MNIST Digit Recognizer: Neural Networks

According to the Kaggle overview, "MNIST ("Modified National Institute of Standards and Technology") is the de facto "hello world" dataset of computer vision." It is a classic dataset to use for measuring and benchmarking classification algorithms. In this research, we will identify correct digits from a dataset of tens of thousands of handwritten images. The dataset contains 700+ columns each indicating a pixel of the chart. We will run a completely-crossed design experiments with neural networks to make predictions on the test set. First, we performed basic exploratory data analysis to better understand the dataset. Figures 1-5 shows 785 columns and int values that range from 0 (black pixel) to 255 (white). Figure 6 shows that there is a fairly even distribution of labels from 0-9. There are no null values. Figures 7-9 show a few more graphs exploring the frequency plot of pixel values, top 10 pixels across the different labels, and then the density plot for the average pixel intensities of each label. These allow us to get a fuller idea of the dataset and what pixel values go into it. Finally, Figure 10 shows that 76 columns have constant values (all 255 or all 0). These will not contribute to any of the classification models we create so we drop these columns. The dataset now has 709 columns and is ready to be worked with.

After splitting the dataset into an 80/20 training/testing split we conducted our experiments. We used a completely crossed design to run three different experiments. The first experiment was without any standard scaling and tested 2 and 5 layers and 10 and 20 nodes. What this means is that we will train and fit neural network models that use 2 hidden layers and 10 nodes, 2 hidden layers and 20 nodes, 5 hidden layers and 10 nodes, and lastly 5 hidden layers and 20 nodes. We will get the training and testing accuracies of each of these models and then use this to create a model to use on the Kaggle testing data. We found that the model that performed the best was 5 hidden layers with 20 nodes. The results and multi-class confusion matrix are shown in figures 11-16. Though this had better results than our random

forest classifier from last week, we knew we could improve upon it. So, next we ran the exact same experiment design with the same number of layers and neurons but first transformed the data using a standard scaler. These results can be seen in figures 17-20. Our Kaggle score for this round of experimentation, using a model with 2 hidden layers and 20 nodes, was 0.94264.

This is a great improvement from last week as well but we wanted to finally test the limits of increasing the layers and nodes before we run into different issues. When building neural networks there are a few common pitfalls to be wary of while designing them. The first is that with too many neurons some may not activate. This is not necessarily going to have negative effects on classification performance and accuracy but instead will result in excess in the model that we do not need. This is fine for a dataset like MNIST digit classifier but for huge datasets can increase the amount of time to run. This can also occur with too many hidden layers. Many hidden layers vastly increases the amount of time it takes to fit along with overfitting in some cases. Lastly, it is easy to run into what is called the vanishing gradient problem in which the gradient becomes so small the neurons stop backpropagating.

With that in mind, we ran one more experiment with 3 and 5 hidden layers and 20 and 30 neurons. As expected, all of the training accuracies were super high with 5 hidden layers and 30 neurons resulting in a perfect score (a sign of overfitting though the testing accuracy still was high at ~0.95). We tested a neural network model of 3 hidden layers and 30 neurons resulting in our highest Kaggle score yet of 0.95157 (figure 26). To test our theory that the 5 hidden layer, 30 neuron model overfit we also tested this on our Kaggle test data where we saw a slight regression and a score of 0.9498. A 2x2 completely crossed experiment design shows a great improvement in classification capabilities. In the future we can further fine tune these parameters to get even better scores.

Appendix

```
from google.colab import drive
drive.mount('/content/drive')
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import sklearn
%cd /content/drive/My Drive/
df = pd.read csv('MNIST Digit/train.csv')
df.head(5)
df = pd.read_csv('MNIST_Digit/train.csv')
df.head((5))
     label pixel0 pixel1 pixel2 pixel3 pixel4 pixel5 pixel6 pixel7 pixel8 ... pixel774 pixel775 pixel776 pixel777 pixel778 pixel779 pixel780 pixel781 pixe
Figure 1
data type counts = df.dtypes.value counts()
print(data_type_counts)
int64 785 Name: count, dtype: int64
len(df.columns)
785
nullseries= df.isna().sum()
```

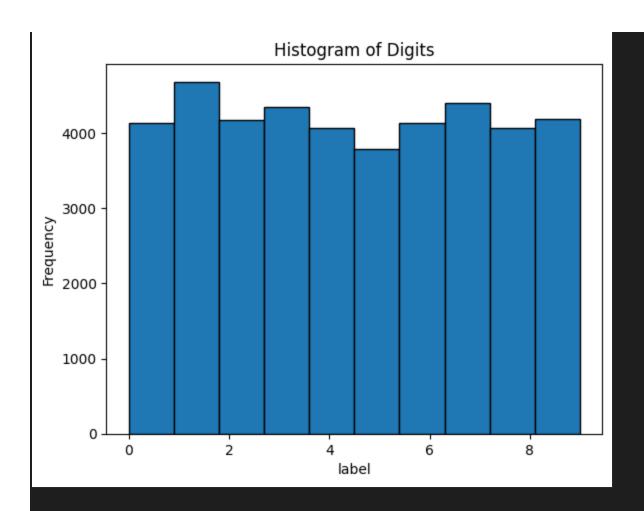
```
print(nullseries[nullseries > 0])
Series([], dtype: int64)
df.describe()
        label pixel0 pixel1 pixel2 pixel3 pixel4 pixel5 pixel6 pixel7 pixel8 ... pixel774 pixel775 pixel776 pixel777 pixel778
                                                                               pixel779
  count 42000.00000 42000.0 42000.0 42000.0 42000.0 42000.0 42000.0 42000.0 42000.0 42000.0 42000.0
                                                                               0.000000
                                                 0.000000
                                                                         0.000000
                                                                               0.000000
       0.00000 0.000000
                                                                               0.000000
                                                 0.000000 0.000000 0.000000
                                                                    0.00000
                                                                        0.000000
       max
import matplotlib.pyplot as plt
plt.hist(df['label'], bins=10, edgecolor='black') # Assuming binary data,
```

plt.xlabel('label')

plt.show()

plt.ylabel('Frequency')

plt.title('Histogram of Digits')

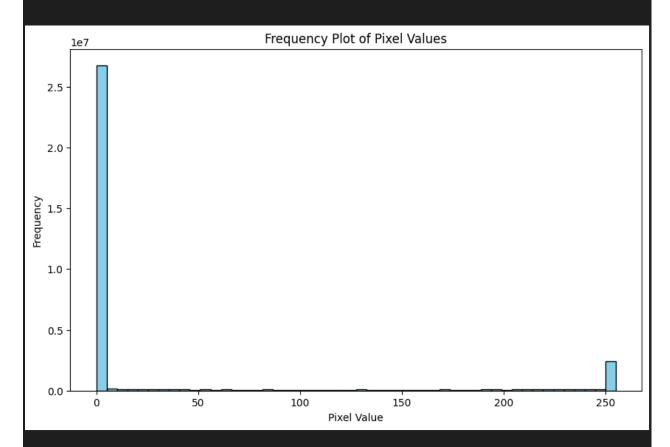


```
#create a heat map of all labels
columns_to_plot = df.columns # Add all relevant column names

# Flatten the selected columns into a single array
values = df[columns_to_plot].values.flatten()

# Plot the frequency of values
plt.figure(figsize=(10, 6))
plt.hist(values, bins=50, color='skyblue', edgecolor='black') # Adjust
bins as needed
plt.title('Frequency Plot of Pixel Values')
plt.xlabel('Pixel Value')
plt.ylabel('Frequency')
plt.grid(False)
plt.show()
```

#Majority of the pixels in the dataset are white while some are black, not many other pixel values.

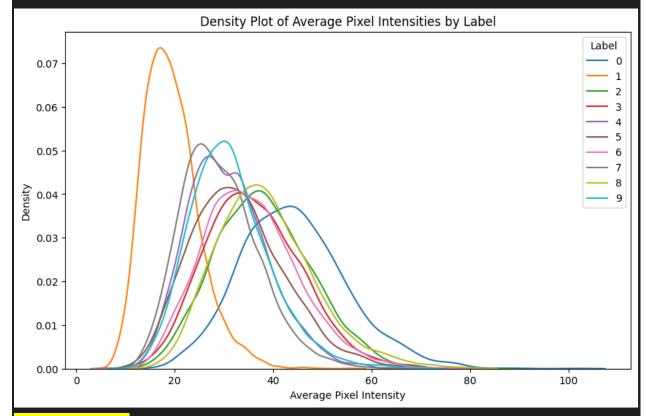


```
average_pixel_values_grouped = df.groupby('label').mean()
# Create a subplot with 10 plots (2 each row)
fig, axs = plt.subplots(5, 2, figsize=(15, 12))

for index, row in average_pixel_values_grouped.iterrows():
largest_10 = row.nlargest(10)
largest_10 = largest_10.sort_values(ascending=False)
ax = axs[index // 2, index % 2] # Calculate row and column index for subplot
ax.bar(largest_10.index, largest_10.values, color='skyblue')
ax.set_xlabel('Pixel Value')
ax.set_ylabel('Pixel Column')
```

```
ax.set title('Top 10 Pixels of Label {}'.format(index))
ax.tick params(axis='x', labelrotation = 45) # Rotate label
plt.tight_layout()
plt.show()
                              Top 10 Pixels of Label 0
                                                                                                       Top 10 Pixels of Label 1
Pixel Column
100
                                                                          Pixel Column
100
                                   Pixel value
                                                                                                             Pixel Value
                              Top 10 Pixels of Label 2
                                                                                                       Top 10 Pixels of Label 3
Pixel Column 100 100 50
                                                                          Pixel Column
                              Top 10 Pixels of Label 4
                                                                                                        Top 10 Pixels of Label 5
                                                                          Dixel Column
100
50
   100
                              Top 10 Pixels of Label 6
                                                                                                        Top 10 Pixels of Label 7
Pixel Column
100
                                                                          Pixel Column
00
                                                                                                             Pixel Value
                              Top 10 Pixels of Label 8
                                                                                                        Top 10 Pixels of Label 9
Pixel Column
100
                                                                          Pixel Column
100
plt.figure(figsize=(10, 6))
```

```
sns.kdeplot(df[df['label'] == label].mean(axis=1), label=label,
fill=False)
plt.title('Density Plot of Average Pixel Intensities by Label')
plt.xlabel('Average Pixel Intensity')
plt.ylabel('Density')
plt.legend(title='Label')
plt.grid(False)
plt.show()
#Most of label 1 has lower intensity than other labels; label 0 has the
highest pixel intensity
```



```
# Remove any columns with constant values. They won't contribute to the
classifiers
clean_df = df.copy()
black_pixels = []
white_pixels = []
print(len(df.columns))
```

```
for pixel in df.columns:
    if max(df[pixel]) == 0:
    black_pixels.append(pixel)
    if min(df[pixel]) == 255:
    white_pixels.append(pixel)

    clean_df = clean_df.drop(black_pixels, axis=1)
    clean_df = clean_df.drop(white_pixels, axis=1)
    print(len(black_pixels))
    print(len(white_pixels))
    print(len(clean_df.columns))

785 76 0 709

Figure 10
```

Split Training and Testing

```
x = clean_df.drop(columns=['label'])
y = clean_df['label']

# Use K-Fold Later
from sklearn.model_selection import train_test_split
# Split the dataset into 80% train and 20% test
x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.2, random_state=42)
```

Neural Network Without Standard Scaling

```
import time
from sklearn.neural_network import MLPClassifier

# Define experimental design
layers = [2, 5]
nodes = [10, 20]
```

```
for layer in layers:
neural net = MLPClassifier(hidden layer sizes=(node,) * layer,
max iter=1000)
start time = time.time()
neural net.fit(x train, y train)
time taken.append(time.time() - start time)
training accuracy.append(neural net.score(x train, y train))
testing accuracy.append(neural net.score(x test, y test))
for i in range(len(layers)):
for j in range(len(nodes)):
print(f"Layers: {layers[i]}, Nodes: {nodes[j]}, Time:
{training accuracy[i*len(nodes)+j]}, Testing Accuracy:
{testing accuracy[i*len(nodes)+j]}")
Layers: 2, Nodes: 10, Time: 313.3716700077057, Training Accuracy:
0.9114583333333334, Testing Accuracy: 0.878333333333333
```

```
Layers: 2, Nodes: 20, Time: 126.3457510471344, Training Accuracy: 0.9778571428571429, Testing Accuracy: 0.9339285714285714

Layers: 5, Nodes: 10, Time: 285.35211634635925, Training Accuracy: 0.9396130952380952, Testing Accuracy: 0.8958333333333334

Layers: 5, Nodes: 20, Time: 176.1007297039032, Training Accuracy: 0.9904761904761905, Testing Accuracy: 0.9355952380952381
```

```
for layer in layers:
for node in nodes:
print((node,) * layer)

(10, 10)
(20, 20)
(10, 10, 10, 10, 10)
(20, 20, 20, 20, 20)
```

Figure 12

```
start time = time.time()
neural net = MLPClassifier(hidden layer sizes=(20, 20, 20, 20, 20),
max iter=1000)
print(f'It takes {time.time() - start time} seconds to train 20 nodes 5
It takes 109.3866958618164 seconds to train 20 nodes 5 layers NetWork
from sklearn.metrics import confusion matrix, classification report
test_conf_matrix = confusion_matrix(y_test, neural_pred)
tick marks = np.arange(len(class names))
plt.xticks(tick marks, class names)
plt.yticks(tick marks, class names)
sns.heatmap(pd.DataFrame(test conf matrix), annot=True,
cmap="YlGnBu" ,fmt='g')
ax.xaxis.set label position("top")
plt.tight layout()
plt.title('Testing data confusion matrix', y=1.1)
plt.ylabel('Actual label')
plt.xlabel('Predicted label')
```

	Testing data confusion matrix												
	Predicted label												_
	0 -	794	0	7	1	2	3	1	0	4	4		
	п-	0	884	7	3	1	1	1	0	12	0		- 800
	2 -	5	4	779	18	11	1	3	10	14	1		- 700
	m -	0	1	14	864	1	19	1	10	23	4		- 600
label	4 -	7	1	5	0	795	1	6	4	1	19		- 500
Actual label	ი -	1	2	1	14	1	660	9	1	10	3		- 400
	9 -	9	1	3	1	1	10	757	0	3	0		- 300
	۲ -	0	1	16	11	6	3	0	837	4	15		- 200
	ω -	5	2	8	10	6	12	4	2	783	3		- 100
	ი -	6	2	1	9	41	4	0	17	11	747		
		0	i	2	3	4	5	6	7	8	9		- 0

Prediction on Test Dataset

```
# Make prediction on test dataset

test_df = pd.read_csv('MNIST_Digit/test.csv')

# Remove any columns with constant values. They won't contribute to the classifiers

clean_test_df = test_df.copy()

black_pixels = []

white_pixels = []

for pixel in df.columns:
```

```
if max(df[pixel]) == 0:
black pixels.append(pixel)
if min(df[pixel]) == 255:
white pixels.append(pixel)
clean test df = clean test df.drop(black pixels, axis=1)
clean test df = clean test df.drop(white pixels, axis=1)
print(len(clean df.columns))
print(len(clean test df.columns)) # should be 1 less than clean df because
709
708
predictions = neural net.predict(clean test df)
imageId = pd.Series(range(1, len(predictions)+1)).astype(int)
result df = pd.DataFrame(result)
x=False)
Neural Network Standard Scale
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
x test scaled = scaler.transform(x test)
from sklearn.neural network import MLPClassifier
layers = [2, 5]
```

```
time taken = []
for layer in layers:
neural net = MLPClassifier(hidden layer sizes=(node,) * layer,
max iter=1000)
start time = time.time()
time taken.append(time.time() - start time)
training accuracy.append(neural net.score(x train scaled, y train))
testing accuracy.append(neural net.score(x test scaled, y test))
for i in range(len(layers)):
for j in range(len(nodes)):
print(f"Layers: {layers[i]}, Nodes: {nodes[j]}, Time:
{training accuracy[i*len(nodes)+j]}, Testing Accuracy:
{testing accuracy[i*len(nodes)+j]}")
```

```
for i in range(len(layers)):
for j in range(len(nodes)):
print(f"Layers: {layers[i]}, Nodes: {nodes[j]}, Time:
{time_taken[i*len(nodes)+j]}, Training Accuracy:
{training_accuracy[i*len(nodes)+j]}, Testing Accuracy:
{testing_accuracy[i*len(nodes)+j]}")

Layers: 2, Nodes: 10, Time: 218.75375127792358, Training Accuracy:
0.9859821428571428, Testing Accuracy: 0.9082142857142858

Layers: 2, Nodes: 20, Time: 107.57854437828064, Training Accuracy:
0.9985416666666667, Testing Accuracy: 0.9458333333333333333

Layers: 5, Nodes: 10, Time: 283.8109927177429, Training Accuracy:
0.9836309523809523, Testing Accuracy: 0.9082142857142858

Layers: 5, Nodes: 20, Time: 141.67477869987488, Training Accuracy:
0.9997619047619047, Testing Accuracy: 0.9432142857142857
```

```
start_time = time.time()
neural_net = MLPClassifier(hidden_layer_sizes=(20, 20), max_iter=1000)
neural_net.fit(x_train_scaled, y_train)
print(f'It takes {time.time() - start_time} seconds to train 20 nodes 2
layers NetWork')
It takes 103.00234508514404 seconds to train 20 nodes 2 layers NetWork
```

```
from sklearn.metrics import confusion_matrix, classification_report

# Testing Data confusion matrix
neural_pred = neural_net.predict(x_test_scaled)
test_conf_matrix = confusion_matrix(y_test, neural_pred)
class_names=[0,1] # name of classes
fig, ax = plt.subplots()
tick_marks = np.arange(len(class_names))
plt.xticks(tick_marks, class_names)
plt.yticks(tick_marks, class_names)
# create heatmap
sns.heatmap(pd.DataFrame(test_conf_matrix), annot=True,
cmap="YlGnBu" ,fmt='g')
ax.xaxis.set_label_position("top")
plt.tight_layout()
plt.title('Testing data confusion matrix', y=1.1)
plt.ylabel('Actual label')
plt.xlabel('Predicted label')
```

	Testing data confusion matrix													
	Predicted label													
	0 -	790	1	4	1	1	6	7	1	3	2			
	н -	0	889	4	0	1	2	1	6	6	0			- 800
	2 -	6	7	778	12	9	6	5	12	10	1			- 700
	m -	4	3	12	854	0	30	0	7	18	9			- 600
label	4 -	3	0	5	4	786	4	8	8	3	18			- 500
Actual label	ი -	3	1	2	13	1	656	15	1	7	3			- 400
	o -	10	4	2	0	4	7	755	0	3	0			- 300
	۲ -	1	3	8	4	6	2	0	844	4	21			- 200
	∞ -	4	8	8	17	3	12	6	2	767	8			- 100
	ი -	3	0	1	11	13	3	0	19	6	782			100
		Ó	i	2	3	4	5	6	7	8	9			- 0

Prediction on Test Dataset

```
# Make prediction on test dataset
test_df = pd.read_csv('MNIST_Digit/test.csv')

# Remove any columns with constant values. They won't contribute to the classifiers
clean_test_df = test_df.copy()
black_pixels = []
white_pixels = []
for pixel in df.columns:
```

```
if max(df[pixel]) == 0:
black pixels.append(pixel)
if min(df[pixel]) == 255:
white pixels.append(pixel)
clean test df = clean test df.drop(black pixels, axis=1)
clean test df = clean test df.drop(white pixels, axis=1)
print(len(clean df.columns))
print(len(clean test df.columns)) # should be 1 less than clean df because
709
scaler = StandardScaler()
predict scaled = scaler.fit transform(clean test df)
predictions = neural net.predict(predict scaled)
imageId = pd.Series(range(1, len(predictions)+1)).astype(int)
result = {'ImageId': imageId, 'Label': predictions}
result df = pd.DataFrame(result)
Neural Net Experiment 2
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
x train scaled = scaler.fit transform(x train)
```

```
layers = [3, 5]
for layer in layers:
neural net = MLPClassifier(hidden layer sizes=(node,) * layer,
max iter=1000)
start time = time.time()
time taken.append(time.time() - start time)
training accuracy.append(neural net.score(x train scaled, y train))
testing accuracy.append(neural net.score(x test scaled, y test))
for i in range(len(layers)):
for j in range(len(nodes)):
```

```
print(f"Layers: {layers[i]}, Nodes: {nodes[j]}, Time:
{training_accuracy[i*len(nodes)+j]}, Testing Accuracy:
{testing accuracy[i*len(nodes)+j]}")
Layers: 3, Nodes: 20, Time: 89.13008999824524, Training Accuracy:
0.9999107142857143, Testing Accuracy: 0.9435714285714286
Layers: 3, Nodes: 30, Time: 55.43762469291687, Training Accuracy:
0.9999404761904762, Testing Accuracy: 0.9566666666666667
Layers: 5, Nodes: 20, Time: 108.07192993164062, Training Accuracy:
0.9999107142857143, Testing Accuracy: 0.9433333333333334
Layers: 5, Nodes: 30, Time: 68.57372498512268, Training Accuracy: 1.0,
Testing Accuracy: 0.9541666666666667
for i in range(len(layers)):
for j in range(len(nodes)):
print(f"Layers: {layers[i]}, Nodes: {nodes[j]}, Time:
{training accuracy[i*len(nodes)+j]}, Testing Accuracy:
{testing accuracy[i*len(nodes)+j]}")
Layers: 3, Nodes: 20, Time: 89.13008999824524, Training Accuracy:
```

```
Layers: 3, Nodes: 20, Time: 89.13008999824524, Training Accuracy: 0.9999107142857143, Testing Accuracy: 0.9435714285714286

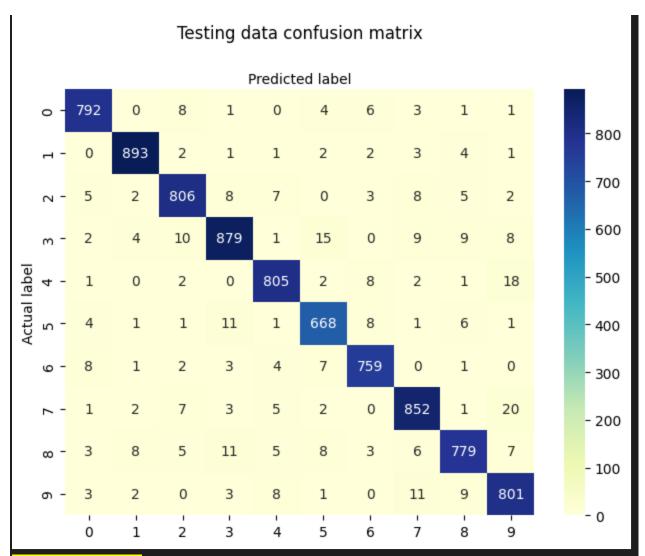
Layers: 3, Nodes: 30, Time: 55.43762469291687, Training Accuracy: 0.9999404761904762, Testing Accuracy: 0.95666666666667

Layers: 5, Nodes: 20, Time: 108.07192993164062, Training Accuracy: 0.9999107142857143, Testing Accuracy: 0.9433333333333334

Layers: 5, Nodes: 30, Time: 68.57372498512268, Training Accuracy: 1.0, Testing Accuracy: 0.9541666666666667
```

```
start_time = time.time()
neural net = MLPClassifier(hidden layer sizes=(30, 30, 30), max iter=1000)
```

```
neural net.fit(x train scaled, y train)
print(f'It takes {time.time() - start time} seconds to train 30 nodes 3
layers NetWork')
It takes 59.0290744304657 seconds to train 30 nodes 3 layers NetWork
from sklearn.metrics import confusion matrix, classification report
neural pred = neural net.predict(x test scaled)
tick marks = np.arange(len(class names))
plt.xticks(tick marks, class names)
plt.yticks(tick marks, class names)
sns.heatmap(pd.DataFrame(test conf matrix), annot=True,
cmap="YlGnBu" ,fmt='g')
ax.xaxis.set label position("top")
plt.tight layout()
plt.title('Testing data confusion matrix', y=1.1)
plt.ylabel('Actual label')
plt.xlabel('Predicted label')
```



Prediction on Test Dataset

```
# Make prediction on test dataset
test_df = pd.read_csv('MNIST_Digit/test.csv')

# Remove any columns with constant values. They won't contribute to the classifiers
clean_test_df = test_df.copy()
black_pixels = []
white_pixels = []
```

```
if max(df[pixel]) == 0:
black pixels.append(pixel)
if min(df[pixel]) == 255:
white pixels.append(pixel)
clean test df = clean test df.drop(black pixels, axis=1)
clean test df = clean test df.drop(white pixels, axis=1)
print(len(clean df.columns))
print(len(clean test df.columns)) # should be 1 less than clean df because
predict scaled = scaler.fit transform(clean test df)
predictions = neural net.predict(predict scaled)
imageId = pd.Series(range(1, len(predictions)+1)).astype(int)
result = {'ImageId': imageId, 'Label': predictions}
result df = pd.DataFrame(result)
x=False)
                               4
    1611
           Zachary Cmiel
                                                             0.95157
                                                                         6
                                                                               34s
                                                                      Tweet this
      Your most recent submission scored 0.95157, which is an improvement of your previous score of 0.95042. Great job!
```