The array element access involves ID, NUM and arithmetic expressions not involving array elements themselves. Therefore,
          the <index> is redefined as <arr element access index> in rule 22 as follows.
```

Where <element\_index\_with\_expressions> is constructed in exactly the same way an arithmetic expression is constructed, but this one does not derive an array element itself. Refer to the details for this in rule number 33 i.

FIRST(<|valueARRStmt>) = {SQBO}

#### 23. $\langle index \rangle$ $\rightarrow$ NUM | ID

Rules to define the range of arrays (accommodating negative and positive, integers and identifiers, alongwith unsigned integers and identifiers)

```
<index_arr>→ <sign><new_index> .....23 a
<new_index> → NUM | ID
<sign>→ PLUS | MINUS | ε
.....23 c
```

```
Rule 23 b, has FIRST(NUM) \cap FIRST(ID) = \Phi
And, FIRST(<new_index>) = {NUM, ID}
Rule 23 c, has FIRST(PLUS) \capFIRST(MINUS) \capFOLLOW(<sign>)
= {PLUS} \cap {MINUS} \cap FIRST(<new_index>)
= {PLUS} \cap {MINUS} \cap{NUM, ID}
= \Phi
FIRST(<sign>) = {PLUS, MINUS, \epsilon}
```

Rule 23 a, is a single rule and its FOLLOW computation is not required.  $FIRST(<index\_arr>) = (FIRST(<sign>)- \{\epsilon\}) \ U \ FIRST(<new\_index>) \\ = \{PLUS, MINUS, NUM, ID\}$ 

### Conforms to LL(1) (trivial)

24. <moduleReuseStmt> → <optional> USE MODULE ID WITH PARAMETERS <idList>SEMICOL

```
FIRST(<moduleReuseStmt>) = FIRST(<optional>) U FOLLOW(<optional>)
={SQBO} U {USE} = {SQBO, USE}
```

Notice that the MODULE keyword remains here as per the updates.

```
25. <optional>
                           \rightarrow SQBO <idList> SQBC ASSIGNOP | \varepsilon
            FIRST(SQBO < idList > SQBC ASSIGNOP) \cap FOLLOW(< optional >) = \varphi
            Therefore there is no need for modification.
                           → <idList> COMMA ID | ID
 26. <idList>
            This requires left recursion elimination
                   <output plist>→
                                         ID < N3 >
                   <N3>
                                  \rightarrow
                                         COMMA ID \langle N3 \rangle | \epsilon
                           → <arithmeticExpr> | <booleanExpr>
 27. <expression>
            This rule needs special care. With given original rules for <arithmeticExpr> and <booleanExpr>, we found that their FIRST
            sets were not disjoint and were same as { BO, ID, NUM, RNUM }. A special care is required to perform left factoring which
            is done by using a single non terminal for both expressions and the expressions are constructed by way of appropriate
            binding.
            Let us redefine this rule (rule 27) as follows
            <expression> > <arithmeticOrBooleanExpr> | <U>
                                                                                 .....new 27.1
            Defining an expression <U> generated by using unary operators plus or minus (type 1)
<U>→ MINUS BO <arithmeticExpr> BC | PLUS BO <arithmeticExpr> BC | MINUS <var id num> | PLUS <var id num> |
            which can be left factored as below
            \langle U \rangle \rightarrow \langle unary op \rangle \langle new NT \rangle
            The new non terminals are defined as follows
            <new NT> \rightarrow BO <arithmeticExpr> BC | <var id num>
                                                                       .....new 27.2
            <unary op> → PLUS | MINUS
                                                                              .....new 27.3
            Consider 27.1 and let us show that the rules for <expression> are LL(1) compatible.
            FIRST(\langle arithmeticOrBooleanExpr \rangle) \cap FIRST(\langle U \rangle)
                                                                        .....see the computation later
            = {ID, NUM, RNUM, BO, TRUE, FALSE} ∩ {PLUS, MINUS}
            because FIRST(<U>) = FIRST(<<unary op>) = {PLUS,MINUS}
```

Consider 27.2 and let us show that the two rules are LL(1) compatible.

 $FIRST(BO < arithmeticExpr > BC) \cap FIRST(< var id num >)$ 

$$= \{BO\} \cap \{ID, NUM, RNUM\} = \emptyset$$

Rule 27.3 is trivially LL(1).

Now we generate a type 2 expression which can be either a

- (i) simple arithmetic expression or
- (ii) an expression containing one boolean expression having two arithmetic expressions combined using relational operators or
- (iii) a combination of boolean expressions constructed by combining with AND and OR operators. Let us observe the following grammar

While <AnyTerm> can either expand to generate a boolean expression in its most atomic form using relational operators or can generate an arithmetic expression. We try to introduce more atomicity in the construction of boolean expression using boolean constants true and false as below

The rules for <arithmeticOrBooleanExpr> and <AnyTerm> are left recursive, hence need modification.

We have now rules

```
      <arithmeticOrBooleanExpr> → <AnyTerm> <N7>
      ....27 a

      <N7> → <logicalOp> <AnyTerm> <N7> | ε
      ....27 b

      <AnyTerm> → <arithmeticExpr> <N8> | <boolConstt> <N8>
      ....27 c

      <N8> → <relationalOp> <arithmeticExpr> <N8> | ε
      ....27 d
```

Rules 27 a is not left recursive, and is LL(1) compatible.

The two Rules of 27 c are having their RHSs FIRST sets disjoint as is described below.

```
FIRST(\langle arithmeticExpr \rangle) \cap FIRST(\langle boolConstt \rangle)
= \{ID, NUM, RNUM, BO\} \cap \{TRUE, FALSE\}
=\Phi
Verifying the LL(1) compatibility of 27 d,
FOLLOW(<N8>) = FOLLOW(<AnyTerm>) = FIRST(<N7>) = FIRST(<logicalOps>)
                                        = \{AND, OR\}
FIRST(<relationalOp> <arithmeticExpr><N8> ) = {LE, LT, GE, GT, EQ, NE}
Both FOLLOW(<N8>) and FIRST(<relationalOp> <arithmeticExpr><N8>) are disjoint.
Hence 27 d is LL(1) compatible.
Now let us verify the LL(1) compatibility of 27 b,
FOLLOW(<N7>) = FOLLOW(<arithmeticOrBooleanExpr>)
                = FOLLOW(<expression>)
               = {SEMICOL}
                                             ...using rules 21 and 22
And FIRST(<logicalOp><AnyTerm><N7>) = FIRST(<logicalOp>)
                                        = \{AND, OR\}
Both of these sets are disjoint.
Hence rules 27 a - d are LL(1) compatible.
We will remove all rules that start with <booleanExpr>. See below.
Now FIRST(<arithmeticOrBooleanExpr>) = FIRST(<AnyTerm>)
                                         = FIRST(<arithmeticExpr>) U FIRST(<boolConstt>)
                                         = {ID, NUM, RNUM, BO} U {TRUE, FALSE}
                                         = {ID, NUM, RNUM, BO, TRUE, FALSE}
```

generates the expression which is either a simple arithmetic expression, or an expression that has negative expression,

FIRST(<arithmeticOrBooleanExpr>) and FIRST(<U>) are disjoint, hence new 27 rule is LL(1) compatible. It

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Consider the rule new 27.1 and check the FIRST sets of both of its RHS strings

or generates a boolean expression as well without having the first sets creating trouble as was the case with the original rule 27.

28. <arithmeticExpr> → <arithmeticExpr> <op> <term> 29. <arithmeticExpr>  $\rightarrow$ <term> To facilitate the precedence of operators, we need to split the rule for <op> into two <op1> and <op2> (see new rules defined in 34) Rule 28 becomes <arithmeticExpr> → <arithmeticExpr> <op1> <term> Above two rules (28 and 29) are used for left recursion elimination as <arithmetic Expr> is left recursive. These become <arithmeticExpr>  $\rightarrow$ <term> <N4> ....29 a <N4>  $\rightarrow$  <op1> <term> <N4>  $\mid \varepsilon \mid$ ...29 b FIRST(<arithmeticExpr>) = FIRST(<term>) = {ID, NUM, RNUM, BO} ..... from 31  $FIRST(\langle op1 \rangle \langle term \rangle \langle N4 \rangle) = FIRST(\langle op1 \rangle) = \{PLUS, MINUS\}$ As <N4> $\rightarrow$   $\epsilon$  is a production, we need to look at the FOLLOW(<N4>) FOLLOW(<N4>) = FOLLOW(<arithmeticExpr>) = FIRST(<N8>) U {BC} ......from 27 c, 27 d and new 27.2 = FIRST(<relationalOp> <arithmeticExpr><N8> ) U {BC}  $= \{LE, LT, GE, GT, EQ, NE, BC\}$ This shows that the rules 29 a and 29 b are LL(1) compatible  $\rightarrow$ <term><op><factor> 30. <term> 31. <term> →<factor> Define rule 30 as <term> $\rightarrow$ <term><op2><factor> ....new rule for replacing 30 Above two rules require left recursion elimination .....31a  $\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle \langle \text{N5} \rangle$ 

```
\rightarrow <op2> <factor> <N5>| \varepsilon
                                                                                         .....31b
           FIRST(<term>) = FIRST(<factor>) = {ID, NUM, RNUM, BO}
                                                                                       .....from 33
           FIRST(\langle op2\rangle \langle factor\rangle \langle N5\rangle) = FIRST(\langle op2\rangle) = \{MUL, DIV\}
           As <N5> \rightarrow \varepsilon is a production then we need to look at the FOLLOW(<N5>)
           FOLLOW(<N5>) = FOLLOW(<term>
                              = FIRST(< N4>)
                                                        .....from 29a
                              = FIRST(<op1>)
                              = {PLUS, MINUS}
           Hence 31a and 31b conform to LL(1).
32. <factor>
                           \rightarrowBO <arithmeticExpr> BC
33. <factor>
                           \rightarrow<var>
            This rule needs modification to accommodate variable identifiers, integers, real numbers, boolean constants true and false,
           and the array elements. The array elements can also be indexed using special expressions not involving array elements
           themselves. [Note that the nonterminal <array element for print> cannot use expression to access the element.
           Let us define a new nonterminal <array element>, then
           <factor> > <id_num_rnum> | <boolConstt> | <array_element>
                                                                                                                         .....33 a
           You will require to left factor rules of <id num rnum> and <array element> as FIRST(<id num rnum>) ∩
           FIRST(<array element>) = {ID}
           We define, <array element> as follows.
           <array element>→ ID SQBO <element_index_with_expressions> SQBC
                                                                                                                        .....33 b
           Using 33 a and b, the factor is defined below.
           <factor> → NUM | RNUM | <boolConstt> | ID <N 11>
           \langle N | 11 \rangle \rightarrow SOBO \langle element | index | with | expressions \rangle SOBC | \epsilon
```

To incorporate access differently as in A[+5], A[-5], A[+k], A[-k], A[5], A[k], we use <sign> and <new\_index>. To derive special expressions, a new nonterminal <arrExpr> is defined. To also accommodate, the negative expressions, we use <sign>

Notice that <element index with expressions> is different than just the <new index>.

```
and the expression in parentheses pair as follows.
<element index with expressions> > > <sign> <new index> | <arrExpr> | <sign> BO <arrExpr> BC
                                                                                                          .....33 c
The <arrExpr> is defined exactly in the same way we define arithmetic expressions, but the factor rule does not derive an
array element here. The LL(1) compatibility of the rules 33 d-h can be established similarly to the arithmetic expressions.
              →<arrTerm> <arr N4>
<arrExpr>
                                                                                                          .....33 d
<arr N4>
              \rightarrow <op1> <arr Term> <arr N4> | \epsilon
                                                                                                          .....33 e
              → <arr Factor> <arr N5>
<arrTerm>
                                                                                                          .....33 f
<arr N5>
              \rightarrow <op2> <arrFactor> <arr N5>| \varepsilon
                                                                                                          .....33 g
<arrFactor> → <id num rnum> | <boolConstt> | BO <arrExpr> BC
                                                                                                          .....33 h
FIRST(<arrFactor>) = FIRST(<id num rnum>) U FIRST(<boolConstt>) U FIRST(BO <arrExpr> BC)
                    = {ID, NUM, RNUM} U {TRUE, FALSE} U {BO}
FIRST(<arrExpr>) = FIRST(<arrFactor>) = {ID, NUM, RNUM, TRUE, FALSE, BO}
We can apply left factoring on rule 33 c to get
```

The two rules of 33 i and those of 33 j have disjoint first sets.

### 34. $\langle op \rangle$ $\rightarrow$ PLUS | MINUS | MUL | DIV

This rule needs split to facilitate precedence of operators Instead of , we have two new non terminals defined as

35. <booleanExpr> -> <booleanExpr> <logicalOp> <booleanExpr> See the description above in 27

```
36. <logicalOp>
                       →AND | OR
         FIRST sets of the RHS are disjoint.
                      -><arithmeticExpr> < relationalOp> < arithmeticExpr> refer 27
37. <booleanExpr>
38. <booleanExpr>
                      -> BO <booleanExpr> BC to incorporate this we have 27.1
39. <relationalOp>
                       \rightarrow LT | LE | GT | GE | EQ | NE
           FIRST sets of the RHS are disjoint.
40. <declareStmt>
                       → DECLARE <idList> COLON <dataType> SEMICOL
         FIRST(<declareStmt>) = {DECLARE}
                       →SWITCH BO ID BC START <caseStmts><default> END
41. <condionalStmt>
         FIRST(<conditionalStmt>) = { SWITCH}
                       →CASE <value> COLON <statements> BREAK SEMICOL <caseStmt>
42. <caseStmt>
         This rule is modified to facilitate any number of case statements (essentially one or more). We introduce a new nonterminal
          <aseStmts>. We modify the nonterminal in rule 41, while change is reflected using red color in rule 41.
         The rules become
   <caseStmts>
                       → CASE <value> COLON <statements> BREAK SEMICOL <N9>
                       → CASE <value> COLON <statements> BREAK SEMICOL <N9> | ε
   < N9 >
         Here FIRST(<caseStmts>)={CASE}
          As <N9> is a nullable production
         FIRST (CASE <value> COLON <statements> BREAK SEMICOL <N9>) and FOLOW(<N9>) should be disjoint.
          FOLLOW(<N9>) = FOLLOW(<caseStmts>) = FIRST(<default>) = {DEFAULT}
         The rules therefore are LL(1) compatible.
                       →NUM | TRUE | FALSE
43. <value>
         FIRST(<value>) = {NUM, TRUE, FALSE}
          The FIRST sets of the RHS of the three rules are disjoint.
                       →DEFAULT COLON <statements> BREAK SEMICOL | ∈
44. <default>
         FIRST(DEFAULT COLON <statements> BREAK SEMICOL) = {DEFAULT}
         FOLLOW(<default>) = {END}
         Hence both rules are LL(1) compatible.
```

#### 45. <iterativeStmt> →FOR BO ID IN <range> BC START <statements> END |

WHILE BO <booleanExpr> BC START <statements> END

The new rules are as follows

<iterativeStmt>→ FOR BO ID IN <range for loop> BC START <statements> END | .......45a WHILE BO <arithmeticOrBooleanExpr> BC START <statements> END ......45 b

The range for for loop is constructed in rule 46 [refer to rules 46 a, b, c]

In While construct, the boolean expression construct is replaced with the non-terminal <arithmeticOrBooleanExpr>. It is considered syntactically correct to receive even an arithmetic expression here, based on the newly defined grammar rules (27 a-d). Hence your parser will not report error on while(a+b-c) ...kind of statements. However, later the error of this type will be detected by the type checker module of semantic analysis phase. Similarly, an expression a+ (b<c) is also syntactically correct and will be reported as type error later.

FIRST(<iterativeStmt>) = {FOR, WHILE}

The FIRST sets of the RHS of both rules are disjoint, hence LL(1)

#### 46. <range> →NUM RANGEOP NUM

For the for loop range, negative integers are required to be introduced in the grammar.

The <range> for the for loop is modified as <range for loop>

<range for loop> → <index for loop> RANGEOP <index for loop>

This is a single rule and is considered LL(1) compatible.

Rules for <index for loop> are given as follows,

```
\langle \text{index for loop} \rangle \rightarrow \langle \text{sign for loop} \rangle \langle \text{new index for loop} \rangle
                                                                                                                                                                                         .....46 a
<new index for loop > \rightarrow NUM
                                                                                                                                                                                         .....46 b
\langle \text{sign for loop} \rangle \rightarrow \text{PLUS} \mid \text{MINUS} \mid \varepsilon
                                                                                                                                                                                         .....46 c
```

Rule 46 b, is a single rule and is LL(1) compatible,

And,  $FIRST(< new index >) = {NUM}$ 

Rule 46 c, has FIRST(PLUS) ∩FIRST(MINUS) ∩FOLLOW(<sign for loop >)

=  $\{PLUS\} \cap \{MINUS\} \cap FIRST(< new index for loop >)$ 

 $= \{PLUS\} \cap \{MINUS\} \cap \{NUM\}$