ACTIVITY ...

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Al P be the statement "Maria learns discrete Mathematics" and 9 the statement "Maria will find a good Job" Express the statement P-> 2 as a statement in English. From the defination of Conditional Statements, we see that when p is the statement "maria learns discrease Mathematics" and 9 is the statement "maria will find a good Job. "P-9 suprements the statement "If movie learns discrete mathematics, then she swill find a good job".

Lind a good job". Statement in English. Among the most natural of there are "Maria will fend a good yob when she leaves the dieveale mathematics" "For Maria to get a good job, it is sufficient for her to learn discrete mathematics". "Moria will find a good job unless she does not learen disorde mathematics. 2) longtruct the truth table of the lampand Peropoetion (PV~9) -> (PN9)

Because this bruth table involves two propositional Variable Pand 9, there are four rows in this truth table, one for each of the spairs of truth Value. TI, TF, FF, FF. The first two colomns are seed for the truth Values of P and 9 respectively. In the third Column we find the bruth Values of ~9, needed

to find the truth Values of PV~9, found in the fourth Column. The fifth Column gives the truth Value of PN9. Finally, the truth value (PV~9) -> (PN9) is found in the last Johnn. The resulting truth table is shown table 1.

ng Prng

Equivalent.

3) Show that ~ (PV9) and ~PA~9 are logically Equivalent

Lable 2 Louth Lables for ~ (PV9) and ~PA~9

Prq ~(Prq) ~P

The bruth tables for their lampound Propositions are displayed

in table 2. Because the buth Values of the Compound propositions ~ (PV4) and ~Pn~9 agree for all possible Combination of

the truth Values of Pand 9, it follows that ~ (PV9) - (~Pnog) is a tantology and that there Compound Poropositions are logically

Prove

Step (1)

Step (2):

Step (3)

Nou

ourth Column. 4) Prove by PMI that 1+2+3+ +n= n(n+1) ally the det P(n) be the statement that 1+2+3.... +n=n(n+1) Step (1) = Put n=1 RHS = 1(141) = 2 = 1 19) · LHS = RHS . P(1) is true Step(2): Assume that P(n) is true for n=h

det P(h) is true

1+2+3+....+K=K(K+1) Step B): Now, we have to prove that f(n) is here for n: (k+1) LHS of P(K+1) 1+2+3......+K+K-1= (K+1)(3K+2) Now ièplayed ropoeitions ation of) (~Pnag) 1+2+3+ +K+K+1 · K(KH) +K+1 · logically = (K+1) (K+2) = (K+1) (K+2) = RHS : P(n) is true for NEN : By PMI P(A) in the VNEN

Find the Sontraporitive, the Sonurrue, and the sinverse of the Sanditional Statement.

"The home team wins whenever it is raining" alt Because "I whenever P" is one of the ways to Enpur the landitional statement I on be suwritten as. " It is graining, then the home team wins" Consequently, the Montrapositive of this Conditional Material is "It is home learn does not win, then it is not raining" The Conscree is "If the home team wine, then it is training". " If it is not raining, then the home team done not wis." Only the Montrapacitive is Equivalent to the original

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6) What is the truth Value of $\forall x P(n)$, whom P(x) is the Statement "n" \(10" and the Somain longuits of the positive integers not exceeding 4?

The Statement $\sqrt{n} P(n)$ is the same as the languation $P(1) \cap P(2) \cap P(3) \cap P(4)$

Because the domain lanciets of the integers 1, 2, 3 and 4. Because P(4), which is the estatement "42 < 10", is false, it follows that Vn P(n) is false.

Similarly, when the elements of the domain are $x_1, x_2 \dots$ x_n where in is a specifive integer, the excitential greatification $z_n P(x)$ is the same as the disjustion.

P(x1) V P(x2) V VP (xn).

nent is

What do the statement for < 0 (220), Vy # 0 (y3 +0) and $\exists z > 0$ ($z^2 = 2$) mean, where the domain in each Cou lancits of the real numbers? The Statement In <0 (n2>0) statement that for every red number n with n<0, n2>0. That is, it startes "The square of a regative real number eis positive? This etalement is the same as $V_{x}(x<0\rightarrow x^{2}>0)$. The Statement $\forall y \neq 0 (y^3 \neq 0)$ States that for every real enumber y with $y \neq 0$, we have $y^3 \neq 0$. That is, it States "The lube of Every nonzero real number is nonzero! This statement is equivalent to $\forall y (y \neq 0 \Rightarrow y^3 \neq 0)$. Finally, the statement 32>0 (=2=2) states that there exiels a real number 2 with 270 such that 22=2. That, is, it states "There is a paritive sequere root of 2". This statement is equivalent to 2, (2) 0 n 2° = 2). Note that the of a universal qualification is the same as the Universal quapication of a landification is the same For instance, (In < 0/ n²>0) is another way of Expressing same as the existential qualification of a largintion. For instance Jz>0 (2²=2) is another way of Suprawing J2 (7>n n =²-2) J2 (Z70NZ2=2).

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y real real & States !! This That, me rent. rusking For

8) Enpress the Statement: Every student in this class has Studied lakelied lakelied predicates and quantified

First, we travite the Statement so that we lan Mearly indentify the appopriate quantifies to us. Doing so, we abtain "For Every student in this class, that student has student Cakulus."

Nest, we introduce a Variable ne o that our statement becomes "For Every student nin this class, nhas studied Calculas".

Soutinuing, We introduce (n), which is the elatement "I has studied calculus." Consequently, if the domain for a Consider of the students in the class, cure lan travale vous statement as Vn C(n).

However, there are other larvest approaches different damain of discourse and other predicts Can be used. The approach we select depends on the Sublequent reasoning we want to Cany out. For, Enample, we may be interested in a wider group of people than only those in this Islaw. If we change the domain to someist of all people we will ned to enjour our etalement as.

Monally, when we are interested in the body ground of people in subject besides Calculus, we may prefer to use the two Variable (n,y) for the electement "Student n has related Subject

J. "Then we should suplou c(n) by a (n Cakulate) in both approaches to obtain In a (n, Lakeuline). from a man who has 6 low, 5 pig and 8 here how many thoice does the farmer have. $C_3 = Cows$ $C_2 = \rho c c c c$ $C_3 = Cows$ $C_4 = c c c c c$ According to principle of lounting 6c3 x 3c2 x 4c8 = 6! x 5! x 8! 3!3! 2!3! 4!x4! = 6×5×4 × 5×4 × 8×7×6×5 3×2 1×2 4×3×2 = 20×10×70 10) 6 min, 5 Women do form the Lone Here of 5 members show have 2 womens. Given Zotal = 11 Members = 5

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According to Combinations

1(n-n)!

 $^{3}C_{2}\times C_{3} = 5! \times 6!$ 2!3! 3!3!

= 5×4×3×2×1 x 6×5×4×3×2×1 2×1×3×2×1 3×2×1×3×2×1

= 5×4 × 6×5×4 2×1 3×2×1

= 20 x 120

= 10 x 20 = 200.