

3rd Year B.S. (Honors) 2019
Math Lab Assignment 03
Course: AMTH 350 (Math Lab III)
Department of Applied Mathematics
University of Dhaka

Name: Roll No: Write MATLAB program to solve the following problems using Script file.

No:	Problems
1	<p>Consider the following linear system of equations:</p> $10x_1 - x_2 + 2x_3 = 6$ $-x_1 + 11x_2 - x_3 + 3x_4 = 25$ $2x_1 - x_2 + 10x_3 - x_4 = -11$ $3x_2 - x_3 + 8x_4 = 15$ <p>Solve the above system, correct up to 5 decimal places, with initial guess $x_0 = (0,0,0,0)$ using:</p> <ul style="list-style-type: none"> (i) Jacobi iterative method. (ii) Gauss-Seidel iterative method. (iii) SOR iterative method with $\omega = 1.1$.
2	<p>Consider the system of equations given below</p> $2x_1 - 3x_2 + 2x_3 = 5$ $-4x_1 + 2x_2 - 6x_3 = 14$ $2x_1 + 2x_2 + 4x_3 = 8$ <ul style="list-style-type: none"> (a) Solve the system using Gaussian elimination method. (b) Solve the system using Gaussian-Jordan elimination method.
3	<p>Use the Power method to approximate the dominant eigenvalue of the matrix</p> $A = \begin{pmatrix} -4 & 14 & 0 \\ 0 & 0 & 0 \\ -5 & 13 & 0 \end{pmatrix}$

	<p style="text-align: center;">-102</p> <p>Let $\mathbf{y}^0 = (1, 1, 1)$</p>
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4	<p>Solve the following initial value problem over the interval [0,2]. Display all your results graphically.</p> <p>$y''' = y^3 - 1.5y, y(0) = 1$</p> <p>(a) ode solver.</p> <p>(b) Using Euler's method with h =0.5 and 0.25.</p> <p>(c) Using the midpoint method with h =0.5.</p> <p>(d) Using Heun's method with h=0.5.</p> <p>(e) Using the fourth-order RK method with h =0.5.</p>
5(a)	<p>Solve the following system of ODEs</p> $\begin{aligned} y' &= x^2 - yz \\ z' &= -xy + y^2 \\ y(0) &= 2, z(0) = 1 \end{aligned}$ <p>Taking $x = 1.2, y = 0.6, z = 0.8, \Delta x = 0.3$.</p>
5(b)	<p>The van der Pol equation is a second order ODE</p> $y'' - \mu(1 - y^2)y' = 0, y(0) = 2, y'(0) = 0$ <p>where $\mu > 0$ is a scalar parameter. Solve the above equation using shooting method (ode45 solver) and then show the result graphically.</p>

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Consider the heat conduction equation

$$\begin{aligned}
 & \frac{\partial^2 T}{\partial x^2} = \frac{\partial T}{\partial t} \\
 & T(0, t) = 100, T(10, t) = 0, T(x, 0) = 0, \\
 & 0 \leq x \leq 10, t > 0
 \end{aligned}$$

Solve the above equation using finite difference method and the show the result graphically. (In particular case let $\Delta x = 1, \Delta t = 1$)