

OPTIONAL PROJECT: AE 625 CFD

Simulate a lid driven cavity problem using the below information.

Consider the system of differential equations: two equations for the velocity components u, v and one equation for pressure to simulate a 2D Channel flow.

$$\begin{aligned}\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} &= -\frac{1}{\rho} \frac{\partial p}{\partial x} + \nu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \\ \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} &= -\frac{1}{\rho} \frac{\partial p}{\partial y} + \nu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) \\ \frac{\partial^2 p}{\partial x^2} + \frac{\partial^2 p}{\partial y^2} &= -\rho \left(\frac{\partial u}{\partial x} \frac{\partial u}{\partial x} + 2 \frac{\partial u}{\partial y} \frac{\partial v}{\partial x} + \frac{\partial v}{\partial y} \frac{\partial v}{\partial y} \right)\end{aligned}$$

The initial condition is $u, v, p = 0$ everywhere, and the boundary conditions are:

$$u = 1 \text{ at } y = 2 \text{ (the "lid")};$$

$$u, v = 0 \text{ on the other boundaries};$$

$$\frac{\partial p}{\partial y} = 0 \text{ at } y = 0;$$

$$p = 0 \text{ at } y = 2$$

$$\frac{\partial p}{\partial x} = 0 \text{ at } x = 0, 2$$

Plot the results of the cavity flow solver for different lengths of time.