

Frugal:

Input is the same as the input in the problem set for Frugal.

Output:

Is there some subset of recipes  $R' \subset R$  with size  $|R'| < M$  such that all together the recipes in  $R'$  use some ingredients in  $G$  ( $\cup_{r \in R'} r = G \wedge r_1 \cap r_2 \neq \emptyset, \exists r_1, r_2 \in R'$ )

Verifying Frugal:

VerifyFrugal( $G, R, M, R'$ ):

If  $R'$  is a subset of recipes from  $R$  with size  $|R'| < M$ :

If for all elements  $r_1$  and  $r_2 \in R' = G, r_1 \cap r_2 = \emptyset$ :

Return True

Return false

ShortPaths:

Input: an undirected graph  $G = (V, E)$  and a positive integer  $k$

Output:

Are there any simple paths in  $G$  that contain more than  $k$  edges

VerifyShortPaths( $G, k, P$ ): #not the complement!

If  $P$  is a simple path in  $G$  and there are more than  $K$  edges in  $P$

Return false

Return true