

raman.shinde15@gmail.com_23

July 22, 2019

Social network Graph Link Prediction - Facebook Challenge

0.0.1 Problem statement:

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

0.0.2 Data Overview

Taken data from facebook's recruiting challenge on kaggle
<https://www.kaggle.com/c/FacebookRecruiting>

data contains two columns source and destination eac edge in graph - Data columns (total 2 columns):

- source_node int64
- destination_node int64

0.0.3 Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos :
 - <https://www.cs.cornell.edu/home/kleinber/link-pred.pdf>
 - <https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf>
 - https://kaggle2.blob.core.windows.net/forum-message-attachments/2594/supervised_link_prediction.pdf
 - <https://www.youtube.com/watch?v=2M77Hgy17cg>

0.0.4 Business objectives and constraints:

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

0.0.5 Performance metric for supervised learning:

- Both precision and recall is important so F1 score is good choice

- Confusion matrix

```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")

        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do arithmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pyplot as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xgboost: pip3 install xgboost
        import xgboost as xgb

        import warnings
        import networkx as nx
        import pdb
        import pickle

        from pandas import HDFStore,DataFrame
        from pandas import read_hdf

        import gc
        from tqdm import tqdm
        from scipy.sparse.linalg import svds, eigs

        from sklearn.metrics import f1_score
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1_score
        from sklearn.model_selection import RandomizedSearchCV
        from scipy.stats import randint as sp_randint
        from scipy.stats import uniform
        from sklearn.metrics import f1_score

In [2]: #reading graph
        if not os.path.isfile('data/after_eda/train_woheader.csv'):
            traincsv = pd.read_csv('data/train.csv')
```

```

print(traincsv[traincsv.isna().any(1)])
print(traincsv.info())
print("Number of duplicate entries: ",sum(traincsv.duplicated()))
traincsv.to_csv('data/after_eda/train_woheader.csv',header=False,index=False)
print("saved the graph into file")
else:
    g=nx.read_edgelist('data/after_eda/train_woheader.csv',delimiter=',',create_using=nx.DiGraph)
    print(nx.info(g))

```

Name:
 Type: DiGraph
 Number of nodes: 1862220
 Number of edges: 9437519
 Average in degree: 5.0679
 Average out degree: 5.0679

Displaying a sub graph

```

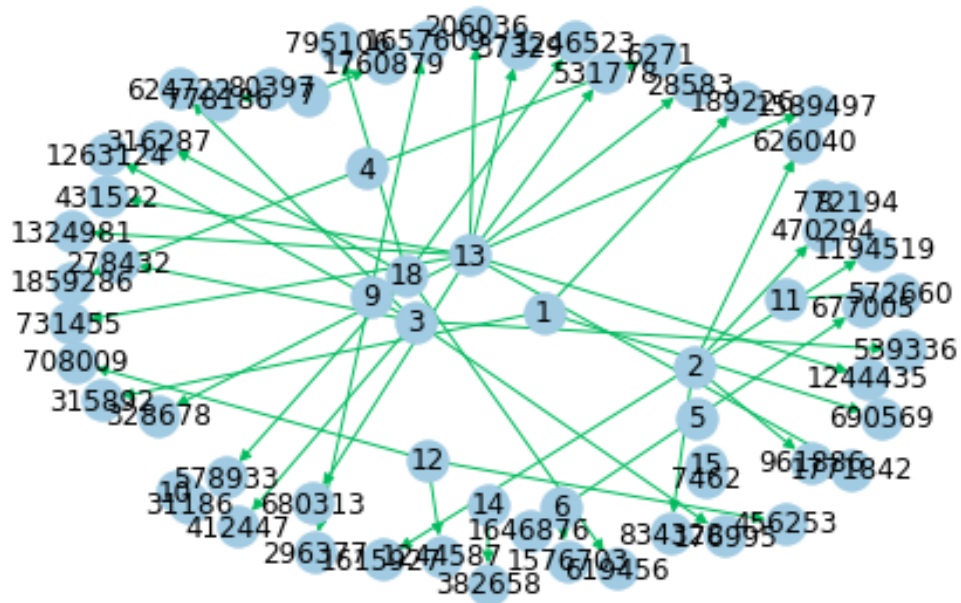
In [3]: if not os.path.isfile('train_woheader_sample.csv'):
        pd.read_csv('data/train.csv', nrows=50).to_csv('train_woheader_sample.csv',header=False,index=False)

        subgraph=nx.read_edgelist('train_woheader_sample.csv',delimiter=',',create_using=nx.DiGraph)
        # https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with-networkx-and-matplotlib

        pos=nx.spring_layout(subgraph)
        nx.draw(subgraph,pos,node_color='#A0CBE2',edge_color='#00bb5e',width=1,edge_cmap=plt.cm.viridis)
        plt.savefig("graph_sample.pdf")
        print(nx.info(subgraph))

```

Name:
 Type: DiGraph
 Number of nodes: 66
 Number of edges: 50
 Average in degree: 0.7576
 Average out degree: 0.7576



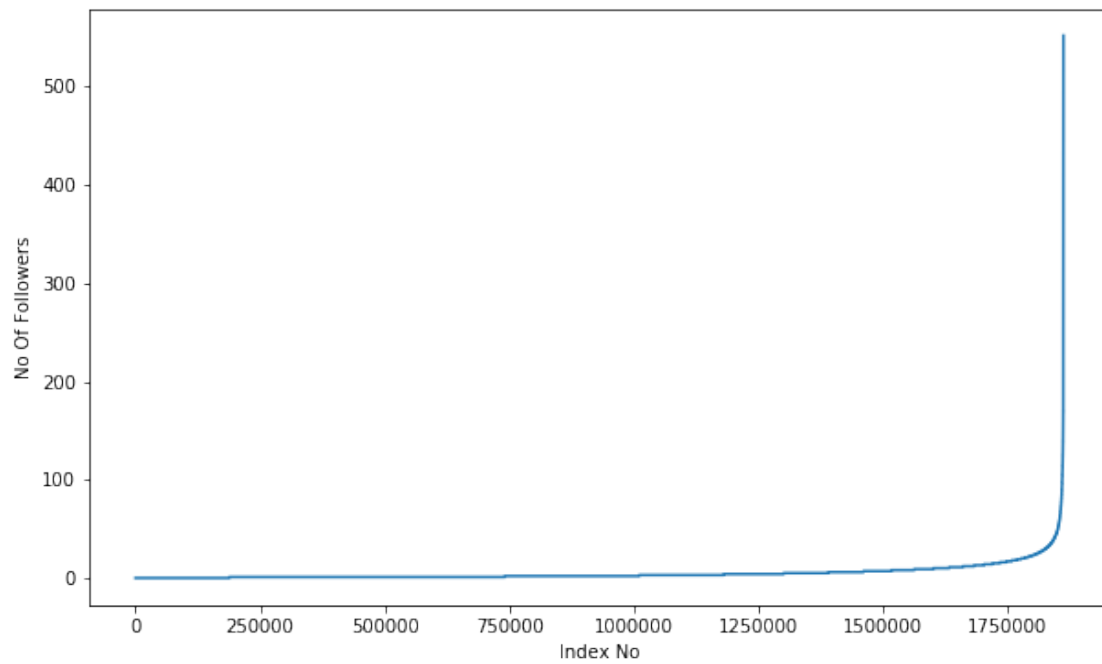
1 1. Exploratory Data Analysis

```
In [11]: # No of Unique persons
print("The number of unique persons",len(g.nodes()))
```

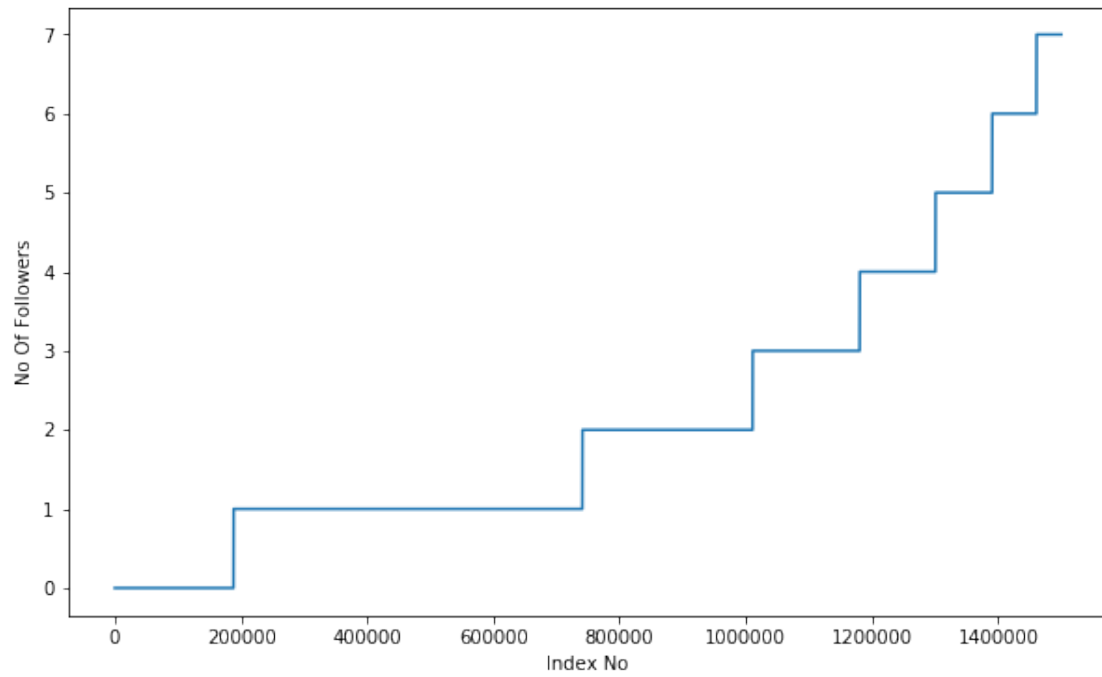
The number of unique persons 1862220

1.1 1.1 No of followers for each person

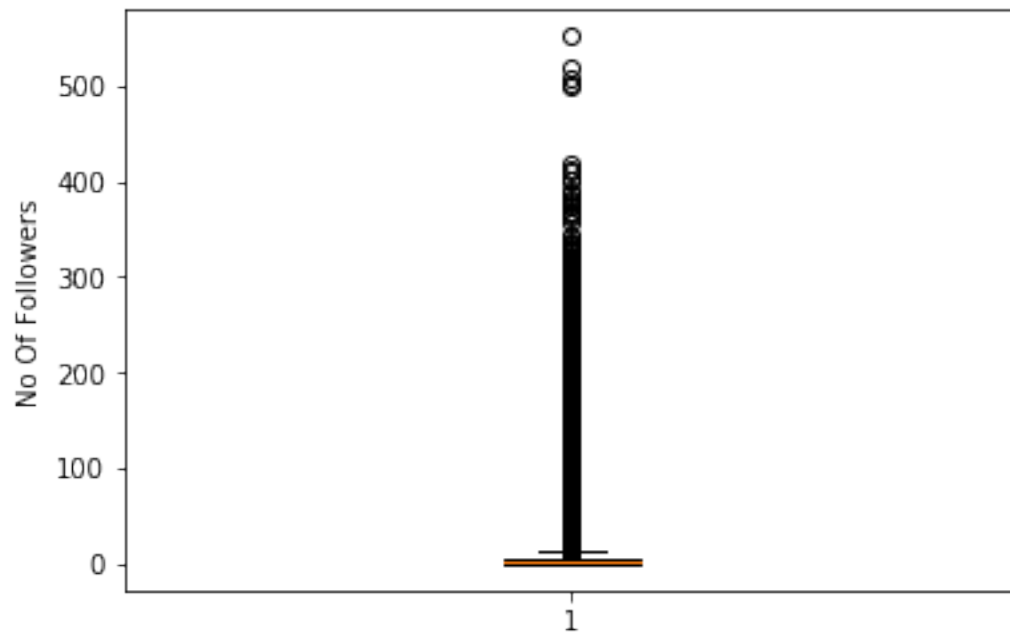
```
In [12]: indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(indegree_dist)
plt.xlabel('Index No')
plt.ylabel('No Of Followers')
plt.show()
```



```
In [6]: indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(indegree_dist[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of Followers')
plt.show()
```



```
In [7]: plt.boxplot(indegree_dist)
plt.ylabel('No Of Followers')
plt.show()
```



```
In [8]: ### 90-100 percentile
        for i in range(0,11):
            print(90+i,'percentile value is',np.percentile(indegree_dist,90+i))
```

```
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 552.0
```

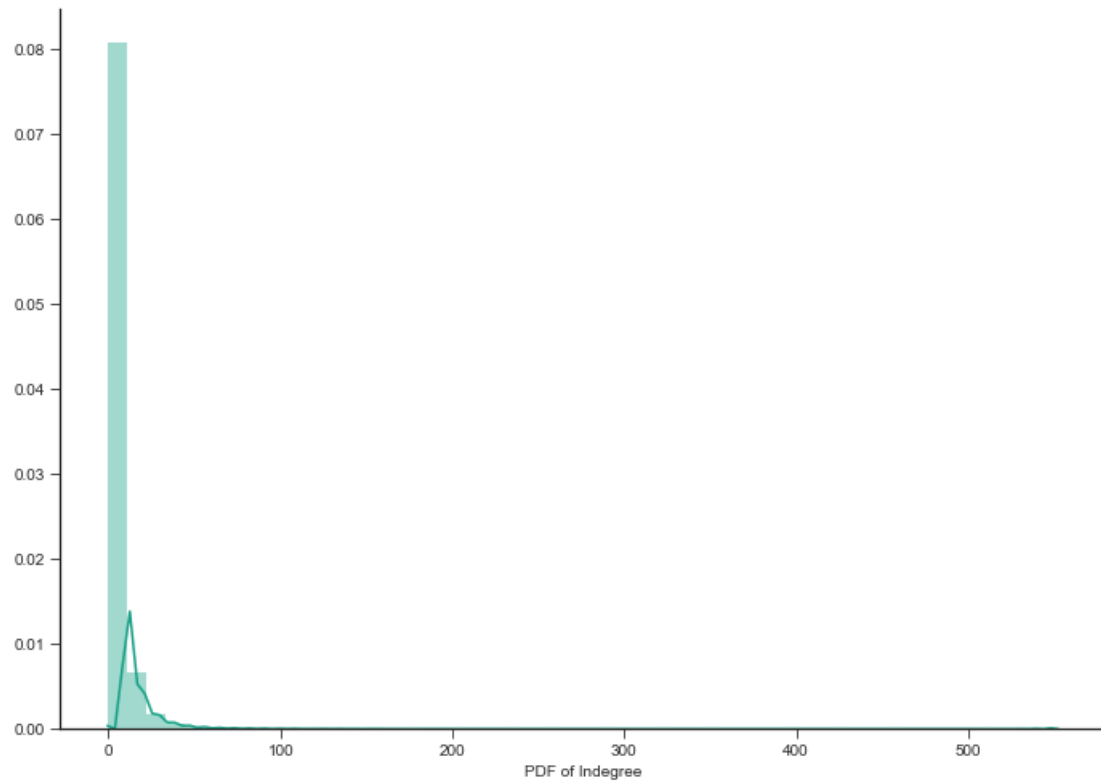
99% of data having followers of 40 only.

```
In [9]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100),'percentile value is',np.percentile(indegree_dist,99+(i/100)))
```

```
99.1 percentile value is 42.0
99.2 percentile value is 44.0
99.3 percentile value is 47.0
99.4 percentile value is 50.0
99.5 percentile value is 55.0
99.6 percentile value is 61.0
99.7 percentile value is 70.0
99.8 percentile value is 84.0
99.9 percentile value is 112.0
100.0 percentile value is 552.0
```

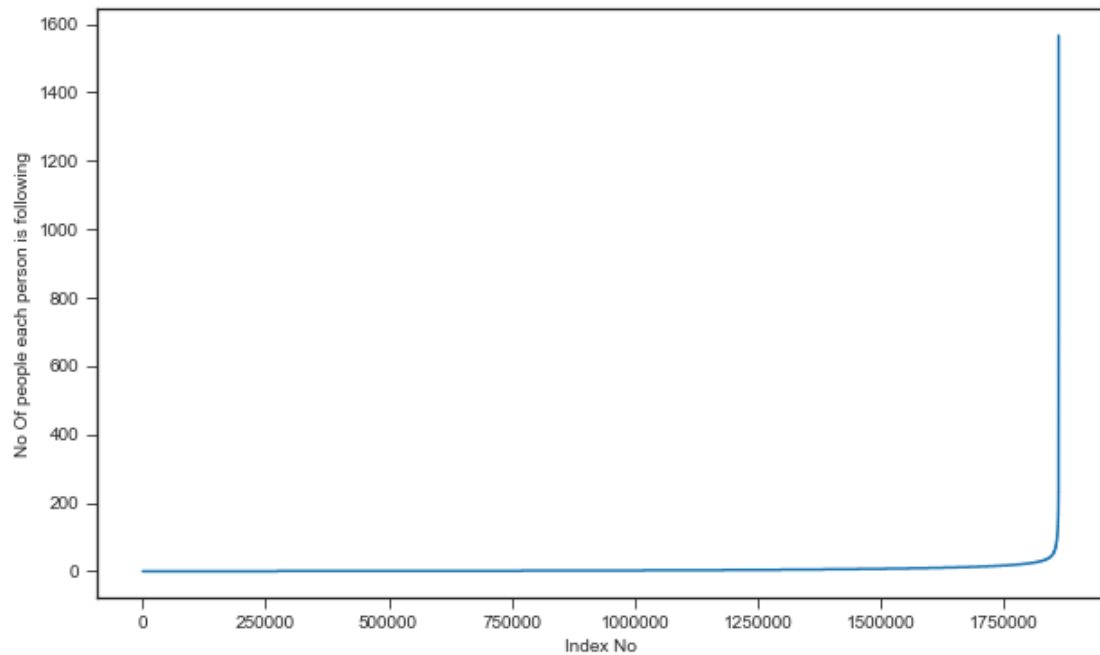
```
In [10]: %matplotlib inline
         sns.set_style('ticks')
         fig, ax = plt.subplots()
         fig.set_size_inches(11.7, 8.27)
         sns.distplot(indegree_dist, color='#16A085')
         plt.xlabel('PDF of Indegree')
         sns.despine()
         #plt.show()
```

D:\installed\Anaconda3\lib\site-packages\matplotlib\axes_axes.py:6571: UserWarning: The 'norm' warnings.warn("The 'normed' kwarg is deprecated, and has been "

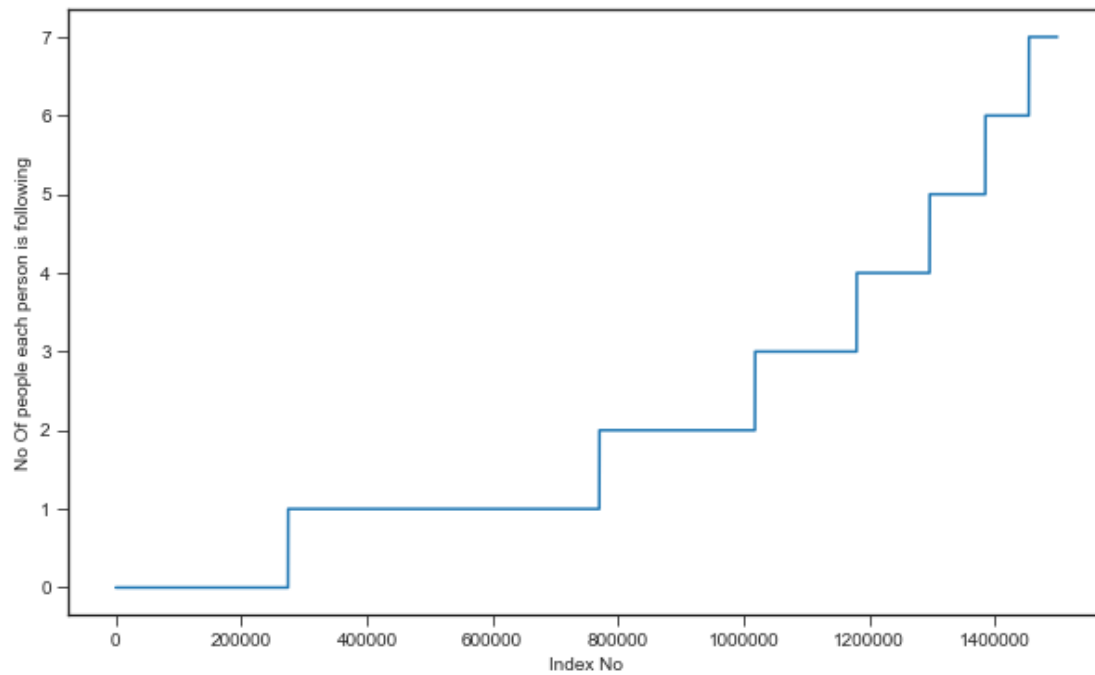


1.2 1.2 No of people each person is following

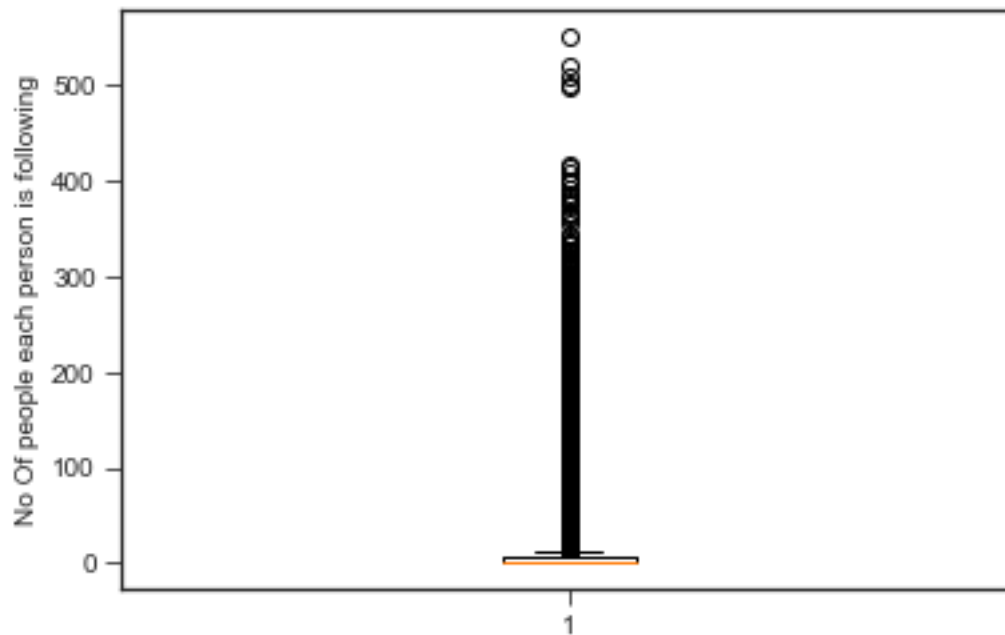
```
In [11]: outdegree_dist = list(dict(g.out_degree()).values())
         outdegree_dist.sort()
         plt.figure(figsize=(10,6))
         plt.plot(outdegree_dist)
         plt.xlabel('Index No')
         plt.ylabel('No Of people each person is following')
         plt.show()
```

```
In [12]: indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(outdegree_dist[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following')
plt.show()
```



```
In [13]: plt.boxplot(indegree_dist)
plt.ylabel('No Of people each person is following')
plt.show()
```



```
In [14]: ### 90-100 percentile
        for i in range(0,11):
            print(90+i,'percentile value is',np.percentile(outdegree_dist,90+i))
```

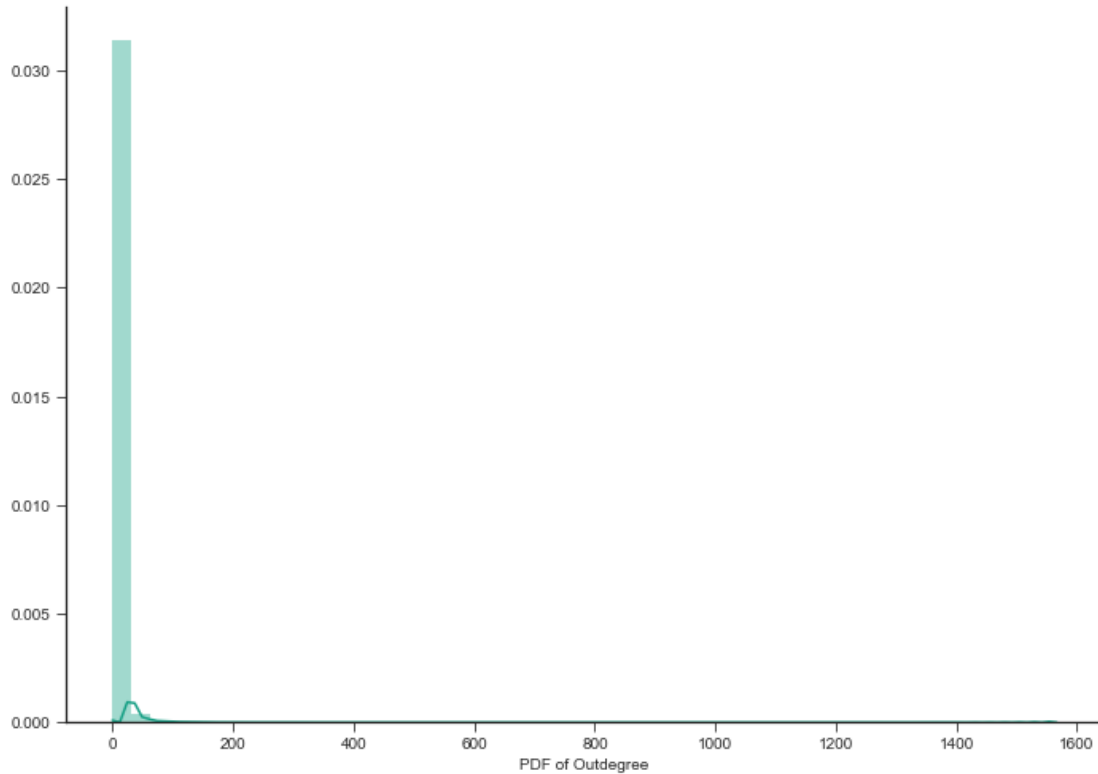
```
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 1566.0
```

```
In [15]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100),'percentile value is',np.percentile(outdegree_dist,99+(i/100)))
```

```
99.1 percentile value is 42.0
99.2 percentile value is 45.0
99.3 percentile value is 48.0
99.4 percentile value is 52.0
99.5 percentile value is 56.0
99.6 percentile value is 63.0
99.7 percentile value is 73.0
99.8 percentile value is 90.0
99.9 percentile value is 123.0
100.0 percentile value is 1566.0
```

```
In [16]: sns.set_style('ticks')
        fig, ax = plt.subplots()
        fig.set_size_inches(11.7, 8.27)
        sns.distplot(outdegree_dist, color='#16A085')
        plt.xlabel('PDF of Outdegree')
        sns.despine()
```

D:\installed\Anaconda3\lib\site-packages\matplotlib\axes_axes.py:6571: UserWarning: The 'norm' warnings.warn("The 'normed' kwarg is deprecated, and has been "



```
In [17]: print('No of persons those are not following anyone are' ,sum(np.array(outdegree_dist.
sum(np.array(outdegree_dist)==0)*100/len(outdegree_dist))
```

No of persons those are not following anyone are 274512 and % is 14.741115442858524

```
In [18]: print('No of persons having zero followers are' ,sum(np.array(indegree_dist)==0),'and
sum(np.array(indegree_dist)==0)*100/len(indegree_dist))
```

No of persons having zero followers are 188043 and % is 10.097786512871734

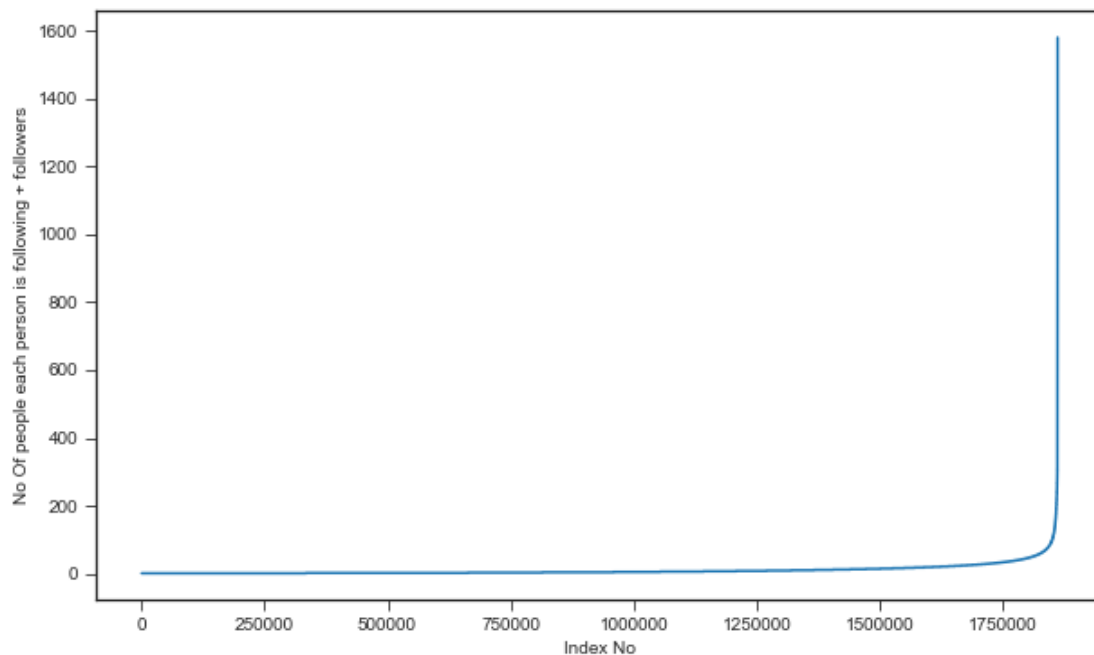
```
In [19]: count=0
for i in g.nodes():
    if len(list(g.predecessors(i)))==0 :
        if len(list(g.successors(i)))==0:
            count+=1
print('No of persons those are not not following anyone and also not having any follow
```

No of persons those are not not following anyone and also not having any followers are 0

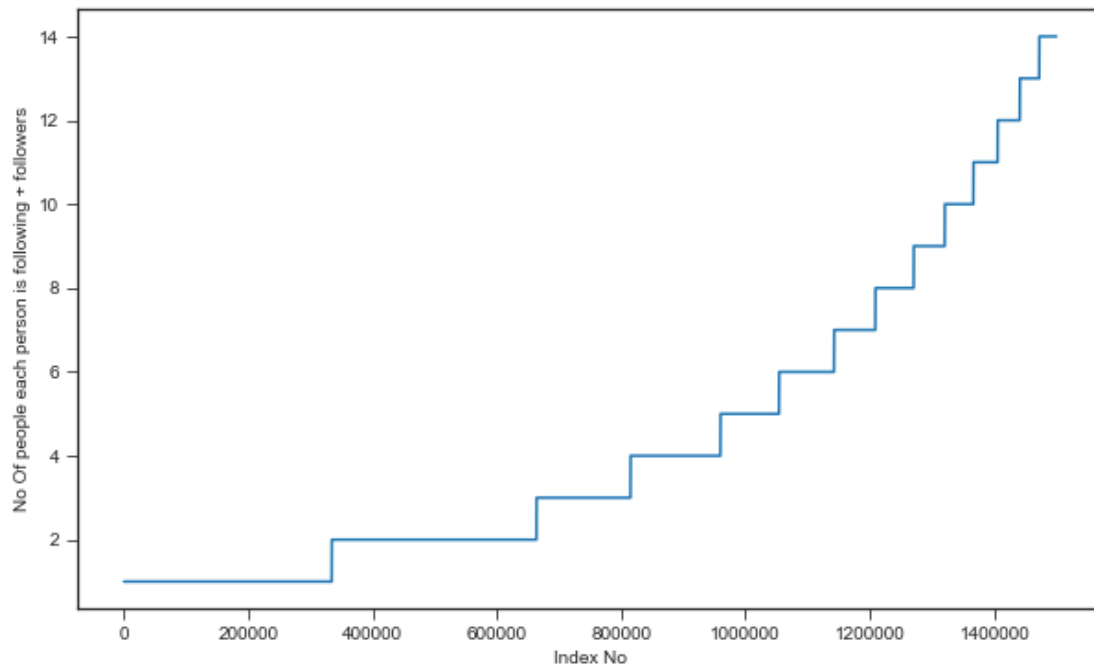
1.3 1.3 both followers + following

```
In [20]: from collections import Counter
dict_in = dict(g.in_degree())
dict_out = dict(g.out_degree())
d = Counter(dict_in) + Counter(dict_out)
in_out_degree = np.array(list(d.values()))
```

```
In [21]: in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort)
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



```
In [22]: in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



```
In [23]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i,'percentile value is',np.percentile(in_out_degree_sort,90+i))
```

```
90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
```

```
In [24]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100),'percentile value is',np.percentile(in_out_degree_sort,99+(i/100)))
```

```
99.1 percentile value is 83.0
99.2 percentile value is 87.0
99.3 percentile value is 93.0
99.4 percentile value is 99.0
```

```

99.5 percentile value is 108.0
99.6 percentile value is 120.0
99.7 percentile value is 138.0
99.8 percentile value is 168.0
99.9 percentile value is 221.0
100.0 percentile value is 1579.0

```

```

In [25]: print('Min of no of followers + following is',in_out_degree.min())
         print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of follow

```

```

Min of no of followers + following is 1
334291 persons having minimum no of followers + following

```

```

In [26]: print('Max of no of followers + following is',in_out_degree.max())
         print(np.sum(in_out_degree==in_out_degree.max()),' persons having maximum no of follow

```

```

Max of no of followers + following is 1579
1 persons having maximum no of followers + following

```

```

In [27]: print('No of persons having followers + following less than 10 are',np.sum(in_out_deg

```

```

No of persons having followers + following less than 10 are 1320326

```

```

In [28]: print('No of weakly connected components',len(list(nx.weakly_connected_components(g))).
         count=0
         for i in list(nx.weakly_connected_components(g)):
             if len(i)==2:
                 count+=1
         print('weakly connected components wit 2 nodes',count)

```

```

No of weakly connected components 45558
weakly connected components wit 2 nodes 32195

```

2 2. Posing a problem as classification problem

2.1 2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```

In [7]: %%time
        ###generating bad edges from given graph
        import random
        if not os.path.isfile('data/after_eda/missing_edges_final.p'):
            #getting all set of edges

```

```

r = csv.reader(open('data/after_eda/train_woheader.csv', 'r'))
edges = dict()
for edge in r:
    edges[(edge[0], edge[1])] = 1

missing_edges = set([])
while (len(missing_edges) < 9437519):
    a = random.randint(1, 1862220)
    b = random.randint(1, 1862220)
    tmp = edges.get((a, b), -1)
    if tmp == -1 and a != b:
        try:
            if nx.shortest_path_length(g, source=a, target=b) > 2:
                missing_edges.add((a, b))
        except:
            missing_edges.add((a, b))
    else:
        continue
    except:
        continue
pickle.dump(missing_edges, open('data/after_eda/missing_edges_final.p', 'wb'))
else:
    missing_edges = pickle.load(open('data/after_eda/missing_edges_final.p', 'rb'))

```

Wall time: 3.17 s

2.2 Training and Test data split:

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

```

In [48]: from sklearn.model_selection import train_test_split
if (not os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and (not os.path.isfile('data/after_eda/train_neg_after_eda.csv')):
    #reading total data df
    df_pos = pd.read_csv('data/train.csv')
    df_neg = pd.DataFrame(list(missing_edges), columns=['source_node', 'destination_node'])

    print("Number of nodes in the graph with edges", df_pos.shape[0])
    print("Number of nodes in the graph without edges", df_neg.shape[0])

    #Train test split
    #Spiltted data into 80-20
    #positive links and negative links seperatly because we need positive training data and negative training data
    #and for feature generation
    X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos, np.ones(df_pos.shape[0]), test_size=0.2, random_state=42)
    X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg, np.zeros(df_neg.shape[0]), test_size=0.2, random_state=42)

```



```

X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,np.zeros(df_neg.shape[0]),
print('='*60)
print("Number of nodes in the train data graph with edges", X_train_pos.shape[0],)
print("Number of nodes in the train data graph without edges", X_train_neg.shape[0],)
print('='*60)
print("Number of nodes in the test data graph with edges", X_test_pos.shape[0],)
print("Number of nodes in the test data graph without edges", X_test_neg.shape[0],)

#removing header and saving
X_train_pos.to_csv('data/after_eda/train_pos_after_eda.csv',header=False, index=False)
X_test_pos.to_csv('data/after_eda/test_pos_after_eda.csv',header=False, index=False)
X_train_neg.to_csv('data/after_eda/train_neg_after_eda.csv',header=False, index=False)
X_test_neg.to_csv('data/after_eda/test_neg_after_eda.csv',header=False, index=False)
else:
    #Graph from Traing data only
    del missing_edges

Number of nodes in the graph with edges 9437519
Number of nodes in the graph without edges 9437519
=====
Number of nodes in the train data graph with edges 7550015 = 7550015
Number of nodes in the train data graph without edges 7550015 = 7550015
=====
Number of nodes in the test data graph with edges 1887504 = 1887504
Number of nodes in the test data graph without edges 1887504 = 1887504

In [49]: if (os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and (os.path.isfile('data/after_eda/test_pos_after_eda.csv')):
    train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter=',')
    test_graph=nx.read_edgelist('data/after_eda/test_pos_after_eda.csv',delimiter=',')
    print(nx.info(train_graph))
    print(nx.info(test_graph))

    # finding the unique nodes in the both train and test graphs
    train_nodes_pos = set(train_graph.nodes())
    test_nodes_pos = set(test_graph.nodes())

    trY_teY = len(train_nodes_pos.intersection(test_nodes_pos))
    trY_teN = len(train_nodes_pos - test_nodes_pos)
    teY_trN = len(test_nodes_pos - train_nodes_pos)

    print('no of people common in train and test -- ',trY_teY)
    print('no of people present in train but not present in test -- ',trY_teN)

    print('no of people present in test but not present in train -- ',teY_trN)
    print(' % of people not there in Train but exist in Test in total Test data are {')

```

Name :

```

Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree: 4.2399
Average out degree: 4.2399
Name:
Type: DiGraph
Number of nodes: 1144623
Number of edges: 1887504
Average in degree: 1.6490
Average out degree: 1.6490
no of people common in train and test -- 1063125
no of people present in train but not present in test -- 717597
no of people present in test but not present in train -- 81498
% of people not there in Train but exist in Test in total Test data are 7.1200735962845405 %

```

we have a cold start problem here

```

In [50]: #final train and test data sets
if (not os.path.isfile('data/after_eda/train_after_eda.csv')) and \
(not os.path.isfile('data/after_eda/test_after_eda.csv')) and \
(not os.path.isfile('data/train_y.csv')) and \
(not os.path.isfile('data/test_y.csv')) and \
(os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and \
(os.path.isfile('data/after_eda/test_pos_after_eda.csv')) and \
(os.path.isfile('data/after_eda/train_neg_after_eda.csv')) and \
(os.path.isfile('data/after_eda/test_neg_after_eda.csv')):

    X_train_pos = pd.read_csv('data/after_eda/train_pos_after_eda.csv', names=['source', 'target'])
    X_test_pos = pd.read_csv('data/after_eda/test_pos_after_eda.csv', names=['source', 'target'])
    X_train_neg = pd.read_csv('data/after_eda/train_neg_after_eda.csv', names=['source', 'target'])
    X_test_neg = pd.read_csv('data/after_eda/test_neg_after_eda.csv', names=['source', 'target'])

    print('='*60)
    print("Number of nodes in the train data graph with edges", X_train_pos.shape[0])
    print("Number of nodes in the train data graph without edges", X_train_neg.shape[0])
    print('='*60)
    print("Number of nodes in the test data graph with edges", X_test_pos.shape[0])
    print("Number of nodes in the test data graph without edges", X_test_neg.shape[0])

    X_train = X_train_pos.append(X_train_neg, ignore_index=True)
    y_train = np.concatenate((y_train_pos, y_train_neg))
    X_test = X_test_pos.append(X_test_neg, ignore_index=True)
    y_test = np.concatenate((y_test_pos, y_test_neg))

    X_train.to_csv('data/after_eda/train_after_eda.csv', header=False, index=False)
    X_test.to_csv('data/after_eda/test_after_eda.csv', header=False, index=False)

```

```
pd.DataFrame(y_train.astype(int)).to_csv('data/train_y.csv',header=False,index=False)
pd.DataFrame(y_test.astype(int)).to_csv('data/test_y.csv',header=False,index=False)
```

```
=====
Number of nodes in the train data graph with edges 7550015
Number of nodes in the train data graph without edges 7550015
=====
Number of nodes in the test data graph with edges 1887504
Number of nodes in the test data graph without edges 1887504
```

```
In [51]: print("Data points in train data",X_train.shape)
         print("Data points in test data",X_test.shape)
         print("Shape of trarget variable in train",y_train.shape)
         print("Shape of trarget variable in test", y_test.shape)
```

```
Data points in train data (15100030, 2)
Data points in test data (3775008, 2)
Shape of trarget variable in train (15100030,)
Shape of trarget variable in test (3775008,)
```

```
In [53]: # computed and store the data for featurization
         # please check out FB_featurization.ipynb
```

3 3. Featurization

```
In [3]: if os.path.isfile('data/after_eda/train_pos_after_eda.csv'):
         train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter=',',
         print(nx.info(train_graph))
         else:
         print("please run the FB_EDA.ipynb or download the files from drive")
```

```
Name:
Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree: 4.2399
Average out degree: 4.2399
```

3.1 3. Similarity measures

3.2 3.1 Jaccard Distance:

<http://www.statisticshowto.com/jaccard-index/>

```
In [4]: #for followees
         def jaccard_for_followees(a,b):
```

```

    try:
        if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
            return 0
        sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))) /
                (len(set(train_graph.successors(a)).union(set(train_graph.successors(b))))))
    except:
        return 0
    return sim

In [5]: #for followers
def jaccard_for_followers(a,b):
    try:
        if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
            return 0
        sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b)))) /
                (len(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(b))))))
    except:
        return 0
    return sim

```

3.3 3.2 Cosine distance

```

In [6]: #for followees
def cosine_for_followees(a,b):
    try:
        if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
            return 0
        sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))) /
                (math.sqrt(len(set(train_graph.successors(a))))*len(set(train_graph.successors(b)))))
    except:
        return 0
    return sim

In [7]: def cosine_for_followers(a,b):
    try:
        if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.predecessors(b))) == 0:
            return 0
        sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b)))) /
                (math.sqrt(len(set(train_graph.predecessors(a))))*len(set(train_graph.predecessors(b)))))
    except:
        return 0
    return sim

```

3.4 3.3 Ranking Measures

3.4.1 3.3.1 Page Ranking

```

In [8]: if not os.path.isfile('data/fea_sample/page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)

```

```

        pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
    else:
        pr = pickle.load(open('data/fea_sample/page_rank.p','rb'))

In [9]: print('min',pr[min(pr, key=pr.get)])
        print('max',pr[max(pr, key=pr.get)])
        print('mean',float(sum(pr.values())) / len(pr))

min 1.6556497245737814e-07
max 2.7098251341935827e-05
mean 5.615699699389075e-07

```

```

In [10]: #for imputing to nodes which are not there in Train data
        mean_pr = float(sum(pr.values())) / len(pr)
        print(mean_pr)

5.615699699389075e-07

```

3.5 4. Other Graph Features

3.5.1 4.1 Shortest path:

```

In [11]: #if has direct edge then deleting that edge and calculating shortest path
        def compute_shortest_path_length(a,b):
            p=-1
            try:
                if train_graph.has_edge(a,b):
                    train_graph.remove_edge(a,b)
                    p= nx.shortest_path_length(train_graph,source=a,target=b)
                    train_graph.add_edge(a,b)
            else:
                p= nx.shortest_path_length(train_graph,source=a,target=b)
            return p
        except:
            return -1

```

3.5.2 4.2 Checking for same community

```

In [12]: #getting weekly connected edges from graph
        wcc=list(nx.weakly_connected_components(train_graph))
        def belongs_to_same_wcc(a,b):
            index = []
            if train_graph.has_edge(b,a):
                return 1
            if train_graph.has_edge(a,b):
                for i in wcc:
                    if a in i:

```

```

        index= i
        break
    if (b in index):
        train_graph.remove_edge(a,b)
        if compute_shortest_path_length(a,b)==-1:
            train_graph.add_edge(a,b)
            return 0
        else:
            train_graph.add_edge(a,b)
            return 1
    else:
        return 0
else:
    for i in wcc:
        if a in i:
            index= i
            break
    if(b in index):
        return 1
    else:
        return 0

```

3.5.3 4.3 Adamic/Adar Index:

In [13]: *#adar index*

```

def calc_adar_in(a,b):
    sum=0
    try:
        n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors
        if len(n)!=0:
            for i in n:
                sum=sum+(1/np.log10(len(list(train_graph.predecessors(i)))))
            return sum
        else:
            return 0
    except:
        return 0

```

3.5.4 4.4 Is person was following back:

```

In [14]: def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0

```

3.5.5 4.5 Katz Centrality:

```
In [15]: if not os.path.isfile('data/fea_sample/katz.p'):
        katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
        pickle.dump(katz,open('data/fea_sample/katz.p','wb'))
    else:
        katz = pickle.load(open('data/fea_sample/katz.p','rb'))
```

```
In [16]: print('min',katz[min(katz, key=katz.get)])
        print('max',katz[max(katz, key=katz.get)])
        print('mean',float(sum(katz.values())) / len(katz))
```

```
min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018
```

```
In [17]: mean_katz = float(sum(katz.values())) / len(katz)
        print(mean_katz)
```

```
0.0007483800935562018
```

3.5.6 4.6 Hits Score

```
In [18]: if not os.path.isfile('data/fea_sample/hits.p'):
        hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
        pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
    else:
        hits = pickle.load(open('data/fea_sample/hits.p','rb'))
```

```
In [19]: print('min',hits[0][min(hits[0], key=hits[0].get)])
        print('max',hits[0][max(hits[0], key=hits[0].get)])
        print('mean',float(sum(hits[0].values())) / len(hits[0]))
```

```
min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
```

3.6 5. Featurization

3.6.1 5.1 Reading a sample of Data from both train and test

```
In [20]: import random
        if os.path.isfile('data/after_eda/train_after_eda.csv'):
            filename = "data/after_eda/train_after_eda.csv"
            # you uncomment this line, if you dont know the lentgh of the file name
            # here we have hardcoded the number of lines as 15100030
            # n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)
```

```

n_train = 15100028
s = 100000 #desired sample size
skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
#https://stackoverflow.com/a/22259008/4084039

```

```

In [21]: if os.path.isfile('data/after_eda/test_after_eda.csv'):
        filename = "data/after_eda/test_after_eda.csv"
        # you uncomment this line, if you dont know the lentgh of the file name
        # here we have hardcoded the number of lines as 3775008
        # n_test = sum(1 for line in open(filename)) #number of records in file (excludes
        n_test = 3775006
        s = 50000 #desired sample size
        skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
        #https://stackoverflow.com/a/22259008/4084039

```

```

In [22]: print("Number of rows in the train data file:", n_train)
        print("Number of rows we are going to elimiate in train data are",len(skip_train))
        print("Number of rows in the test data file:", n_test)
        print("Number of rows we are going to elimiate in test data are",len(skip_test))

```

```

Number of rows in the train data file: 15100028
Number of rows we are going to elimiate in train data are 15000028
Number of rows in the test data file: 3775006
Number of rows we are going to elimiate in test data are 3725006

```

```

In [23]: df_final_train = pd.read_csv('data/after_eda/train_after_eda.csv', skiprows=skip_train)
        df_final_train['indicator_link'] = pd.read_csv('data/train_y.csv', skiprows=skip_train)
        print("Our train matrix size ",df_final_train.shape)
        df_final_train.head(2)

```

```

Our train matrix size  (100002, 3)

```

```

Out[23]:
   source_node  destination_node  indicator_link
0         273084             1505602             1
1        1371356             325548             1

```

```

In [24]: df_final_test = pd.read_csv('data/after_eda/test_after_eda.csv', skiprows=skip_test, n
        df_final_test['indicator_link'] = pd.read_csv('data/test_y.csv', skiprows=skip_test, n
        print("Our test matrix size ",df_final_test.shape)
        df_final_test.head(2)

```

```

Our test matrix size  (50002, 3)

```

```

Out[24]:
   source_node  destination_node  indicator_link
0         848424             784690             1
1         539301             164255             1

```


3.6.2 5.2 Adding a set of features

we will create these each of these features for both train and test data points

jaccard_followers
jaccard_followees
cosine_followers
cosine_followees
num_followers_s
num_followees_s
num_followers_d
num_followees_d
inter_followers
inter_followees

```
In [25]: if not os.path.isfile('data/fea_sample/storage_sample_stage1.h5'):
        print("Inside if")
        #mapping jaccard followers to train and test data
        df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
                                                                    jaccard_for_followers(row['source_node'], row['target_node']),
                                                                    axis=1)
        df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                                                    jaccard_for_followers(row['source_node'], row['target_node']),
                                                                    axis=1)

        #mapping jaccard followees to train and test data
        df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                                                    jaccard_for_followees(row['source_node'], row['target_node']),
                                                                    axis=1)
        df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                                                    jaccard_for_followees(row['source_node'], row['target_node']),
                                                                    axis=1)

        #mapping cosine followers to train and test data
        df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
                                                                    cosine_for_followers(row['source_node'], row['target_node']),
                                                                    axis=1)
        df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                                    cosine_for_followers(row['source_node'], row['target_node']),
                                                                    axis=1)

        #mapping cosine followees to train and test data
        df_final_train['cosine_followees'] = df_final_train.apply(lambda row:
                                                                    cosine_for_followees(row['source_node'], row['target_node']),
                                                                    axis=1)
        df_final_test['cosine_followees'] = df_final_test.apply(lambda row:
                                                                    cosine_for_followees(row['source_node'], row['target_node']),
                                                                    axis=1)
```

Inside if

```
In [26]: def compute_features_stage1(df_final):
        #calculating no of followers followees for source and destination
        #calculating intersection of followers and followees for source and destination
        num_followers_s=[]
        num_followees_s=[]
```

```

num_followers_d=[]
num_followees_d=[]
inter_followers=[]
inter_followees=[]
for i,row in df_final.iterrows():
    try:
        s1=set(train_graph.predecessors(row['source_node']))
        s2=set(train_graph.successors(row['source_node']))
    except:
        s1 = set()
        s2 = set()
    try:
        d1=set(train_graph.predecessors(row['destination_node']))
        d2=set(train_graph.successors(row['destination_node']))
    except:
        d1 = set()
        d2 = set()
    num_followers_s.append(len(s1))
    num_followees_s.append(len(s2))

    num_followers_d.append(len(d1))
    num_followees_d.append(len(d2))

    inter_followers.append(len(s1.intersection(d1)))
    inter_followees.append(len(s2.intersection(d2)))

return num_followers_s, num_followers_d, num_followees_s, num_followees_d, inter_

```

```

In [33]: if not os.path.isfile('storage_sample_stage1.h5'):
    df_final_train['num_followers_s'], df_final_train['num_followers_d'], \
    df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
    df_final_train['inter_followers'], df_final_train['inter_followees']= compute_featu

    df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
    df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
    df_final_test['inter_followers'], df_final_test['inter_followees']= compute_featu

    hdf = HDFStore('storage_sample_stage1.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df_final_train = read_hdf('storage_sample_stage1.h5', 'train_df',mode='r')
    df_final_test = read_hdf('storage_sample_stage1.h5', 'test_df',mode='r')

```

3.6.3 5.3 Adding new set of features

we will create these each of these features for both train and test data points

adar index
 is following back
 belongs to same weakly connect components
 shortest path between source and destination

```
In [28]: if not os.path.isfile('data/fea_sample/storage_sample_stage2.h5'):
    #mapping adar index on train
    df_final_train['adar_index'] = df_final_train.apply(lambda row: calc_adar_in(row['source'], row['target']), axis=1)
    #mapping adar index on test
    df_final_test['adar_index'] = df_final_test.apply(lambda row: calc_adar_in(row['source'], row['target']), axis=1)

    #-----
    #mapping followback or not on train
    df_final_train['follows_back'] = df_final_train.apply(lambda row: follows_back(row['source'], row['target']), axis=1)

    #mapping followback or not on test
    df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_back(row['source'], row['target']), axis=1)

    #-----
    #mapping same component of wcc or not on train
    df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_to_same_wcc(row['source'], row['target']), axis=1)

    ##mapping same component of wcc or not on train
    df_final_test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_wcc(row['source'], row['target']), axis=1)

    #-----
    #mapping shortest path on train
    df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path(row['source'], row['target']), axis=1)
    #mapping shortest path on test
    df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_shortest_path(row['source'], row['target']), axis=1)

    hdf = HDFStore('data/fea_sample/storage_sample_stage2.h5')
    hdf.put('train_df', df_final_train, format='table', data_columns=True)
    hdf.put('test_df', df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df_final_train = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'train_df', mode='r')
    df_final_test = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'test_df', mode='r')
```

3.6.4 5.4 Adding new set of features

we will create these each of these features for both train and test data points

Weight Features
 weight of incoming edges
 weight of outgoing edges
 weight of incoming edges + weight of outgoing edges
 weight of incoming edges * weight of outgoing edges
 2*weight of incoming edges + weight of outgoing edges

weight of incoming edges + 2*weight of outgoing edges

Page Ranking of source

Page Ranking of dest

katz of source

katz of dest

hubs of source

hubs of dest

authorities_s of source

authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

```
In [29]: #weight for source and destination of each link
```

```
Weight_in = {}
Weight_out = {}
for i in tqdm(train_graph.nodes()):
    s1=set(train_graph.predecessors(i))
    w_in = 1.0/(np.sqrt(1+len(s1)))
    Weight_in[i]=w_in

    s2=set(train_graph.successors(i))
    w_out = 1.0/(np.sqrt(1+len(s2)))
    Weight_out[i]=w_out

    #for imputing with mean
    mean_weight_in = np.mean(list(Weight_in.values()))
    mean_weight_out = np.mean(list(Weight_out.values()))
```

```
100%|| 1780722/1780722 [00:13<00:00, 133302.15it/s]
```

```
In [30]: if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
```

```
    print("File not present")
    #mapping to pandas train
    df_final_train['weight_in'] = df_final_train.destination_node.apply(lambda x: Weight_in[x])
    df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out[x])

    #mapping to pandas test
    df_final_test['weight_in'] = df_final_test.destination_node.apply(lambda x: Weight_in[x])
    df_final_test['weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out[x])

    #some features engineerings on the in and out weights
```

```

df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_out
df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_out)
df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_out)

#some features engineerings on the in and out weights
df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)

```

File not present

```
In [31]: if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
```

```

    #page rank for source and destination in Train and Test
    #if anything not there in train graph then adding mean page rank
    df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda x: pr.get(x, pr.mean))
    df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x: pr.get(x, pr.mean))

    df_final_test['page_rank_s'] = df_final_test.source_node.apply(lambda x: pr.get(x, pr.mean))
    df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x: pr.get(x, pr.mean))
    #=====

    #Katz centrality score for source and destination in Train and test
    #if anything not there in train graph then adding mean katz score
    df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x, katz.mean))
    df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x, katz.mean))

    df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x, katz.mean))
    df_final_test['katz_d'] = df_final_test.destination_node.apply(lambda x: katz.get(x, katz.mean))
    #=====

    #Hits algorithm score for source and destination in Train and test
    #if anything not there in train graph then adding 0
    df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x, 0))
    df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x: hits[0].get(x, 0))

    df_final_test['hubs_s'] = df_final_test.source_node.apply(lambda x: hits[0].get(x, 0))
    df_final_test['hubs_d'] = df_final_test.destination_node.apply(lambda x: hits[0].get(x, 0))
    #=====

    #Hits algorithm score for source and destination in Train and Test
    #if anything not there in train graph then adding 0
    df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda x: hits[1].get(x, 0))
    df_final_train['authorities_d'] = df_final_train.destination_node.apply(lambda x: hits[1].get(x, 0))

```

```

df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hits[1])
df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: h
#=====

hdf = HDFStore('data/fea_sample/storage_sample_stage3.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
else:
    df_final_train = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'train_df',m
    df_final_test = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'test_df',mo

```

In [34]: df_final_train.head()

```

Out[34]:
  source_node  destination_node  indicator_link  jaccard_followers \
0         273084         1505602             1             0
1         832016         1543415             1             0
2        1325247          760242             1             0
3        1368400         1006992             1             0
4         140165         1708748             1             0

  jaccard_followees  cosine_followers  cosine_followees  num_followers_s \
0             0.000000             0.000000             0.000000         11
1             0.187135             0.028382             0.343828         17
2             0.369565             0.156957             0.566038         35
3             0.000000             0.000000             0.000000          2
4             0.000000             0.000000             0.000000          5

  num_followees_s  num_followees_d  ...  weight_f3  weight_f4  page_rank_s \
0              15              8  ...   1.005929   0.877964  2.045290e-06
1              61             142  ...   0.332196   0.356598  2.353458e-07
2              41              22  ...   0.525694   0.494302  6.211019e-07
3               5               7  ...   0.985599   1.105172  2.998153e-07
4              10               3  ...   2.301511   1.603023  4.349180e-07

  page_rank_d  katz_s  katz_d  hubs_s  hubs_d \
0  3.459963e-07  0.000773  0.000756  1.943132e-13  1.941103e-13
1  6.427660e-07  0.000845  0.001317  3.906648e-11  9.424102e-11
2  5.179801e-07  0.000885  0.000855  7.730764e-114  4.067322e-114
3  1.704245e-06  0.000739  0.000773  5.443738e-17  4.139999e-16
4  2.089590e-07  0.000751  0.000735  3.887821e-16  4.721269e-16

  authorities_s  authorities_d
0  9.226339e-16  2.231877e-15
1  1.208074e-11  1.273080e-10
2  2.681298e-113  2.199205e-113
3  2.413250e-14  6.688064e-15
4  7.552255e-16  2.734009e-18

```

```
[5 rows x 31 columns]
```

3.6.5 5.5 Adding new set of features

we will create these each of these features for both train and test data points

SVD features for both source and destination

```
In [35]: def svd(x, S):
          try:
              z = sadj_dict[x]
              return S[z]
          except:
              return [0,0,0,0,0,0]
```

```
In [36]: #for svd features to get feature vector creating a dict node val and inedx in svd vec
sadj_col = sorted(train_graph.nodes())
sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
```

```
In [37]: Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).astype('float64')
```

```
In [38]: U, s, V = svds(Adj, k = 6)
          print('Adjacency matrix Shape', Adj.shape)
          print('U Shape', U.shape)
          print('V Shape', V.shape)
          print('s Shape', s.shape)
```

Adjacency matrix Shape (1780722, 1780722)

U Shape (1780722, 6)

V Shape (6, 1780722)

s Shape (6,)

```
In [39]: if os.path.isfile('data/fea_sample/storage_sample_stage4.h5'):
#=====

df_final_train[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', ...],
df_final_train.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)

df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', ...],
df_final_train.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
#=====

df_final_train[['svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', ...],
df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)

df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', ...],
df_final_train.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
#=====
```

```

df_final_test[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6'],
df_final_test.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)

df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6'],
df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)

#=====

df_final_test[['svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6'],
df_final_test.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)

df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
df_final_test.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
#=====

hdf = HDFStore('data/fea_sample/storage_sample_stage4.h5')
hdf.put('train_df', df_final_train, format='table', data_columns=True)
hdf.put('test_df', df_final_test, format='table', data_columns=True)
hdf.close()

```

In [40]: df_final_train.columns

```

Out[40]: Index(['source_node', 'destination_node', 'indicator_link',
'jaccard_followers', 'jaccard_followees', 'cosine_followers',
'cosine_followees', 'num_followers_s', 'num_followees_s',
'num_followees_d', 'inter_followers', 'inter_followees',
'num_followers_d', 'adar_index', 'follows_back', 'same_comp',
'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
dtype='object')

```

3.6.6 5.6 Preferential Attachment

Preferential Attachement for followers

In [41]: *#for train dataset*

```

train_followers_s = np.array(df_final_train['num_followers_s'])
train_followers_d = np.array(df_final_train['num_followers_d'])
preferential_followers=[]
for i in range(len(train_followers_s)):
    preferential_followers.append(train_followers_d[i]*train_followers_s[i])

```



```
df_final_train['preferential_followers']= preferential_followers
df_final_train.head()
```

```
Out[41]:
```

	source_node	destination_node	indicator_link	jaccard_followers	\
0	273084	1505602	1	0	
1	832016	1543415	1	0	
2	1325247	760242	1	0	
3	1368400	1006992	1	0	
4	140165	1708748	1	0	

	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	\
0	0.000000	0.000000	0.000000	11	
1	0.187135	0.028382	0.343828	17	
2	0.369565	0.156957	0.566038	35	
3	0.000000	0.000000	0.000000	2	
4	0.000000	0.000000	0.000000	5	

	num_followees_s	num_followees_d	...	svd_v_s_4	svd_v_s_5	\
0	15	8	...	1.545075e-13	8.108434e-13	
1	61	142	...	1.345726e-02	3.703479e-12	
2	41	22	...	-7.021227e-19	1.940403e-19	
3	5	7	...	1.514614e-11	1.513483e-12	
4	10	3	...	1.999809e-14	3.360247e-13	

	svd_v_s_6	svd_v_d_1	svd_v_d_2	svd_v_d_3	svd_v_d_4	\
0	1.719702e-14	-1.355368e-12	4.675307e-13	1.128591e-06	6.616550e-14	
1	2.251737e-10	1.245101e-12	-1.636948e-10	-3.112650e-10	6.738902e-02	
2	-3.365389e-19	-1.238370e-18	1.438175e-19	-1.852863e-19	-5.901864e-19	
3	4.498061e-13	-9.818087e-10	3.454672e-11	5.213635e-08	9.595823e-13	
4	1.407670e-14	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	

	svd_v_d_5	svd_v_d_6	preferential_followers
0	9.771077e-13	4.159752e-14	66
1	2.607801e-11	2.372904e-09	1598
2	1.629341e-19	-2.572452e-19	980
3	3.047045e-10	1.246592e-13	22
4	0.000000e+00	0.000000e+00	0

[5 rows x 56 columns]

```
In [42]: # for test dataset
```

```
test_followers_s = np.array(df_final_test['num_followers_s'])
test_followers_d = np.array(df_final_test['num_followers_d'])
preferential_followers=[]
for i in range(len(test_followers_s)):
    preferential_followers.append(test_followers_d[i]*test_followers_s[i])
df_final_test['preferential_followers']= preferential_followers
df_final_test.head()
```

```

Out [42]:
  source_node  destination_node  indicator_link  jaccard_followers  \
0      848424           784690                1                0
1      483294          1255532                1                0
2      626190          1729265                1                0
3      947219          425228                 1                0
4      991374          975044                1                0

  jaccard_followees  cosine_followers  cosine_followees  num_followers_s  \
0                0.0           0.029161           0.000000                6
1                0.0           0.000000           0.000000                2
2                0.0           0.000000           0.000000               15
3                0.0           0.000000           0.000000               11
4                0.2           0.042767           0.347833               12

  num_followees_s  num_followees_d  ...  svd_v_s_4  svd_v_s_5  \
0                6                9  ...  2.701538e-12  4.341620e-13
1                1               19  ...  2.248568e-14  3.600957e-13
2               16                9  ...  1.778927e-12  2.740535e-13
3               10               34  ...  7.917166e-13  4.020707e-12
4               15               27  ...  1.361574e-13  1.154623e-12

  svd_v_s_6  svd_v_d_1  svd_v_d_2  svd_v_d_3  svd_v_d_4  \
0  5.535503e-14 -9.994076e-10  5.791910e-10  3.512364e-07  2.486658e-09
1  4.701436e-15 -9.360516e-12  3.206809e-10  4.668696e-08  6.665777e-12
2  4.199834e-14 -4.253075e-13  4.789463e-13  3.479824e-07  1.630549e-13
3  2.817657e-13 -2.162590e-11  6.939194e-12  1.879861e-05  4.384816e-12
4  9.656662e-14 -8.742904e-12  7.467370e-12  1.256880e-05  3.636983e-12

  svd_v_d_5  svd_v_d_6  preferential_followers
0  2.771146e-09  1.727694e-12                84
1  1.495979e-10  9.836670e-14                34
2  3.954708e-13  3.875785e-14               150
3  1.239414e-11  6.483485e-13               407
4  3.948463e-12  2.415863e-13               324

[5 rows x 56 columns]

```

Preferential Attachment for followees

```
In [43]: #for train dataset
```

```

train_followees_s = np.array(df_final_train['num_followees_s'])
train_followees_d = np.array(df_final_train['num_followees_d'])
preferential_followees=[]
for i in range(len(train_followees_s)):
    preferential_followees.append(train_followees_d[i]*train_followees_s[i])
df_final_train['preferential_followees']= preferential_followees
df_final_train.head()

```

```

Out[43]:
  source_node  destination_node  indicator_link  jaccard_followers  \
0      273084      1505602             1             0
1      832016      1543415             1             0
2     1325247       760242             1             0
3     1368400      1006992             1             0
4      140165      1708748             1             0

  jaccard_followees  cosine_followers  cosine_followees  num_followers_s  \
0      0.000000      0.000000      0.000000      11
1      0.187135      0.028382      0.343828      17
2      0.369565      0.156957      0.566038      35
3      0.000000      0.000000      0.000000       2
4      0.000000      0.000000      0.000000       5

  num_followees_s  num_followees_d  ...  svd_v_s_5  svd_v_s_6  \
0      15      8  ...  8.108434e-13  1.719702e-14
1      61     142  ...  3.703479e-12  2.251737e-10
2      41      22  ...  1.940403e-19 -3.365389e-19
3       5       7  ...  1.513483e-12  4.498061e-13
4      10       3  ...  3.360247e-13  1.407670e-14

  svd_v_d_1  svd_v_d_2  svd_v_d_3  svd_v_d_4  svd_v_d_5  \
0 -1.355368e-12  4.675307e-13  1.128591e-06  6.616550e-14  9.771077e-13
1  1.245101e-12 -1.636948e-10 -3.112650e-10  6.738902e-02  2.607801e-11
2 -1.238370e-18  1.438175e-19 -1.852863e-19 -5.901864e-19  1.629341e-19
3 -9.818087e-10  3.454672e-11  5.213635e-08  9.595823e-13  3.047045e-10
4  0.000000e+00  0.000000e+00  0.000000e+00  0.000000e+00  0.000000e+00

  svd_v_d_6  preferential_followers  preferential_followees
0  4.159752e-14      66      120
1  2.372904e-09     1598     8662
2 -2.572452e-19      980      902
3  1.246592e-13       22       35
4  0.000000e+00        0       30

```

[5 rows x 57 columns]

```
In [44]: #for test dataset
```

```

test_followees_s = np.array(df_final_test['num_followees_s'])
test_followees_d = np.array(df_final_test['num_followees_d'])
preferential_followees=[]
for i in range(len(test_followees_s)):
    preferential_followees.append(test_followees_d[i]*test_followees_s[i])
df_final_test['preferential_followees']= preferential_followees
df_final_test.head()

```

```

Out[44]:
  source_node  destination_node  indicator_link  jaccard_followers  \
0      848424      784690             1             0

```

1	483294	1255532	1	0
2	626190	1729265	1	0
3	947219	425228	1	0
4	991374	975044	1	0

	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	\
0	0.0	0.029161	0.000000	6	
1	0.0	0.000000	0.000000	2	
2	0.0	0.000000	0.000000	15	
3	0.0	0.000000	0.000000	11	
4	0.2	0.042767	0.347833	12	

	num_followees_s	num_followees_d	...	svd_v_s_5	svd_v_s_6	\
0	6	9	...	4.341620e-13	5.535503e-14	
1	1	19	...	3.600957e-13	4.701436e-15	
2	16	9	...	2.740535e-13	4.199834e-14	
3	10	34	...	4.020707e-12	2.817657e-13	
4	15	27	...	1.154623e-12	9.656662e-14	

	svd_v_d_1	svd_v_d_2	svd_v_d_3	svd_v_d_4	svd_v_d_5	\
0	-9.994076e-10	5.791910e-10	3.512364e-07	2.486658e-09	2.771146e-09	
1	-9.360516e-12	3.206809e-10	4.668696e-08	6.665777e-12	1.495979e-10	
2	-4.253075e-13	4.789463e-13	3.479824e-07	1.630549e-13	3.954708e-13	
3	-2.162590e-11	6.939194e-12	1.879861e-05	4.384816e-12	1.239414e-11	
4	-8.742904e-12	7.467370e-12	1.256880e-05	3.636983e-12	3.948463e-12	

	svd_v_d_6	preferential_followers	preferential_followees
0	1.727694e-12	84	54
1	9.836670e-14	34	19
2	3.875785e-14	150	144
3	6.483485e-13	407	340
4	2.415863e-13	324	405

[5 rows x 57 columns]

3.6.7 5.7 SVD_dot

In [45]: *#for train datasets*

```

su1,su2,su3,su4,su5,su6=df_final_train['svd_u_s_1'],df_final_train['svd_u_s_2'],df_final_train['svd_u_s_3'],df_final_train['svd_u_s_4'],df_final_train['svd_u_s_5'],df_final_train['svd_u_s_6']
sv1,sv2,sv3,sv4,sv5,sv6=df_final_train['svd_v_s_1'],df_final_train['svd_v_s_2'],df_final_train['svd_v_s_3'],df_final_train['svd_v_s_4'],df_final_train['svd_v_s_5'],df_final_train['svd_v_s_6']

du1,du2,du3,du4,du5,du6=df_final_train['svd_u_d_1'],df_final_train['svd_u_d_2'],df_final_train['svd_u_d_3'],df_final_train['svd_u_d_4'],df_final_train['svd_u_d_5'],df_final_train['svd_u_d_6']
dv1,dv2,dv3,dv4,dv5,dv6=df_final_train['svd_v_d_1'],df_final_train['svd_v_d_2'],df_final_train['svd_v_d_3'],df_final_train['svd_v_d_4'],df_final_train['svd_v_d_5'],df_final_train['svd_v_d_6']

```

```

In [46]: su = np.array([su1,su2,su3,su4,su5,su6]).T
sv = np.array([sv1,sv2,sv3,sv4,sv5,sv6]).T
print(su.shape)

```

```

        print(sv.shape)

(100002, 6)
(100002, 6)

In [48]: du = np.array([du1,du2,du3,du4,du5,du6]).T
        dv = np.array([dv1,dv2,dv3,dv4,dv5,dv6]).T
        print(du.shape)
        print(dv.shape)

(100002, 6)
(100002, 6)

In [50]: u_dot = []
        v_dot = []
        for ea in range(su.shape[0]):
            u_dot.append(np.dot(su[ea],du[ea]))
            v_dot.append(np.dot(sv[ea],dv[ea]))
        df_final_train['ud_dot']=u_dot
        df_final_train['vd_dot']=v_dot

In [51]: #for test datasets
        su1,su2,su3,su4,su5,su6=df_final_test['svd_u_s_1'],df_final_test['svd_u_s_2'],df_final_test['svd_u_s_3'],df_final_test['svd_u_s_4'],df_final_test['svd_u_s_5'],df_final_test['svd_u_s_6']
        sv1,sv2,sv3,sv4,sv5,sv6=df_final_test['svd_v_s_1'],df_final_test['svd_v_s_2'],df_final_test['svd_v_s_3'],df_final_test['svd_v_s_4'],df_final_test['svd_v_s_5'],df_final_test['svd_v_s_6']

        du1,du2,du3,du4,du5,du6=df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_3'],df_final_test['svd_u_d_4'],df_final_test['svd_u_d_5'],df_final_test['svd_u_d_6']
        dv1,dv2,dv3,dv4,dv5,dv6=df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_3'],df_final_test['svd_v_d_4'],df_final_test['svd_v_d_5'],df_final_test['svd_v_d_6']

In [52]: su = np.array([su1,su2,su3,su4,su5,su6]).T
        sv = np.array([sv1,sv2,sv3,sv4,sv5,sv6]).T
        print(su.shape)
        print(sv.shape)

        du = np.array([du1,du2,du3,du4,du5,du6]).T
        dv = np.array([dv1,dv2,dv3,dv4,dv5,dv6]).T
        print(du.shape)
        print(dv.shape)

(50002, 6)
(50002, 6)
(50002, 6)
(50002, 6)

In [53]: u_dot = []
        v_dot = []

```

```

for ea in range(su.shape[0]):
    u_dot.append(np.dot(su[ea],du[ea]))
    v_dot.append(np.dot(sv[ea],dv[ea]))
df_final_test['ud_dot']=u_dot
df_final_test['vd_dot']=v_dot

```

```

In [54]: hdf = HDFStore('storage_sample_stage4.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()

```

4 Models

```

In [92]: #reading
from pandas import read_hdf
df_final_train = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'train_df',mode='r')
df_final_test = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'test_df',mode='r')

```

```

In [55]: df_final_train.columns

```

```

Out[55]: Index(['source_node', 'destination_node', 'indicator_link',
                'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                'cosine_followees', 'num_followers_s', 'num_followees_s',
                'num_followees_d', 'inter_followers', 'inter_followees',
                'num_followers_d', 'adar_index', 'follows_back', 'same_comp',
                'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
                'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
                'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
                'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
                'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
                'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
                'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
                'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                'preferential_followers', 'preferential_followees', 'ud_dot', 'vd_dot'],
                dtype='object')

```

```

In [56]: y_train = df_final_train.indicator_link
y_test = df_final_test.indicator_link

```

```

In [57]: df_final_train.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=True)
df_final_test.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=True)

```

4.1 6.1 Random Forest

```

In [58]: estimators = [10,50,100,250,450]
train_scores = []
test_scores = []
for i in estimators:

```

```

clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                             max_depth=5, max_features='auto', max_leaf_nodes=None,
                             min_impurity_decrease=0.0, min_impurity_split=None,
                             min_samples_leaf=52, min_samples_split=120,
                             min_weight_fraction_leaf=0.0, n_estimators=i, n_jobs=-1, random_state=25, verbose=0)
clf.fit(df_final_train,y_train)
train_sc = f1_score(y_train,clf.predict(df_final_train))
test_sc = f1_score(y_test,clf.predict(df_final_test))
test_scores.append(test_sc)
train_scores.append(train_sc)
print('Estimators = ',i,'Train Score',train_sc,'test Score',test_sc)
plt.plot(estimators,train_scores,label='Train Score')
plt.plot(estimators,test_scores,label='Test Score')
plt.xlabel('Estimators')
plt.ylabel('Score')
plt.title('Estimators vs score at depth of 5')

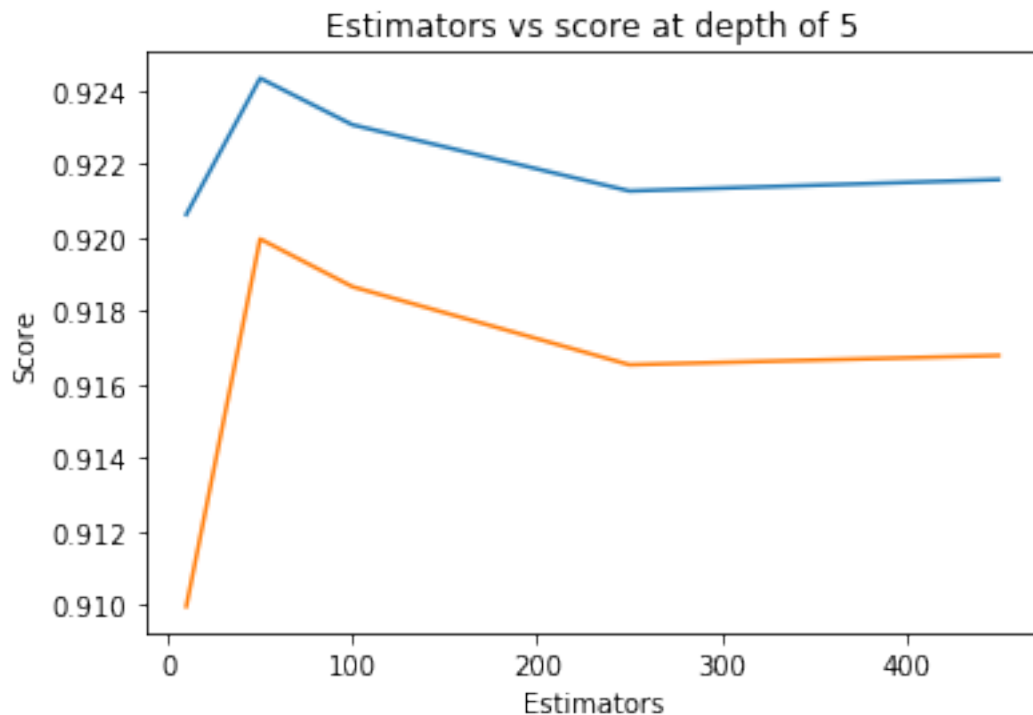
```

```

Estimators = 10 Train Score 0.9206276581363669 test Score 0.9099420606264169
Estimators = 50 Train Score 0.9243443808565498 test Score 0.919961264788851
Estimators = 100 Train Score 0.9230737062205958 test Score 0.9186600861073191
Estimators = 250 Train Score 0.9212693899736589 test Score 0.9165319957185133
Estimators = 450 Train Score 0.9215796838126267 test Score 0.9167837299507284

```

Out[58]: Text(0.5, 1.0, 'Estimators vs score at depth of 5')



```

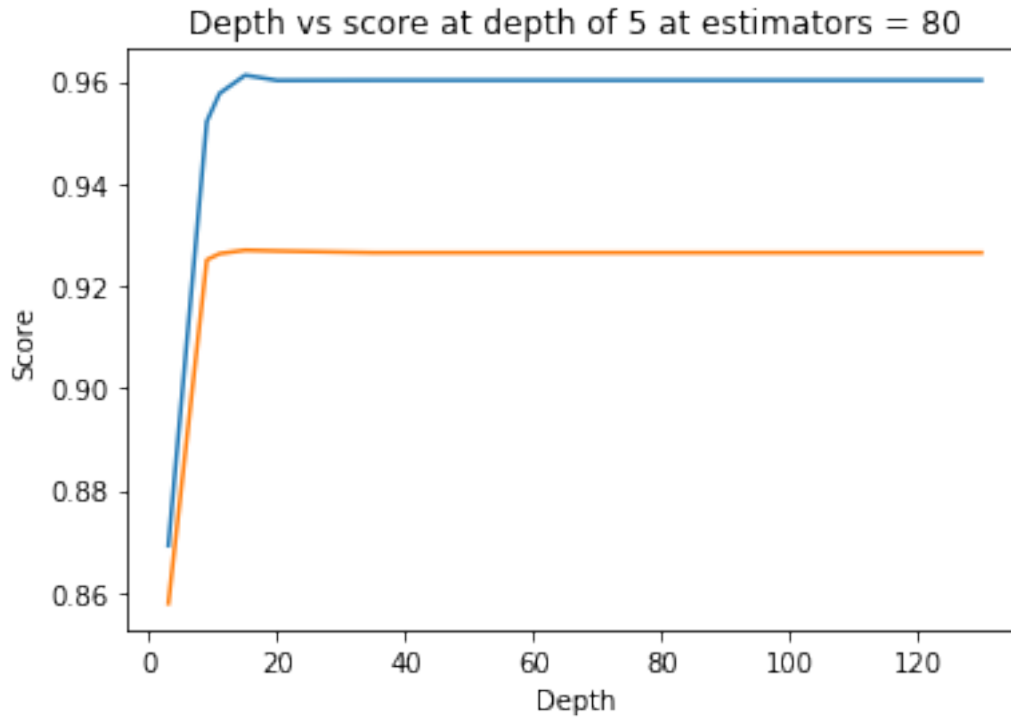
In [61]: depths = [3,9,11,15,20,35,50,70,130]
        train_scores = []
        test_scores = []
        for i in depths:
            clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                                       max_depth=i, max_features='auto', max_leaf_nodes=None,
                                       min_impurity_decrease=0.0, min_impurity_split=None,
                                       min_samples_leaf=52, min_samples_split=120,
                                       min_weight_fraction_leaf=0.0, n_estimators=80, n_jobs=-1, random_state=25,
                                       )
            clf.fit(df_final_train,y_train)
            train_sc = f1_score(y_train,clf.predict(df_final_train))
            test_sc = f1_score(y_test,clf.predict(df_final_test))
            test_scores.append(test_sc)
            train_scores.append(train_sc)
            print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
        plt.plot(depths,train_scores,label='Train Score')
        plt.plot(depths,test_scores,label='Test Score')
        plt.xlabel('Depth')
        plt.ylabel('Score')
        plt.title('Depth vs score at depth of 5 at estimators = 80')
        plt.show()

```

```

depth = 3 Train Score 0.8691679564498052 test Score 0.8578205183492174
depth = 9 Train Score 0.9521841009321695 test Score 0.9250940264324586
depth = 11 Train Score 0.9576999204195319 test Score 0.9263131323755233
depth = 15 Train Score 0.9612562252261408 test Score 0.9269964055241419
depth = 20 Train Score 0.9602348599912336 test Score 0.9268426263349693
depth = 35 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 50 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 70 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 130 Train Score 0.9602689486552567 test Score 0.9265046540032852

```

```
In [62]: from sklearn.metrics import f1_score
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import f1_score
from sklearn.model_selection import RandomizedSearchCV
from scipy.stats import randint as sp_randint
from scipy.stats import uniform

param_dist = {"n_estimators": sp_randint(50,100),
              "max_depth": sp_randint(10,20),
              "min_samples_split": sp_randint(110,190),
              "min_samples_leaf": sp_randint(25,65)}

clf = RandomForestClassifier(random_state=25,n_jobs=-1)

rf_random = RandomizedSearchCV(clf, param_distributions=param_dist,
                              n_iter=5,cv=10,scoring='f1',random_state=25)

rf_random.fit(df_final_train,y_train)
print('mean test scores',rf_random.cv_results_['mean_test_score'])
print('mean train scores',rf_random.cv_results_['mean_train_score'])

mean test scores [0.95942393 0.95962772 0.9588493  0.96084579 0.9609113 ]
mean train scores [0.96016827 0.96014306 0.95956999 0.96201388 0.96198856]
```

```
In [63]: print(rf_random.best_estimator_)
```

```
RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                        max_depth=14, max_features='auto', max_leaf_nodes=None,
                        min_impurity_decrease=0.0, min_impurity_split=None,
                        min_samples_leaf=28, min_samples_split=111,
                        min_weight_fraction_leaf=0.0, n_estimators=72, n_jobs=-1,
                        oob_score=False, random_state=25, verbose=0, warm_start=False)
```

Best Parameters found

- max_depth = 14
- n_estimators = 72
- min_samples_leaf=28
- min_samples_split=111

```
In [64]: clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                                     max_depth=14, max_features='auto', max_leaf_nodes=None,
                                     min_impurity_decrease=0.0, min_impurity_split=None,
                                     min_samples_leaf=28, min_samples_split=111,
                                     min_weight_fraction_leaf=0.0, n_estimators=72, n_jobs=-1,
                                     oob_score=False, random_state=25, verbose=0, warm_start=False)
```

```
In [65]: clf.fit(df_final_train,y_train)
y_train_pred = clf.predict(df_final_train)
y_test_pred = clf.predict(df_final_test)
```

```
In [66]: from sklearn.metrics import f1_score
print('Train f1 score',f1_score(y_train,y_train_pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
```

Train f1 score 0.962169849654612

Test f1 score 0.9273067148348071

Confusion Matrix

```
In [67]: from sklearn.metrics import confusion_matrix
def plot_confusion_matrix(test_y, predict_y):
    C = confusion_matrix(test_y, predict_y)

    A = (((C.T)/(C.sum(axis=1))).T)

    B = (C/C.sum(axis=0))
    plt.figure(figsize=(20,4))

    labels = [0,1]
    # representing A in heatmap format
```

```

cmap=sns.light_palette("blue")
plt.subplot(1, 3, 1)
sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Confusion matrix")

plt.subplot(1, 3, 2)
sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Precision matrix")

plt.subplot(1, 3, 3)
# representing B in heatmap format
sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Recall matrix")

plt.show()

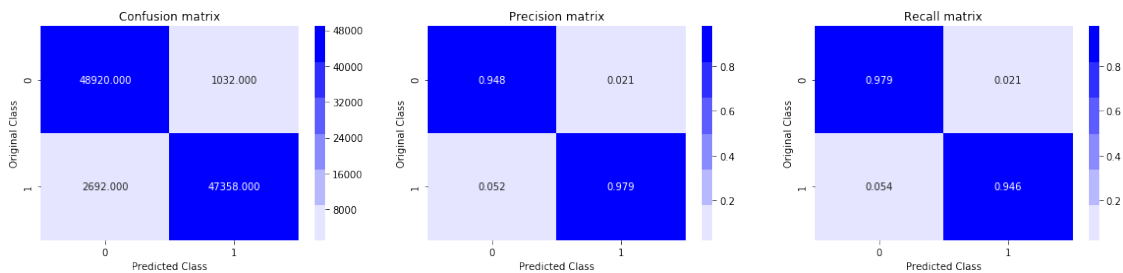
```

```

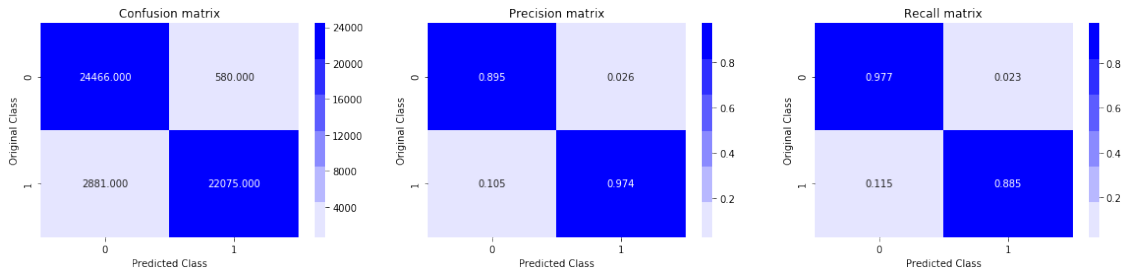
In [68]: print('Train confusion_matrix')
         plot_confusion_matrix(y_train,y_train_pred)
         print('Test confusion_matrix')
         plot_confusion_matrix(y_test,y_test_pred)

```

Train confusion_matrix

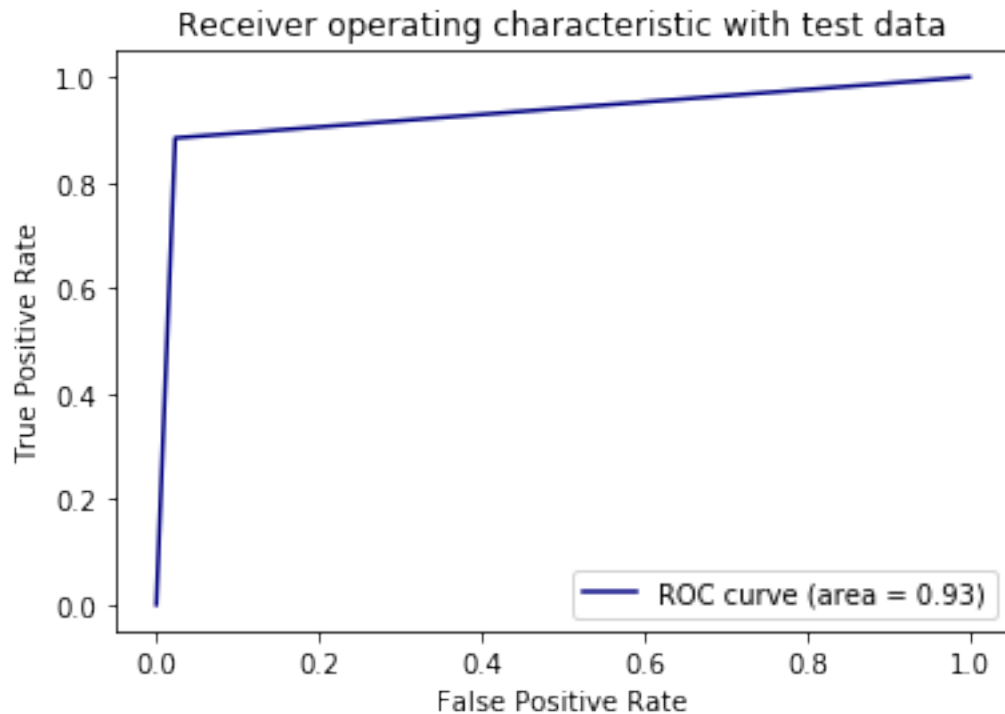


Test confusion_matrix



ROC/AUC Curve

```
In [69]: from sklearn.metrics import roc_curve, auc
fpr, tpr, ths = roc_curve(y_test, y_test_pred)
auc_sc = auc(fpr, tpr)
plt.plot(fpr, tpr, color='navy', label='ROC curve (area = %0.2f)' % auc_sc)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic with test data')
plt.legend()
plt.show()
```

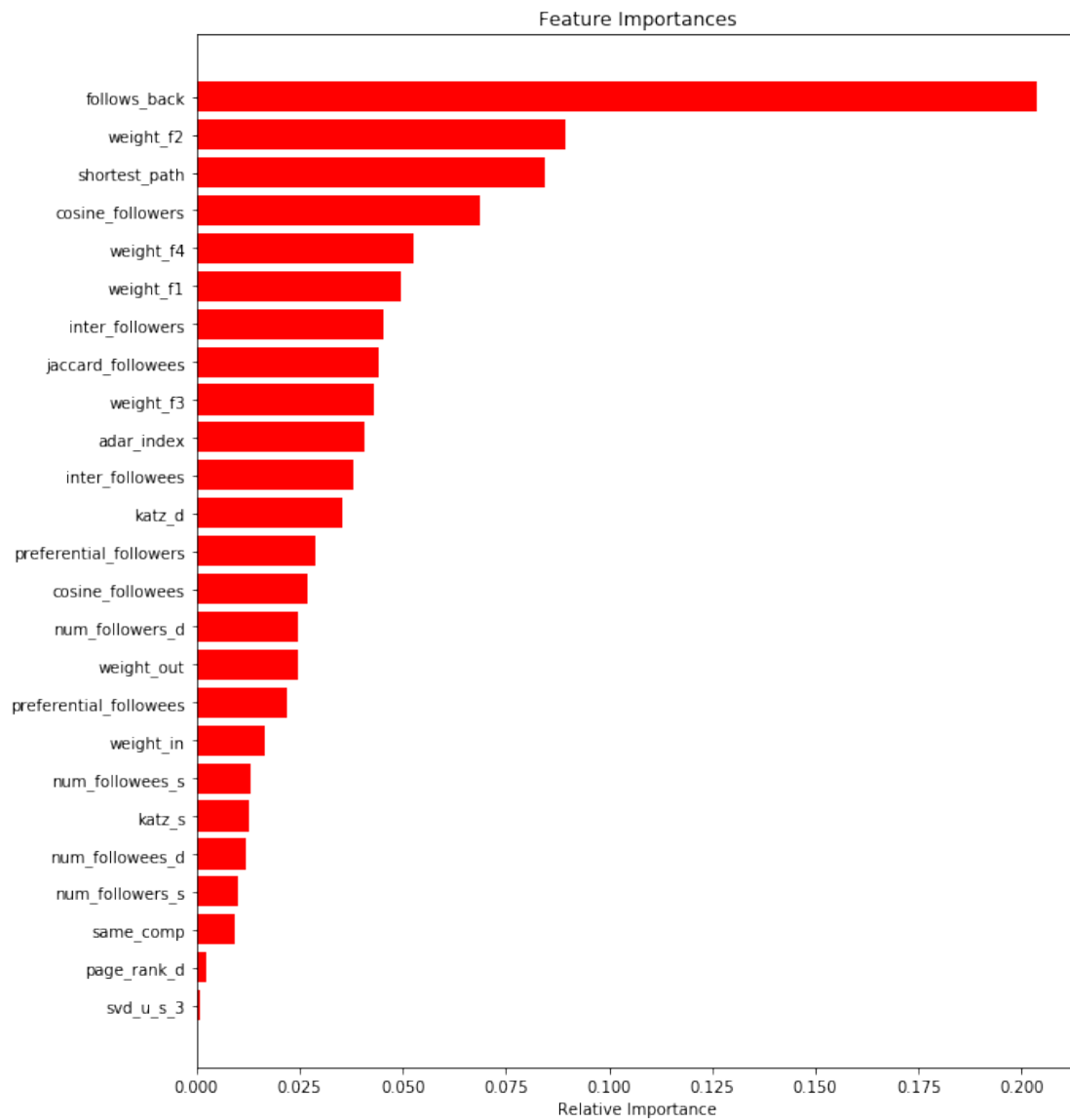


```
In [70]: features = df_final_train.columns
importances = clf.feature_importances_
```

```

indices = (np.argsort(importances))[-25:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()

```



4.2 6.2 XGBOOST (Tuning)

```

In [71]: import xgboost as xgb
         clf = xgb.XGBClassifier()

```

```

param_dist = {"n_estimators":sp_randint(50,100),
              "max_depth": sp_randint(10,20)
              }
model = RandomizedSearchCV(clf, param_distributions=param_dist,
                           n_iter=5,cv=3,scoring='f1',random_state=25)

```

```

model.fit(df_final_train,y_train)
print('mean test scores',model.cv_results_['mean_test_score'])
print('mean train scores',model.cv_results_['mean_train_score'])

```

```

mean test scores [0.97826592 0.97824537 0.97757468 0.97824576 0.97728859]
mean train scores [0.99795819 0.99945028 0.99139832 0.99788798 0.99650233]

```

```

In [72]: print(model.best_estimator_)

```

```

XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,
              colsample_bynode=1, colsample_bytree=1, gamma=0, learning_rate=0.1,
              max_delta_step=0, max_depth=14, min_child_weight=1, missing=None,
              n_estimators=76, n_jobs=1, nthread=None,
              objective='binary:logistic', random_state=0, reg_alpha=0,
              reg_lambda=1, scale_pos_weight=1, seed=None, silent=None,
              subsample=1, verbosity=1)

```

Best Parameter found

- max_depth = 14
- n_estimators = 76

```

In [73]: clf=xgb.XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,
                              colsample_bytree=1, gamma=0, learning_rate=0.1, max_delta_step=0,
                              max_depth=14, min_child_weight=1, missing=None, n_estimators=76,
                              n_jobs=1, nthread=None, objective='binary:logistic', random_state=0,
                              reg_alpha=0, reg_lambda=1, scale_pos_weight=1, seed=None,
                              silent=True, subsample=1)

```

```

In [74]: clf.fit(df_final_train,y_train)
          y_train_pred = clf.predict(df_final_train)
          y_test_pred = clf.predict(df_final_test)

```

```

In [75]: from sklearn.metrics import f1_score
          print('Train f1 score',f1_score(y_train,y_train_pred))
          print('Test f1 score',f1_score(y_test,y_test_pred))

```

```

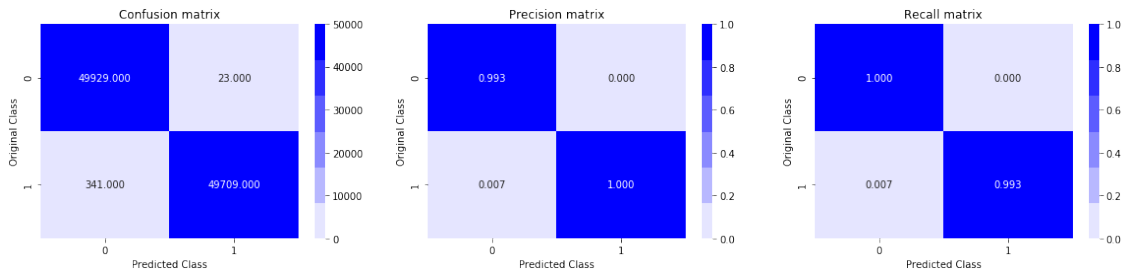
Train f1 score 0.9963520474634704
Test f1 score 0.9279735542794176

```

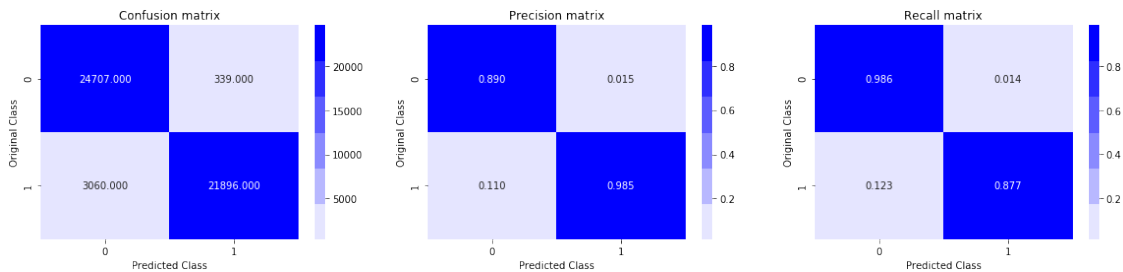
Confusion Matrix

```
In [76]: print('Train confusion_matrix')
         plot_confusion_matrix(y_train,y_train_pred)
         print('Test confusion_matrix')
         plot_confusion_matrix(y_test,y_test_pred)
```

Train confusion_matrix

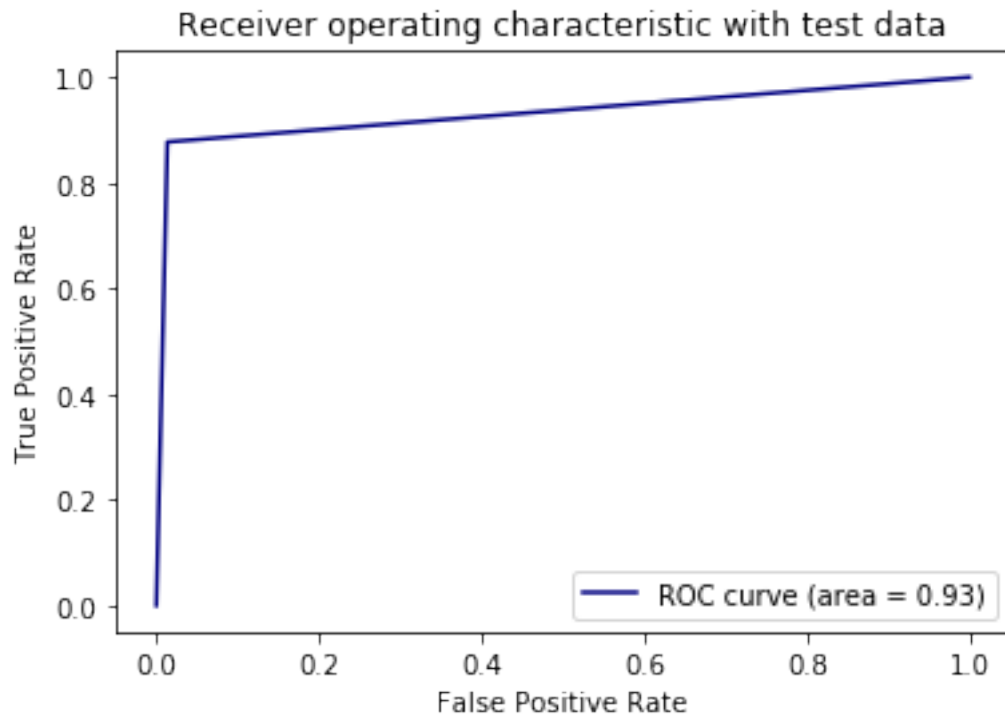


Test confusion_matrix



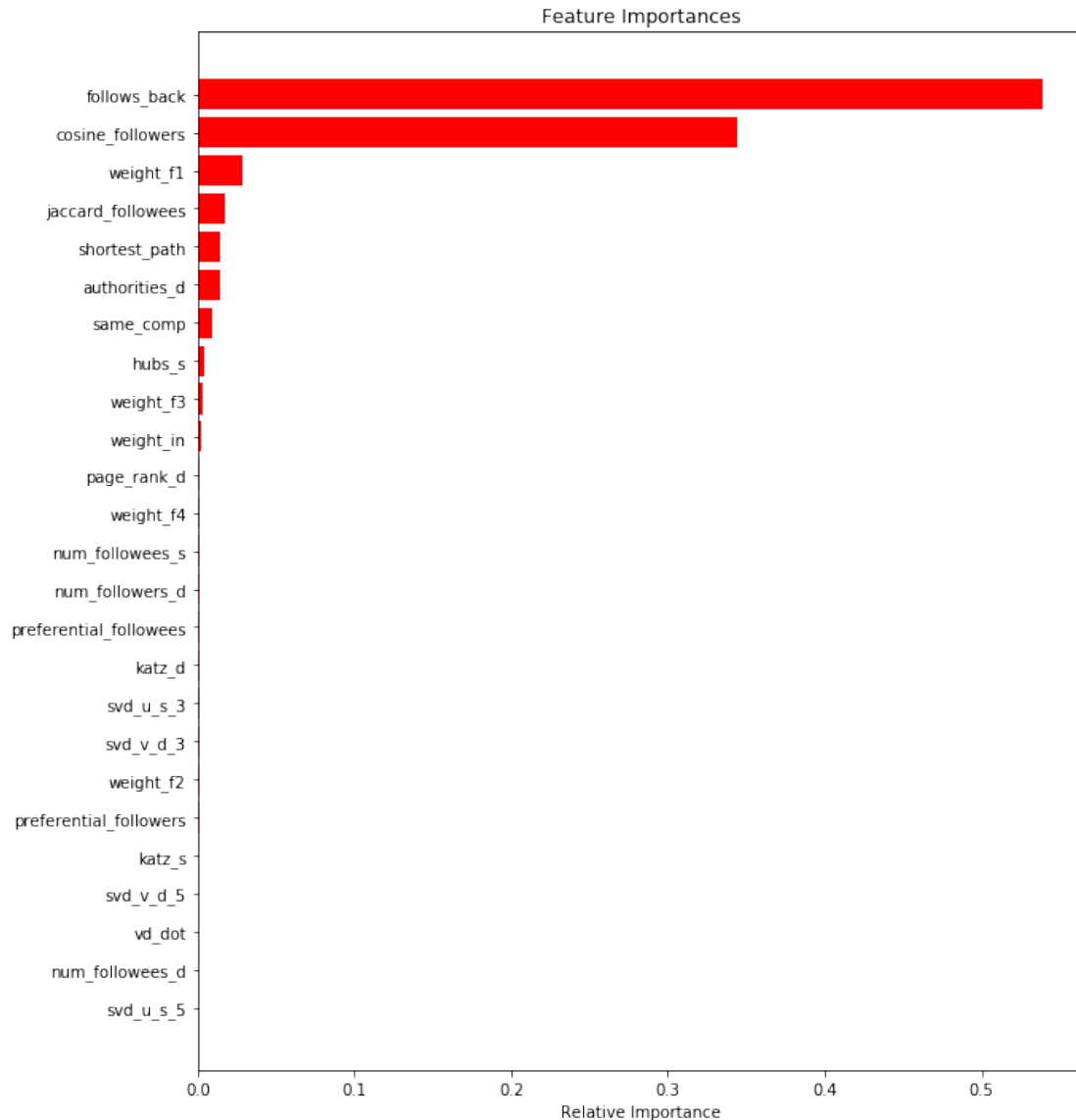
ROC/AUC Curve

```
In [77]: from sklearn.metrics import roc_curve, auc
         fpr,tpr,ths = roc_curve(y_test,y_test_pred)
         auc_sc = auc(fpr, tpr)
         plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc_sc)
         plt.xlabel('False Positive Rate')
         plt.ylabel('True Positive Rate')
         plt.title('Receiver operating characteristic with test data')
         plt.legend()
         plt.show()
```



Feature Importance

```
In [78]: features = df_final_train.columns
importances = clf.feature_importances_
indices = (np.argsort(importances))[-25:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```

5 ## Observations:

1. Understanding of graph and feature engineering was the most important part of this case study.
2. For Random Forest, Follow_back was the most important feature found, followed by weight_f2 and shortest_path.
3. Best result was obtained in case of XGBOOST.
4. XGBOOST took most of time.
5. For XGBOOST, **follows_back** was the most important feature. Followed by **cosine_follower** and **weight_f1**.
6. XGBOOST gave the best result.

5.1 Summary:

```
In [79]: from prettytable import PrettyTable
         summary = PrettyTable()
         summary.field_names = ["Model", "n_estimators", "max_depth", "Train f1-Score", "Test f1-Score"]

In [80]: summary.add_row(['Random Forest', '72', '14', '0.962', '0.926'])
         summary.add_row(['XGBOOST', '76', '14', '0.996', '0.927'])
         print(summary)
```

Model	n_estimators	max_depth	Train f1-Score	Test f1-Score
Random Forest	72	14	0.962	0.926
XGBOOST	76	14	0.996	0.927

6 ## Case Study Flow:

1. The dataset provided is directed graph data
2. For the given dataset, We have approx. 1.86M nodes and 9.43M edges.
3. Data was obtained from kaggle. You can get data from here <https://www.kaggle.com/c/FacebookRecruiting>
4. We have provided only connected nodes. i.e. 9.43M edges. But for each user among n user's, there is n-1 edges. So, for n nodes total possible edges are of 10^{12} order.
5. On EDA, it is found that, number of followers are less than 12 for 90% of users.
6. The given dataset was highly imbalanced, as only one classification label is present.
7. We decided $y = 0$, is link is not present and took random sample from it.
8. In training and test dataset were exactly balanced.
9. Featurization is the most important part of this case study. We extracted various features types of features...
 - Similarity measures
 - Ranking Measure
 - Various Graph Features
 - Various Weight Features
 - SVD features using Adjacency matrix. (n_components = 6)
10. We Trained two models Random Forest and XGBOOST
11. XGBOST took most time for run.

```
In [ ]:
```