

$$B_{(k+1)\Delta} = B_0 + \sum_{i=0}^k \varepsilon_{(i+1)\Delta}, \text{ где } \varepsilon_{(i+1)\Delta} \sim N(0, \Delta)$$

$$M\left[B_{(k+1)\Delta}\right] = M\left[B_0 + \sum_{i=0}^k \varepsilon_{(i+1)\Delta}\right] = M[B_0] + \sum_{i=0}^k M\left[\varepsilon_{(i+1)\Delta}\right]$$

Так как $B_0 = 0 \Rightarrow M\left[B_{(k+1)\Delta}\right] = \sum_{i=0}^k M\left[\varepsilon_{(i+1)\Delta}\right]$, где $\varepsilon_{(i+1)\Delta}$ нормальные величины с нулевым средним

Таким образом $M\left[B_{(k+1)\Delta}\right] = 0$

$$M\left[B_{(k+1)\Delta}^2\right] = M\left(\sum_{i=0}^k \varepsilon_{(i+1)\Delta}\right)^2 = M\left(\sum_{i=0}^k \varepsilon_{(i+1)\Delta}^2 + \sum_{j \neq i=0}^k \varepsilon_{(i+1)\Delta} \varepsilon_{(j+1)\Delta}\right) = M\left(\sum_{i=0}^k \varepsilon_{(i+1)\Delta}^2\right) = \sum_{i=0}^k M\varepsilon_{(i+1)\Delta}^2 = \Delta \sum_{i=0}^k 1 = \Delta k$$

$$\begin{aligned} M\left[B_{k\Delta} B_{l\Delta}\right] &= M\left(\sum_{i=1}^k \varepsilon_{i\Delta} \sum_{j=1}^l \varepsilon_{j\Delta}\right) = M\left(\sum_{i=1}^{\min(k,l)} \varepsilon_{i\Delta}^2 + \sum_{j \neq i=1}^{\min(k,l)} \varepsilon_{i\Delta} \varepsilon_{j\Delta} + \sum_{i=\min(k,l)+1}^{\max(k,l)} \varepsilon_{i\Delta} \sum_{j=1}^{\min(k,l)} \varepsilon_{j\Delta}\right) = M\left(\sum_{i=1}^{\min(k,l)} \varepsilon_{i\Delta}^2\right) + 0 + 0 = \sum_{i=1}^{\min(k,l)} M\varepsilon_{i\Delta}^2 = \\ &= \Delta \sum_{i=1}^{\min(k,l)} 1 = \Delta \min(k, l) \end{aligned}$$