

# Measuring the runtime complexity of the algorithms using Big O notation

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In this NoteBook you will find different algorithm implementation and their test result on plots.

Results shown on plots present Big O notation of each algorithms

*Because some plots might look similar (but have different runtime-complexity) the plots are numbered.*

You can also check test cases in Required-Functions Before implementation of algorithms

- For example Bubble Sort goes from 1000 to 15000 with 1000 step in each iteration

List of sorting algorithms included in the tests:

- Bubble Sort
- Insertion sort
- Merge sort
- Quick sort
- Linear Search
- Binary Search

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## Python

In the cells below we get the environment ready and prepare needed functions

```
In [12]: from pprint import pprint
import rx7 as rx
import matplotlib.pyplot as plt
```

```
In [13]: # return an array[int] with length of n (between [first,last])
def make_random_list(n:int,first=0,last=0):
    if not last: last=n
    a = []
    for i in range(n):
        a.append(rx.random.integer(first,last))
    return a

# Prepare ranges for different algorithms
```

```

def Range(a,b): return range(a,b+1)
Groups = {
    "Bubble"      : list(Range(1_000,15_000))[::1000],
    "Insertion"   : list(Range(1_000,20_000))[::1000],
    "Merge"       : list(Range(50_000,1_000_000))[::50_000],
    "Quick"       : list(Range(150_000,2_400_000))[::150_000],
    "Linear"      : list(Range(250_000,5_000_000))[::500_000],
    "Binary"      : list(Range(400_000,4_000_000))[::400_000]
}

# shows plot of given sort_name
def generate_plot(sort_name,TIMES):
    # plt.figure(figsize=(11,8),dpi=50)
    plt.plot(Groups[sort_name],list(i for i in TIMES))
    plt.title(f"{sort_name} Sort")
    plt.xlabel(f"Length")
    plt.ylabel("Time (s)")
    # plt.xticks(Groups[sort_name],[int(i/devide_by[0]) for i in Groups[sort_name]])
    plt.show()

```

## Algorithms in python:

```

In [14]: def bubble_sort(array): # O(n^2)
    n = len(array)
    for i in range(n):
        for j in range(n - i - 1):
            if array[j] > array[j + 1]:
                array[j], array[j + 1] = array[j + 1], array[j]
    return array

def insertion_sort(array): # O(n^2)
    for i in range(1, len(array)):
        key_item = array[i]
        j = i - 1
        while j >= 0 and array[j] > key_item:
            array[j + 1] = array[j]
            j -= 1
        array[j + 1] = key_item
        # array.insert(j+1,key_item)
    return array

def merge(left, right):
    if len(left) == 0:
        return right
    if len(right) == 0:
        return left
    result = []
    index_left = index_right = 0
    while len(result) < len(left) + len(right):
        if left[index_left] <= right[index_right]:
            result.append(left[index_left])
            index_left += 1
        else:
            result.append(right[index_right])

```

```

        index_right += 1
    if index_right == len(right):
        result += left[index_left:]
        break
    if index_left == len(left):
        result += right[index_right:]
        break
    return result
def merge_sort(array): # O(n.Lg(n))
    if len(array) < 2:
        return array
    midpoint = len(array) // 2
    return merge(
        left=merge_sort(array[:midpoint]),
        right=merge_sort(array[midpoint:]))

def quicksort(array): # O(n.Lg(n))
    if len(array) <= 1:
        return array
    low, same, high = [], [], []
    pivot = array[0]
    for item in array:
        if item < pivot: low.append(item)
        elif item == pivot: same.append(item)
        elif item > pivot: high.append(item)
    return quicksort(low) + same + quicksort(high)

def LinearSearch(lst, element): # O(n)
    for i in range(len(lst)):
        if lst[i] == element:
            return i
    return -1

def BinarySearch(lst, val): # O(Log(n))
    first = 0
    last = len(lst)-1
    index = -1
    while (first <= last) and (index == -1):
        mid = (first+last)//2
        if lst[mid] == val:
            index = mid
        else:
            if val < lst[mid]:
                last = mid -1
            else:
                first = mid +1
    return index

```

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## Bubble Sort ( $O(n^2)$ )

In [4]: TIMES = []

```

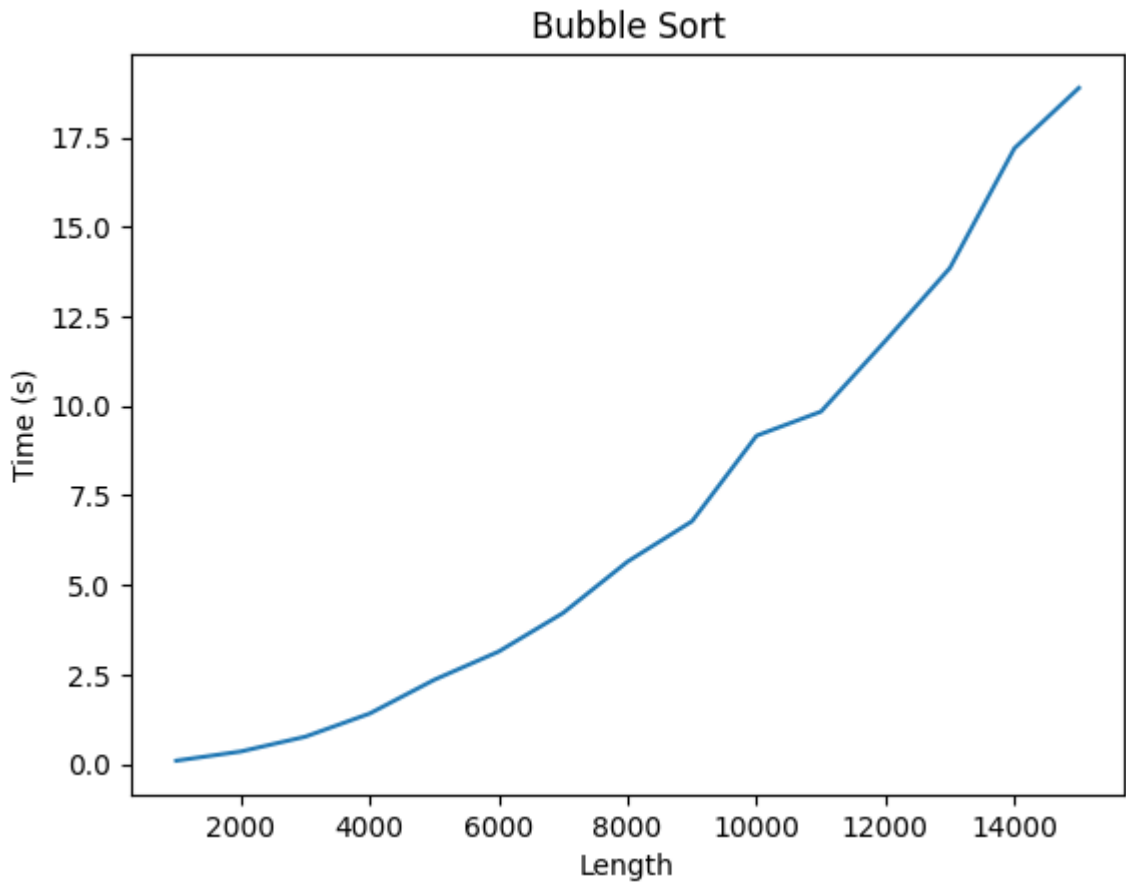
t = rx.record()
for n in Groups["Bubble"]:
    bubble_sort(make_random_list(n))
    TIMES.append(t.last_lap())
lap = t.lap()

```

```

In [5]: generate_plot("Bubble",TIMES)
print(lap)

```



105.512619972229

```

In [6]: pprint(dict(zip(Groups["Bubble"],TIMES)))

```

```

{1000: 0.090032815933228,
 2000: 0.34674596786499,
 3000: 0.7595036029815669,
 4000: 1.407308340072632,
 5000: 2.348259449005127,
 6000: 3.1385657787323,
 7000: 4.217178106307983,
 8000: 5.6525163650512695,
 9000: 6.779584884643555,
10000: 9.168732166290283,
11000: 9.843254804611206,
12000: 11.821351766586304,
13000: 13.856062412261963,
14000: 17.199060440063477,
15000: 18.88446307182312}

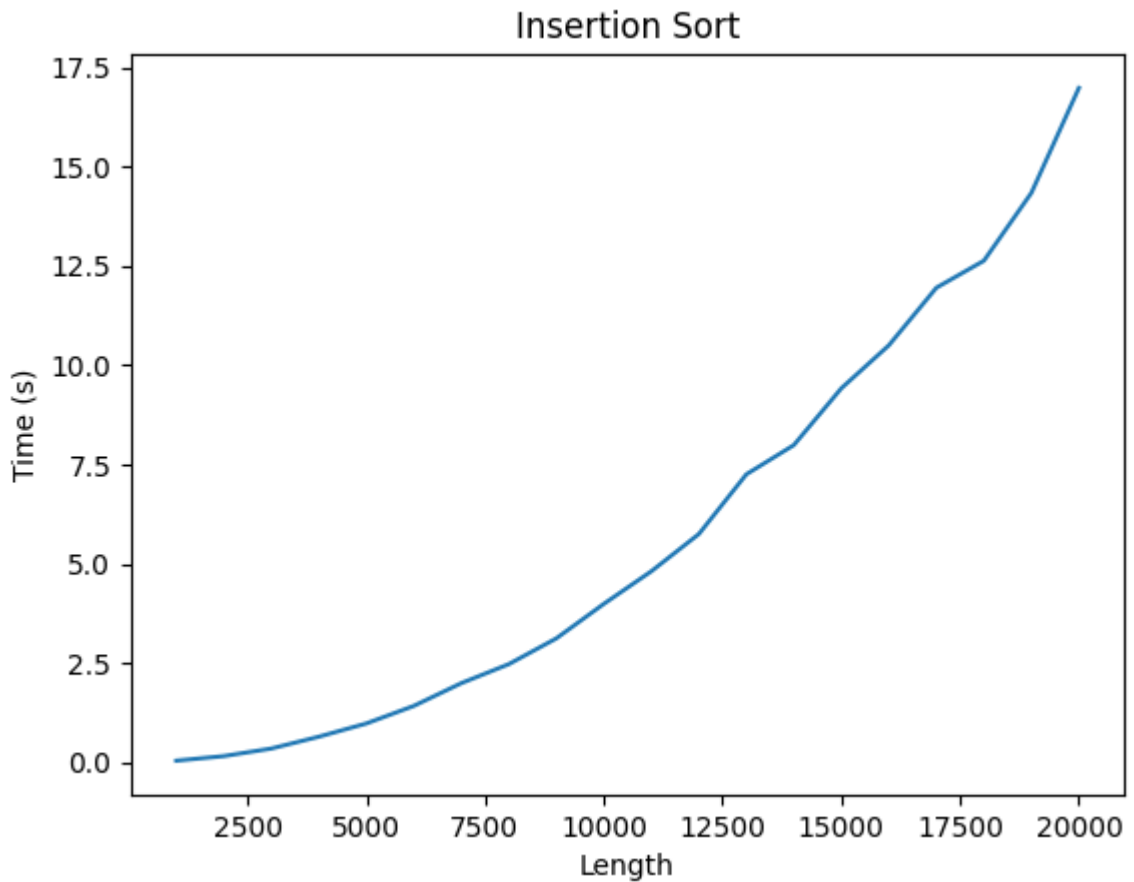
```

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## Insertion Sort ( $O(n^2)$ )

```
In [15]: TIMES = []
t = rx.record()
for n in Groups["Insertion"]:
    insertion_sort(make_random_list(n))
    TIMES.append(t.last_lap())
lap = t.lap()
```

```
In [16]: generate_plot("Insertion",TIMES)
print(lap)
```



116.745201587677

```
In [17]: pprint(dict(zip(Groups["Insertion"],TIMES)))
```

```
{1000: 0.041163682937622,  
 2000: 0.15600085258483898,  
 3000: 0.346583366394043,  
 4000: 0.6440470218658451,  
 5000: 0.9770770072937007,  
 6000: 1.419577836990356,  
 7000: 1.992505788803101,  
 8000: 2.4711520671844482,  
 9000: 3.1194286346435547,  
10000: 3.988490104675293,  
11000: 4.809168100357056,  
12000: 5.746230363845825,  
13000: 7.249871015548706,  
14000: 7.98595929145813,  
15000: 9.416332721710205,  
16000: 10.497888326644897,  
17000: 11.946320295333862,  
18000: 12.626477718353271,  
19000: 14.335059404373169,  
20000: 16.975867986679077}
```

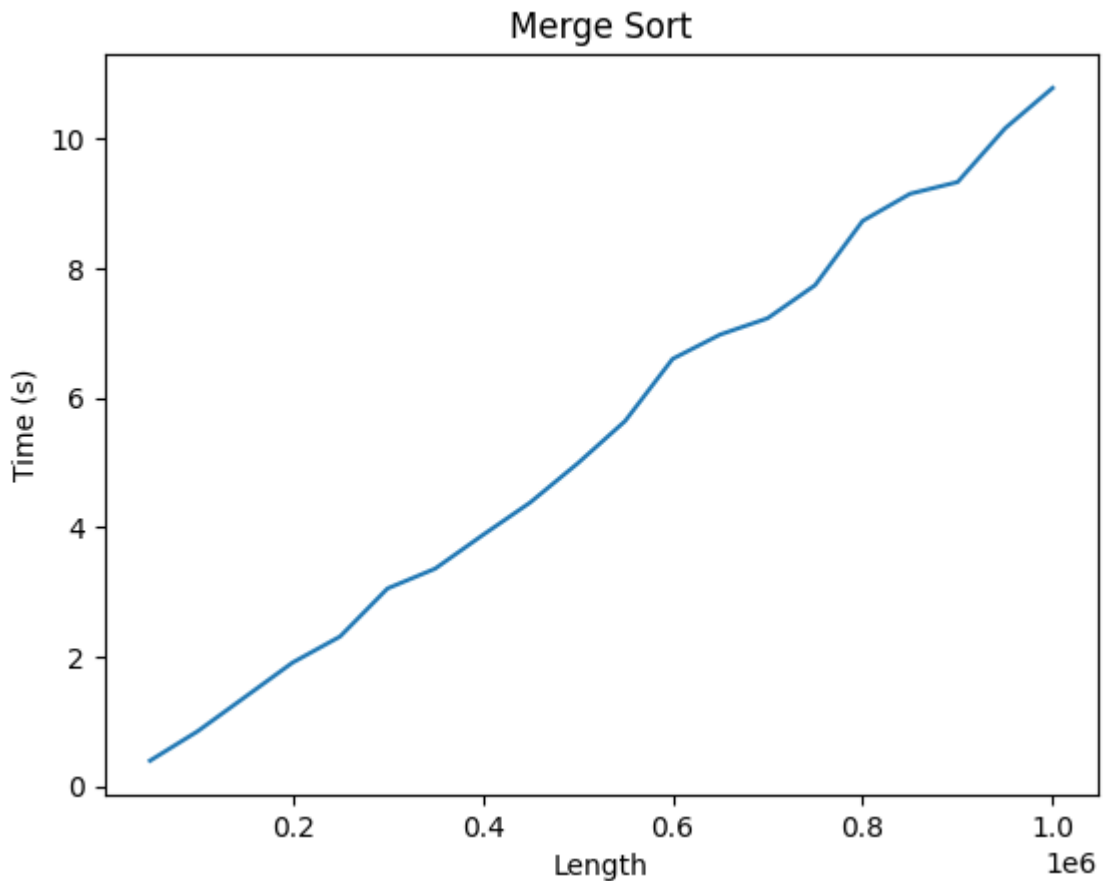
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## Merge Sort ( $O(n \cdot \lg(n))$ )

```
In [18]: TIMES = []  
         t = rx.record()  
         for n in Groups["Merge"]:  
             merge_sort(make_random_list(n))  
             TIMES.append(t.last_lap())  
         lap = t.lap()
```

```
In [19]: generate_plot("Merge", TIMES)  
         print(lap)
```



108.8369390964508

```
In [20]: pprint(dict(zip(Groups["Merge"],TIMES)))
```

```
{50000: 0.394999980926514,
 100000: 0.848061800003051,
 150000: 1.3780486583709721,
 200000: 1.9095399379730225,
 250000: 2.3120198249816895,
 300000: 3.0545804500579834,
 350000: 3.3596394062042236,
 400000: 3.8773605823516846,
 450000: 4.380809307098389,
 500000: 4.984855651855469,
 550000: 5.639374017715454,
 600000: 6.59976053237915,
 650000: 6.975269317626953,
 700000: 7.227179527282715,
 750000: 7.738732099533081,
 800000: 8.730546712875366,
 850000: 9.150113821029663,
 900000: 9.33069396018982,
 950000: 10.16140866279602,
 1000000: 10.783944845199585}
```

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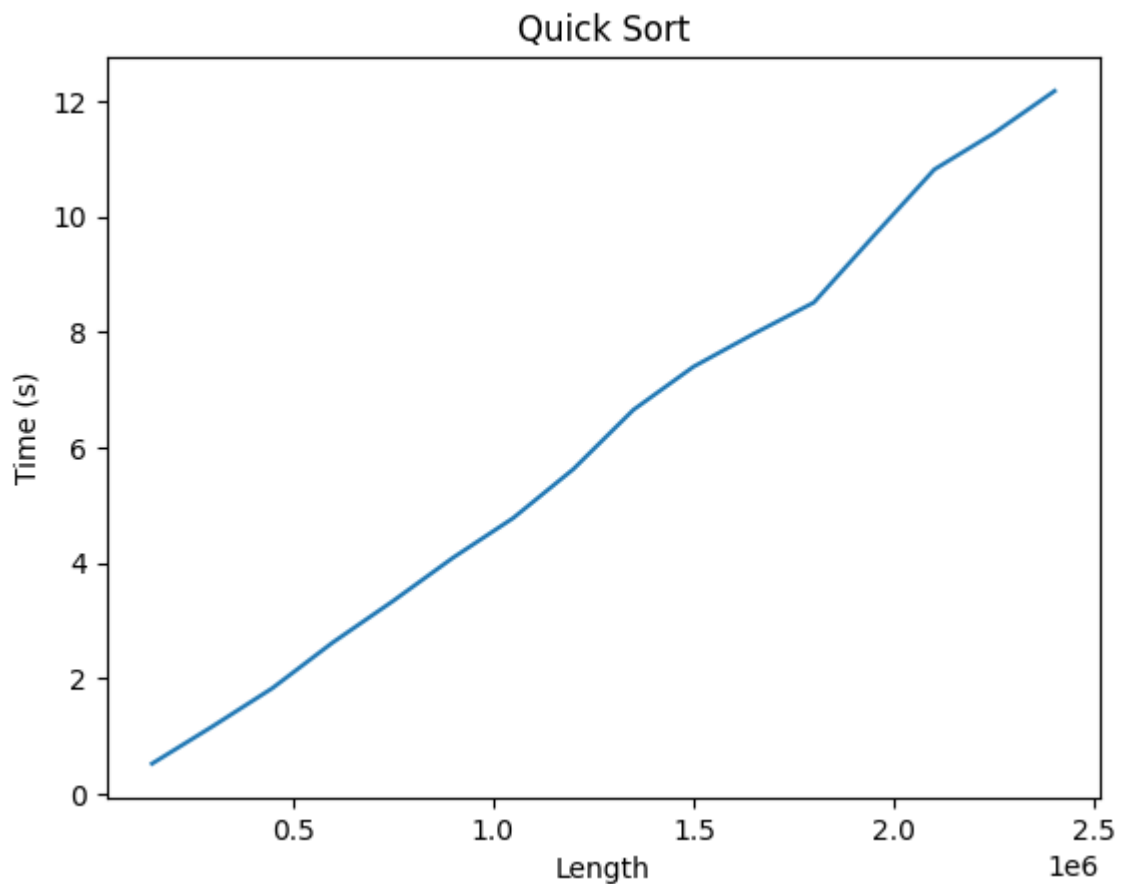
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**Quick Sort ( $O(n \cdot \lg(n))$ )**



```
In [24]: TIMES = []
t = rx.record()
for n in Groups["Quick"]:
    quicksort(make_random_list(n))
    TIMES.append(t.last_lap())
lap = t.lap()
```

```
In [25]: generate_plot("Quick",TIMES)
print(lap)
```



98.58925938606262

```
In [26]: pprint(dict(zip(Groups["Quick"],TIMES)))
```

```
{150000: 0.520304441452026,  
 300000: 1.162804603576661,  
 450000: 1.8285608291625972,  
 600000: 2.617499351501465,  
 750000: 3.3348910808563232,  
 900000: 4.087334632873535,  
 1050000: 4.774444341659546,  
 1200000: 5.621495246887207,  
 1350000: 6.650914430618286,  
 1500000: 7.399137496948242,  
 1650000: 7.9683427810668945,  
 1800000: 8.511287927627563,  
 1950000: 9.672201871871948,  
 2100000: 10.814805507659912,  
 2250000: 11.449729681015015,  
 2400000: 12.1755051612854}
```

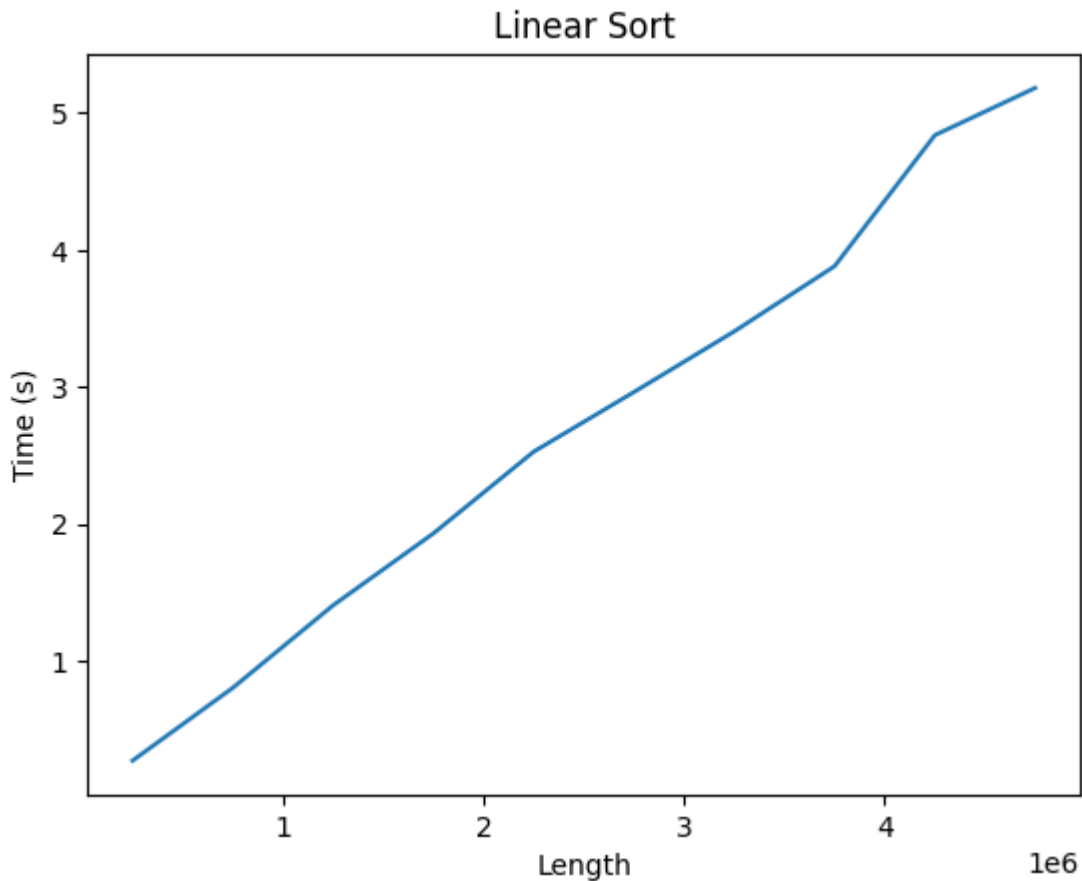
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## Linear Search

```
In [27]: TIMES = []  
t = rx.record()  
for n in Groups["Linear"]:  
    LinearSearch(make_random_list(n),-1)  
    TIMES.append(t.last_lap())  
lap = t.lap()
```

```
In [28]: generate_plot("Linear",TIMES)  
print(lap)
```



27.219929933547974

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## Binary Search

Binary Search algorithm is so fast that needs at least **1B** long list.

*(Takes around 0.002 seconds for 250,000,000 long list)*

This is not possible considering the limited RAM a common computer have

Thats why it is not used in the plots but the code for algorithm is available in algorithms section

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## Using C++ for the same algorithms

*Codes below run through terminal to get result from cpp code.*

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*Results will be saved in `database.json` and in python cells, it will be interpreted to show plots*

C++ Code

► [Click here to see C++ Algorithms](#)

```
In [29]: rx.terminal.run("Data_Structure.exe")
```

```
In [2]: from collections import OrderedDict
import json

"""
    Bubbles = list(Range(2_000,40_000))[:2000],
    Insertions = list(Range(4_000,60_000))[:4000],
    Merges = list(Range(250_000,4_000_000))[:250_000],
    Quicks = list(Range(750_000,12_000_000))[:750_000],
    Linears = list(Range(1_000_000,20_000_000))[:1_000_000],
    Linears = list(Range(1_000_000,20_000_000))[:1_000_000],
"""

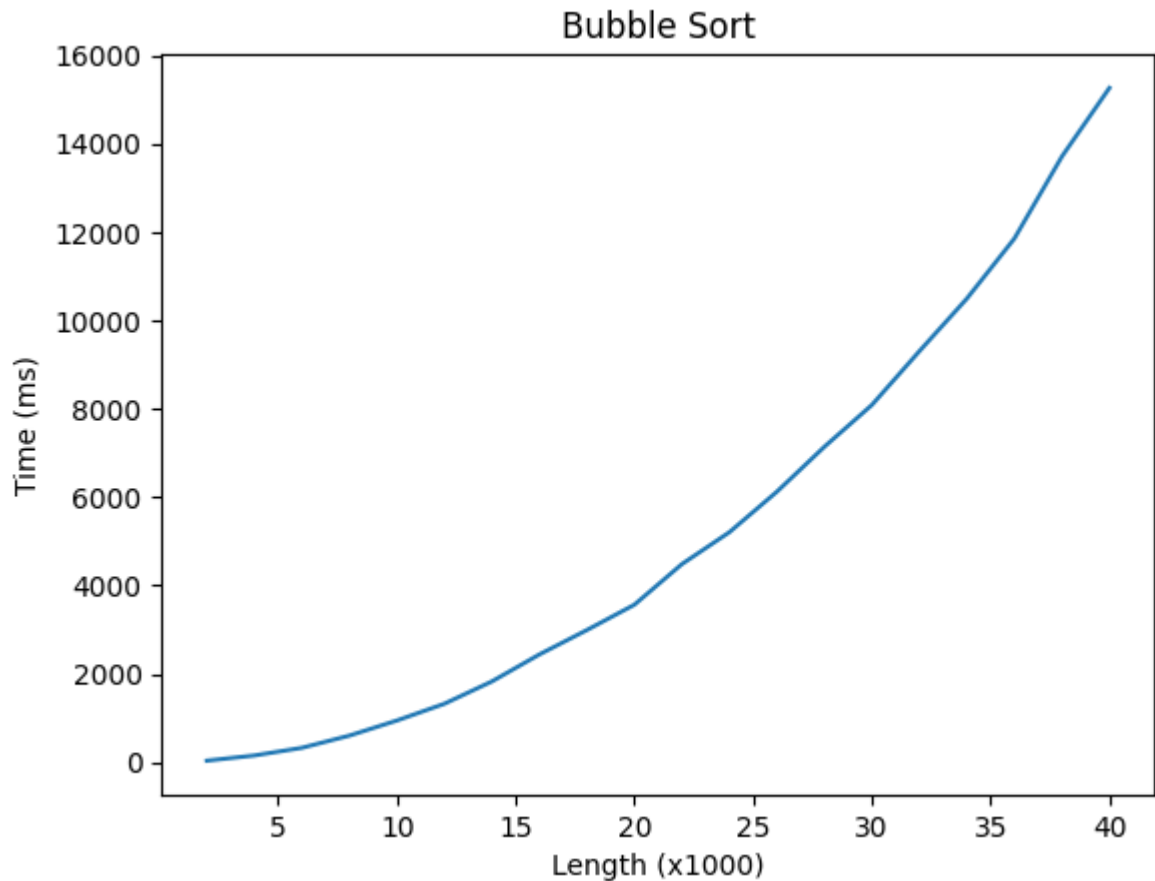
# Loading Database
with open("database.json") as f:
    loaded = json.load(f)
database = {}
for sort in list(loaded.keys())[:-1]:
    database[sort] = {}
    for k,v in loaded[sort].items():
        database[sort][int(k)] = v
for key,value in database.items():
    database[key] = OrderedDict(sorted(database[key].items()))
database["conclusion"] = loaded["conclusion"]

# function to generate plot for c++ database
def generate_plot(sort_name):
    db = database[sort_name]
    keys = [int(i)/1000 for i in db.keys()]
    values = [i/1000 for i in db.values()]
    plt.plot(keys,values)
    plt.title(f"{sort_name} Sort")
    plt.xlabel("Length (x1000)")
    plt.ylabel("Time (ms)")
    # plt.xticks(keys)
    plt.show()
```

## Algorithms Results in C++

### Bubble Sort ( $O(n^2)$ )

```
In [31]: generate_plot("Bubble")
```

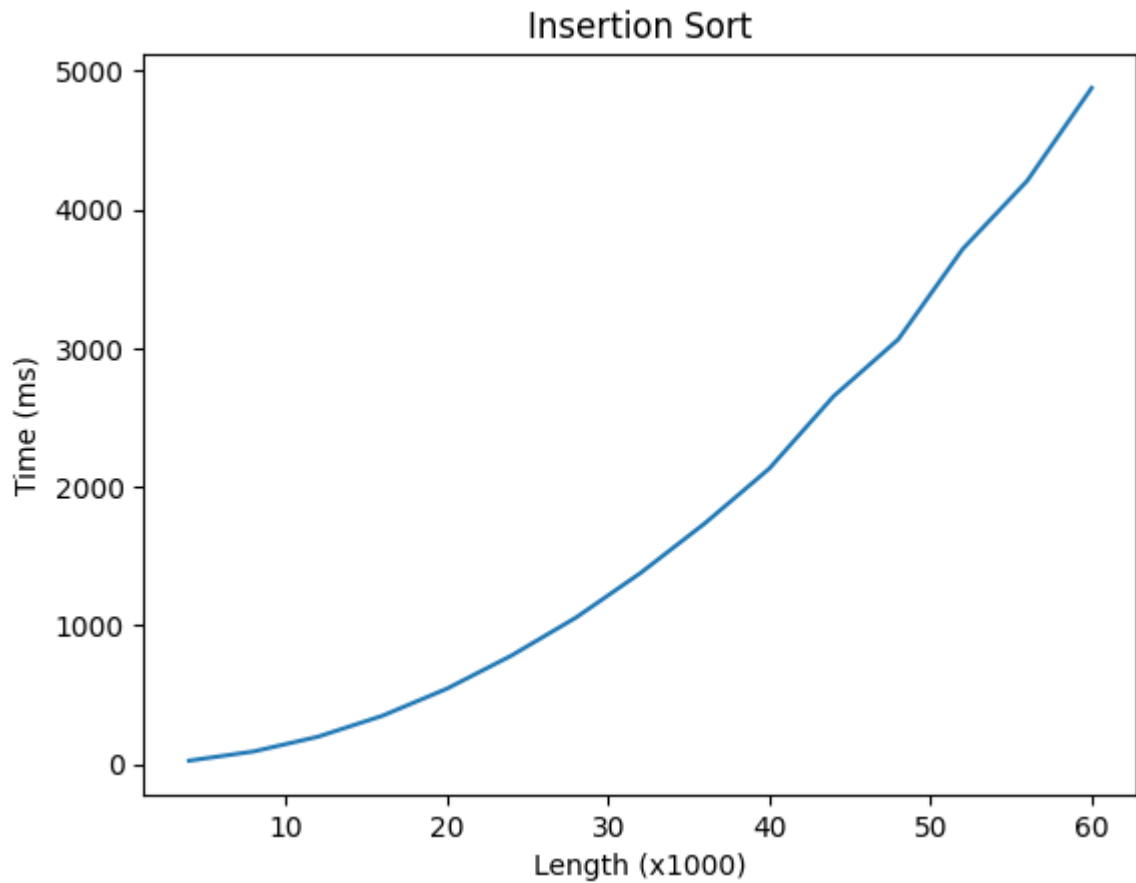


```
In [32]: pprint(dict(database["Bubble"]))
```

```
{2000: 38278,  
 4000: 155455,  
 6000: 328520,  
 8000: 604723,  
10000: 946157,  
12000: 1325007,  
14000: 1830161,  
16000: 2440564,  
18000: 2992593,  
20000: 3565520,  
22000: 4484009,  
24000: 5206022,  
26000: 6122150,  
28000: 7138679,  
30000: 8084628,  
32000: 9301274,  
34000: 10491659,  
36000: 11850219,  
38000: 13704406,  
40000: 15256222}
```

## Insertion Sort ( $O(n^2)$ )

```
In [33]: generate_plot("Insertion")
```

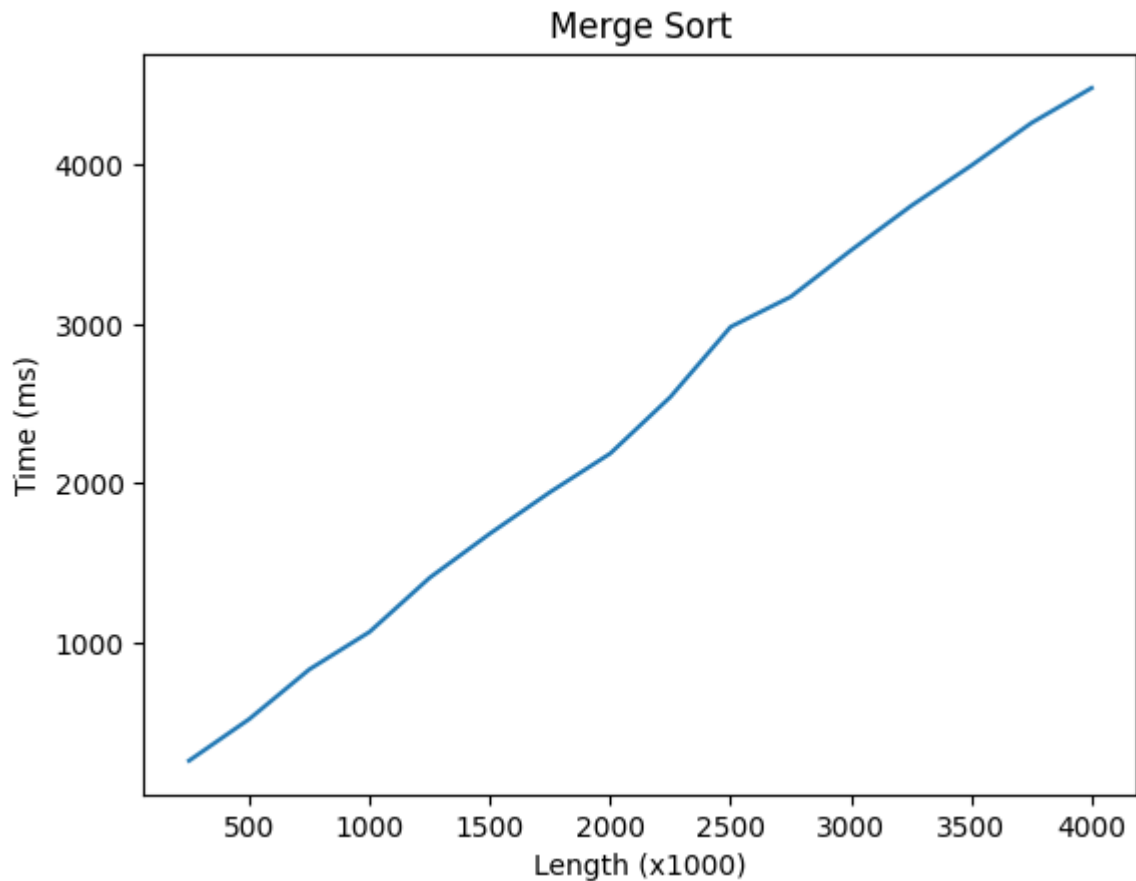


```
In [34]: pprint(dict(database["Insertion"]))
```

```
{4000: 25430,  
 8000: 91735,  
12000: 198155,  
16000: 349476,  
20000: 544733,  
24000: 783321,  
28000: 1057185,  
32000: 1378178,  
36000: 1737103,  
40000: 2132199,  
44000: 2655276,  
48000: 3064086,  
52000: 3716002,  
56000: 4207716,  
60000: 4877649}
```

## Merge Sort ( $O(n \cdot \lg(n))$ )

```
In [35]: generate_plot("Merge")
```

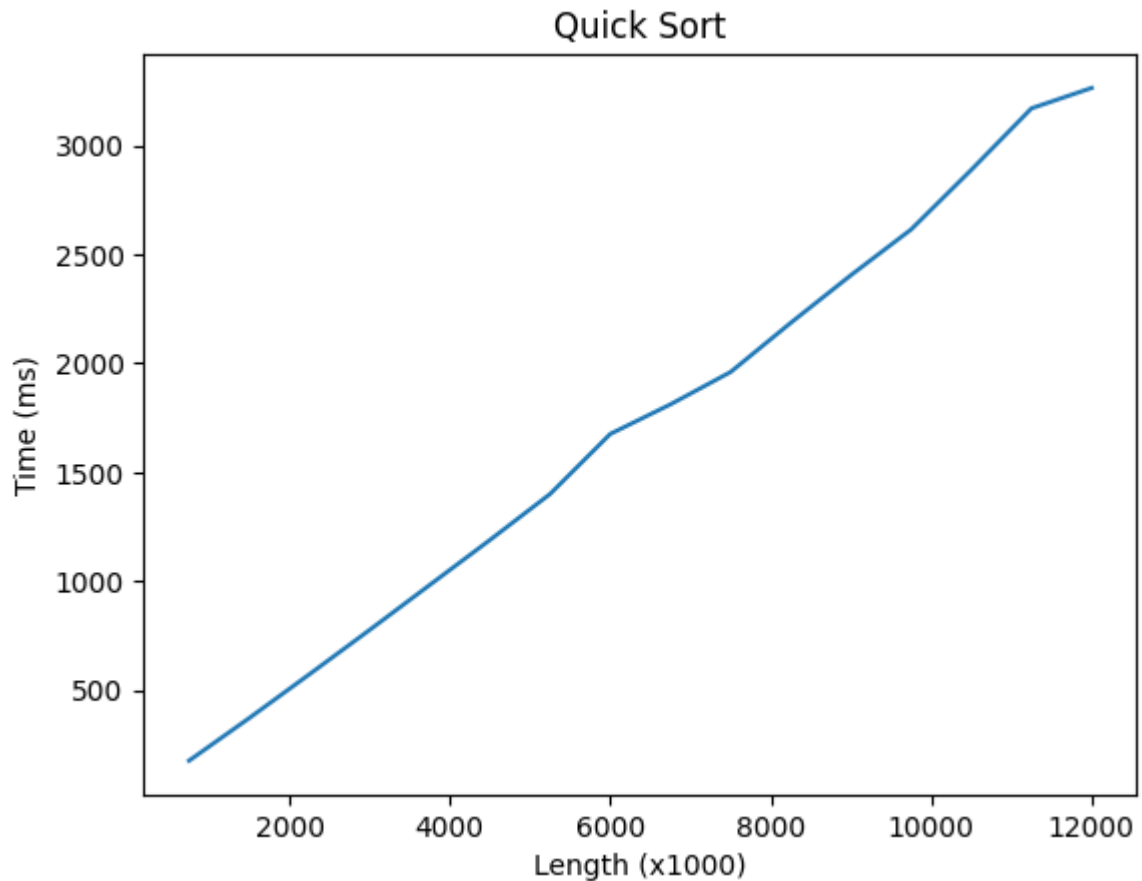


```
In [36]: pprint(dict(database["Merge"]))
```

```
{250000: 258072,  
 500000: 519523,  
 750000: 831805,  
1000000: 1067436,  
1250000: 1407902,  
1500000: 1685029,  
1750000: 1945815,  
2000000: 2188528,  
2250000: 2543748,  
2500000: 2983901,  
2750000: 3173100,  
3000000: 3464910,  
3250000: 3744333,  
3500000: 3997770,  
3750000: 4265385,  
4000000: 4485192}
```

## Quick Sort ( $O(n \cdot \lg(n))$ )

```
In [37]: generate_plot("Quick")
```



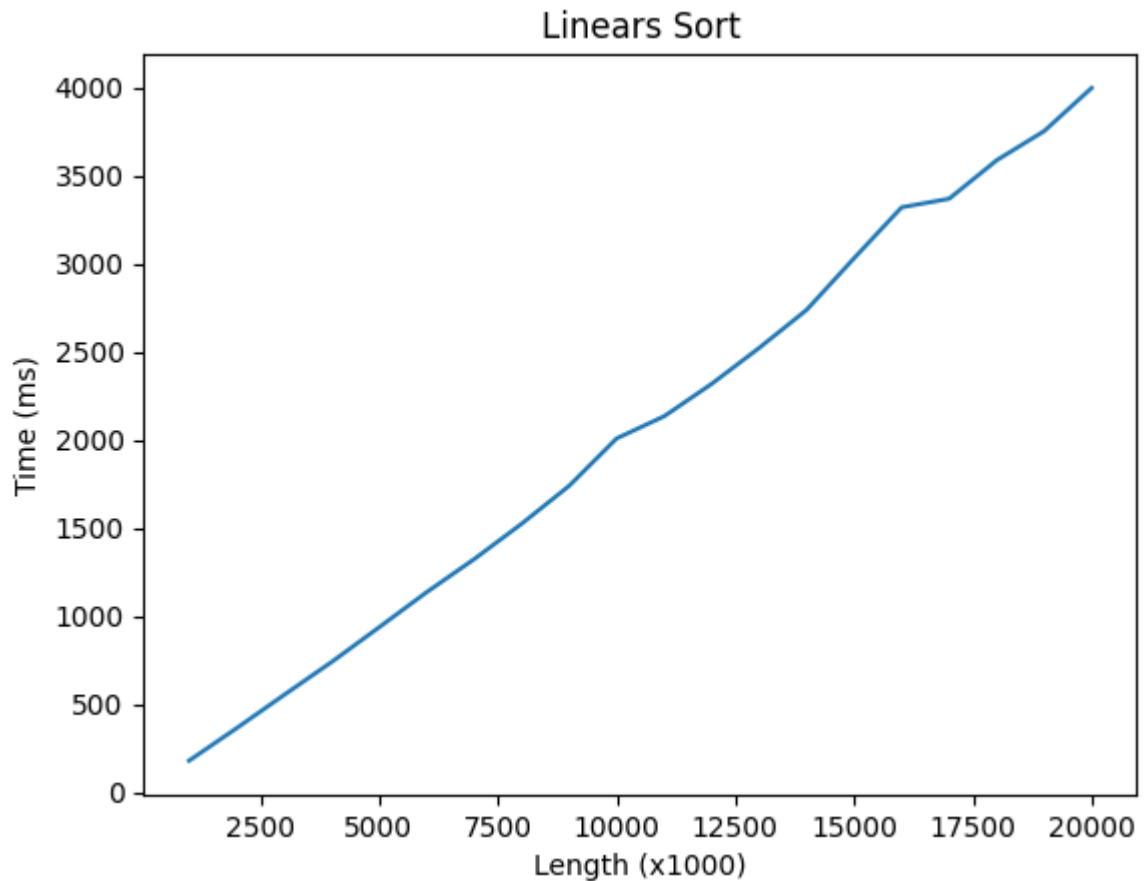
```
In [38]: pprint(dict(database["Quick"]))
```

```
{750000: 176254,  
1500000: 371645,  
2250000: 572601,  
3000000: 775936,  
3750000: 982448,  
4500000: 1188824,  
5250000: 1399847,  
6000000: 1675284,  
6750000: 1810986,  
7500000: 1959595,  
8250000: 2185320,  
9000000: 2403979,  
9750000: 2613671,  
10500000: 2887143,  
11250000: 3169348,  
12000000: 3262918}
```

## Linear Search ( $O(n)$ )

```
In [39]: generate_plot("Linears")
```



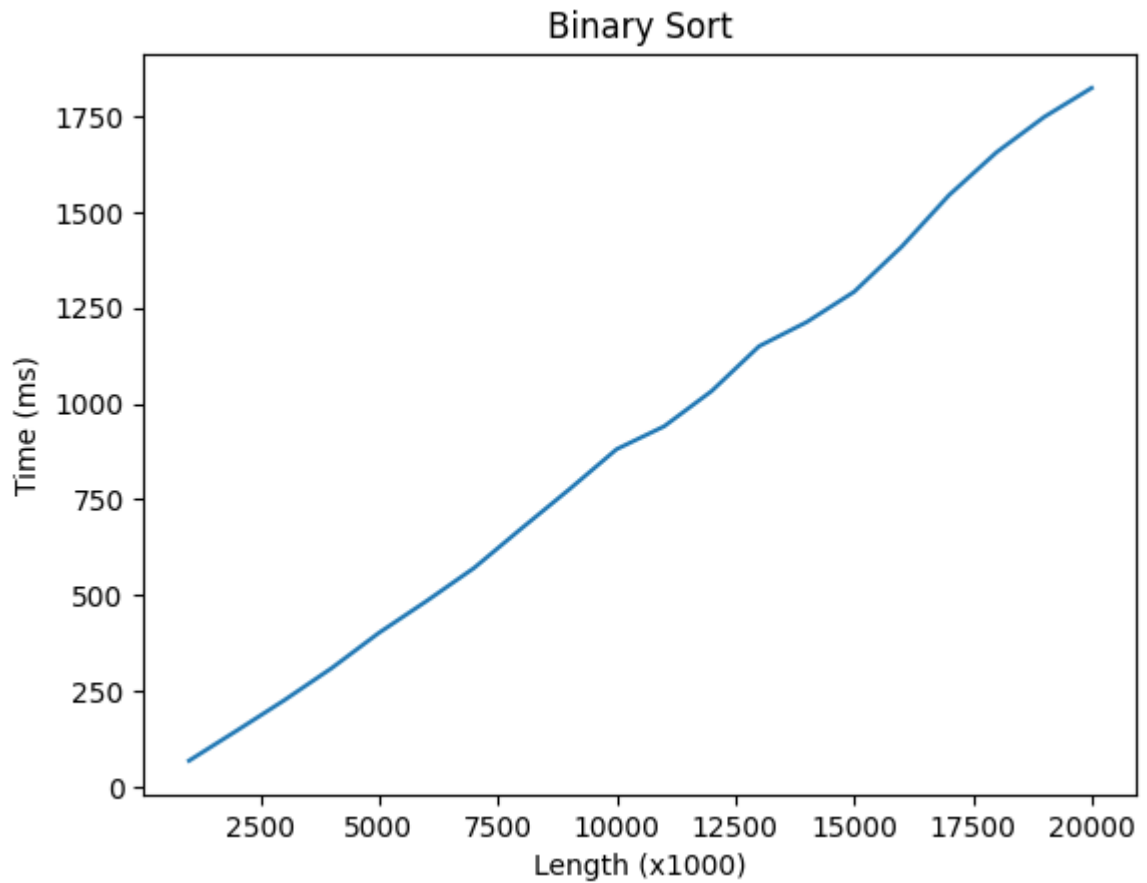


```
In [41]: pprint(dict(database["Linears"]))
```

```
{1000000: 179465,  
 2000000: 363653,  
 3000000: 552598,  
 4000000: 739291,  
 5000000: 936401,  
 6000000: 1135539,  
 7000000: 1322952,  
 8000000: 1523933,  
 9000000: 1739115,  
 10000000: 2008422,  
 11000000: 2134202,  
 12000000: 2318000,  
 13000000: 2522028,  
 14000000: 2738134,  
 15000000: 3031808,  
 16000000: 3320411,  
 17000000: 3369133,  
 18000000: 3587394,  
 19000000: 3752932,  
 20000000: 3998014}
```

## Binary Search ( $O(\lg(n))$ )

```
In [42]: generate_plot("Binary")
```



```
In [43]: pprint(dict(database["Binary"]))
```

```
{1000000: 68019,  
 2000000: 146102,  
 3000000: 225486,  
 4000000: 309447,  
 5000000: 401977,  
 6000000: 484795,  
 7000000: 571158,  
 8000000: 674534,  
 9000000: 775959,  
10000000: 881124,  
11000000: 940793,  
12000000: 1032865,  
13000000: 1150035,  
14000000: 1212944,  
15000000: 1292106,  
16000000: 1409654,  
17000000: 1544635,  
18000000: 1656497,  
19000000: 1748409,  
20000000: 1824242}
```

---

## Conclusion

```

In [10]: i = 1
for sort in ("Bubble", "Insertion", "Merge", "Quick"): #, "Linears", "Binary"
    db = database[sort]
    keys = [int(i)/1000 for i in db.keys()]
    values = [i/1000 for i in db.values()]
    plt.subplot(3,2,i)
    plt.plot(keys, values)
    plt.title(f"{sort} Sort")
    plt.xticks([], [])
    plt.yticks([], [])
    i += 1
plt.suptitle("Comparison")
plt.show()

db = {}
for sort in list(database["conclusion"].keys()):
    db[sort] = {}
    for k,v in database["conclusion"][sort].items():
        db[sort][int(k)] = v
for key,value in db.items():
    db[key] = dict(OrderedDict(sorted(db[key].items()))))

# print(db["Insertion"])
print("\n")

for sort in ("Bubble", "Insertion", "Merge", "Quick"):
    a = (db[sort])
    plt.plot(a.keys(), a.values())

plt.legend(["Bubble", "Insertion", "Merge", "Quick"])
plt.show()

```

## Comparison

