

Contest Math Cheat Sheet

1. Combinatorics & Counting

- $C(n, k) = n! / (k! * (n-k)!)$
- Pascal's Rule: $C(n, k) = C(n-1, k-1) + C(n-1, k)$
- Symmetry: $C(n, k) = C(n, n-k)$
- Sum over k : $\sum_{k=0}^n C(n, k) = 2^n$
- Sum over n : $\sum_{m=0}^n C(m, k) = C(n+1, k+1)$
- Stars & Bars: Allow empty: $C(n+k-1, k-1)$, No empty: $C(n-1, k-1)$
- Catalan Numbers: $Cat(n) = (1 / (n+1)) * C(2n, n)$

2. Number Theory

- $LCM(a, b) = (a * b) / GCD(a, b)$
- $(a+b) \bmod m = (a \bmod m + b \bmod m) \bmod m$
- $(a-b) \bmod m = (a \bmod m - b \bmod m + m) \bmod m$
- $(a*b) \bmod m = (a \bmod m * b \bmod m) \bmod m$
- Fast exponentiation: $O(\log b)$
- Fermat: $a^{(p-1)} \equiv 1 \pmod{p}$ if p prime
- Mod inverse (prime p): $a^{(p-2)} \bmod p$
- Chinese Remainder Theorem: solve congruences when moduli coprime

3. Algebra & Sums

- AP sum: $S_n = n/2 * (2a + (n-1)d)$
- GP sum: $S_n = a * (r^n - 1) / (r - 1)$
- Sum first n : $n(n+1)/2$
- Sum squares: $n(n+1)(2n+1)/6$
- Sum cubes: $[n(n+1)/2]^2$

4. Probability

- $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
- Independent: $P(A \cap B) = P(A) * P(B)$
- Conditional: $P(A|B) = P(A \cap B) / P(B)$

5. Graph & Paths

- Grid paths (no obstacles): $C(r+c, r)$
- Floyd-Warshall: $O(n^3)$

- Dijkstra: $O((n+m) \log n)$

6. Geometry

- Heron's formula: $A = \sqrt{s(s-a)(s-b)(s-c)}$, $s = (a+b+c)/2$
- Distance 2D: $\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$
- Point-line dist: $|Ax_0 + By_0 + C| / \sqrt{A^2+B^2}$