

### Task-3

Dijkstra algorithm pseudocode is in the following:

dijkstra( $G, s$ ):

$O(V)$  [ for each  $v \in V[G]$ :  
do  $d[v] \leftarrow \infty$   
 $p[v] \leftarrow \text{None}$

$d[s] \leftarrow 0$

$Q \leftarrow V[G]$

$O(V)$  while  $Q$  not empty:

$O(\log(V)) \leftarrow$  do  $u \leftarrow \text{extract\_min}(Q)$   
Uses heap data structure

[ for each vertex  $v \in \text{Adj}[u]$ :

do if  $d[v] > d[u] + w(u, v)$

then  $d[v] \leftarrow d[u] + w(u, v)$

$p[v] \leftarrow u$

works as

BFS, so, ~~is~~

$O(V+E)$

$$\begin{aligned}\therefore \text{Time complexity} &= O(V) + O(1) + O(V \log V) \\ &\quad + O(V+E) \\ &= O(V \log V) \text{ [By ignoring} \\ &\quad \text{the lowest terms]}\end{aligned}$$

As in task 1 and task 2, dijkstra algorithm has been used. So, for both task 1 and task 2 the time complexity will be  $O(V \log V)$ .  
 $= O(N \log N)$

~~Else~~

[Here,  $N$  = number of places/vertices]

If ~~the~~ the number of titans is set to 1, then the graph will be as an BFS. Moreover, the time complexity of BFS is  $O(V+E)$  which will be  $O(N+N)$  according to this problem statement. Thus, we can solve this problem using BFS. The inputs for BFS

algorithm will be graph (list of all vertices)  
and the start vertex.