

Haskell: How is <*> pronounced?

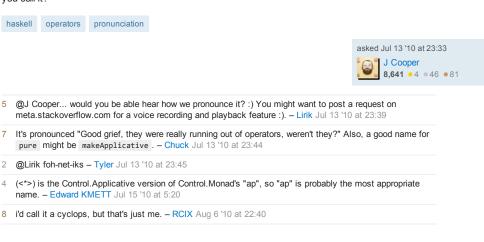


Sorry, I don't really know my math, so I'm curious how to pronounce the functions in the Applicative typeclass:

```
(<*>) :: f (a -> b) -> f a -> f b
(*>) :: f a -> f b -> f b
(<*) :: f a -> f b -> f a
```

(That is, if they weren't operators, what might they be called?)

As a side note, if you could rename pure to something more friendly to podunks like me, what would you call it?



3 Answers

Sorry, I don't really know my math, so I'm curious how to pronounce the functions in the Applicative typeclass

Knowing your math, or not, is largely irrelevant here, I think. As you're probably aware, Haskell borrows a few bits of terminology from various fields of abstract math, most notably Category Theory, from whence we get functors and monads. The use of these terms in Haskell diverges somewhat from the formal mathematical definitions, but they're usually close enough to be good descriptive terms anyway.

The Applicative type class sits somewhere between Functor and Monad, so one would expect it to have a similar mathematical basis. The documentation for the Control.Applicative module begins with:

This module describes a structure intermediate between a functor and a monad: it provides pure expressions and sequencing, but no binding. (Technically, a strong lax monoidal functor.)

Hmm.

```
class (Functor f) => StrongLaxMonoidalFunctor f where
     . . .
```

Not quite as catchy as Monad, I think.

What all this basically boils down to is that Applicative doesn't correspond to any concept that's

particularly *interesting* mathematically, so there's no ready-made terms lying around that capture the way it's used in Haskell. So, set the math aside for now.

If we want to know what to call (<*>) it might help to know what it basically means.

So what's up with Applicative, anyway, and why do we call it that?

What Applicative amounts to in practice is a way to lift arbitrary functions into a Functor. Consider the combination of Maybe (arguably the simplest non-trivial Functor) and Bool (likewise the simplest non-trivial data type).

```
maybeNot :: Maybe Bool -> Maybe Bool
maybeNot = fmap not
```

The function fmap lets us lift not from working on Bool to working on Maybe Bool. But what if we want to lift (&&) ?

```
maybeAnd' :: Maybe Bool -> Maybe (Bool -> Bool)
maybeAnd' = fmap (&&)
```

Well, that's not what we want at all! In fact, it's pretty much useless. We can try to be clever and sneak another Bool into Maybe through the back...

```
maybeAnd'' :: Maybe Bool -> Bool -> Maybe Bool maybeAnd'' x y = fmap (\$ y) (fmap (\&\&) x)
```

...but that's no good. For one thing, it's wrong. For another thing, it's ugly. We could keep trying, but it turns out that there's no way to lift a function of multiple arguments to work on an arbitrary <code>Functor</code>. Annoying!

On the other hand, we could do it easily if we used Maybe 's Monad instance:

Now, that's a lot of hassle just to translate a simple function--which is why <code>control.Monad</code> provides a function to do it automatically, <code>liftm2</code>. The 2 in its name refers to the fact that it works on functions of exactly two arguments; similar functions exist for 3, 4, and 5 argument functions. These functions are <code>better</code>, but not perfect, and specifying the number of arguments is ugly and clumsy.

Which brings us to the paper that introduced the Applicative type class. In it, the authors make essentially two observations:

- Lifting multi-argument functions into a Functor is a very natural thing to do
- Doing so doesn't require the full capabilities of a Monad

Normal function application is written by simple juxtaposition of terms, so to make "lifted application" as simple and natural as possible, the paper introduces *infix operators to stand in for application*. *lifted into the Functor*, and a type class to provide what's needed for that.

All of which brings us to the following point: (<*>) simply represents function application--so why pronounce it any differently than you do the whitespace "juxtaposition operator"?

But if that's not very satisfying, we can observe that the <code>control.Monad</code> module also provides a function that does the same thing for monads:

```
ap :: (Monad m) => m (a -> b) -> m a -> m b
```

Where ap is, of course, short for "apply". Since any Monad can be Applicative, and ap needs only the subset of features present in the latter, we can perhaps say that if (<*>) weren't an operator, it should be called ap.

We can also approach things from the other direction. The Functor lifting operation is called fmap because it's a generalization of the map operation on lists. What sort of function on lists would work like (<*>)? There's what ap does on lists, of course, but that's not particularly useful on its own.

In fact, there's a perhaps more natural interpretation for lists. What comes to mind when you look at the following type signature?

```
listApply :: [a -> b] -> [a] -> [b]
```

There's something just so tempting about the idea of lining the lists up in parallel, applying each function in the first to the corresponding element of the second. Unfortunately for our old friend Monad, this simple operation *violates the monad laws* if the lists are of different lengths. But it makes a fine Applicative, in which case (<*>) becomes a way of stringing together a generalized version of zipwith, so perhaps we can imagine calling it fzipwith?

This zipping idea actually brings us full circle. Recall that math stuff earlier, about monoidal functors? As the name suggests, these are a way of combining the structure of monoids and functors, both of which are familiar Haskell type classes:

```
class Functor f where
   fmap :: (a -> b) -> f a -> f b

class Monoid a where
   mempty :: a
   mappend :: a -> a -> a
```

What would these look like if you put them in a box together and shook it up a bit? From Functor we'll keep the idea of a *structure independent of its type parameter*, and from Monoid we'll keep the overall form of the functions:

```
class (Functor f) => MonoidalFunctor f where
    mfEmpty :: f ?
    mfAppend :: f ? -> f ? -> f ?
```

We don't want to assume that there's a way to create an truly "empty" Functor, and we can't conjure up a value of an arbitrary type, so we'll fix the type of <code>mfEmpty</code> as <code>f()</code>.

We also don't want to force mfAppend to need a consistent type parameter, so now we have this:

```
class (Functor f) => MonoidalFunctor f where
    mfEmpty :: f ()
    mfAppend :: f a -> f b -> f ?
```

What's the result type for mfAppend? We have two arbitrary types we know nothing about, so we don't have many options. The most sensible thing is to just keep both:

```
class (Functor f) => MonoidalFunctor f where
    mfEmpty :: f ()
    mfAppend :: f a -> f b -> f (a, b)
```

At which point mfAppend is now clearly a generalized version of zip on lists, and we can reconstruct Applicative easily:

```
mfPure x = fmap (\() \rightarrow x) mfEmpty
mfApply f x = fmap (\(f, x) \rightarrow f x) (mfAppend f x)
```

This also shows us that pure is related to the identity element of a Monoid, so other good names for it might be anything suggesting a unit value, a null operation, or such.

That was lengthy, so to summarize:

- (<*>) is just a modified function application, so you can either read it as "ap" or "apply", or elide it entirely the way you would normal function application.
- (<*>) also roughly generalizes zipWith on lists, so you can read it as "zip functors with", similarly to reading fmap as "map a functor with".

The first is closer to the intent of the Applicative type class--as the name suggests--so that's what I recommend.

In fact, I encourage liberal use, and non-pronunciation, of all lifted application operators:

- (<\$>) , which lifts a single-argument function into a Functor
- (<*>), which chains a multi-argument function through an Applicative
- $\bullet \quad \text{(=<<)}$, which binds a function that enters a $\, \text{Monad} \,$ onto an existing computation

All three are, at heart, just regular function application, spiced up a little bit.



- 14 This is a fantastic answer. Extremely informative and very well-written. Colin Cochrane Jul 14 '10 at 2:09
- @Colin Cochrane: Are you sure you didn't misspell "long-winded" there?:) But hey, I'll take it! I always feel that Applicative and the functional idiomatic style it promotes don't get enough love, so I couldn't resist the chance to extol its virtues a bit as a means to explain how I (don't) pronounce (<*>>) . C. A. McCann Jul 14 '10 at 2:16
- Would that Haskell had syntax sugar for Applicative 's! Something like [| f a b c d |] (as suggested by the original paper). Then we wouldn't need the <*> combinator and you would refer to such an expression as an example of "function application in a functorial context" Tom Crockett Jan 6 '11 at 0.19
- @FredOverflow: No, I meant Monad . Or Functor or Monoid or anything else that has a well-established term involving fewer than three adjectives. "Applicative" is merely an uninspiring, albeit reasonably descriptive, name slapped onto something that rather needed one. C. A. McCann Sep 23 '11 at 18:30 *
- @pelotom: see [stackoverflow.com/questions/12014524/... where kind people showed me two ways to get almost that notation. – AndrewC Aug 22 '12 at 18:04



Since I have no ambitions of improving on C. A. McCann's technical answer, I'll tackle the more fluffy one:

If you could rename pure to something more friendly to podunks like me, what would you call it?

As an alternative, especially since there is no end to the constant angst-and-betrayal-filled cried against the Monad version, called "return", I propose another name, which suggests its function in a way that can satisfy the most imperative of imperative programmers, and the most functional of...well, hopefully, everyone can complain the same about: inject.

Take a value. "Inject" it into the <code>Functor</code>, <code>Applicative</code>, <code>Monad</code>, or what-have-you. I vote for "inject", and I approved this message.



answered Jul 14 '10 at 22:15



3 I usually lean toward something like "unit" or "lift", but those already have too many other meanings in Haskell. inject is an excellent name and probably better than mine, though as a minor side note, "inject" is used in–I think–Smalltalk and Ruby for a left-fold method of some sort. I never understood that choice of name, though... – C. A. McCann Jul 14 '10 at 23:45

3 This is a very old thread, but I think that inject in Ruby & Smalltalk is used because it is like you are "injecting" an operator between each element in the list. At least, that's how I always thought of it. – Jonathan Sterling Jun 7 '12 at 18:48

To again pick up that old side-thread: You're not injecting operators, you're replacing (eliminating) constructors that are already there. (Viewed the other way round, you're injecting old data into a new type.) For lists, elimination is just foldr. (You replace (:) and [], where (:) takes 2 args and [] is a constant, hence foldr (+) 0 (1:2:3:[]) \sim 1+2+3+0.) On Bool it's just if - then - else (two constants, pick one) and for Maybe it's called maybe ... Haskell has no single name/function for this, as all have different types (in general elim is just recursion/induction) – nobody Mar 16 '13 at 3:56

I always liked wrap. Take a value and wrap it in a Functor, Applicative, Monad. It also works well when used in a sentence with concrete instances: [], Maybe, etc. "It takes a value and wraps it in a x".

answered Apr 18 '15 at 15:48

Peter Hall

4,162 • 1 • 17 • 50