Is624 Assignment3

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Question 7.2

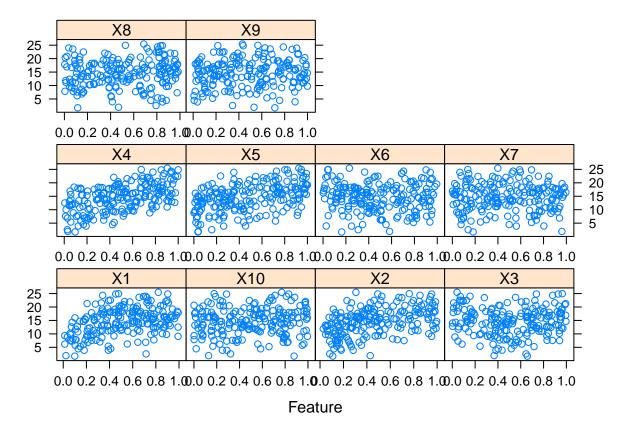
Question

Friedman (1991) introduced several benchmark data sets create by simulation. One of these simulations used the following nonlinear equation to create data:

$$y = 10sin(nx_1x_2) + 20(x_3 - 0.5)2 + 10x_4 + 5x_5 + N(0, alpha^2)$$

where the x values are random variables uniformly distributed between [0, 1] (there are also 5 other non-informative variables also created in the simulation). The package mlbench contains a function called mlbench.friedman1 that simulates these data:

```
trainingData <- mlbench.friedman1(200, sd = 1)
## We convert the ' x ' data from a matrix to a data
## frame One reason is that this will give the
## columns names.
trainingData$x <- data.frame(trainingData$x)
## Look at the data using
featurePlot(trainingData$x, trainingData$y)</pre>
```



```
## or other methods. This creates a list with a
## vector ' y ' and a matrix of predictors ' x ' .
## Also simulate a large test set to estimate the
## true error rate with good precision:
testData <- mlbench.friedman1(5000, sd = 1)
testData$x <- data.frame(testData$x)</pre>
```

Tune several models on these data. For example:

```
knnModel <- train(x = trainingData$x, y = trainingData$y,
    method = "knn", preProc = c("center", "scale"),
    tuneLength = 10)
knnModel</pre>
```

```
## k-Nearest Neighbors
##
## 200 samples
    10 predictors
##
##
## Pre-processing: centered, scaled
## Resampling: Bootstrapped (25 reps)
##
## Summary of sample sizes: 200, 200, 200, 200, 200, 200, ...
##
## Resampling results across tuning parameters:
##
                               RMSE SD
                                          Rsquared SD
##
         RMSE
                   Rsquared
     k
```

```
5 3.492611 0.5514878 0.1890666 0.05654488
##
##
     7 3.367499 0.5919769 0.1854113 0.05577892
     9 3.309609 0.6182302 0.2022743 0.05494413
##
##
    11 3.289578 0.6367648 0.2270144 0.04463323
    13 3.281397 0.6559647 0.2285598 0.04659637
##
##
    15 3.287363 0.6661678 0.2404266 0.04807383
    17 3.334535 0.6641188 0.2509047 0.05246330
    19 3.370126 0.6642655 0.2527395 0.05007358
##
##
    21 3.403700 0.6655961 0.2556742 0.05093303
##
    23 3.435312 0.6667585 0.2498849 0.05135945
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was k = 13.
knnPred <- predict(knnModel, newdata = testData$x)</pre>
## The function ' postResample ' can be used to get
## the test set perforamnce values
postResample(pred = knnPred, obs = testData$y)
```

Answer

A kNN model was generated for us above. We have three options: train a neural network, a MARS model, and a SVM model (with potentially different kernels). Lets first look at a neural net model.

Neural Net Model

RMSE Rsquared

1.4423934 0.9167035

```
# Create a Neural Net model
nnetFit <- nnet(trainingData$x, trainingData$y, size = 5,</pre>
    decay = 0.01, linout = TRUE, trace = FALSE, maxit = 500,
    MaxNWts = 5 * (ncol(trainingData$x) + 1) + 5 +
        1)
# Show the fit
nnetFit
## a 10-5-1 network with 61 weights
## options were - linear output units decay=0.01
summary(nnetFit)
## a 10-5-1 network with 61 weights
## options were - linear output units decay=0.01
##
     b->h1
           i1->h1 i2->h1 i3->h1
                                     i4->h1 i5->h1
                                                     i6->h1
                                                             i7->h1
                                                                      i8->h1
##
     -0.87
             -0.97
                     -0.67
                               1.04
                                       1.20
                                               0.50
                                                       0.00
                                                                0.12
                                                                        0.03
##
    i9->h1 i10->h1
##
      0.08
             -0.15
##
     b->h2 i1->h2 i2->h2 i3->h2
                                     i4->h2 i5->h2
                                                     i6->h2 i7->h2
                                                                      i8->h2
##
      0.70
            -0.94
                     -0.56
                             -6.14
                                       0.33
                                               0.16
                                                       0.41
                                                                0.16
                                                                        0.42
##
    i9->h2 i10->h2
##
     -0.13
              0.09
##
     b->h3 i1->h3 i2->h3 i3->h3
                                     i4->h3 i5->h3
                                                     i6->h3
                                                              i7->h3
                                                                      i8->h3
     -4.22
              3.73
                     12.72
                               1.24
                                      -0.99
                                              -0.10
                                                                       -0.51
##
                                                       0.07
                                                               -0.69
##
    i9->h3 i10->h3
##
     -0.19
              0.40
     b->h4 i1->h4 i2->h4 i3->h4
##
                                     i4->h4
                                             i5->h4
                                                     i6->h4
                                                              i7->h4
                                                                      i8->h4
            -7.52
                      0.88
                             -1.00
                                       0.16
                                              -0.03
                                                       0.23
                                                                0.26
                                                                        0.74
##
      0.02
##
    i9->h4 i10->h4
##
      0.42
             -0.08
           i1->h5
##
     b->h5
                    i2->h5 i3->h5
                                     i4->h5
                                             i5->h5
                                                     i6->h5
                                                              i7->h5
                                                                      i8->h5
##
     -8.50
              7.68
                      7.82
                             -0.09
                                      -0.40
                                               0.44
                                                      -0.31
                                                                0.12
                                                                       -0.11
##
    i9->h5 i10->h5
##
      0.13
              0.70
##
     b->o h1->o h2->o h3->o h4->o
## -12.65 37.16 18.40
                          6.72 - 11.46
# Predict on the test set and see how well it did
nnetPredict <- predict(nnetFit, testData$x)</pre>
postResample(pred = nnetPredict, obs = testData$y)
```

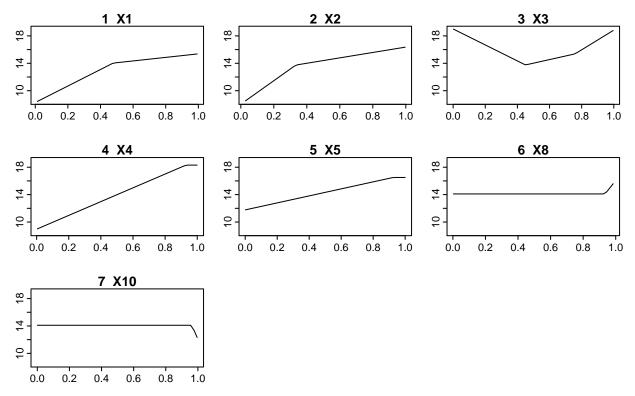
Discussion: This basic model ends up with a high \mathbb{R}^2 with no tuning of any model parameters. Lets see what we can do with better tuning.

 $\mathbf{TODO} \mathbf{:}$ Grid search params using train like example in book

MARS Model

```
# Create a MARS model
marsFit <- earth(trainingData$x, trainingData$y)</pre>
# Show the fit
marsFit
## Selected 12 of 20 terms, and 7 of 10 predictors
## Termination condition: Reached nk 21
## Importance: X4, X2, X1, X5, X3, X10, X8, X6-unused, X7-unused, ...
## Number of terms at each degree of interaction: 1 11 (additive model)
## GCV 2.802104
                   RSS 438.9356
                                    GRSq 0.8927606
                                                      RSq 0.9151612
summary(marsFit)
## Call: earth(x=trainingData$x, y=trainingData$y)
##
##
                   coefficients
## (Intercept)
                      19.942097
## h(0.47762-X1)
                     -12.049125
## h(X1-0.47762)
                       2.584661
## h(0.333521-X2)
                     -17.108629
## h(X2-0.333521)
                       3.938851
## h(0.450485-X3)
                      11.661496
## h(X3-0.450485)
                       5.244239
## h(X3-0.758697)
                       9.131904
## h(0.929743-X4)
                     -10.060992
## h(0.925323-X5)
                      -5.119769
## h(X8-0.934716)
                      29.960793
## h(X10-0.961949)
                     -53.215152
##
## Selected 12 of 20 terms, and 7 of 10 predictors
## Termination condition: Reached nk 21
## Importance: X4, X2, X1, X5, X3, X10, X8, X6-unused, X7-unused, ...
## Number of terms at each degree of interaction: 1 11 (additive model)
## GCV 2.802104
                   RSS 438.9356
                                    GRSq 0.8927606
                                                      RSq 0.9151612
# Predict on the test set and see how well it did
marsPredict <- predict(marsFit, testData$x)</pre>
postResample(pred = marsPredict, obs = testData$y)
        RMSE Rsquared
## 1.8871553 0.8598973
# Inspect the model's use of predictors
plotmo(marsFit, caption = "Predictors vs Observed in Additive MARS Model")
                                  ХЗ
                                            Х4
                                                    Х5
                                                               Х6
                                                                         X7
##
    grid:
##
      0.5054907 0.4244831 0.5158712 0.5114502 0.45547 0.4441768 0.4696555
##
## 0.4949538 0.4917092 0.5036008
```

Predictors vs Observed in Additive MARS Model



Discussion: It does seem like the first 5 predictors are noted as important, and left the other predictors out. Pretty impressive there, MARS.

Support Vector Machine Model

```
svmFit <- ksvm(y ~ ., data = as.data.frame(trainingData),</pre>
   kernel = "rbfdot", kpar = "automatic", C = 1, epsilon = 0.1)
## Using automatic sigma estimation (sigest) for RBF or laplace kernel
svmFit
## Support Vector Machine object of class "ksvm"
##
## SV type: eps-svr (regression)
## parameter : epsilon = 0.1 \cos C = 1
## Gaussian Radial Basis kernel function.
## Hyperparameter : sigma = 0.0617877542444368
##
## Number of Support Vectors : 170
##
## Objective Function Value : -42.2388
## Training error: 0.083273
summary(svmFit)
## Length Class
                   Mode
##
       1
           ksvm
svmPredict <- predict(svmFit, as.data.frame(testData))</pre>
postResample(pred = svmPredict, obs = testData$y)
##
        RMSE Rsquared
## 2.4201570 0.7770665
Lets tune a hopefuly better SVM model:
svmRTuned <- train(trainingData$x, trainingData$y,</pre>
    method = "svmRadial", preProc = c("center", "scale"),
   tuneLength = 14, trControl = trainControl(method = "cv"))
svmRTuned
## Support Vector Machines with Radial Basis Function Kernel
## 200 samples
## 10 predictors
##
## Pre-processing: centered, scaled
## Resampling: Cross-Validated (10 fold)
##
```

```
## Summary of sample sizes: 180, 180, 180, 180, 180, 180, ...
##
## Resampling results across tuning parameters:
##
##
             RMSE
                       Rsquared
                                  RMSE SD
                                             Rsquared SD
##
       0.25 2.595022 0.7929425 0.3592234 0.07841429
##
       0.50 2.359706 0.8062457 0.3528681 0.08495943
##
       1.00 2.249207
                       0.8183889 0.3751124
                                             0.07884515
##
       2.00 2.177391
                       0.8291890 0.3386386
                                             0.06241932
##
       4.00 2.133625
                       0.8354071 0.3228081
                                            0.05105185
##
       8.00 2.105195
                       0.8388782 0.2884709
                                             0.04641157
##
      16.00 2.104702
                      0.8389732 0.2840710 0.04436779
##
      32.00 2.104702 0.8389732 0.2840710 0.04436779
##
      64.00 2.104702 0.8389732 0.2840710 0.04436779
##
     128.00 2.104702
                       0.8389732 0.2840710 0.04436779
##
     256.00 2.104702
                       0.8389732
                                  0.2840710
                                             0.04436779
##
     512.00 2.104702 0.8389732 0.2840710
                                             0.04436779
##
    1024.00 2.104702 0.8389732 0.2840710
                                             0.04436779
##
    2048.00 2.104702 0.8389732 0.2840710 0.04436779
##
## Tuning parameter 'sigma' was held constant at a value of 0.0664479
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were sigma = 0.0664479 and C = 16.
summary(svmRTuned)
## Length Class
                  Mode
                    S4
           ksvm
svmTunedPredict <- predict(svmRTuned, testData$x)</pre>
postResample(pred = svmTunedPredict, obs = testData$y)
       RMSE Rsquared
## 1.9861165 0.8427245
```

TODO: Try other kernels

Question 7.4

Question

Return to the permeability problem outlined in Exercise 6.2. Train several nonlinear regression models and evaluate the resampling and test set performance.

- (a) Which nonlinear regression model gives the optimal resampling and test set performance?
- (b) Do any of the nonlinear models outperform the optimal linear model you previously developed in Exercise 6.2? If so, what might this tell you about the underlying relationship between the predictors and the response?
- (c) Would you recommend any of the models you have developed to replace the permeability laboratory experiment?

Answer

Like above, we will try out three kinds of models, and we'll see which one does the best and if these models are better than the linear models created in the previous assignment.

Data Pre-Processing

Before creating models, we should make sure the data is properly pre-processed. I will follow the same exact moethodology as per the previous assignment:

The three models will be presented next, with results to follow.

Neural Net Model

a 110-5-1 network with 561 weights
options were - linear output units decay=0.01

summary(nnetFit)

```
## a 110-5-1 network with 561 weights
## options were - linear output units decay=0.01
##
      b->h1
              i1->h1
                       i2->h1
                                i3->h1
                                          i4->h1
                                                   i5->h1
                                                            i6->h1
                                                                     i7->h1
##
      -3.61
                1.36
                        10.87
                                  0.97
                                           -3.17
                                                    -2.07
                                                              1.44
                                                                      -0.57
##
     i8->h1
              i9->h1 i10->h1 i11->h1
                                       i12->h1
                                                 i13->h1
                                                           i14->h1
                                                                    i15->h1
                                                             -8.34
##
      -1.40
                1.68
                         0.07
                                 -0.79
                                          -0.99
                                                    -1.91
                                                                      -0.31
##
   i16->h1 i17->h1
                     i18->h1 i19->h1
                                        i20->h1
                                                 i21->h1
                                                           i22->h1
                                                                    i23->h1
##
               -0.23
                                                     1.07
      -1.07
                        -0.65
                                 -4.56
                                          -1.52
                                                             -2.43
                                                                      -0.09
##
   i24->h1
            i25->h1 i26->h1 i27->h1
                                        i28->h1
                                                 i29->h1
                                                           i30->h1 i31->h1
##
       0.60
               -1.74
                         6.68
                                 -2.57
                                          -0.36
                                                    -2.76
                                                             -2.22
                                                                       3.51
##
   i32->h1
                      i34->h1 i35->h1
                                        i36->h1
                                                 i37->h1
                                                           i38->h1
                                                                    i39->h1
            i33->h1
##
      -1.96
               -2.44
                         0.29
                                 -0.13
                                          -2.27
                                                     1.20
                                                             -0.48
                                                                      -5.96
##
   i40->h1
            i41->h1
                     i42->h1 i43->h1
                                        i44->h1
                                                 i45->h1
                                                           i46->h1
                                                                   i47->h1
##
      -0.62
               -1.93
                         1.54
                                 -1.52
                                            1.87
                                                    -4.20
                                                             -0.90
                                                                      -1.70
            i49->h1
                      i50->h1
                                                  i53->h1
##
   i48->h1
                               i51->h1
                                        i52->h1
                                                           i54->h1
                                                                    i55->h1
##
       1.29
               -0.28
                         1.55
                                  -0.89
                                           -1.16
                                                     0.77
                                                             -1.55
            i57->h1
##
    i56->h1
                      i58->h1 i59->h1
                                        i60->h1
                                                 i61->h1
                                                           i62->h1 i63->h1
##
      -2.10
                2.98
                        -3.15
                                  -0.69
                                            3.58
                                                     6.13
                                                              3.76
                                                                       0.57
##
                      i66->h1 i67->h1
                                                           i70->h1 i71->h1
   i64->h1
            i65->h1
                                       i68->h1
                                                 i69->h1
      -0.62
               -0.49
                         0.97
                                  5.20
                                            2.37
                                                    -1.00
                                                              3.18
                                                                      -2.21
##
   i72->h1 i73->h1 i74->h1 i75->h1
                                                 i77->h1
                                                           i78->h1 i79->h1
                                        i76->h1
##
       1.52
               -1.60
                         4.75
                                 -0.79
                                            2.75
                                                    -2.24
                                                             -0.79
                                                                      -2.51
##
   i80->h1 i81->h1
                      i82->h1
                              i83->h1
                                        i84->h1
                                                 i85->h1
                                                           i86->h1 i87->h1
##
       1.19
                2.46
                         1.56
                                 -1.79
                                            0.76
                                                     0.16
                                                              0.22
                                                                       0.55
##
                      i90->h1 i91->h1 i92->h1
                                                 i93->h1
                                                           i94->h1 i95->h1
    i88->h1
            i89->h1
##
      -0.05
                1.93
                        -0.97
                                  -3.47
                                            0.85
                                                     5.46
                                                             -3.06
                                                                       1.18
##
    i96->h1
            i97->h1
                      i98->h1 i99->h1 i100->h1 i101->h1 i102->h1 i103->h1
##
                        -1.34
                                 -1.50
                                           -2.85
                                                    -1.68
                                                             -1.38
       1.51
                2.18
                                                                       1.46
##
  i104->h1 i105->h1 i106->h1 i107->h1 i108->h1 i109->h1 i110->h1
##
      -2.27
               -0.97
                         2.81
                                 -2.13
                                          -1.04
                                                    -0.85
                                                             -0.92
##
      b->h2
              i1->h2
                       i2->h2
                                i3->h2
                                          i4->h2
                                                   i5->h2
                                                            i6->h2
                                                                     i7->h2
##
     -1.93
               -0.14
                         8.83
                                  0.11
                                          -3.69
                                                     1.79
                                                             -0.21
                                                                       5.12
##
     i8->h2
              i9->h2 i10->h2 i11->h2 i12->h2
                                                  i13->h2
                                                           i14->h2
                                                                    i15->h2
##
     -0.18
                0.21
                        -1.49
                                  -0.16
                                           -0.65
                                                     0.44
                                                             -1.43
                                                                       0.14
##
   i16->h2 i17->h2 i18->h2 i19->h2 i20->h2
                                                 i21->h2 i22->h2
                                                                   i23->h2
               -2.79
                                            0.25
                                                                      -2.90
##
      -3.54
                         0.54
                                  0.31
                                                    -2.97
                                                              0.95
```

```
i24->h2 i25->h2 i26->h2 i27->h2 i28->h2 i29->h2 i30->h2 i31->h2
##
     -0.93
             -1.16
                     -3.69
                            -0.62
                                       0.40
                                              -2.10
                                                       -2.05
                                                               -0.35
##
   i32->h2 i33->h2 i34->h2 i35->h2 i36->h2 i37->h2 i38->h2 i39->h2
                                      -0.38
                                              0.06
                                                      -0.63
##
     -1.85
             -0.65
                       1.78
                             -0.82
                                                              -0.39
##
   i40->h2 i41->h2 i42->h2 i43->h2 i44->h2
                                            i45->h2 i46->h2 i47->h2
##
     -0.50
             -0.04
                       0.14
                               0.23
                                      -0.31
                                               0.12
                                                       -1.87
                                                               -2.18
##
   i48->h2 i49->h2 i50->h2 i51->h2 i52->h2 i53->h2 i54->h2 i55->h2
##
     0.03
             -0.12
                       0.04
                              -0.35
                                      -0.34
                                              -1.56
                                                       -0.21
                                                               -0.17
##
   i56->h2 i57->h2 i58->h2 i59->h2 i60->h2 i61->h2 i62->h2 i63->h2
##
     -0.76
           -0.22
                    -0.09
                            -0.59
                                    -0.10
                                             -2.06
                                                     -0.04
                                                              -1.31
   i64->h2 i65->h2 i66->h2 i67->h2 i68->h2 i69->h2 i70->h2 i71->h2
                                             1.42
                                                      -0.09
##
    -0.08
           0.08
                    0.16
                            0.08
                                    -0.12
                                                              -0.16
   i72->h2 i73->h2 i74->h2 i75->h2 i76->h2
                                            i77->h2 i78->h2 i79->h2
##
##
     -0.09
           0.10
                      0.13
                            -0.12
                                      1.06
                                               1.77
                                                       1.88
                                                              0.16
##
   i80->h2 i81->h2 i82->h2 i83->h2 i84->h2 i85->h2 i86->h2 i87->h2
##
    -1.68
            -2.89
                       0.12
                            -0.30
                                     -0.28
                                               0.06
                                                      -0.05
                                                              0.06
##
   i88->h2 i89->h2 i90->h2 i91->h2 i92->h2 i93->h2 i94->h2 i95->h2
##
     -0.02
              0.11
                    -0.05
                            -1.58
                                      -0.01
                                               0.04
                                                       -0.27
##
   i96->h2 i97->h2 i98->h2 i99->h2 i100->h2 i101->h2 i102->h2 i103->h2
##
     -0.20
             0.09
                     -0.23
                            -0.42
                                      -1.45
                                              -0.18
                                                      -1.60
                                                                0.77
## i104->h2 i105->h2 i106->h2 i107->h2 i108->h2 i109->h2 i110->h2
##
     -1.38
             -1.51
                      0.02
                             -1.43
                                    -1.48
                                              -0.10
                                                       0.21
                                                     i6->h3
##
     b->h3
            i1->h3
                   i2->h3
                            i3->h3
                                    i4->h3
                                              i5->h3
                                                              i7->h3
##
     3.47
             5.63
                     -1.86
                               1.05
                                       1.14
                                               1.90
                                                        2.05
                                                               -2.43
##
           i9->h3 i10->h3 i11->h3 i12->h3 i13->h3 i14->h3 i15->h3
    i8->h3
##
      1.16
             1.04
                      5.71
                              1.46
                                      0.40
                                             0.02
                                                      -0.46
                                                                2.10
##
   i16->h3 i17->h3 i18->h3 i19->h3 i20->h3
                                            i21->h3 i22->h3 i23->h3
                                      0.65
                                               1.52
##
     1.13
            -0.02
                     0.21
                              1.78
                                                       1.23
                                                                1.60
##
   i24->h3 i25->h3 i26->h3 i27->h3 i28->h3
                                            i29->h3 i30->h3 i31->h3
##
     2.12
             1.38
                     -3.74
                              1.12
                                       0.06
                                              -0.43
                                                       -0.93
                                                                0.20
                                            i37->h3 i38->h3 i39->h3
##
   i32->h3 i33->h3 i34->h3 i35->h3 i36->h3
##
      9.65
             -3.70
                       2.79
                               2.75
                                       0.40
                                               2.00
                                                       -4.62
                                                               -2.48
           i41->h3 i42->h3 i43->h3 i44->h3
##
   i40->h3
                                            i45->h3
                                                     i46->h3 i47->h3
##
            -0.62
                       0.07
                              0.53
                                    -0.26
                                              -0.40
                                                      -0.25
     0.05
                                                              -0.42
##
   i48->h3 i49->h3 i50->h3 i51->h3 i52->h3
                                            i53->h3
                                                     i54->h3 i55->h3
##
     -0.52
             -2.87
                      0.48
                             -1.51
                                       0.30
                                               0.75
                                                       0.84
                                                                0.66
##
   i56->h3 i57->h3 i58->h3 i59->h3 i60->h3
                                            i61->h3 i62->h3 i63->h3
##
     -1.14
             -0.12
                       0.72
                              -0.67
                                      -1.40
                                               0.34
                                                        0.88
                                                               -0.96
##
   i64->h3 i65->h3 i66->h3 i67->h3 i68->h3
                                            i69->h3 i70->h3 i71->h3
             -2.56
                                              -3.02
##
     -1.17
                       2.28
                              -0.32
                                       0.09
                                                      -0.56
                                                              -1.29
   i72->h3 i73->h3 i74->h3 i75->h3 i76->h3
                                            i77->h3 i78->h3 i79->h3
##
##
     -2.36
             2.21
                       0.63
                             -0.64
                                       2.96
                                               0.98
                                                        0.99
                                                               1.71
   i80->h3 i81->h3 i82->h3 i83->h3 i84->h3
                                            i85->h3
                                                     i86->h3 i87->h3
##
##
     1.93
              0.62
                      1.57
                              1.04
                                       0.96
                                              -0.56
                                                        0.77
                                                                0.93
   i88->h3 i89->h3 i90->h3 i91->h3 i92->h3
                                            i93->h3 i94->h3 i95->h3
##
                       1.58
                                      -0.40
                                              -1.60
                                                        0.12
##
      0.64
              2.03
                            -0.40
                                                                0.96
   i96->h3 i97->h3 i98->h3 i99->h3 i100->h3 i101->h3 i102->h3 i103->h3
##
##
     -0.16
              0.94
                              -0.38
                                       1.22
                                               1.59
                                                        0.26
                                                               -5.08
                     -0.15
##
  i104->h3 i105->h3 i106->h3 i107->h3 i108->h3 i109->h3 i110->h3
##
     -2.87
             0.15
                      6.04
                             -3.96
                                      1.69
                                               0.75
                                                        0.12
                            i3->h4
                                    i4->h4
##
     b->h4
           i1->h4
                    i2->h4
                                              i5->h4
                                                     i6->h4
                                                              i7->h4
##
     -0.67
             -2.30
                     -1.51
                              0.86
                                      -0.05
                                               2.63
                                                        1.45
                                                               -3.85
##
    i8->h4 i9->h4 i10->h4 i11->h4 i12->h4 i13->h4 i14->h4 i15->h4
    0.47
##
             1.97
                    -3.50
                            -2.46
                                      -1.94
                                               1.56
                                                     0.03
                                                              0.61
```

```
i16->h4 i17->h4 i18->h4 i19->h4 i20->h4 i21->h4 i22->h4 i23->h4
##
     -1.61
              1.48
                       2.18
                            -1.90
                                       1.75
                                              -0.60
                                                        1.42
                                                                0.24
##
   i24->h4 i25->h4 i26->h4 i27->h4 i28->h4
                                            i29->h4 i30->h4 i31->h4
                                       0.94
                                              -0.47
##
      1.61
              1.81
                       4.98
                             -0.02
                                                       -2.13
                                                               -4.17
##
   i32->h4 i33->h4 i34->h4 i35->h4 i36->h4
                                            i37->h4
                                                     i38->h4 i39->h4
##
      0.45
             -1.87
                      -0.56
                              -0.60
                                      -1.34
                                                0.92
                                                       -0.09
                                                                0.02
   i40->h4 i41->h4 i42->h4 i43->h4 i44->h4
                                            i45->h4 i46->h4 i47->h4
##
     -0.96
              0.28
                      -0.62
                               1.23
                                      -0.48
                                                0.59
                                                        0.77
##
                                                               -0.67
##
   i48->h4 i49->h4 i50->h4 i51->h4 i52->h4 i53->h4 i54->h4 i55->h4
                             1.08
##
     -0.96
            -0.91
                    -0.47
                                     -2.12
                                             -0.74
                                                       -0.28
                                                                 0.06
   i56->h4 i57->h4 i58->h4 i59->h4 i60->h4 i61->h4 i62->h4 i63->h4
                                     1.22
                                                        2.27
##
    -0.05
            1.49
                    -0.13
                            0.30
                                             -0.47
                                                               1.07
           i65->h4 i66->h4 i67->h4 i68->h4
##
   i64->h4
                                            i69->h4
                                                     i70->h4 i71->h4
##
    -0.46
            0.87
                    -0.82
                                       2.64
                                              -4.79
                                                       -1.61
                                                                0.24
                            2.10
##
   i72->h4 i73->h4 i74->h4 i75->h4 i76->h4
                                            i77->h4 i78->h4 i79->h4
##
    1.68
            -0.59
                    -0.91
                             -1.25
                                     -0.82
                                                0.77
                                                       -0.85
                                                               -0.25
##
   i80->h4
           i81->h4 i82->h4 i83->h4 i84->h4
                                            i85->h4
                                                     i86->h4 i87->h4
##
     -0.21
              1.11
                       2.34
                            -1.18
                                       0.14
                                                1.16
                                                        0.05
                                                               1.43
##
   i88->h4 i89->h4 i90->h4 i91->h4 i92->h4 i93->h4 i94->h4 i95->h4
##
     0.36
            0.14
                       0.03
                             -0.31
                                       0.57
                                               -0.88
                                                       -1.06
                                                               -0.32
##
   i96->h4 i97->h4 i98->h4 i99->h4 i100->h4 i101->h4 i102->h4 i103->h4
##
      1.56
              1.03
                      -1.36
                              -0.55
                                      -1.07
                                               -0.75
                                                       -1.12
                                                               -2.83
## i104->h4 i105->h4 i106->h4 i107->h4 i108->h4 i109->h4 i110->h4
     -1.00
             0.82
                      0.64
                             -0.47
                                      -0.37
                                               1.12
                                                       1.91
##
##
     b->h5
           i1->h5
                    i2->h5 i3->h5
                                                      i6->h5
                                    i4->h5
                                              i5->h5
                                                              i7->h5
##
     -0.16
            -0.91
                     2.92
                            -2.79
                                    -3.83
                                              -1.90
                                                        2.06
                                                              -0.83
##
    i8->h5
           i9->h5 i10->h5 i11->h5 i12->h5
                                            i13->h5 i14->h5 i15->h5
                                              0.78
                                                       -0.37
                                                                0.68
##
     -1.40
             -1.07
                     -3.12
                             -3.52
                                      0.43
##
   i16->h5 i17->h5 i18->h5 i19->h5 i20->h5
                                            i21->h5
                                                     i22->h5 i23->h5
##
     0.73
             1.36
                     -0.36
                             -1.86
                                       2.96
                                               -0.02
                                                       -0.72
                                                               -3.74
##
   i24->h5 i25->h5 i26->h5 i27->h5 i28->h5
                                            i29->h5 i30->h5 i31->h5
##
      0.57
             -0.03
                       0.26
                              -4.92
                                      -0.45
                                              -2.36
                                                       -0.51
                                                               -3.63
##
   i32->h5
           i33->h5 i34->h5 i35->h5
                                    i36->h5
                                            i37->h5
                                                     i38->h5 i39->h5
##
    -1.23
            -0.87
                    -0.48
                              2.88
                                      1.77
                                              -0.53
                                                       1.37
                                                              -1.15
##
   i40->h5
           i41->h5 i42->h5 i43->h5 i44->h5
                                            i45->h5
                                                     i46->h5 i47->h5
                                                               0.80
##
     1.55
             -0.49
                     1.43
                              0.12
                                       2.02
                                              -2.13
                                                       -1.79
##
   i48->h5 i49->h5 i50->h5 i51->h5 i52->h5 i53->h5
                                                     i54->h5 i55->h5
##
     2.21
             0.53
                     1.45
                               2.19
                                      -2.92
                                              -2.64
                                                        0.05
                                                               -1.91
##
   i56->h5 i57->h5 i58->h5 i59->h5 i60->h5 i61->h5
                                                     i62->h5 i63->h5
                    -0.42
     -0.66
                                              -1.28
##
             1.13
                            -0.48
                                       2.81
                                                        0.58
                                                                0.04
   i64->h5 i65->h5 i66->h5 i67->h5 i68->h5 i69->h5
                                                     i70->h5 i71->h5
##
                    -0.61
##
     -1.40
            -0.94
                             0.62
                                     -1.17
                                              -3.45
                                                        1.07
                                                              -0.66
   i72->h5 i73->h5 i74->h5 i75->h5 i76->h5
                                            i77->h5
                                                     i78->h5 i79->h5
##
##
     -5.86
            -0.59
                    1.03
                            1.39
                                       5.95
                                               0.50
                                                       1.10
                                                               -2.12
   i80->h5 i81->h5 i82->h5 i83->h5 i84->h5
                                            i85->h5 i86->h5 i87->h5
##
                             -0.05
                    -1.11
                                       0.73
                                              -2.33
                                                       -2.15
##
     3.29
              3.61
                                                              -1.59
##
   i88->h5
           i89->h5 i90->h5 i91->h5 i92->h5 i93->h5 i94->h5 i95->h5
##
     -0.92
              0.40
                       0.36
                            -3.49
                                      -3.77
                                               -0.35
                                                       -0.19
                                                               -0.20
##
   i96->h5 i97->h5 i98->h5 i99->h5 i100->h5 i101->h5 i102->h5 i103->h5
##
     -0.67
             -0.88
                       0.86
                            -0.27
                                       1.01
                                              -1.48
                                                       -2.31
                                                                2.50
## i104->h5 i105->h5 i106->h5 i107->h5 i108->h5 i109->h5 i110->h5
##
     -0.65
              1.65
                     -0.01
                              1.63
                                       1.51
                                              -0.22
                                                       0.09
##
    b->o h1->o h2->o h3->o h4->o h5->o
   18.13 5.21 -22.07 -17.34 27.54 22.45
##
```

```
# Predict on the test set and see how well it did
nnetPredict <- predict(nnetFit, fingerprints.test)
postResample(pred = nnetPredict, obs = permeability.test)</pre>
```

RMSE Rsquared ## 2.2985847 0.9779633

Discussion:

MARS Model

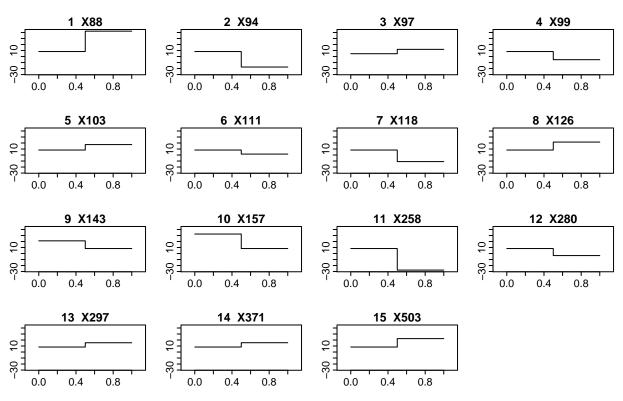
7.9943264 0.7332244

```
# Create a MARS model
marsFit <- earth(fingerprints.train, permeability.train)</pre>
# Show the fit
marsFit
## Selected 16 of 55 terms, and 15 of 110 predictors
## Termination condition: GRSq -10 at 55 terms
## Importance: X157, X503, X698-unused, X6-unused, X141-unused, X371, ...
## Number of terms at each degree of interaction: 1 15 (additive model)
## GCV 113.6165
                   RSS 7924.748
                                   GRSq 0.5333509
                                                      RSq 0.7332244
summary(marsFit)
## Call: earth(x=fingerprints.train, y=permeability.train)
##
##
               coefficients
## (Intercept)
                  41.602269
                  33.911235
## X88
## X94
                 -25.793638
## X97
                   7.231244
## X99
                 -13.560189
## X103
                   9.060141
## X111
                  -6.731119
## X118
                 -19.261123
## X126
                  13.264522
## X143
                 -12.805263
## X157
                 -24.116205
## X258
                 -35.873602
## X280
                 -11.735595
## X297
                   7.127412
                   7.197599
## X371
## X503
                  13.991710
## Selected 16 of 55 terms, and 15 of 110 predictors
## Termination condition: GRSq -10 at 55 terms
## Importance: X157, X503, X698-unused, X6-unused, X141-unused, X371, ...
## Number of terms at each degree of interaction: 1 15 (additive model)
## GCV 113.6165
                   RSS 7924.748
                                   GRSq 0.5333509
                                                      RSq 0.7332244
\# Predict on the test set and see how well it did
marsPredict <- predict(marsFit, fingerprints.test)</pre>
postResample(pred = marsPredict, obs = permeability.test)
        RMSE Rsquared
```

Inspect the model's use of predictors
plotmo(marsFit, caption = "Predictors vs Observed in Additive MARS Model")



Predictors vs Observed in Additive MARS Model



Discussion:

Support Vector Machine Model

Results and Discussions