

ASSIGNMENT 2

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Download all python codes from

<https://github.com/BatharajuRamana/Assignment2/tree/main/Assignment2/codes>

and latex-tikz codes from

<https://github.com/BatharajuRamana/Assignment2/tree/main/Assignment2/main.tex>

1 QUESTION No 2.10

Find the intersection of the following lines

1)

$$\begin{pmatrix} \sqrt{2} & \sqrt{3} \end{pmatrix} \mathbf{x} = 0$$

$$\begin{pmatrix} \sqrt{3} & \sqrt{8} \end{pmatrix} \mathbf{x} = 0 \quad (1.0.1)$$

2)

$$\begin{pmatrix} \frac{3}{2} & -\frac{5}{3} \end{pmatrix} \mathbf{x} = -2$$

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{2} \end{pmatrix} \mathbf{x} = \frac{13}{6} \quad (1.0.2)$$

2 SOLUTION

1)

$$\begin{pmatrix} \sqrt{2} & \sqrt{3} \end{pmatrix} \mathbf{x} = 0$$

$$\begin{pmatrix} \sqrt{3} & \sqrt{8} \end{pmatrix} \mathbf{x} = 0 \quad (2.0.1)$$

The above equations can be expressed as the matrix equation

$$\begin{pmatrix} \sqrt{2} & \sqrt{3} \\ \sqrt{3} & \sqrt{8} \end{pmatrix} \mathbf{x} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad (2.0.2)$$

The augmented matrix for the above equation is row reduced as follows

$$\begin{pmatrix} \sqrt{2} & \sqrt{3} & 0 \\ \sqrt{3} & \sqrt{8} & 0 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - \frac{\sqrt{3}}{\sqrt{2}} R_1} \begin{pmatrix} \sqrt{2} & \sqrt{3} & 0 \\ 0 & \frac{1}{\sqrt{2}} & 0 \end{pmatrix} \quad (2.0.3)$$

$$(2.0.4)$$

As left part is converted into identity matrix the intersection vector is $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

Plot of (1.0.1) -

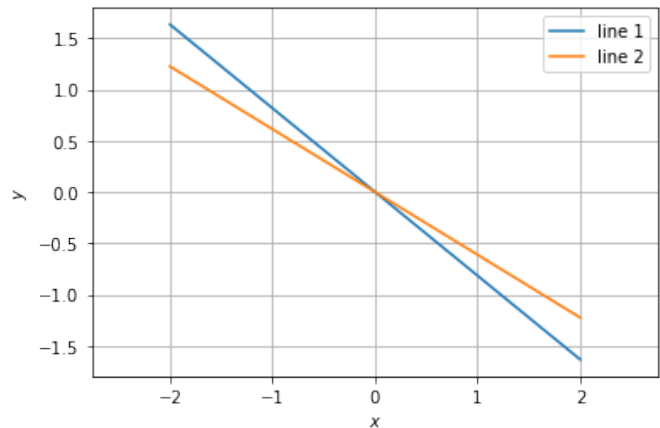


Fig. 2.1: intersecting lines

2)

PLOT OF GIVEN LINES -

$$\begin{pmatrix} \frac{3}{2} & -\frac{5}{3} \end{pmatrix} \mathbf{x} = -2$$

$$\begin{pmatrix} \frac{1}{3} & \frac{1}{2} \end{pmatrix} \mathbf{x} = \frac{13}{6} \quad (2.0.5)$$

The above equations can be expressed as the matrix equation

$$\begin{pmatrix} \frac{3}{2} & -\frac{5}{3} \\ \frac{1}{3} & \frac{1}{2} \end{pmatrix} \mathbf{x} = \begin{pmatrix} -2 \\ \frac{13}{6} \end{pmatrix} \quad (2.0.6)$$

The augmented matrix for the above equation

is row reduced as follows

$$\begin{pmatrix} \frac{3}{2} & -\frac{5}{3} & -2 \\ \frac{1}{3} & \frac{1}{2} & \frac{13}{6} \end{pmatrix} \xleftrightarrow{R_1 \leftarrow 6R_1, R_2 \leftarrow 6R_2} \begin{pmatrix} 9 & -10 & -12 \\ 2 & 3 & 13 \end{pmatrix} \quad (2.0.7)$$

$$\xleftrightarrow{R_1 \leftarrow R_1 - 4R_2} \begin{pmatrix} 1 & -22 & -64 \\ 2 & 3 & 13 \end{pmatrix} \quad (2.0.8)$$

$$\xleftrightarrow{R_2 \leftarrow R_2 - 2R_1} \begin{pmatrix} 1 & -22 & -64 \\ 0 & 47 & 141 \end{pmatrix} \quad (2.0.9)$$

$$\xleftrightarrow{R_2 \leftarrow R_2 / 47} \begin{pmatrix} 1 & -22 & -64 \\ 0 & 1 & 3 \end{pmatrix} \quad (2.0.10)$$

$$\xleftrightarrow{R_1 \leftarrow R_1 + 22R_2} \begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 3 \end{pmatrix} \quad (2.0.11)$$

As left part is converted into identity matrix

the intersection vector is $\begin{pmatrix} 2 \\ 3 \end{pmatrix}$

3) PLOT OF GIVEN LINES -

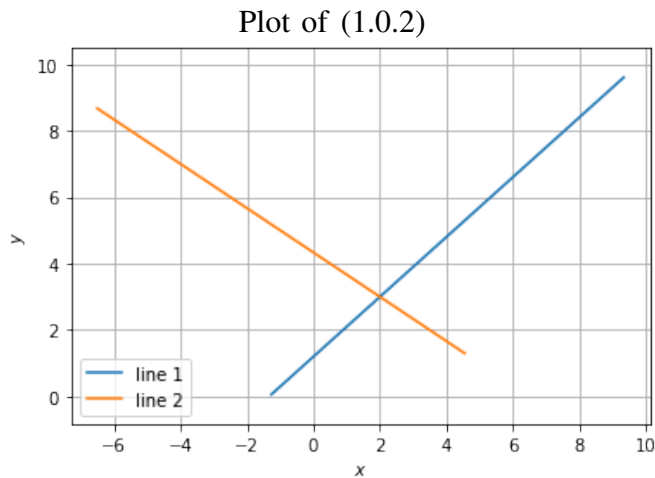


Fig. 2.2: intersecting lines